

Fizika 1

GRUPA 1.03
SAŠA ILIJIĆ

PREDAVANJA 2010.

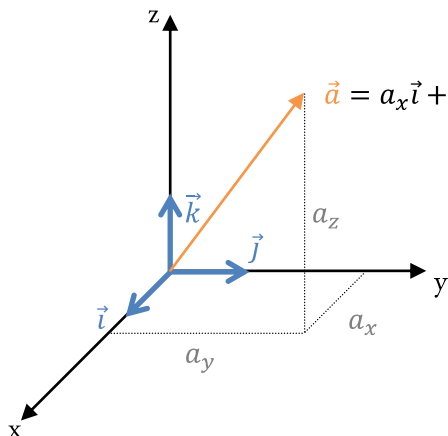
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FIZIKALNE VELIČINE: -SKALARI (imaju samo iznos ~ temperatura, tlak, gustoća...)
 -VEKTORI (imaju iznos i smjer ~ brzina, akceleracija, struja...)
 -TENZORI

VEKTORI

PRAVOKUTNI KOORDINATNI SUSTAV (desno orijentirani)



$$\vec{a} = a_x \vec{i} + a_y \vec{j} + a_z \vec{k}$$

$\vec{i}, \vec{j}, \vec{k}$ - jedinični vektori

a_x, a_y, a_z - komponente vektora **a**

ZBRAJANJE VEKTORA

$$\vec{a} + \vec{b} = (a_x + b_x)\vec{i} + (a_y + b_y)\vec{j} + (a_z + b_z)\vec{k}$$

MNOŽENJE VEKTORA SKALAROM

$$\lambda \vec{a} = \lambda a_x \vec{i} + \lambda a_y \vec{j} + \lambda a_z \vec{k}$$

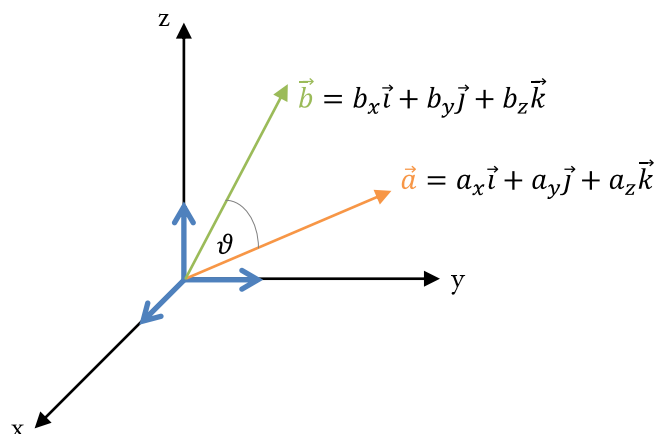
skalar

SKALARNO MNOŽENJE VEKTORA

$$\vec{a} \cdot \vec{b} \equiv \underbrace{a_x b_x + a_y b_y + a_z b_z}_{\text{skalar}}$$

$$\vec{a} \cdot \vec{a} = a_x^2 + a_y^2 + a_z^2$$

$$a = |\vec{a}| = \sqrt{\vec{a} \cdot \vec{a}} = \sqrt{a_x^2 + a_y^2 + a_z^2}$$



$$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \vartheta$$

theta, kut među vektorima

$$|\vec{a} + \vec{b}|^2 = |\vec{a}|^2 + 2|\vec{a}| |\vec{b}| \cos \vartheta + |\vec{b}|^2$$

$$|\vec{a} + \vec{a}|^2 = 4|\vec{a}|^2 = |\vec{a}|^2 + 2|\vec{a}| |\vec{a}| \cos \vartheta + |\vec{a}|^2 \quad \blacksquare$$

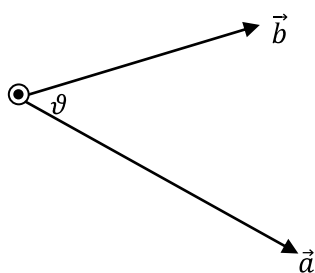
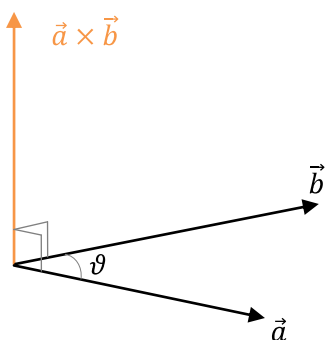
=1

$$|\vec{a} - \vec{a}|^2 = 0 = |\vec{a}|^2 + 2|\vec{a}| |\vec{a}| \cos \vartheta + |\vec{a}|^2 \quad \blacksquare$$

