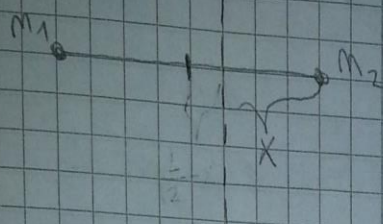


Treće demonstrature

1. Dekanski 2012.



$$L = 1 \text{ m}$$

$$\frac{m_2}{m_1} = 2$$

$$\frac{A(\omega_0)_{\min} = ?}{x = ?}$$

$$F_1 + A = F_2$$

$$0 + A = \frac{1}{2} I \omega^2$$

$$I = m_2 x^2 + m_1 (L-x)^2$$

$$\frac{dI}{dx} = 2m_2 x + 2m_1 (L-x) \cdot (-1) = 0$$

$$2m_2 x = 2m_1 (L-x)$$

$$2x = L - x$$

$$x = \frac{L}{3}$$

2. M1 2011

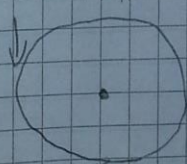
$$m_1 = 45 \text{ kg}$$

$$r = 2 \text{ m}$$

$$M_N = 2 \text{ Nm}$$

$$v_0 = 5 \frac{\text{m}}{\text{s}}$$

$$t_{\text{stop}} = ?$$



$$L_1 = m_1 v_1 r$$

$$L_2 = I \cdot \omega$$

$$L_1 = L_2$$

$$m_1 v_0 r = I \cdot \omega \quad \omega = \frac{m_1 v_0 r}{I}$$

$$v = v_0 - a t = v_0 - \frac{F}{m} t$$

$$\omega = \omega_0 - \frac{M}{I} t$$

$$t_{\text{stop}} = \frac{\omega_0 I}{M} = \frac{I}{M} \frac{m_1 v_0 r}{I} = \frac{m_1 v_0 r}{M}$$

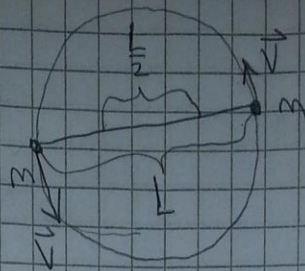
3.

$$m = 100 \text{ t}$$

$$v = 10 \frac{\text{m}}{\text{s}}$$

$$L \rightarrow \frac{L}{2}$$

$$A = ?$$



$$E_1 + A = E_2$$

$$A = E_2 - E_1$$

$$L_1 = m v \frac{L}{2} \cdot 2$$

$$L_1 = L_2$$

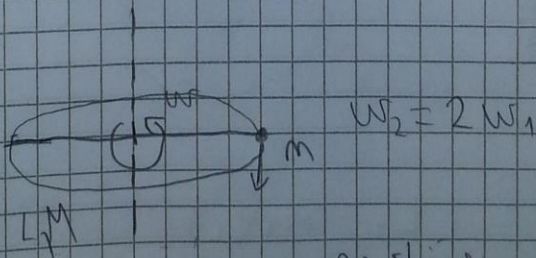
$$L_2 = m v_2 \frac{L}{4} \cdot 2$$

$$m v \frac{L}{2} = m v_2 \frac{L}{2}$$

$$v_2 = 2v$$

$$A = m \cdot 4v^2 - mv^2 = 3mv^2$$

4.



prije eksplozije:

$$L_1 = I \cdot \omega$$

$$I = I_{\text{rod}} + I_m = \frac{1}{12} M l^2 + \left(\frac{l}{2}\right)^2 \cdot m$$

$$L_1 = L_2$$

$$\left(\frac{1}{12} M l^2 + \left(\frac{l}{2}\right)^2 \cdot m\right) \omega = \frac{1}{12} M l^2 \cdot 2\omega - m \cdot \frac{v}{2}$$

$$\omega \left(\frac{1}{12} M l^2 + \left(\frac{l}{2}\right)^2 \cdot m\right) = m \cdot \frac{v}{2}$$

poslije eksplozije:

