

periodični

neperiodični

$$c_k = \frac{1}{T_0} \int_{-T_0/2}^{T_0/2} x(t) e^{-jk\omega_0 t} dt = |c_k| e^{-j\theta_k} = \frac{A\tau}{T} \frac{\sin(\frac{k\omega\tau}{2})}{\frac{k\omega\tau}{2}}$$

$$c = \frac{A}{2} \sin/\cos \text{ signal}$$

$$\text{Ovojnica} = 0 \text{ za } \frac{k}{\tau}$$

$$x(t) = \sum_{k=-\infty}^{\infty} c_k e^{jk\omega_0 t}$$

$$P = \lim_{k \rightarrow \infty} \left[\frac{1}{kT_0} \int_0^{T_0} |x(t)|^2 dt \right] = \frac{1}{T_0} \int_0^{T_0} |x(t)|^2 dt = \sum_{k=-\infty}^{\infty} |c_k|^2$$

$$P = |c_0|^2 + 2 \sum_{k=1}^{\infty} |c_k|^2 = A^2 \frac{\tau}{T}$$

$$P = \frac{A^2}{2} \sin/\cos \text{ signal}$$

$$X(f) = \int_{-\infty}^{\infty} x(t) e^{-j2\pi ft} dt \text{ ili } X(\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt, \omega = 2\pi f$$

$$X(f) = |X(f)| e^{j\theta(f)}$$

$$X(f) = A\tau * \frac{\sin(\frac{2\pi f\tau}{2})}{\frac{2\pi f\tau}{2}}$$

$$x(t) = \int_{-\infty}^{\infty} X(f) e^{j2\pi ft} df \text{ ili } x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(\omega) e^{j\omega t} d\omega$$

$$E = \int_{-\infty}^{\infty} |x(t)|^2 dt = \int_{-\infty}^{\infty} |X(f)|^2 df = \frac{1}{2\pi} \int_{-\infty}^{\infty} |X(\omega)|^2 d\omega$$

$$E = A^2 \tau \text{ pravokutni impuls}$$

$$E = \lim_{T \rightarrow \infty} \int_{-T}^T |x(t)|^2 dt = \int_{-\infty}^{\infty} |x(t)|^2 dt,$$

$$P = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^T |x(t)|^2 dt.$$

$\cos \omega t = \frac{1}{2} (e^{j\omega t} + e^{-j\omega t})$	$E < \infty \rightarrow P = 0$	$x_{db} = 10 \log_{10} X$	$\int_{-\infty}^{\infty} \delta(t-t_0) x(t) dt = x(t_0)$
$\sin \omega t = \frac{1}{2} (e^{j\omega t} - e^{-j\omega t})$	$P > 0 \rightarrow E \rightarrow \infty$	$e^{-at} \leftrightarrow \frac{1}{s+a}$	
$\sin(x) = \cos(x - \frac{\pi}{2})$	$E \rightarrow \infty \text{ i } P \rightarrow \infty$		

Slučajni signali (63)

npr. Gaussov bijeli šum (64)

$$\text{srednja vrijednost slučajnog procesa } \mu_X(t) = E[X(t)] = \int_{-\infty}^{\infty} x f_X(x, t) dx \quad \mu_Y = \mu_X H(0)$$

$n(t)$ = signal šuma

N_0 = spektralna gustoća gaussovog bijelog šuma

$S_n(f)$ = spektralna gustoća snage,

$$S_X(f) = \int_{-\infty}^{\infty} R_X(\tau) e^{-j2\pi f\tau} d\tau \text{ [W/Hz]}$$

$$S_Y(f) = S_X(f) |H(f)|^2$$

$$S_W(f) = \sigma^2 \int_{-\infty}^{\infty} \delta(t) e^{-j2\pi ft} dt = \sigma^2$$

$$S_N(f) = \frac{N_0}{2}, \forall f \in \mathbb{R} \text{ za bijeli šum}$$

$$R_X(\tau) = \int_{-\infty}^{\infty} S_X(f) e^{j2\pi f\tau} df$$

$$R_W(\tau) = \sigma^2 \delta(\tau) \text{ za bijeli šum}$$

$R_n(t)$ = autokorelacijska funkcija

$P(t)$ = srednja snaga šuma

$$P = E[X^2(t)] = R_X(0) = \int_{-\infty}^{\infty} S_X(f) df$$

LTI (67)

$h(t), H(f)$ = impulsni odziv sustava

$$y(t) = \int_{-\infty}^{\infty} x(\tau) h(t-\tau) d\tau = \int_{-\infty}^{\infty} h(\tau) x(t-\tau) d\tau$$

$$H(f) = \int_{-\infty}^{\infty} h(t) e^{-j2\pi ft} dt$$

$$y(t) = x(t) * h(t) = h(t) * x(t)$$

$$h(t) = \int_{-\infty}^{\infty} H(f) e^{j2\pi ft} df$$

prigušenje kanala $A(f) = \frac{1}{|H(f)|}$

NPK: $|X(f)| \approx 0$ za $|f| > fg, B = fg$

PPK: $|X(f)| > 0$ samo ako je $fg > |f| > fd, B = fg - fd$

A/D pretvorba (79)

1. UZORKOVANJE (79)

$R = fu * r$ = brzina prijenosa bita

$fu = 2B$ Nyquist

2. KVANTIZACIJA PCM (95)

Kvantizacijske razine $L = 2^r$

$$\text{Kvantizacijski šum } (S/N) = \frac{3}{2} * 2^{2r} \quad (S/N) = \frac{S}{\sigma_Q^2} = \left(\frac{3S}{m_{\max}^2} \right) 2^{2r}$$

amplitude ulaznog signala (-mmax, mmax)

$$\text{korak kvantizacije } \Delta = \frac{2m_{\max}}{L}$$

kvantizacijski šum je ograničen: $-\frac{\Delta}{2} \leq q \leq \frac{\Delta}{2}$

funkcija vjerojatnosti razine $u(t)$: $p(u)$

$$\text{srednja kvadratna greška } Oq^2 = \frac{1}{3} m_{\max}^2 * 2^{-2r}$$

KAPACITET (101)

$$N = BN_0 \quad S_N(f) = \frac{N_0}{2}, \forall f \in \mathbb{R} \text{ za bijeli šum}$$

AWGN kanal

$$R = C = B \log \left(1 + \frac{S}{N_0 B} \right) \text{ [bit/s]} = 2BD \text{ (D=dinamika)}$$

$$\text{Pojačanje: } A = (S_2/S_1)$$