

SPIT

$$(1) \quad f_1 = 90,2 \text{ MHz} \quad f_2 = 10 \text{ MHz}$$

$$T = 5 \text{ km}$$

$$E = 10 \mu\text{V/m}$$

$$U = h_{\text{eff}} * E$$

↳ efektivna visina antene

$$h_{\text{eff}} = \frac{\lambda}{4} \quad \lambda = \frac{c}{f}$$

$$\lambda_1 = \frac{c}{f_1} = \frac{3 \cdot 10^8}{90,2 \cdot 10^6} = 3,33 \text{ m}$$

$$\lambda_2 = \frac{c}{f_2} = \frac{3 \cdot 10^8}{10 \cdot 10^6} = 30 \text{ m}$$

$$h_{\text{eff}} = \frac{\lambda_1}{4} = 0,83 \text{ m}$$

$$h_{\text{eff}} = \frac{30}{4} = 7,5 \text{ m}$$

$$U_{\text{eff}} = 0,83 \text{ m} \cdot 10 \frac{\mu\text{V}}{\text{m}} = 8,3 \mu\text{V}$$

$$U_{\text{eff}} = 7,5 \text{ m} \cdot \frac{10 \mu\text{V}}{\text{m}} = 7,5 \mu\text{V}$$

* Troškovi antena s obzirom na frekvenciju
podnute na kojem odasilje



Niza frekvencija - velike antene, sedan odasiljač
Više frekvencije - manje antene ali više odasiljača

$$(2) \quad h_{\text{eff1}} = \frac{\lambda_1}{4}$$

$$h_{\text{eff2}} = \frac{\lambda_2}{4}$$

$$\frac{h_{\text{eff1}}}{h_{\text{eff2}}} = \frac{\frac{\lambda_1}{4}}{\frac{\lambda_2}{4}} = \frac{\lambda_1}{\lambda_2} = \frac{\frac{c}{f_1}}{\frac{c}{f_2}} = \frac{f_2}{f_1} //$$

* gulanje na većim frekvencijama je puno veće

(3)

$$f_{VF} = 800 \text{ kHz}$$

$$U_{VF} = 3$$

$$f_m = 2 \text{ kHz}$$

dBV

$$m = 0,5$$

a) amplitudni spektar

b) $U_{AM(\max)}$, $U_{AM(\min)}$, D

c) P_{VF} , P_{BP1} , P_{BP2}

d) D kada je $m_a = 1$

$$a) u_{AM}(t) = U_{VF} [1 + m_a \cos(\omega_m t)] \cos(\omega_{VF} t)$$

$$u_{AM}(t) = [U_{VF} + k \cdot u_m(t)] \cos(\omega_{VF} t)$$

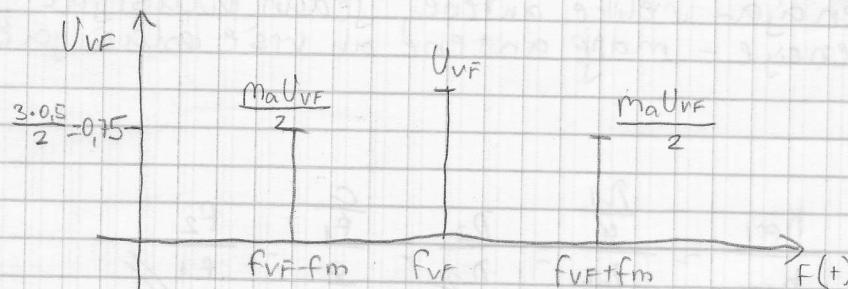
$$u_{AM}(t) = U_{VF} \left[1 + \frac{k \cdot u_m(t)}{U_{VF}} \right] \cos(\omega_{VF} t)$$

$$u_{AM}(t) = U_{VF} \left[1 + k \frac{u_m}{U_{VF}} \cos(\omega_m t) \right] \cos(\omega_{VF} t)$$

$$u_{AM}(t) = U_{VF} [1 + m_a \cos(\omega_m t)] \cos(\omega_{VF} t)$$

$$u_{AM} = U_{VF} \cos(\omega_{VF} t) + U_{VF} m_a \cos(\omega_m t) \cos(\omega_{VF} t)$$

$$u_{AM}(t) = U_{VF} \cos(\omega_{VF} t) + \frac{m_a U_{VF}}{2} \cos[(\omega_{VF} + \omega_m)t] + \frac{m_a U_{VF}}{2} \cos[(\omega_{VF} - \omega_m)t]$$



