

Z-1 nacrtati i proračunati zaštitu

VDR

$$U = 500 \cdot I^{0,032} \text{ [V]}$$

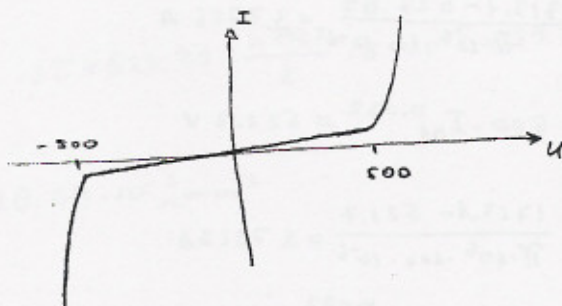
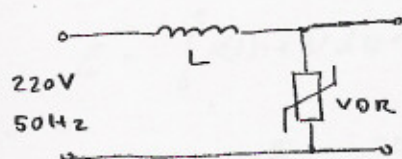
$$U = 1800 \cdot \sin(\pi \cdot 10^6 t) \cdot \exp(-10^5 t) \text{ [V]}$$

a) prenapon na uređaju = ?

b) Volumen VDR = ?

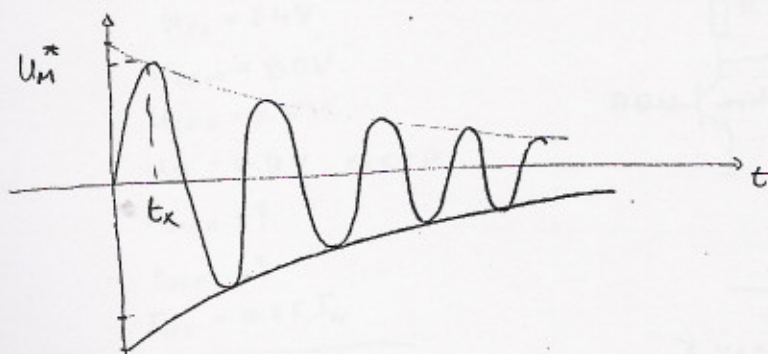
$$L = 100 \mu\text{H}$$

$$A = 1000 \text{ W/s/cm}^3$$



$$X_L = \omega L$$

↳ predstavlja veliku impedanciju za visoke frekvencije i zbog toga ograničava ulaznu struju kod prenapona



a) najviši napon U_n^* (najveći ulazni prenapon)

$$\frac{du}{dt} \equiv 0 \quad u = U_n \sin \omega t \cdot e^{-t/\tau}$$

$$\omega = 2\pi f = \pi \cdot 10^6 \Rightarrow f = 500 \text{ kHz}$$

$$\tau = 10^{-5}$$

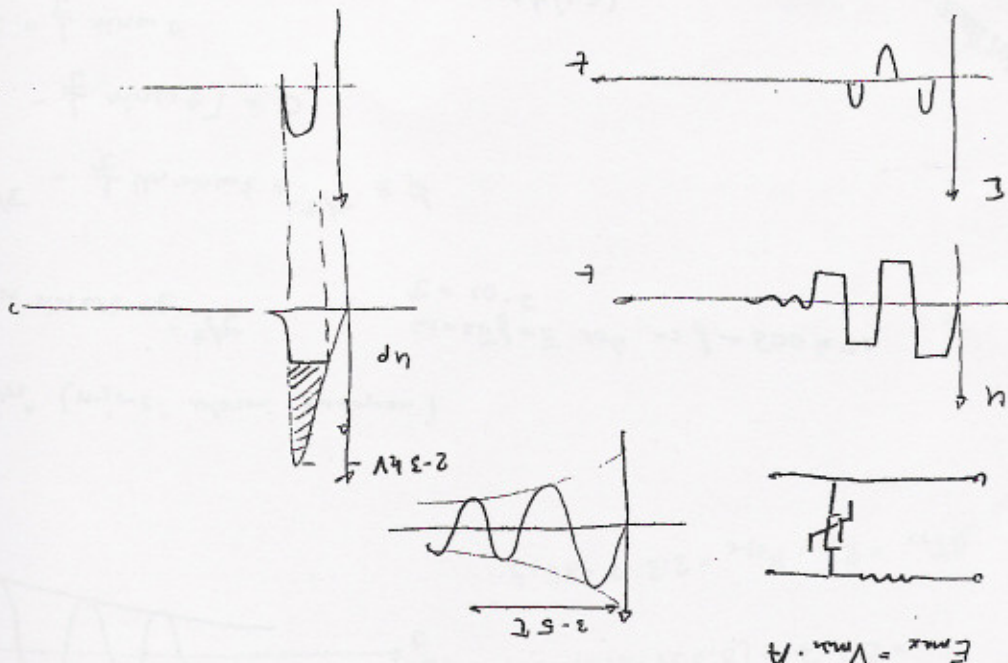
$$\frac{du}{dt} = U_n \omega \cos \omega t \cdot e^{-t/\tau} - \frac{1}{\tau} U_n \sin \omega t \cdot e^{-t/\tau} \equiv 0$$

$$U_n e^{-t/\tau} \left[\omega \cos \omega t - \frac{1}{\tau} \sin \omega t \right] = 0$$

$$\omega \cos \omega t = \frac{1}{\tau} \sin \omega t$$

$$\tan \omega t_x = \omega \tau = \pi \cdot 10^6 \cdot 10^{-5} \Rightarrow t_x = \frac{\arctan(10\pi)}{\pi \cdot 10^6} = 489.87 \text{ ns}$$