=-1

VEKTORSKI PRODUKT

$$\vec{a} \times \vec{b} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$$

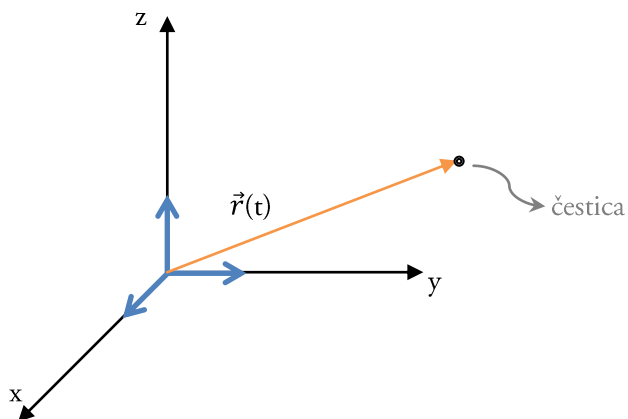


⊗ - „u ploču“
⊙ - prema nama

$$\vec{a} \times \vec{b} = -(\vec{b} \times \vec{a})$$

$$|\vec{a} \times \vec{b}| = |\vec{a}| |\vec{b}| \sin \vartheta$$

KINEMATIKA TOČKE



POLOŽAJ:

$$\vec{r}(t) = x(t)\vec{i} + y(t)\vec{j} + z(t)\vec{k}$$

BRZINA:

$$\vec{v}(t) = \frac{d}{dt} \vec{r}(t)$$

- vremenska derivacija vektora koji opisuje položaj

$$= \frac{d}{dt} x(t)\vec{i} + y(t)\vec{j} + z(t)\vec{k} = \frac{dx(t)}{dt} \vec{i} + \frac{dy(t)}{dt} \vec{j} + \frac{dz(t)}{dt} \vec{k}$$

$$= v_x(t)\vec{i} + v_y(t)\vec{j} + v_z(t)\vec{k}$$

$$\vec{v} \equiv \dot{\vec{r}} \rightarrow \frac{d}{dt}$$

$$v_x\vec{i} + v_y\vec{j} + v_z\vec{k} = \dot{x}\vec{i} + \dot{y}\vec{j} + \dot{z}\vec{k}$$

INTEGRALNI ZAPIS:

$$\vec{v}(t) = \frac{d}{dt} \vec{r}(t) \quad / \cdot dt$$

$$d\vec{r}(t) = \vec{v}(t)dt \quad \int_{t_0}^{t_1}$$

$$\int_{t_0}^{t_1} d\vec{r} = \int_{t_0}^{t_1} \vec{v}(t) dt$$

$$\vec{r}(t_1) - \vec{r}(t_0) = \int_{t_0}^{t_1} \vec{v}(t) dt$$

$$t_1 \rightarrow t, \quad t \rightarrow t'$$

$$\vec{r}(t) - \vec{r}(t_0) = \int_{t_0}^t \vec{v}(t') dt'$$

„početni uvjet“

brzina!

AKCELERACIJA:

$$\vec{a}(t) \equiv \frac{d}{dt} \vec{v}(t)$$

- derivacija brzine po vremenu

$$= \frac{d^2}{dt^2} \vec{v}(t)$$

$$\vec{a}(t) = a_x(t)\vec{i} + a_y(t)\vec{j} + a_z(t)\vec{k}$$

$$= \frac{d}{dt} v_x(t)\vec{i} + \frac{d}{dt} v_y(t)\vec{j} + \frac{d}{dt} v_z(t)\vec{k} = \frac{d^2 x(t)}{dt^2} \vec{i} + \frac{d^2 y(t)}{dt^2} \vec{j} + \frac{d^2 z(t)}{dt^2} \vec{k}$$