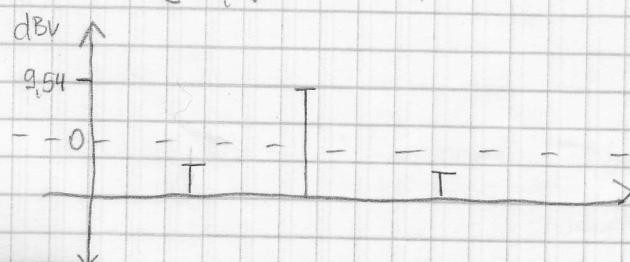
$$U \rightarrow \text{dBV}$$

referentni

$$3V \Rightarrow 20 \log \frac{3V}{1V} = 20 \log 3 = 9,54 \text{ dBV}$$

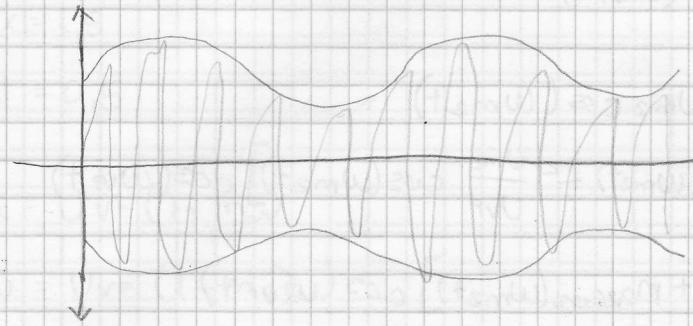
$$3V \Rightarrow 20 \log \frac{3V}{1mV} = 69,54 \text{ dBmV}$$

$$0,75V \Rightarrow 20 \log \frac{0,75V}{1V} = -2,5 \text{ dBV}$$



b)

$$U_{AM}(t) = U_{VF} [1 + m \cos(\omega_m t)] \cos(\omega_{VF} t)$$



kada je $m=1$ onda
je dinamika
beskonačna

$$|A_{MAX}| = U_{VF} (1 + ma)$$

$$D = \left| \frac{A_{MAX}}{A_{MIN}} \right| - \frac{1+ma}{1-ma}$$

$$|A_{MIN}| = U_{VF} (1 - ma)$$

$$D_{[dB]} = 20 \log \frac{1+ma}{1-ma} = 20 \log \frac{1,5}{0,5} = 9,54 \text{ dB}$$

c)

$$P = \frac{U_{VFEF}^2}{Z} \Rightarrow U_{VFEF} = \frac{U_{VF}}{\sqrt{2}} \Rightarrow P_{VF} = \frac{U_{VF}^2}{2Z} \rightarrow \text{snaga na nosiocu}$$

$$P_{VF} [\text{dBmW}] = 10 \log \frac{P_{VF}}{1 \text{mW}}$$

$$P_{BP1} = \frac{U_{EF\text{b1}}^2}{Z} = \frac{\left(\frac{maU_{VF}}{2\sqrt{2}}\right)^2}{Z} = \frac{ma^2 U_{VF}^2}{8Z}$$

$$U_{b1} = \frac{maU_{VF}}{2} \Rightarrow U_{EF\text{b1}} = \frac{maU_{VF}}{2\sqrt{2}}$$

$$P_{BP2} = \frac{ma^2 U_{VF}^2}{8Z}$$

$$P_{b1} [\text{dBmW}] = 10 \log \frac{P_{b1}}{1 \text{mW}}$$

(3)

$$U_{AM}(t) = [U_{VF} + k U_m(t)] \cos(\omega_{VF} t)$$

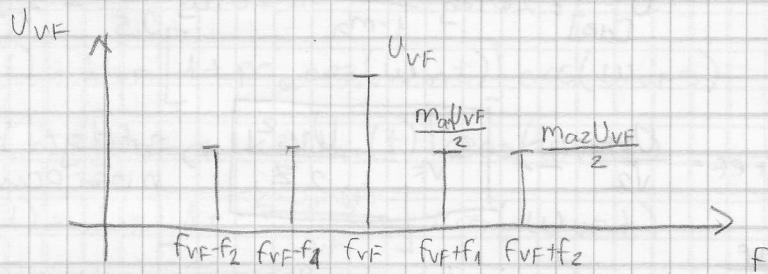
$$U_m(t) = U_{m1} \cos(\omega_{m1} t) + U_{m2} \cos(\omega_{m2} t)$$