Samo je jedan Meš Potrdi!



možemo znati energiju koju apsorbuje VDR

b) $V_{min} = ?$

$$= u_{izmereno} \quad U_p = 524.79V$$

$$U_{p2} = 500 \cdot I_{m2}^{0.032} = 524.79V$$

$$3) I_{m1} = \frac{1713.4 - 521.7}{\frac{11 \cdot 10^6 \cdot 100 \cdot 10^{-6}}{2}} = 3.7925A$$

$$U_{p1} = 500 \cdot I_{m1}^{0.032} = 524.7V$$

$$2) I_{m1} = \frac{1713.4 - 527.89}{\frac{11 \cdot 10^6 \cdot 100 \cdot 10^{-6}}{2}} = 3.7726A$$

$$U_{p0} = 500 \cdot I_{m0}^{0.032} = 527.89V$$

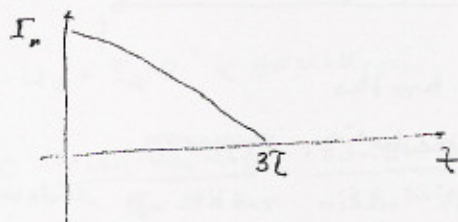
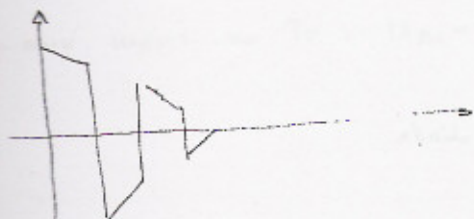
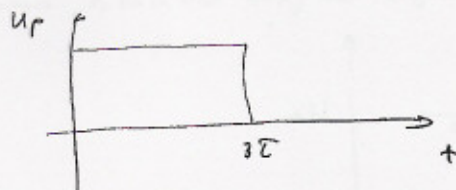
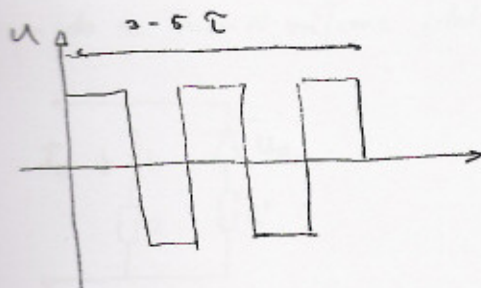
$$1) I_{m0} = \frac{U_{p0} - U_p}{\frac{11 \cdot 10^6 \cdot 100 \cdot 10^{-6}}{2}} = 5.453A$$

Računamo napin na VDR-u za najgori slučaj U_H^* (iterativnim postupkom)

$$\rightarrow \text{možemo za } t_{max} \approx \frac{1}{f} \rightarrow U_H^* = 1712.2V$$

$$U_H^* = 1713.1V$$

$$U_H^* = 1800 \cdot \ln(\pi \cdot 10^6 \cdot 483.87 \cdot 10^{-3}) \cdot \exp(-10^5 \cdot 489.87 \cdot 10^{-9})$$



uzet ćemo 3τ

$$E = \int_0^t u(t) \cdot i(t) dt = U_P \cdot \frac{I_P}{2} \cdot 3\tau = 521.75 \cdot \frac{3.7923}{2} \cdot 3 \cdot 10^{-5} = 29.68 \text{ mJ}$$

$$V_{\min} = \frac{E}{A} = \frac{29.68 \cdot 10^{-3}}{10^3} = 29.68 \cdot 10^{-3} \text{ mm}^2$$