$$\vec{a} = a_x \vec{i} + a_y \vec{j} + a_z \vec{k} = \dot{v}_x \vec{i} + \dot{v}_y \vec{j} + \dot{v}_z \vec{k}$$

$$= \ddot{x} \vec{i} + \ddot{y} \vec{j} + \ddot{z} \vec{k}$$

$$\vec{a}(t) = \frac{d}{dt} \vec{v}(t) \quad / \cdot dt$$

$$d\vec{v}(t) = \vec{a}(t) dt \quad \int_{t_0}^{t_1}$$

$$\int_{t_0}^{t_1} d\vec{v} = \int_{t_0}^{t_1} \vec{a}(t) dt$$

$$\vec{v}(t_1) - \vec{v}(t_0) = \int_{t_0}^{t_1} \vec{a}(t) dt$$

$$t_1 \rightarrow t, \quad t \rightarrow t'$$

$$\vec{v}(t) = \vec{v}(t_0) + \int_{t_0}^t \vec{a}(t') dt'$$

PRIMJER 1 – HARMONIČKO TITRANJE

položaj čestice na x-osi:

$$x(t) = A \cos(\omega t)$$

$A, \omega \rightarrow \text{konstante}$

$$v(t) = ?, \quad a(t) = ?$$

$$x(t) = A \cdot \cos(\omega t + \Phi)$$

amplituda

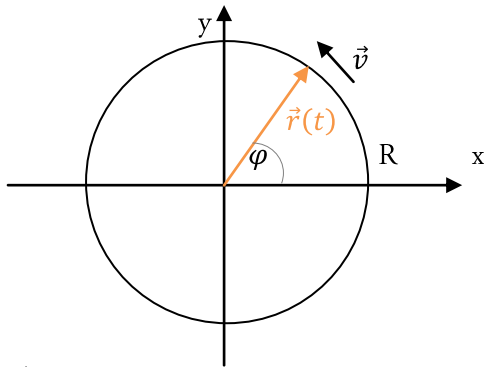
frekvencija

fazni pomak

$$v(t) = \frac{d}{dt} x(t) = \frac{d}{dt} (A \cos(\omega t + \Phi)) = -A\omega \cdot \sin(\omega t + \Phi)$$

$$a(t) = \frac{d}{dt} v(t) = \frac{d}{dt} (-A\omega \cdot \sin(\omega t + \Phi)) = -\omega^2 A \cdot \cos(\omega t + \Phi) \\ = -\omega^2 x(t)$$

PRIMJER 2 – GIBANJE PO KRUŽNICI POLUMJERA R BRZINOM STALNOG IZNOSA v



položaj:

$$\vec{r}(t) = R\cos(\varphi)\vec{i} + R\sin(\varphi)\vec{j}$$

φ – raste linearno u vremenu

$$\varphi = \omega t$$

$$\vec{r}(t) = R(\vec{i}\cos(\omega t) + \vec{j}\sin(\omega t))$$

$$\vec{v}(t) = R(\vec{i}(-\omega\sin(\omega t)) + \vec{j}(\omega\cos(\omega t))) = -\omega R(\vec{i}\sin(\omega t) - \vec{j}\cos(\omega t))$$

$$\vec{a}(t) = -\omega^2 R(\vec{i}\cos(\omega t) + \vec{j}\sin(\omega t)) = -\omega^2 \vec{r}(t)$$

$$\omega T = 2\pi$$

$$v = \frac{2R\pi}{T} = \frac{2R\pi}{\frac{2\pi}{\omega}} = \omega R \rightarrow \omega = \frac{v}{R}$$

$$\begin{aligned} |\vec{v}| &= \sqrt{\vec{v} \cdot \vec{v}} = \sqrt{[-\omega R(\vec{i}\sin(\omega t) - \vec{j}\cos(\omega t))] \cdot [-\omega R(\vec{i}\sin(\omega t) - \vec{j}\cos(\omega t))]} \\ &= \sqrt{(-\omega R)^2 \cdot (\vec{i}\sin(\omega t) - \vec{j}\cos(\omega t)) \cdot (\vec{i}\sin(\omega t) - \vec{j}\cos(\omega t))} \\ &= \sqrt{(-\omega R)^2 \cdot [(\vec{i} \cdot \vec{i})\sin^2(\omega t) - (\vec{i} \cdot \vec{j})\sin(\omega t)\cos(\omega t) - (\vec{j} \cdot \vec{i})\sin(\omega t)\cos(\omega t) + (\vec{j} \cdot \vec{j})\cos^2(\omega t)]} \\ &= \omega R \sqrt{\sin^2(\omega t) + \cos^2(\omega t)} = \omega R \quad \blacksquare \end{aligned}$$