$$L_2 = I_{\text{rod}} \cdot \omega_2 - m \cdot \frac{v}{2}$$

$$V = \left(\omega \frac{1}{2} - \omega \right) \frac{1}{2}$$

$$V = \frac{1}{2} \omega \left(-1 + \frac{\frac{1}{12} M L^2}{m \frac{L^2}{4}} \right)$$

$$V = \frac{\omega L}{2} \left(-1 + \frac{M}{m} \frac{1}{3} \right)$$

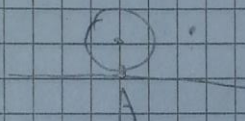
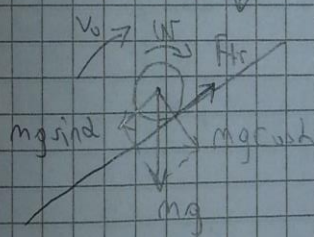
$$V = \frac{\omega L}{2} \left(\frac{M}{3m} - 1 \right)$$

$$V' = V + \omega_2 \frac{1}{2}$$

5. JR 2013 (Kulisić 6.6)

$$v_0 = 1 \frac{m}{s}$$

$$\alpha = 30^\circ$$



u točki A

$$v_c - \omega \cdot r = 0$$

$$v_c = \omega \cdot r$$

$$v = v_0 - at$$

$$F = mg \sin \alpha - F_{tr}$$

$$a = \frac{F}{m} = g \sin \alpha - \frac{mg \sin \alpha}{m}$$

$$\omega = \omega_0 - at = \omega_0 - \frac{a}{r} t$$

$$\omega = \omega_0 - at$$

$$= v_0 - at$$

$$a = \frac{a}{r}$$

$$a = \frac{M}{I} = \frac{\frac{1}{2} m r^2}{\frac{1}{2} m r^2} = \frac{2 F_{tr}}{m r} = \frac{a}{r}$$

$$a = \frac{2 F_{tr}}{m} = \frac{2 m g \cos \alpha}{m}$$

$$a = 2 g \cos \alpha$$

$$a = g \sin \alpha - \frac{a}{2}$$

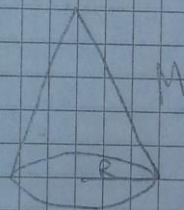
$$a = \frac{3}{2} g \sin \alpha$$

$$0 = v_0 - at$$

Nesto je krivo rješenje pogledati na materijalima

6.

R
M



$$dl = dm r^2 \quad \int$$

$$I = \frac{1}{2} m r^2$$

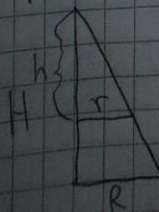
$$dl = \frac{1}{2} \underbrace{dm}_{m_0 = \rho \cdot V} r^2$$

$$dl = \frac{1}{2} \rho dV \cdot r_0^2$$

presek slozka:

$$dl = \frac{1}{2} \rho \underbrace{S_0 dh_0}_{r_0^2 \pi} r_0^2 = \frac{1}{2} \rho r_0^4 \pi dh_0$$

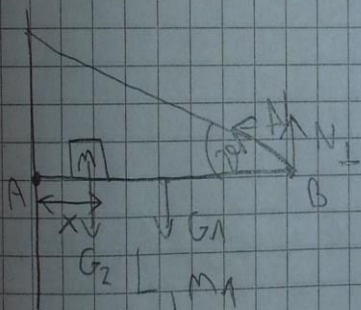
$$\rho = \frac{M}{V} = \frac{M}{\frac{1}{3} R^2 \pi \cdot H}$$



$$r_0 = \frac{R}{H} \cdot h$$

$$\begin{aligned}
 I &= \int dI = \int_0^H \frac{1}{2} \rho r_0^4 dh \\
 &= \frac{1}{2} \rho \left(\frac{R}{H} \right)^4 \int_0^H h^4 dh \\
 &= \frac{\rho}{2} \frac{R^4}{H^4} \frac{1}{5} h^5 \Big|_0^H \\
 &= \frac{\rho}{2} \frac{R^4}{H^4} \frac{1}{5} H^5 \\
 &= \frac{\rho}{2} \frac{M}{\frac{1}{3} \pi R^2 H} \cdot \frac{1}{5} H^2 \\
 &= \frac{3}{10} R^2 M
 \end{aligned}$$

