

1.) Ekspanzija po Shannonovom teoremu: varijabli x dodeli:

$$f(x+y) + f(xy) = f(x) + f(y)$$

$$x \cdot [f(1+y) + f(y)] + x' \cdot [f(y) + f(0)] =$$

(pozitivni faktor, umesto $x \rightarrow 1$; umesto $\bar{x} \rightarrow 0$ negativni faktor)

$$= x \cdot f(1) + x \cdot f(y) + x' \cdot f(y) + x' \cdot f(0) =$$

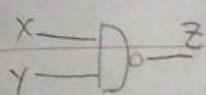
$$= \underbrace{x \cdot f(1) + x' \cdot f(0)}_{f(x)} + \underbrace{x \cdot f(y) + x' \cdot f(y)}_{f(y)} =$$

$$= f(x) + f(y)$$

← Shannon

► Birc: b, b, a, b, b, b, a, b, a, b

► NI (NAND) $NI(x, y) = ite(x, y', 1)$



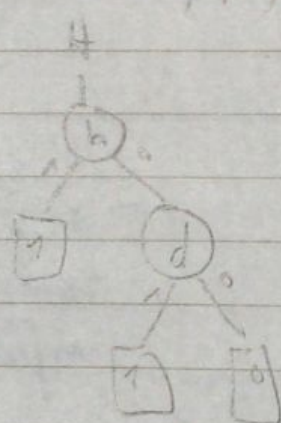
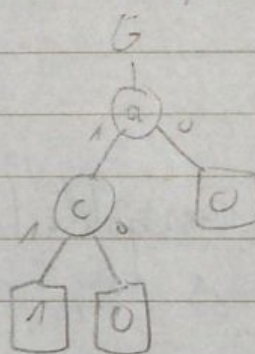
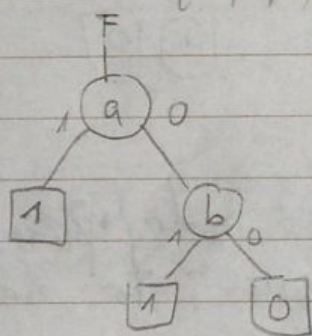
x	y	z
0	0	1
0	1	1
1	0	1
1	1	0

$\left. \begin{matrix} 0 & 0 & 1 \\ 0 & 1 & 1 \end{matrix} \right\} x=0$
 $\left. \begin{matrix} 1 & 0 & 1 \\ 1 & 1 & 0 \end{matrix} \right\} x=1$

2.) $F = a + b$ $G = ac$ $H = b + d$

a) Nacrtaj BOD-ove za svaki od ovih funkcija

$$F = a + b = ite(a, 1, b) \quad G = ac = ite(a, c, 0) \quad H = b + d = ite(b, 1, d)$$

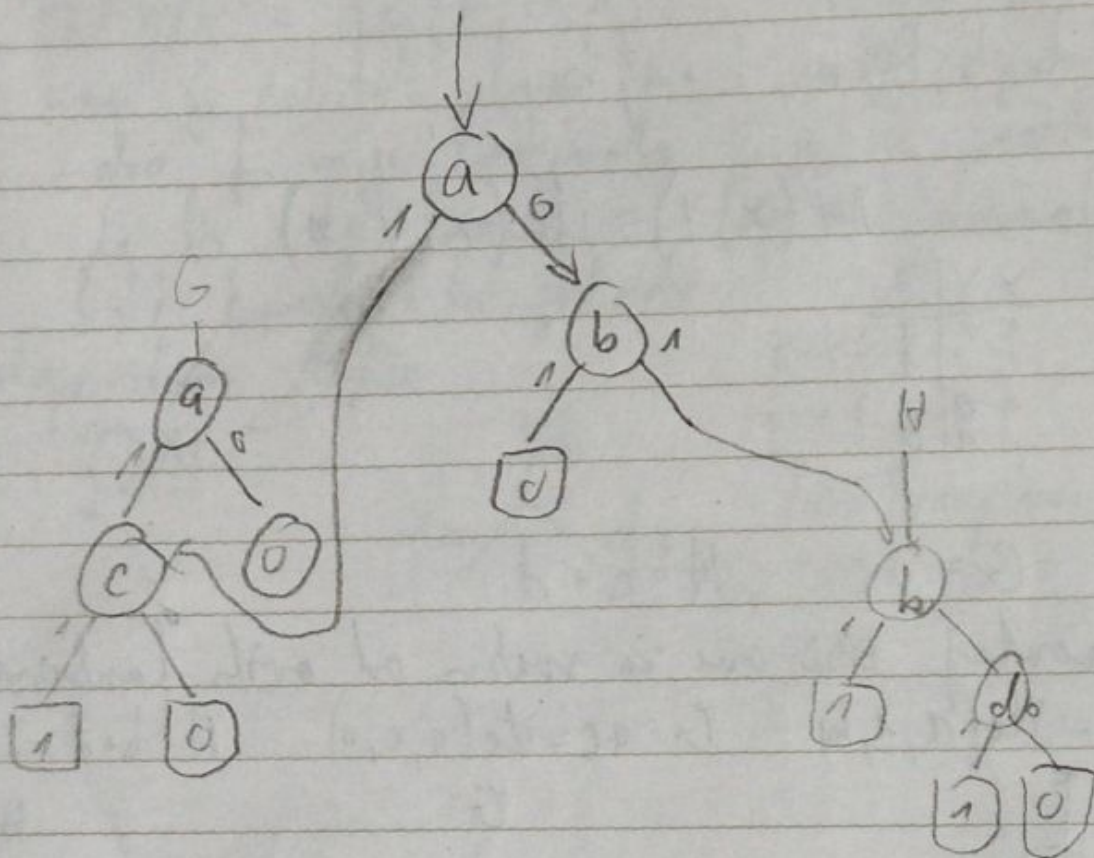
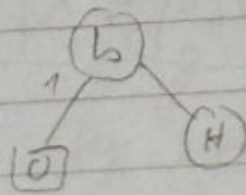