Z-2

bipolarno sklopka

$$R = 300 \Omega$$

$$L = 10 \text{ mH}$$

$$U_{CC} = 24 \text{ V}$$

$$U_{CEM} = 30 \text{ V}$$

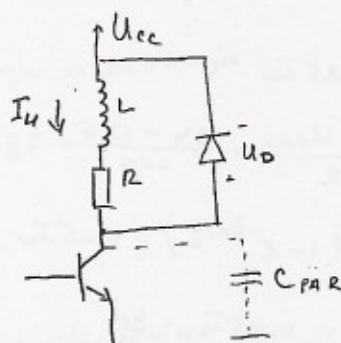
$$U_{CES} = 0.5 \text{ V}$$

$$U_D = 0.8 \text{ V}, r_D \ll R$$

$$R_{\max} = ?$$

$$t_{\text{OFF}} = ?$$

$$I_{\text{OFF}} = 0.25 I_H$$

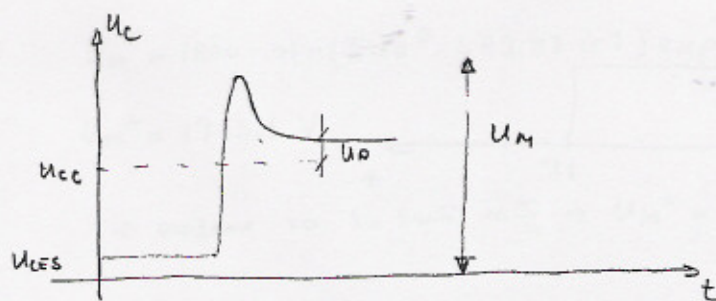


- isključujemo tranzistor
- otpor u zatvara prema masi preko C_{PAR} → paraziti kondenzator

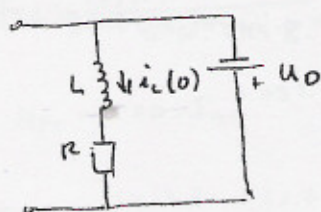
$$E_{ZAV} = \frac{L I_H^2}{2} = \frac{C U_H^2}{2} \Rightarrow U_H = \sqrt{\frac{L \cdot I_H^2}{C_{PAR}}}$$

- jako poraste napon na kondenzatoru (100 - 1000 V)

Samo je jedan Mali Ivica!



- ovo ove traje kratko
- kritičan je, nestabilan, prenos
- najjednostavniji način zaštite je dodavanje diode
- nade je : $U_M = U_{CE} + U_O = 24.8V$



$$i_L(t) = i_L(0) e^{-t/\tau} - \frac{U_O}{R} (1 - e^{-t/\tau})$$

$$\tau = \frac{L}{R} = \frac{10mH}{300} = 33.3\mu s$$

$$i_L(0) = I_L$$

$I_{eff} = 0.25 I_L \rightarrow$ otpuštanje radnog kontakta

$$t_x = ? \text{ za } i_L(t) = 0.25 I_L$$

$$I_L = \frac{U_{CE} - U_{CES}}{R} = \frac{24 - 0.5}{300} = 78.33mA$$

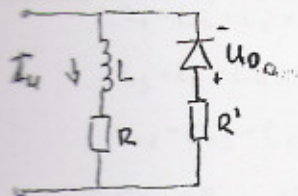
$$I_L e^{-t_x/\tau} - \frac{U_O}{R} (1 - e^{-t_x/\tau}) = 0.25 I_L$$

$$(I_L + \frac{U_O}{R}) e^{-t_x/\tau} = 0.25 I_L + \frac{U_O}{R}$$

$$e^{-t_x/\tau} = \frac{0.25 I_L + \frac{U_O}{R}}{I_L + \frac{U_O}{R}} = \frac{U_O + 0.25 I_L \cdot R}{U_O + I_L \cdot R} \quad / \ln$$

$$t_x = -\tau \ln \frac{U_O + I_L \cdot R \cdot 0.25}{U_O + I_L \cdot R} = -33.3 \cdot \ln \frac{0.8 + 78.33 \cdot 0.3 \cdot 0.25}{0.8 + 78.33 \cdot 0.3} = 43.03\mu s$$

- da se smanji vrijeme isključivanja, stavimo serijski otpor



- max. napon na Tr: $U_M = U_{CE} + U_D + I_A \cdot R' < 80V = U_{CEM}$

$$R' < \frac{U_{CEM} - U_{CE} - U_D}{I_N} = \frac{80 - 24 - 0.8}{78.33 \cdot 10^{-3}} = 704.7 \Omega$$

- efektivno imamo $R'' = R + R' = 300 + 704.7 = 1004.7 \Omega$, $\tau = \frac{L}{R''} = \frac{10mH}{1004.7} = 9.953 \mu s$

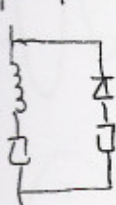
$$t_x' = -\tau \ln \frac{U_D + I_L \cdot R'' \cdot 0.25}{U_D + I_L \cdot R''} = -9.953 \ln \frac{0.8 + 78.33 \cdot 1.0047 \cdot 0.25}{0.8 + 78.33 \cdot 1.0047}$$

$$t_x' = 13.51 \mu s$$

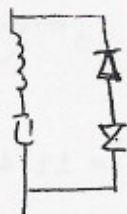
$$\Delta t_x = t_x - t_x' = 29.52 \mu s$$

→ Ovo je relativno loš način smanjenja otpođivanja

- bolji primjeri zaštite

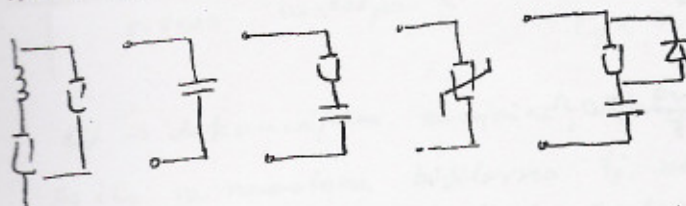


=>



$$U_M = U_{CE} + U_D + U_Z$$

AC i DC



Samo je jedan Mali Ivica!