$$U_{AM}(t) = U_{VF} \left[1 + k \cdot \frac{U_{m1}}{U_{VF}} \cos(\omega_{m1} t) + k \cdot \frac{U_{m2}}{U_{VF}} \cos(\omega_{m2} t) \right] \cos(\omega_{VF} t)$$

$$U_{AM}(t) = U_{VF} \left[1 + m_{a1} \cos(\omega_{m1} t) + m_{a2} \cos(\omega_{m2} t) \right] \cos(\omega_{VF} t)$$

$$U_{AM}(t) = U_{VF} \cos(\omega_{VF} t) + \frac{m_{a1} U_{VF}}{2} \cos[(\omega_{VF} - \omega_{m1})t] + \frac{m_{a2} U_{VF}}{2} \cos[(\omega_{VF} + \omega_{m2})t]$$

$$+ \frac{m_{a2} U_{VF}}{2} \cos((\omega_{VF} - \omega_{m2})t) + \frac{m_{a2} U_{VF}}{2} \cos[(\omega_{VF} + \omega_{m2})t]$$



$$P_{UK} = \frac{\left(\frac{U_{VF}}{\sqrt{2}}\right)^2}{Z} + 4 \cdot \frac{\left(\frac{m_a \cdot U_{VF}}{2\sqrt{2}}\right)^2}{Z}$$

$$U_{AM}(t) = U_{VF} \left[1 + m_{a1} \cos(\omega_{m1} t) + m_{a2} \cos(\omega_{m2} t) \right] \cos(\omega_{VF} t)$$

$$A_{MAX} = U_{VF} \left[1 + 2 m_a \right] \quad U_{VF} \left[1 + m_{a1} + m_{a2} \right]$$

$$A_{MIN} = U_{VF} \left[1 - 2 m_a \right]$$

4.

$$U_{AM}(t) = U_{VF} [1 + m_a \cos(\omega_m t)] \cos(\omega_{VF} t)$$

$$|A_{MAX}| = 1,5$$

$$|A_{MIN}| = 0,5$$

$$A_{MAX} = U_{VF} (1 + m_a)$$

$$A_{MIN} = U_{VF} (1 - m_a)$$

$$\left| \frac{A_{MAX}}{A_{MIN}} \right| = \frac{1 + m_a}{1 - m_a} \Rightarrow m_a = ?$$

$$T_m = 0,005 \text{ s}$$

$$f_m = \frac{1}{T_m} = 200 \text{ Hz}$$

* Premodulacija \Rightarrow signal se na prijamniku ne može rekonstruirati,

* Vrste AM modulacije

* FM modulacija je u području od 150 kHz do 30,55 MHz

(5)

$$U_{\text{mod}} = U_{VF} + k U_m(t)$$

$$U_m(t) = U_m \cos(\omega_m t)$$

$$U_{\text{mod}}(t) = U_{VF} + k_F \cdot U_m \cos(\omega_m t)$$

$$\Delta f_{\text{mod}} = k_F \cdot U_m =$$

$$\Delta f = \frac{20 \text{ kHz}}{V} \cdot 0.2V$$

$$\Delta \omega = 2\pi \cdot \Delta f$$

$$\omega_{\text{mod}} = \omega_{VF} + \Delta \omega \cos(\omega_m t)$$

$$f_{\text{mod}} = f_{VF} + \Delta f \cos(\omega_m t)$$

$$\omega = \frac{d\phi}{dt} \Rightarrow \phi(t) = \int_0^t \omega(\tau) d\tau$$

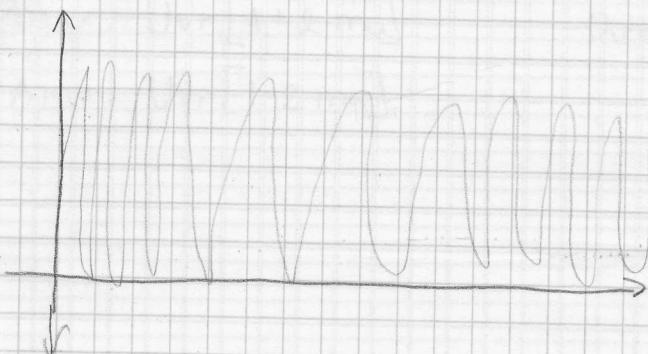
$$\phi(t) = \omega_{VF} t + \frac{\Delta \omega_{\text{mod}}}{\omega_m} \sin(\omega_m t)$$

