TRIGONOMETRIJSKI FOURIEROV RED

$$f(x) \sim \frac{a_0}{2} + \sum_{n=1}^{\infty} \left(a_n \cos \frac{2n\pi x}{T} + b_n \sin \frac{2n\pi x}{T} \right)$$

$$a_0 = \frac{2}{T} \int_a^b f(x) dx$$

$$a_n = \frac{2}{T} \int_a^b f(x) \cos \left(\frac{2n\pi x}{T} \right) dx$$

$$b_n = \frac{2}{T} \int_a^b f(x) \sin \left(\frac{2n\pi x}{T} \right) dx$$

FOURIEROV RED PARNIH I NEPARNIH FUNKCIJA - parna:

$$f(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} a_n \cos\left(\frac{n\pi x}{L}\right)$$

$$a_0 = \frac{2}{L} \int_0^L f(x) dx$$

$$a_n = \frac{2}{L} \int_0^L f(x) \cos\left(\frac{n\pi x}{L}\right) dx$$

$$b_n = 0$$
- neparna:

$$f(x) = \sum_{n=1}^{\infty} b_n \sin\left(\frac{n\pi x}{L}\right)$$

$$a_0 = a_n = 0$$

$$b_n = \frac{2}{L} \int_0^L f(x) \sin\left(\frac{n\pi x}{L}\right) dx$$

PARSEVALOVA JEDNAKOST

$$\frac{1}{2}a_0^2 + \sum_{n=1}^{\infty} a_n^2 + \sum_{n=1}^{\infty} b_n^2 = \frac{2}{T} \int_a^b |f(x)|^2 dx$$

$$f(x) \sim \frac{1}{\pi} \int_0^\infty d\lambda \int_{-\infty}^\infty f(\xi) \cos\lambda(x - \xi) d\xi$$

FOURIEROV INTEGRAL I SPEKTAR

$$f(x) \sim \int_0^\infty [A(\lambda)\cos(\lambda x) + B(\lambda)\sin(\lambda x)]d\lambda$$
$$A(\lambda) = \frac{1}{\pi} \int_{-\infty}^\infty f(\xi)\cos(\lambda \xi) d\xi$$
$$B(\lambda) = \frac{1}{\pi} \int_{-\infty}^\infty f(\xi)\sin(\lambda \xi) d\xi$$

LINEARNOST LAPLACEOVE TRANSFORMACIJE

$$\alpha f(t) + \beta g(t) \circ -\bullet \alpha F(s) + \beta G(s)$$

TEOREM O PRIGUŠENJU

$$e^{-at}f(t)\circ -\bullet F(s+a)$$

TEOREM O POMAKU

$$f(t-a)u(t-a)\circ -\bullet e^{-as}F(s)$$

LAPLACEOV TRANSFORMAT

$$F(s) = \int_{0}^{\infty} e^{-st} f(t) dt$$

KONVOLUCIJA

$$(f_1 * f_2)(t) = \int_0^t f_1(\tau) f_2(t - \tau) d\tau$$

$$f_1(t)f_2(t) \circ -\bullet F_1(s)F_2(s)$$

TEOREM O DERIVIRANJU INTEGRALA

$$f'(t) \circ -\bullet sF(s) - f(0)$$

$$f^{(n)}(t) \circ -\bullet s^n F(s) - s^{n-1} f(0) - s^{n-2} f'(0) - \cdots$$

$$- f^{(n-1)}(0)$$

TEOREM O DERIVIRANJU SLIKE

$$\frac{f(t)}{t} \circ - \bullet \int_{s}^{\infty} f(s) ds$$

TEOREM O INTEGRIRANJU ORIGINALA

$$\int_0^t f(\tau)d\tau \circ -\bullet \frac{F(s)}{s}$$

RLC KRUGOVI

$$R \circ - \bullet R$$
; $C \circ - \bullet \frac{1}{Cs}$; $L \circ - \bullet Ls$

ČESTE TRANSFORMACIJE

$$1 \circ -\frac{1}{s}$$

$$t \circ -\frac{1}{s^{2}}; t^{n} \circ -\frac{n!}{s^{n+1}}; \frac{t^{n}}{n!} \circ -\frac{1}{s^{n+1}}$$

$$e^{at} \circ -\frac{1}{s-a}; te^{at} \circ -\frac{1}{(s-a)^{2}}$$

$$\frac{1}{a}\sin(at) \circ -\frac{1}{s^{2}+a^{2}}; \cos(at) \circ -\frac{s}{s^{2}+a^{2}}$$

$$\frac{1}{a}\operatorname{sh}(at) \circ -\frac{1}{s^{2}-a^{2}}; \operatorname{ch}(at) \circ -\frac{s}{s^{2}-a^{2}}$$