Z-3

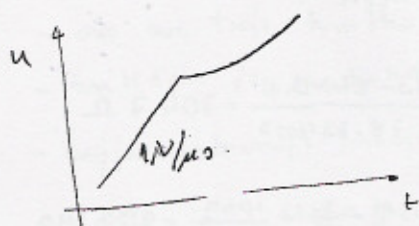
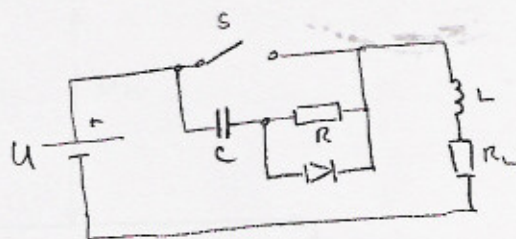
$$R_L = 100 \Omega$$

$$L = 1 \text{ H}$$

$$U = 100 \text{ V}$$

$$I_{KM} = 5 \text{ A}$$

RCD



treba sprečiti:

- lučni izboj
- fuzijski izboj

1) zaštita od lučnog izboja

$$\frac{dU}{dt} = \frac{I_0}{C} < 1 \text{ V}/\mu\text{s}$$

$$i = C \frac{dU}{dt}$$

$$I_0 = \frac{U}{R_L} = \frac{100}{100} = 1 \text{ A}$$

$$C > \frac{1 \text{ A}}{1 \text{ V}/\mu\text{s}} = 1 \mu\text{F}$$

2) zaštita od fuzijskog izboja

$$U_{\max} < 300 \text{ V}$$

$$\frac{1}{2} L I_0^2 = \frac{1}{2} C U_{\max}^2$$

$$C = \frac{L I_0^2}{U_{\max}^2} \Rightarrow C > \frac{L I_0^2}{U_{\max}^2} = 1 \cdot \left(\frac{1}{300}\right)^2 = 11.11 \mu\text{F}$$

3) otpornik bismo tako da ograničimo tuju proizvodnju kondenzatora

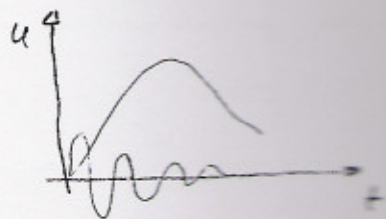
$$I < I_{KM}$$

$$I_{KM} = \frac{U}{R} \Rightarrow R_{\min} = \frac{U}{I_{KM}} = \frac{100}{5} = 20 \Omega$$

4) Neje toliko naisto, da bilo bi dobro da bude

$$C > 4 \frac{L}{R_L^2} = 4 \cdot \frac{1}{100^2} = 400 \mu\text{F}$$

za sprečavanje isključivanja



Samo je jedan Mači Janki

7-4 LC zaštitu (šest stupnjeva)

$$L_1 = L_2 = L_i = 27 \text{ mH}$$

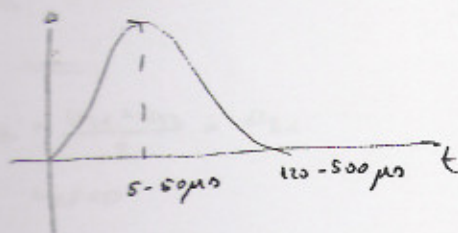
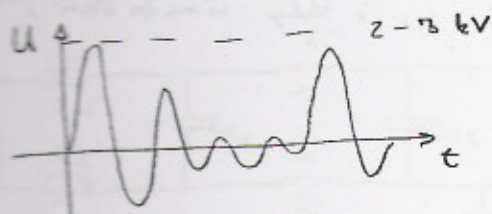
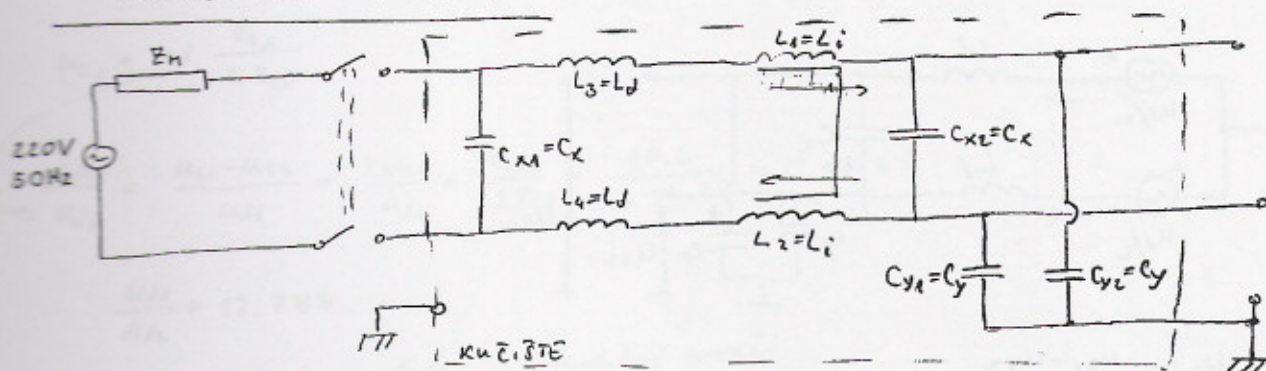
$$L_3 = L_4 = L_d = 100 \mu\text{H}$$