ne moramo spaziti jedinica
i nule, to se pretpostavlja

b) Transformuj $\text{ite}(F, G, H)$; načrtuj BDD diagram
redoslijed: a, b, c, d

$$\text{ite}(F, G, H) = [a, \underset{\substack{\downarrow \\ \text{pozitivni faktor} }}{\text{ite}(F_a, G_a, H_a)}, \underset{\substack{\downarrow \\ \text{negativni faktor} }}{\text{ite}(F_{a'}, G_{a'}, H_{a'})}] =$$

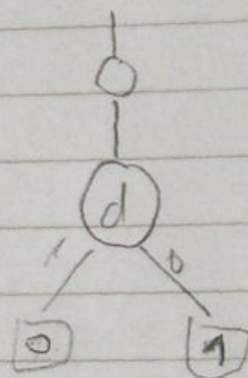
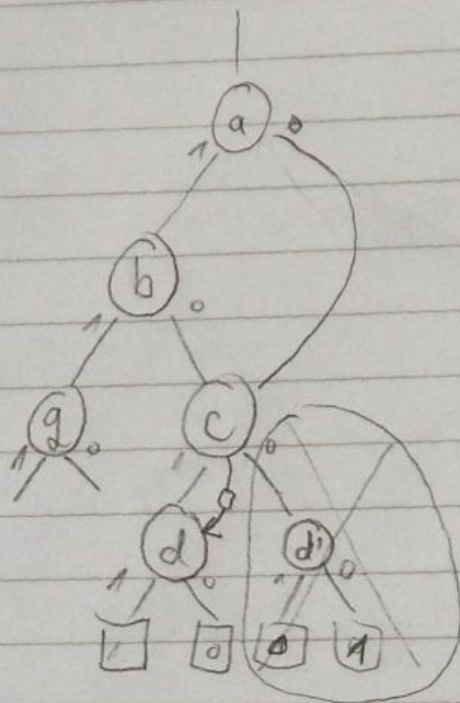
$$= [\underbrace{a, \text{ite}(\underbrace{(1+b)}_1, c, H)}_c, \text{ite}(b, a, H)] =$$



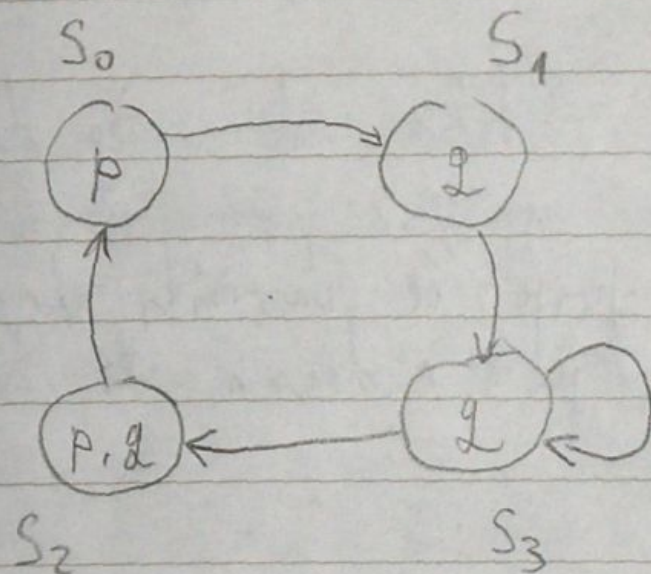
- a je vrna varijabla (odredeno redoslijedom)
- razvija se samo s H , moći smo i to dalje riješiti

2. Neka je rezultat iz $(F, G, H) = (a, \underbrace{(b, q, (c, d, d'))}_{\text{za } q=1}, \underbrace{(c, d, d')}_{\text{za } q=0})$

Nacrtaj ROBDD upotrijebivši komplement na izborima.



- d i d' potpuno različite funkcije, ne ih mogu biti
- za $c=0$, kraj komplementa imamo obrnuto;
onda to sporedimo na d (umjesto d')



Najdi sva stanja za koja
vrijedi $EG q$

$$Q[EG q] = ?$$

$$Q[q] = \{s_1, s_2, s_3\}$$

$$Q[EG q] = Q[q] \cap R^{-1}[Q[EG q]]$$

$$R^{-1}[Q[q]] = R^{-1}\{s_1, s_2, s_3\} = \{s_0, s_1, s_3\}$$

gledano iz krajnjeg stanja
morimo doći u s_1, s_2 ili s_3

$$Z_1 = \{s_1, s_2, s_3\} \cap \{s_0, s_1, s_3\} = \{s_1, s_3\}$$

$$R^{-1}\{s_1, s_3\} = \{s_0, s_1, s_3\}$$

$$Z_2 = \{s_1, s_2, s_3\} \cap \{s_0, s_1, s_3\} = \{s_1, s_3\}$$

Stanja s_1 i s_3 zadovoljavaju $Q[EG q]$