EKSPERIMENT- SLOBODNI PAD

s/m	t/s			\bar{t}/s
0.2000	0.2019		0.2019	0.2019
0.8000	0.4037		0.4037	0.4037
1.8000	0.6062	0.6060	0.6066	0.6063

$$s(t) = At^2$$

$$A = \frac{\sum_{i=1}^N s_i t_i^2}{\sum_{i=1}^N t_i^3}$$

$$s(t) = A't^n$$

$$g = \bar{g} \pm \sigma_g \qquad \bar{g} = \frac{2\bar{s}}{t^2}$$

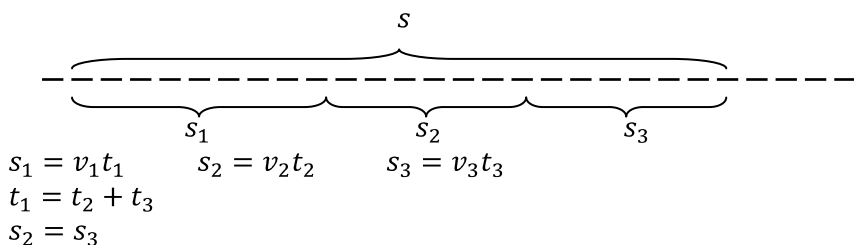
$$s = (1.8000 \pm 0.0005)$$

$$t = (0.6063 \pm 0.0001)$$

ZADATAK – HORVAT – 1.1

-pješač; pola vremena hoda $v_1=2$ km/h, pola preostalog puta trči 7 km/h, a drugu polovicu preostalog puta $v_3=5$ km/h. Izračunaj srednju brzinu gibanja tog pješača!

$$\bar{v} = ?$$



$$\bar{v} = \frac{s}{t} = \frac{s_1 + s_2 + s_3}{t_1 + t_2 + t_3}$$

$$t_2 = \frac{v_3 t_3}{v_2}$$

$$t_3 = \frac{v_2 t_2}{v_3}$$

$$t_2 + t_3 = \frac{v_3 t_3}{v_2} + \frac{v_2 t_2}{v_3}$$

$$t_3 = t_1 - t_2 \rightarrow t_2 + t_1 - t_2 = \frac{v_3(t_1 - t_2)}{v_2} + \frac{v_2 t_2}{v_3}$$

$$\left(1 - \frac{v_3}{v_2}\right) t_1 = \left(\frac{v_2}{v_3} - \frac{v_3}{v_2}\right) t_2 \quad / \cdot v_2 v_3 \quad (...)$$

$$t_3 = \frac{v_2}{v_2 + v_3} t_1$$

$$\bar{v} = \frac{s_1 + s_2 + s_3}{t_1 + t_2 + t_3} = \frac{v_1 t_1 + v_2 t_2 + v_3 t_3}{t_1 + t_2 + t_3} = \frac{v_1 t_1 + \frac{v_2 v_3 t_1}{v_2 + v_3} + \frac{v_2 v_3 t_1}{v_2 + v_3}}{2 t_1} = \frac{v_1}{2} + \frac{v_2 v_3}{v_2 + v_3} = 1 + \frac{35}{12} = \frac{47}{12}$$

ZADATAK – „ELEKTRIJADA“ – 1

Čestica se giba duž x-osi tako da joj se brzina mijenja kao $v(x) = \frac{A}{B}(1 + B(x))$ gdje su A i B konstante, a x je koordinata čestice. Odredi ubrzanje pri položaju $x = \frac{1}{B}$!