$$C_{x1} = C_{x2} = C_x = 100 \text{ nF}$$

$$C_{y1} = C_{y2} = C_y = 2.2 \text{ nF}$$

za snage: 10 - 100 tinjaka W

- potišćenje istofaznih i diferencijalnih smetnji nastalih izvana u mreži
- potišćenje istofaznih smetnji nastalih u uređaju



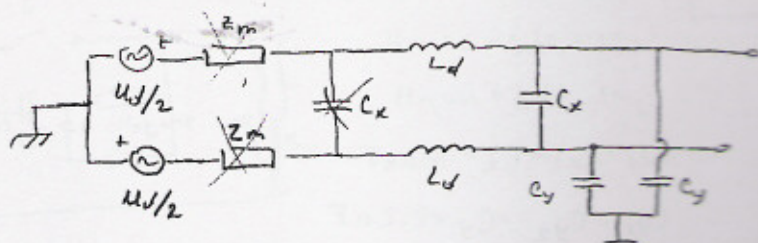
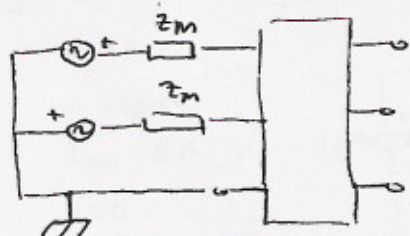
Sklop za $f = 150 \text{ kHz} \div 300 \text{ MHz}$
predstavlja visoku impedanciju na
priključuje prenapone i smetnje na ulazu.
 C_y su posebno bitni za sigurnost jer
ako nepravilno kratki spoj, onda olakšano
dovedu kućište na mrežni napon.

$$C_y < 7.2 \text{ nF}$$

L_d -> diferencijalna zavojnica, djeluje na diferencijalne smetnje
 L_1 i L_2 su namotane bifilarno tj. na isti jezgri i zato se
magnetna polja koja se javljaju uvek otkuče poništavaju

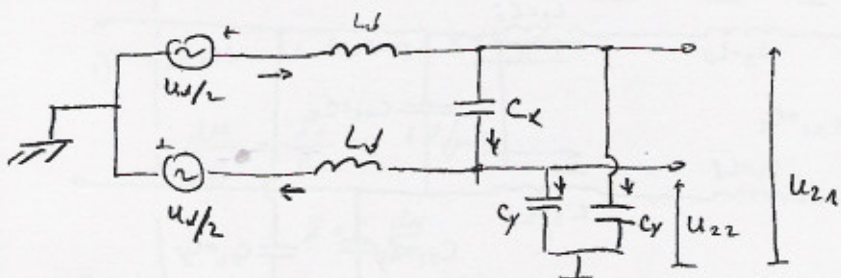
Samo je jedan Mali Ivica!

a) diferencijalne smetnje nastale izvan uređaja



Z_M - impedancija mreže \rightarrow teško ju je modelirati pa nećemo puno pogriješiti i ako je ne uzamemo u razmatranje

C_x na ulazu sad ne utiče na razmatranje (jer je napon direktno na ulazu)



$$U_{2d} = U_{21} - U_{22}$$

$$U_{2i} = \frac{U_{21} + U_{22}}{2}, \quad U_{21} = -U_{22} \rightarrow U_{2i} = 0 \quad (\text{jer je sklop simetričan})$$

$$\frac{U_d}{2} = U$$

$$\frac{U - U_{21}}{Z_{Ld}} = \frac{U_{21} - U_{22}}{Z_{Cx}} + \frac{U_{21}}{Z_{Cy}}$$

$$\frac{U_{21} - U_{22}}{Z_{Cx}} = \frac{U_{22} + U}{Z_{Ld}} + \frac{U_{22}}{Z_{Cy}}$$