faza ↴

$$\phi(t) = \omega_{VF} t + m_f \sin(\omega_m t)$$

$$U_{FM}(t) = U_{VF} \cos[\omega_{VF} t + m_f \sin(\omega_m t)]$$

$$m_f = \frac{\Delta \omega_{\text{mod}}}{\omega_m} = \frac{\Delta f}{f_m} =$$



$$|A_{\max}| = |A_{\min}| = U_{VF}$$

$$D = 1$$

$$20 \log 1 = 0 \text{ dB}$$

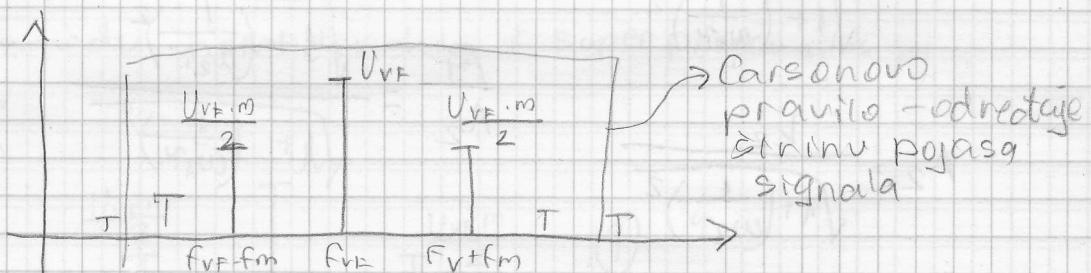
$$\cos(\alpha + \beta) = \cos\alpha \cos\beta - \sin\alpha \sin\beta$$

$$U_{FM} = U_{VF} \cos [w_{VF}t + m_f \sin(w_m t)]$$

$$= U_{VF} \cos(w_{VF}t) \cos[m_f \cdot \sin(w_m t)] - U_{VF} \sin(w_{VF}t) \cdot \sin[m_f \cdot \sin(w_m t)]$$

$$m_f \ll 1 \Rightarrow \cos x \approx 1 \\ \sin x \approx x$$

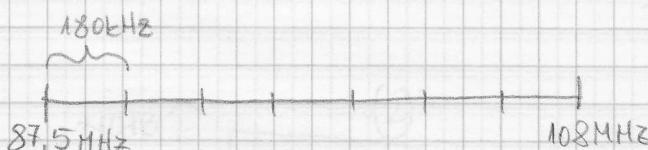
$$U_{FM} = U_{VF} \cos(w_{VF}t) - U_{VF} \sin(w_{VF}t) \cdot m_f \cdot \sin(w_m t)$$



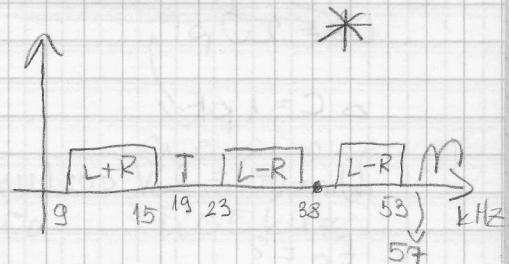
* ako m_f nije $\ll 1$ onda ima puno više bočnih komponenti; uzima se carsonovo pravilo

$$BFM = 2 \cdot f_m (m_f + 1) = 2 \cdot f_m \left[\frac{\Delta f_{mod}}{f_{mmax}} + 1 \right] = 2 (\Delta f_{mod} + f_{mmax})$$

↳ Carsonovo pravilo.