$$\begin{aligned}a(x) &= \frac{d}{dt} v(x) = \frac{d}{dt} v(x(t)) = \frac{dv}{dx} \frac{dx}{dt} = \left[\frac{d}{dx} \left(\frac{A}{B}(1 + B(x)) \right) \right] \left[\frac{A}{B}(1 + B(x)) \right] \\&= \frac{A}{B} B \frac{A}{B}(1 + Bx) = \frac{A^2}{B}(1 + Bx) \\a\left(\frac{1}{B}\right) &= \frac{A^2}{B} \left(1 + B \frac{1}{B}\right) = \frac{2A^2}{B}\end{aligned}$$

ZADATAK

Brzina čestice koja se giba duž x-osi je $v(x) = v_0 e^{-x/b}$. Pri tom su v_0 i b konstante. Odredi položaj kao funkciju vremena ako je poznato da je u početnom trenutku $t_0=0$, $x(t_0)=0$!

$$v = \frac{dx}{dt} = v_0 e^{-\left(\frac{x}{b}\right)} \quad / \cdot e^{\left(\frac{x}{b}\right)} dt$$

$$e^{\frac{x}{b}} dx = v_0 e^{-\left(\frac{x}{b}\right)} \quad \int_{"0"}^{"1"}$$

$$\int_{x_0}^{x_1} e^{\frac{x}{b}} dx = \int_{t_0}^{t_1} v_0 dt$$

$$b e^{\frac{x}{b}} \Big|_{x_0}^{x_1} = v_0 t \Big|_{t_0}^{t_1}$$

$$b \left(e^{\frac{x_1}{b}} - e^{\frac{x_0}{b}} \right) = v_0 (t_1 - t_0)$$

$$b \left(e^{\frac{x_1}{b}} - 1 \right) = v_0 t_1$$

konačno stanje „poopćujemo“

$$t_1 \rightarrow t, x_1 \rightarrow x(t)$$

$$b \left(e^{\frac{x(t)}{b}} - 1 \right) = v_0 t$$

$$e^{\frac{x(t)}{b}} = \frac{v_0 t}{b} + 1$$

$$x(t) = b \cdot \ln \left(\frac{v_0 t}{b} + 1 \right)$$

NEWTONOVI AKSIOMI

Čestica **m** – ima samo masu, nema ni oblik, ni dimenzije, ni orijentaciju

KOLIČINA GIBANJA

$$\vec{p} = m\vec{v}$$

masa

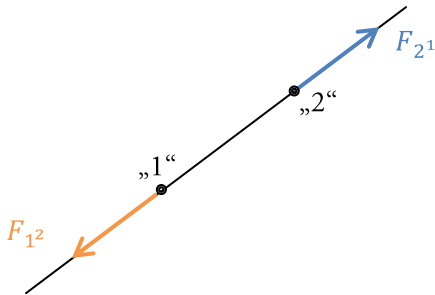
brzina

PRVI AKSIOM – Kad na česticu djeluje sila ona ostaje u stanju mirovanja ili jednolikog gibanja po pravcu
- vrijedi u inercijalnim sustavima

DRUGI AKSIOM – Vremenska promjena količine gibanja čestice je razmjerna sili koja na česticu djeluje

$$\frac{d\vec{p}}{dt} = \vec{F}$$

TREĆI AKSIOM – Ako tijelo/čestica djeluje na drugu česticu silom, tada druga čestica djeluje na prvu silom istog iznosa, ali suprotnog smjera. Te sile leže na istom pravcu (pravcu koji prolazi dvjema česticama).



NEWTONOVA JEDNADŽBA GIBANJA

$$\frac{d}{dt} \vec{p} = \frac{d}{dt} (m\vec{v}) = m \frac{d\vec{v}}{dt} = \mathbf{m}\vec{a} = \vec{F}$$

$$\vec{F}(\vec{r}, t) = \vec{F}_0 \rightarrow \text{konst.}$$

prvi korak: BRZINA

$$\frac{d\vec{p}}{dt} = \vec{F}_0 \rightarrow \frac{d\vec{v}}{dt} = \frac{\vec{F}_0}{m} \quad / \cdot dt$$