$$U_{21} = -U_{22} \rightarrow U_{2d} = 2U_{21}$$

$$\frac{U - U_{21}}{Z_{Ld}} = \frac{2U_{21}}{Z_{Cx}} + \frac{U_{21}}{Z_{Cy}}$$

$$\frac{U - U_{21}}{Z_{Ld}} = \frac{U_{21}(2Z_{Cy} + Z_{Cx})}{Z_{Cx}Z_{Cy}} \quad / \cdot Z_{Cx}Z_{Cy} \cdot Z_{Ld}$$

$$Z_{Cx}Z_{Cy} \cdot U - Z_{Cx}Z_{Cy} \cdot U_{21} = Z_{Ld}(2Z_{Cy} + Z_{Cx}) \cdot U_{21}$$

$$Z_{Cx}Z_{Cy}U = U_{21}[Z_{Ld}(2Z_{Cy} + Z_{Cx}) + Z_{Cx}Z_{Cy}]$$

$$\frac{U}{Z_{Ld}} = U_{21} \left[\underbrace{\left(\frac{1}{Z_{Cx}} + \frac{1}{Z_{Cy}} + \frac{1}{Z_{Ld}} \right)}_{\frac{1}{Z_p}} \cdot \frac{1}{Z_{Cx}} \right]$$

$$\frac{1}{Z_p} = \frac{1}{Z_{Cx}}$$

$$Z_p = Z_{Cx}$$

$$f = 150 \text{ kHz}$$

$$|Z_{cx}| = \frac{1}{2\pi f C_x} = 10.6 \Omega$$

$$|Z_{cy}| = \frac{1}{2\pi f C_y} = 482.3 \Omega$$

$$|Z_{Ld}| = 2\pi f L_d = 94.25 \Omega$$

$$u_{21} = u \frac{-Z_{cx} Z_{cy}}{2 Z_{cy} Z_{Ld} + Z_{Ld} Z_{cx} + Z_{cx} Z_{cy}}$$

$$u_{21} = u \frac{Z_{cx}}{2 Z_{Ld} + \frac{Z_{Ld} Z_{cx}}{Z_{cy}} + Z_{cx}} \approx u \frac{Z_{cx}}{2 Z_{Ld}}$$

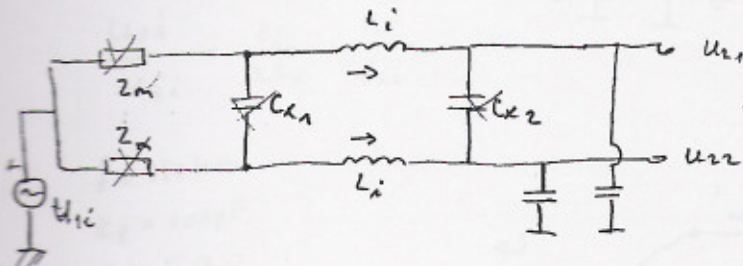
$$u = \frac{u_d}{2}$$

$$u_{21} = u_d \frac{Z_{cx}}{4 Z_{Ld}}$$

$$\frac{u_{d2}}{u_{d1}} = \frac{u_{21} - u_{22}}{u_{d1}} = \frac{2 u_{21}}{u_{d1}} = \frac{Z_{cx}}{2 Z_{Ld}} = \frac{10.6}{2 \cdot 94.25} = 0.0562$$

$$\frac{u_{d1}}{u_{d2}} = 17.783$$

b) izotofazne ometnje nastale u gravitacijskoj mreži



potpuna simetrija - zamjenjivamo Cex

$$u_{21} = u_{22}$$

$$Z_{Li} = 2\pi f L_i = 25446.9 \Omega$$

$$u_{di} = \frac{u_{21} + u_{22}}{2} = u_{21}$$

$$u_{d2} = 0$$

$$\frac{u_{di} - u_{21}}{Z_{Li}} = \frac{u_{21}}{Z_{cy}}$$

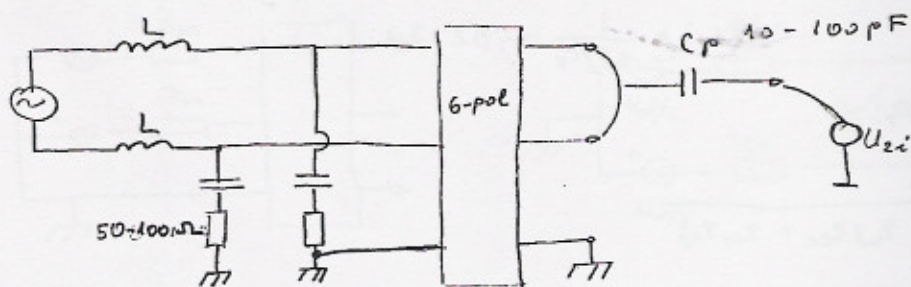
$$u_{di} \cdot Z_{cy} = u_{21} Z_{cy} = u_{21} \cdot Z_{Li}$$

$$u_{di} = u_{21} \frac{Z_{Li} + Z_{cy}}{Z_{cy}}$$

$$\frac{u_{21}}{u_{di}} = \frac{Z_{cy}}{Z_{Li} + Z_{cy}} = \frac{482.3}{25446.9 + 482.3} = 0.0186 \Rightarrow \frac{u_{di}}{u_{21}} = 53.76 \Rightarrow 34.6 \text{ dB}$$

Samo je jedan Mali Ivica!