$$f_{mmax} = 15 \text{ kHz}$$



- koliko kanala stane prema Carsonovom pravilu

$$BFM = 2 f_{mmax} [m_f + 1] = 2 f_{mmax} \left(\frac{\Delta f}{f_{mmax}} + 1 \right) = 2 (\Delta f + f_{mmax})$$

$$BFM = 2 \cdot (75 + 15) = 180 \text{ kHz}$$

$$\Delta f = 108 - 87.5 = 20.5 \text{ MHz}$$

$$N = \frac{\Delta f}{BFM} = \frac{20.5 \text{ MHz}}{108 \text{ kHz}} = 189$$

8. Akcentuacija

- Šum ima ravnu frekvenčku karakteristiku - ima konstantnu energiju u svimnosti o frekvenciji

- kad se sum modulira ispodatka $P_{\text{sum}} \rightarrow F +$

$P_{\text{signal}} \rightarrow f +$

$$A_1 = \frac{k_1}{\sqrt{1 + \left(\frac{1}{\omega_1 r}\right)^2}}$$

$$A_2 = \frac{k_2}{\sqrt{1 + \left(\frac{1}{\omega_2 r}\right)^2}}$$

$$\frac{A_1}{A_2} = \frac{\sqrt{1 + \left(\frac{1}{\omega_2 r}\right)^2}}{\sqrt{1 + \left(\frac{1}{\omega_1 r}\right)^2}}$$

* Objasniti postupak akcentuacije i deakcentuacije

9.

$$L = 1 \text{ mH}$$

$$C_0 = 20 \text{ pF}$$

$$\Delta C = 1 \text{ pF}$$

$$U_m(t) = 2 \sqrt{2} \cos(\omega_m t)$$

$$f_0 = ?$$

$$\Delta f = ?$$

$$\omega = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{L \cdot (C_0 + \Delta C) \cos(\omega_m t)}} = \frac{1}{\sqrt{L \cdot C_0 \left[1 + \frac{\Delta C}{C_0} \cos(\omega_m t)\right]}}$$

$$\omega = \frac{1}{\sqrt{LC_0}} = \frac{1}{\sqrt{1 + \frac{\Delta C}{C_0} \cos(\omega_m t)}} = \omega_0 \left(1 - \frac{\Delta C}{2C_0} \cos(\omega_m t)\right)$$

$$\Delta C \ll C_0 \quad \frac{\Delta C}{C_0} \ll 1$$

$$\frac{1}{\sqrt{1+x}} \approx 1 - \frac{x}{2}$$

$$\omega_0 = \frac{1}{\sqrt{LC_0}}$$

$$f_0 = \frac{1}{2\pi\sqrt{LC_0}}$$

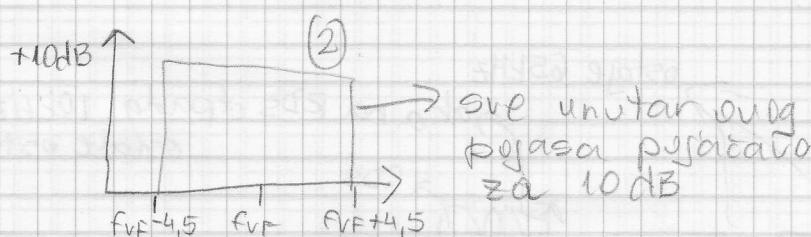
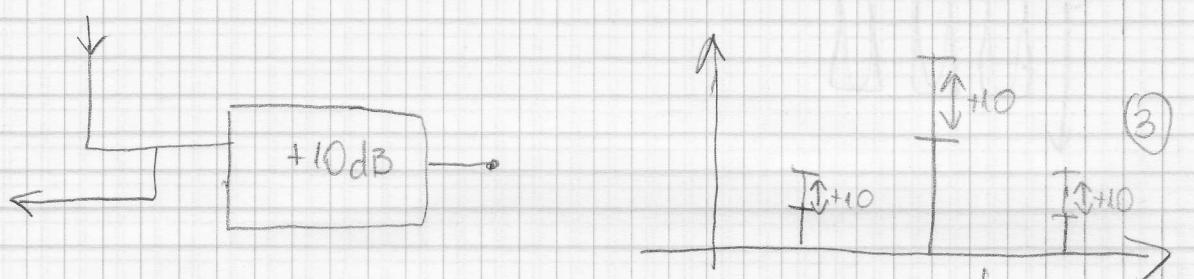
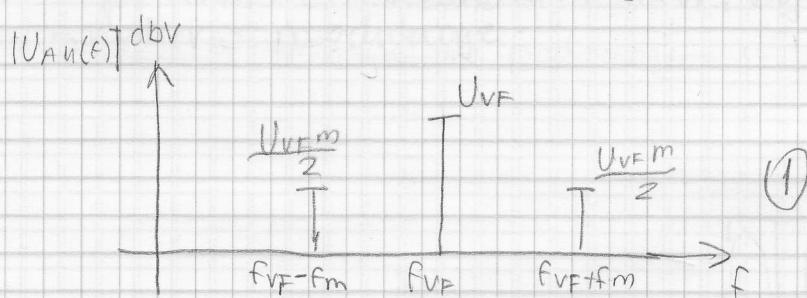
$$\omega(t) = \omega_0 - \omega_0' \cdot \frac{\Delta C}{2C_0} \cos(\omega_m t)$$