$$d\vec{v} = \frac{\vec{F}_0}{m} dt \quad \int_{po\check{c}}^{kon}$$

$$\int_{po\check{c}}^{kon} d\vec{v} = \int_{po\check{c}}^{kon} \frac{\vec{F}_0}{m} dt$$

$$\vec{v} \big|_{po\check{c}}^{kon} = \frac{\vec{F}_0}{m} t \big|_{po\check{c}}^{kon}$$

$$\vec{v}_{kon} - \vec{v}_{po\check{c}} = \frac{\vec{F}_0}{m} (t_{kon} - t_{po\check{c}})$$

$$t_{po\check{c}} \rightarrow t_0, \quad t_{kon} \rightarrow t$$

$$\vec{v}(t) - \vec{v}(t_0) = \frac{\vec{F}_0}{m} (t - t_0)$$

$$\vec{v}(t) = \frac{\vec{F}_0}{m} (t - t_0) + \vec{v}(t_0) \quad \rightarrow \text{početni uvjet}$$

drugi korak: POLOŽAJ

$$\frac{d\vec{r}}{dt} = \vec{v} \quad / \cdot dt$$

$$d\vec{r} = \vec{v} dt$$

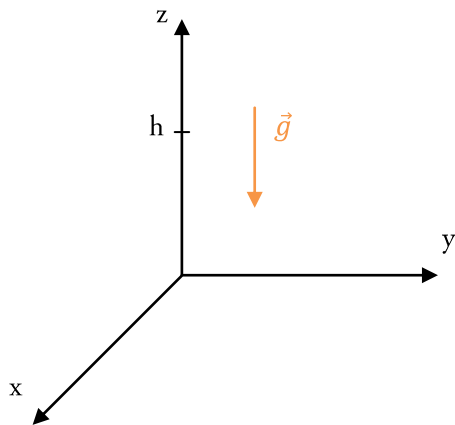
$$\int_{po\check{c}}^{kon} d\vec{r} = \int_{po\check{c}}^{kon} \vec{v} dt$$

$$\vec{r}(t_1) - \vec{r}(t_0) = \int_{t_0}^t \vec{v}(t') dt' = \int_{t_0}^t [\vec{v}(t_0) + \frac{\vec{F}_0}{m} (t' - t_0)] dt'$$

$$= \vec{v}(t_0)(t' - t_0) + \frac{\vec{F}_0}{2m} (t' - t_0)^2$$

$$\vec{r}(t) = \vec{r}(t_0) + \vec{v}(t_0)(t - t_0) + \frac{\vec{F}_0}{2m} (t - t_0)^2$$

PRIMJER – SLOBODNI PAD



sila $\vec{F}_0 = -mg\vec{k}$

početni uvjeti u $t=t_0=0$

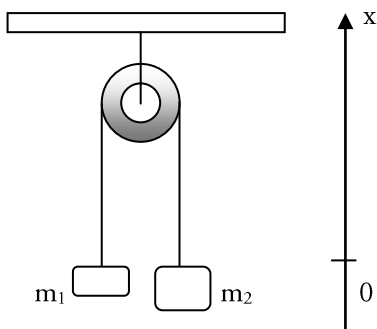
$$\vec{v}(t_0) = \vec{v}(0) = \vec{v}_0 = 0$$