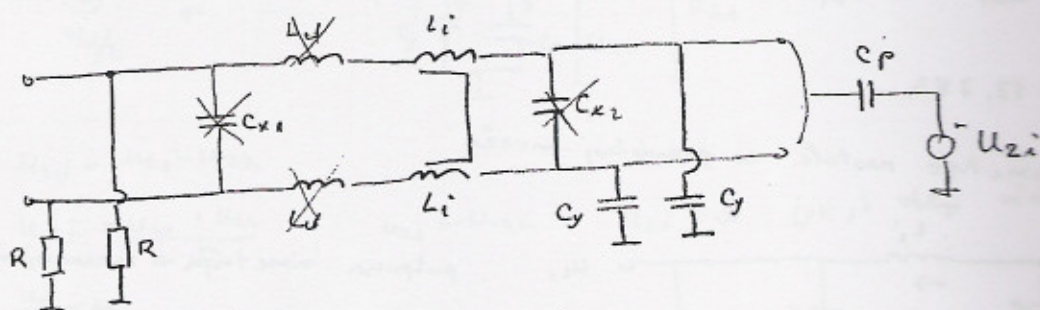
c) istofazne smetnje nastale unutar mrežaja



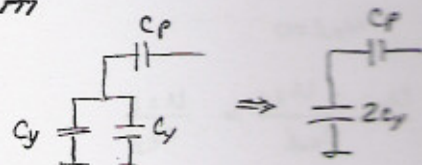
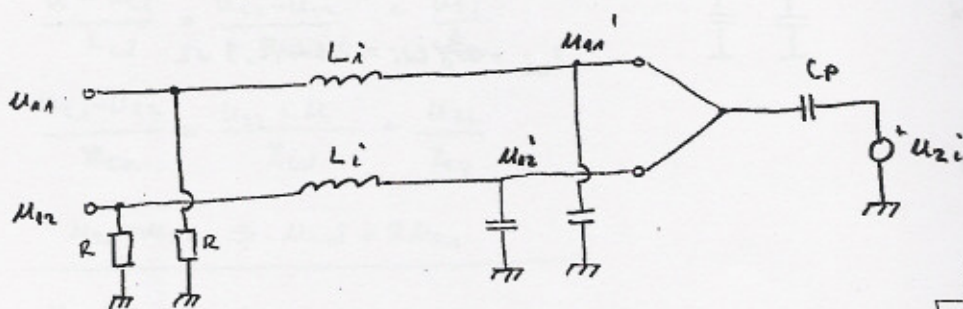
- dodaju se C-ovi koji imaju impedancije takve da u radu ne utiču, a L-ovi predstavljaju visoku impedanciju da smetnje ne bi ušle u mrežu

$$C \gg \frac{1}{2\pi f_c R}, \quad f_c \gg 150 \text{ kHz}$$

$$2\pi f_c L \gg R, \quad f_c \gg 150 \text{ kHz}$$



$$L_d \ll L_i$$



$$f = 150 \text{ kHz}$$

$$|Z_{cy}| = 482.3 \Omega$$

$$|Z_{Li}| = 25.4 \text{ k}\Omega$$

$|Z_{Li}| \gg |Z_{Cy}| \rightarrow$ promatramo kapacitivno dijelo odvajano

$$U_{Ai} = U_{Zi} \frac{Z_{Cy}}{Z_{Cp} + Z_{Cy}} = U_{Zi} \frac{\frac{1}{\omega C_{Cy}}}{\frac{1}{\omega C_p} + \frac{1}{\omega C_{Cy}}} = U_{Zi} \frac{\frac{1}{Z_{Cy}}}{\frac{1}{Z_{Cp}} + \frac{1}{Z_{Cy}}} = U_{Zi} \frac{C_p}{Z_{Cp} + C_y}$$

$$C_p \ll C_y \quad 2.2 \text{ nF} \\ 500 - 100 \text{ pF}$$

- sad promatramo ulaz

$$\frac{U_{Ai} - U_{Aa}}{Z_{Li}} = \frac{U_{ii}}{R}$$

$$U_{Ai} R = U_{Aa} (Z_{Li} + R)$$

$$U_{Aa} = U_{Ai} \frac{R}{R + Z_{Li}}$$

$$U_{ii} = U_{Ai} \cdot \frac{R}{Z_{Li}}$$

$$U_{ii} = U_{Zi} \frac{C_p}{Z_{Cy}} \cdot \frac{R}{Z_{Li}}$$

$$U_{ii} = U_{Ai}$$

$$\frac{U_{Ai}}{U_{Zi}} = \frac{C_p}{Z_{Cy}} \cdot \frac{R}{Z_{Li}}$$

$$f = 150 \text{ kHz}$$

$$C_p = 100 \text{ pF}$$

$$R = 50 \Omega$$

$$\left| \frac{U_{Ai}}{U_{Zi}} \right| = \frac{0.11}{2 \cdot 2.2} \cdot \frac{50}{2\pi \cdot 150 \cdot 10^3 \cdot 2.2 \cdot 10^{-3}} = 4.465 \cdot 10^{-5} \Rightarrow 87 \text{ dB}$$

Samo je jedan Mali Ivica!