$$\Delta \omega = \omega_0 \cdot \frac{\Delta C}{2C_0}$$

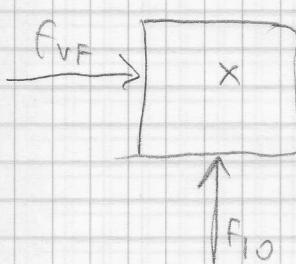
→ promjena

10

* razlika između homodinskog i superprzymišljenja



sve u okolini
spušta na
 455kHz



$$f_{MF} = f_{RF} - f_{LO}$$

$$f_{LO} = f_{RF} - f_{MF} = 950 - 455 = 495\text{ kHz}$$

(11)

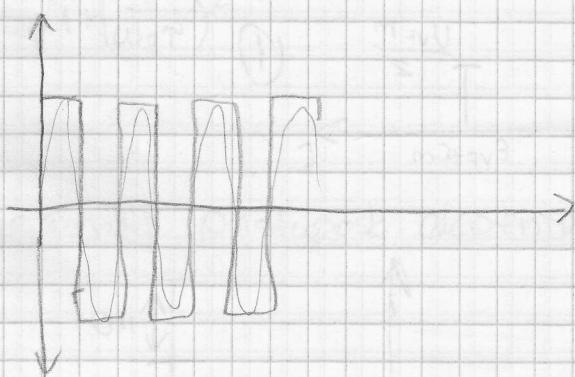
87,5 ms



104 bit

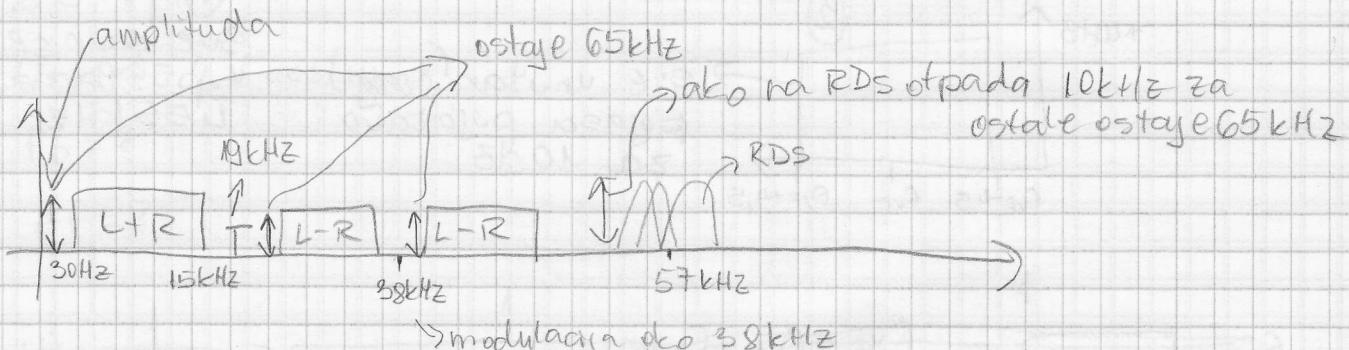
$$R = \frac{104 \text{ bit}}{87,5 \text{ ms}} = 1189 \text{ bit/s}$$

$$R_{kor} = \frac{64 \text{ bit}}{87,5 \text{ ms}}$$



(12)

(13)



* Objasniti stereo multiplex

$$B_{FM} = 2 ((\Delta f) + f_{max})$$

$$\Delta f_{max} = 75 \text{ kHz}$$

75 kHz devijacije se rasporedjuju na 4 komponente