$$\vec{r}(t_0) = \vec{r}_0 = h\vec{k}$$

$$\vec{v}(t) = -g\vec{k}t$$

$$\vec{r}(t) = (h - \frac{g}{2}t^2)\vec{k}$$

PRIMJER – PADOSTROJ



$$\vec{r}_1(t) = x_1(t)\vec{l}$$

$$\vec{r}_2(t) = x_2(t)\vec{l}$$

$$x_1(t) = -x_2(t)$$

$$\dot{x}_1(t) = -\dot{x}_2(t)$$

$$\ddot{x}_1(t) = -\ddot{x}_2(t)$$

JEDNADŽBA GIBANJA

$$m_1\ddot{x}_1 = T - m_1g$$

$$m_2\ddot{x}_2 = T - m_2g$$

napetost niti

$$m_1\ddot{x}_1 - m_2\ddot{x}_2 = (m_2 - m_1)g$$

$$\ddot{x}_1 = -\ddot{x}_2 = \frac{m_2 - m_1}{m_2 + m_1}g$$

ZADATAK – PADOSTROJ

$$m_1 = 400 \text{ g}$$

$$m_2 = 402 \text{ g}$$

iz mirovanja

$$t_1 - t_0 = 6.4 \text{ s}$$

$$x_1(t_1) - x_1(t_0) = 0.5 \text{ m}$$

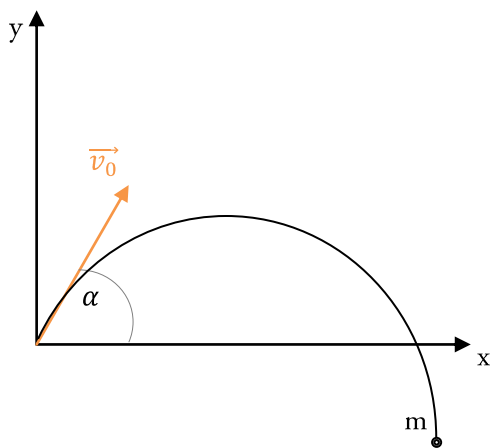
izračunaj g !

$$x_1(t_1) - x_1(t_0) = \frac{a_x}{2} (t_1 - t_0)^2$$

$$x_1(t_1) - x_1(t_0) = \frac{a_x}{2} (t_1 - t_0)^2$$

$$a_x = \frac{m_2 - m_1}{m_2 + m_1} g \rightarrow g = \frac{m_2 + m_1}{m_2 - m_1} \cdot \frac{2[x_1(t_1) - x_1(t_0)]}{(t_1 - t_0)^2} = \frac{400 + 402}{402 - 400} \cdot \frac{(2 \cdot 0.5)}{(6.4)^2} = 9.79 \frac{\text{m}}{\text{s}^2}$$

KOSI HITAC



početni uvjeti u $t=t_0=0$

$$\vec{v}(t_0) = \vec{v}(0) = \vec{v}_0 = v_0(\cos \alpha \vec{i} + \sin \alpha \vec{j})$$

$$\vec{r}(t_0) = \vec{r}(0) = \vec{r}_0 = 0$$

sila:

$$\vec{F}_0 = -mg\vec{j}$$

$$\vec{v}(t) = \frac{\vec{F}_0}{m} (t - t_0) + \vec{v}(t_0)$$

$$\vec{r}(t) = \vec{r}(t_0) + \vec{v}(t_0)(t - t_0) + \frac{\vec{F}_0}{2m} (t - t_0)^2$$

uvrstavanje:

$$\rightarrow \vec{v}(t) = v_0(\cos \alpha \vec{i} + \sin \alpha \vec{j}) - gt\vec{j}$$

$$\rightarrow \vec{r}(t) = v_0(\cos \alpha \vec{i} + \sin \alpha \vec{j})t - \frac{g}{2}t^2\vec{j}$$

po komponentama:

$$v_x(t) = v_0 \cos \alpha$$

$$v_y(t) = v_0 \sin \alpha - gt$$

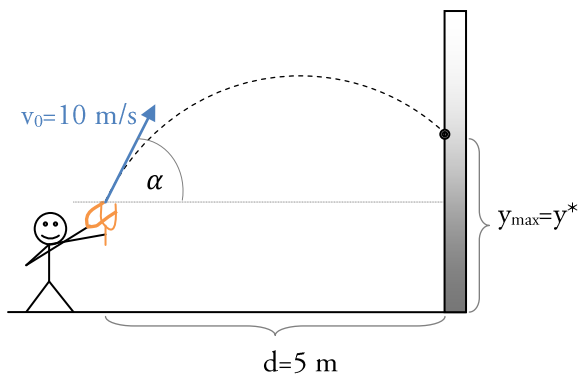
$$x(t) = v_0 \cos \alpha \cdot t$$

$$y(t) = v_0 \sin \alpha \cdot t - \frac{g}{2}t^2$$

$$y = v_0 \sin \alpha \frac{x}{v_0 \cos \alpha} - \frac{g}{2} \left(\frac{x}{v_0 \cos \alpha} \right)^2 = x \cdot \tan \alpha - \frac{g}{2 v_0^2 \cos^2 \alpha} x^2$$

$$y(x) = ux - \frac{gx^2}{2v_0^2} (1 + u^2) \quad \text{gdje je } u = \tan \alpha$$