54

$$l = 10 \text{ m}$$

$$U = 220 \text{ V} / 50 \text{ Hz}$$

$$D = 1 \text{ cm}$$

$$d = 2 \text{ mm}$$

$$U_{om} = ?$$

a) $R \rightarrow \infty$

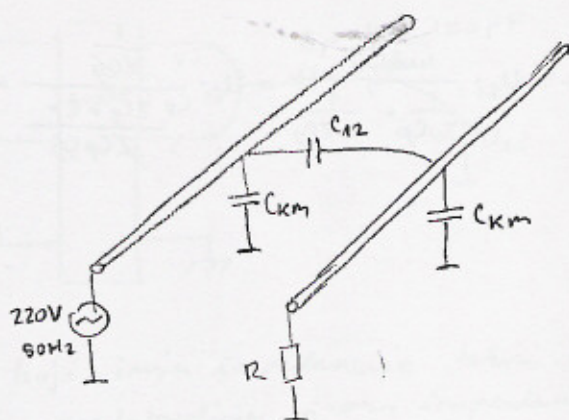
b) $R = 50 \Omega$

$$C_{km} = 2000 \text{ pF}$$

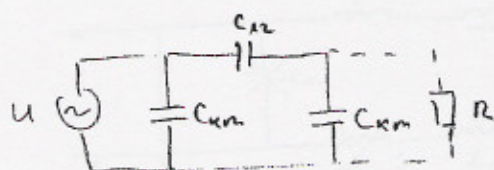
b) odlopljeni kabel

$$C_{12} = 200 \text{ pF/m}$$

$$C_{12}' = 2 \text{ pF}$$



$$C_{12} = \frac{\pi \epsilon l}{\ln(2 \frac{D}{d})} = \frac{\pi \cdot 8.8542 \cdot 10^{-12} \cdot 10}{\ln(2 \frac{10}{2})} = 120.8 \text{ pF}$$



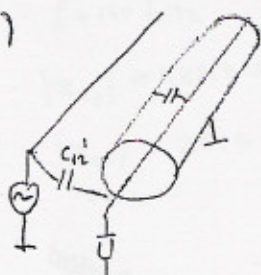
a) $R \rightarrow \infty$ $U_{om} = U \frac{\frac{1}{\omega C_{km}}}{\frac{1}{\omega C_{km}} + \frac{1}{\omega C_{12}}} = U \frac{C_{12}}{C_{12} + C_{km}} = 220 \frac{120.8}{120.8 + 2000} = 12.53 \text{ V}_{ef}$

$R = 50 \Omega$ $U_{om} = U \frac{R \parallel \frac{1}{j\omega C_{km}}}{\frac{1}{j\omega C_{12}} + R \parallel \frac{1}{j\omega C_{km}}} = U \frac{\frac{R}{1 + j\omega R C_{km}}}{\frac{1}{j\omega C_{12}} + \frac{R}{1 + j\omega R C_{km}}} = U \frac{j\omega R C_{12}}{1 + j\omega R (C_{12} + C_{km})}$

120.8, niška frekvencija (npr. 50 Hz) $R \ll \frac{1}{j\omega (C_{12} + C_{km})}$

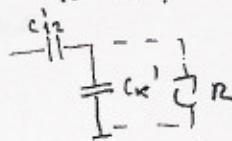
$$U_{om} = j\omega C_{12} R \cdot U \approx j U_{om} = 2\pi \cdot 50 \cdot 120.8 \cdot 10^{-12} \cdot 50 \cdot 220 = 0.417 \text{ mV}_{ef}$$

b)



$$C_k' = 200 \text{ pF/m} \cdot 10 \text{ m} = 2000 \text{ pF}$$

$$C_{12}' = 2 \text{ pF}$$



$R \rightarrow \infty$ $U_{om} = U \frac{C_{12}'}{C_{12}' + C_k'} = 220 \frac{2}{2 + 2000} = 219.78 \text{ mV}_{ef}$

$R = 50 \Omega$ $U_{om} = \omega C_{12}' R \cdot U = 2\pi \cdot 50 \cdot 2 \cdot 10^{-12} \cdot 50 \cdot 220$

$$U_{om} = 6.91 \text{ } \mu\text{V}_{ef}$$