7. M1 2011



$$\sum F = 0$$

$$\sum M = 0$$

$$M_1 = m_1 g \frac{L}{2}$$

$$M_2 = m_2 g x$$

$$M_3 = N \times L = N \cdot L \cdot \sin \theta$$

$$M_1 + M_2 = M_3$$

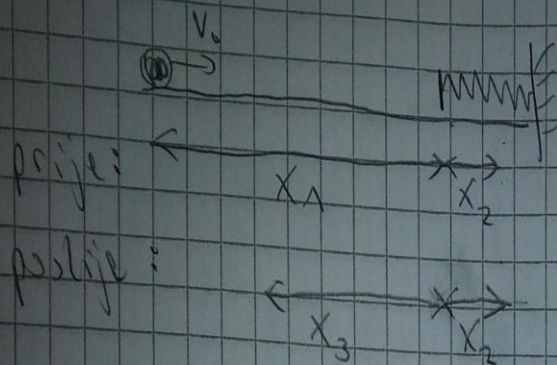
$$m_1 g \frac{L}{2} + m_2 g x = N \cdot L \cdot \sin \theta$$

$$N = \frac{g}{L \sin \theta} (m_1 \frac{L}{2} + m_2 x)$$

$$N = 440 \text{ N}$$

$$x =$$

8. M1, ?



$$D = x_1 + 2x_2 + x_3 = 200 \text{ m}$$

$$v_0 = 10 \text{ m/s}$$

$$E_{K_0} = x_1 \mu mg + x_2 \mu mg + \left(\frac{1}{2} k x_2^2 \right)$$

$$\left(\frac{1}{2} k x_2^2 \right) = x_2 \mu mg + x_3 \mu mg$$

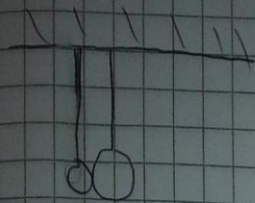
$$E_{K_0} = x_1 \mu mg + x_2 \mu mg + x_2 \mu mg + x_3 \mu mg$$

$$\frac{m v_0^2}{2} = \mu mg (x_1 + 2x_2 + x_3)$$

$$\frac{m v_0^2}{2} = \mu mg \cdot D$$

$$\mu = \frac{v_0^2}{2 \cdot g \cdot D}$$

9. XI, 2013. (sličan kulirić 4.10.)



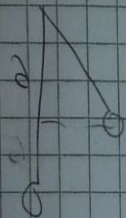
$$m_1 = 0.3 \text{ kg}$$

$$m_2 = 0.2 \text{ kg}$$

$$\alpha = 50^\circ$$

$$\rho = 25^\circ$$

Kugla 1



$$a = L \cos \alpha$$

$$h = L - a$$

$$h = L(1 - \cos \alpha)$$

$$E_{p1} = m_1 g h_1 = \frac{m_1 v_1^2}{2}$$

$$v_1 = \sqrt{2gh_1}$$

$$h_2 = L(1 - \cos \rho)$$

$$v_2 = \sqrt{2gh_2}$$

$$m_1 v_1 - m_2 v_2 = (m_1 + m_2) v$$

$$v = \frac{\sqrt{2g}}{m_1 + m_2} (m_1 \sqrt{h_1} + m_2 \sqrt{h_2})$$

$$E_p = M g H = M \frac{v^2}{2}$$

$$H = \frac{M v^2}{2 M g} = L(1 - \cos \rho)$$

$$\cos \rho = 1 - \frac{v^2}{L \cdot 2 \cdot g}$$

$$\rho = \arccos \left(1 - \frac{v^2}{L \cdot 2 \cdot g} \right)$$