ZADATAK – DJEČAK S PRAČKOM



Pod kojim kutem dječak treba iz pračke ispucati kamen brzinom 10 m/s ako stoji na 5 m od zida a da taj kamen pogodi što višu točku zida?

$$y(x) = ux - \frac{gx^2}{2v_0^2} (1 + u^2) \quad \text{gdje je } u = \tan \alpha$$

tražimo max funkcije y^*

$$0 = \frac{dy^*}{du} = \frac{d}{du} \left(ud - \frac{gd^2}{2v_0^2} (1 + u^2) \right) = d - \frac{gd^2}{2v_0^2} 2u = d - \frac{gd^2}{v_0^2} u$$

$$\rightarrow u = \frac{v_0^2}{gd} = \frac{100}{9.81 \cdot 5} = \frac{20}{9.81} = 2.038$$

$$\arctan u = 63.87^\circ$$

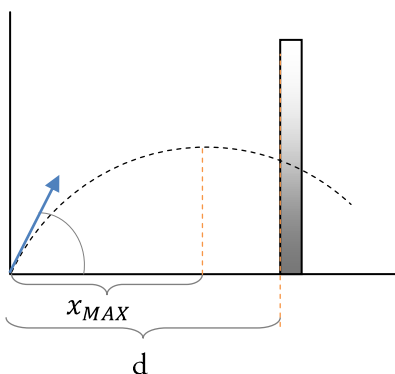
tražimo tjeme parabole

$$y(x) = u^*x - \frac{gx^2}{2v_0^2} (1 + (u^*)^2) = \frac{v_0^2}{gd}x - \frac{gx^2}{2v_0^2} \left(1 + \frac{v_0^4}{g^2d^2} \right) = \frac{v_0^2}{gd}x - \frac{gx^2}{2v_0^2} - \frac{v_0^2gx^2}{2g^2d^2} \quad y = ax^2 + bx + c$$

$$x_{MAX} = -\frac{b}{2a} \rightarrow \text{tjeme parabole} = \frac{\frac{v_0^2}{gd}}{2 \left(\frac{g}{2v_0^2} + \frac{v_0^2}{2gd^2} \right)} = \frac{\frac{v_0^2}{gd}}{\frac{2v_0^2}{gd} \left(\frac{g^2d}{2v_0^4} + \frac{1}{2d} \right)} = \frac{1}{2 \left(\frac{g^2d}{2v_0^4} + \frac{1}{2d} \right)} = \frac{1}{\frac{g^2d}{v_0^4} + \frac{1}{d}}$$

$$= \frac{d}{1 + \frac{g^2d^2}{v_0^4}}$$

$x_{MAX} < d$ a to je ono što smo dokazivali, da će kamen dosegnuti najvišu točku zida ako mu je tjeme parabole po kojoj leti ispred zida ■



RJEŠAVANJE NEWTONOVE JEDNADŽBE GIBANJA ZA SILU RAZMJERNU BRZINI

$$\vec{F} = -\gamma \vec{v} \rightarrow \text{brzina}$$

\downarrow sila \searrow konst.

uvrštavanje:

$$\frac{d\vec{p}}{dt} = \vec{F}$$

$$m \cdot \dot{\vec{v}} = -\gamma \vec{v}$$

x komponenta –

$$m \cdot \dot{v}_x = -\gamma v_x$$

$$m \frac{dv_x}{dt} = -\gamma v_x \quad / \cdot \frac{dt}{mv_x}$$

$$\frac{dv_x}{v_x} = -\frac{\gamma}{m} \int_{poč}^{kon} dt$$

$$\ln v_x(kon) - \ln v_x(poč) = -\frac{\gamma}{m} (t(kon) - t(poč))$$

\downarrow $v(t)$ \downarrow $v(t_0)$ \downarrow t \downarrow t_0

$$v_x(t) = v_x(t_0) \cdot e^{-\frac{\gamma}{m}(t-t_0)}$$

zaključno sa predavanjem 08.03.'10.