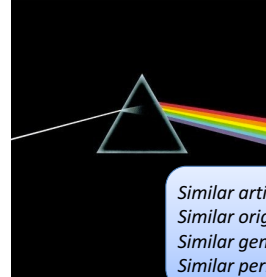


## Recommender Systems Topic Modeling

Rodrygo Santos  
rodrygo@dcc.ufmg.br

## Content-based recommendation

You bought

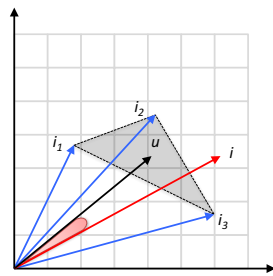


You may like



Similar artist: Pink Floyd  
Similar origin: England  
Similar genre: Rock  
Similar period: 1970s

## Vector space representation



- Each item is a vector
  - One component for each term in the vocabulary
- Each user is a vector
  - Some combination of item vectors
- Prediction by similarity
  - Cosine of the angle between the user and item vectors

## The curse of dimensionality

- The space of terms is very **high-dimensional**!

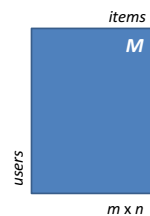
- Google Web N-grams [Franz and Brants, 2006]

- Problems**
  - Efficiency**  
It will take longer to compute similarities
  - Effectiveness**  
It will be harder to match similar **concepts**

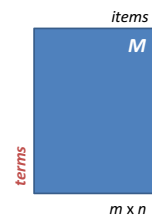
# tokens	1,024,908,267,229
# sentences	95,119,665,584
# 1-grams	13,588,391
# 2-grams	314,843,401
# 3-grams	977,069,902
# 4-grams	1,313,818,354
# 5-grams	1,176,470,663

## The curse of dimensionality

Collaborative filtering

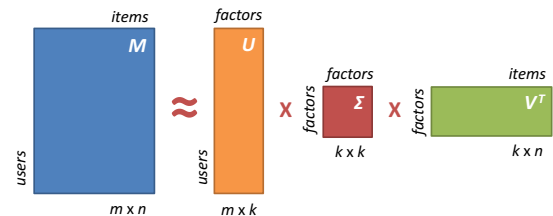


Content-based filtering



## Latent semantic analysis

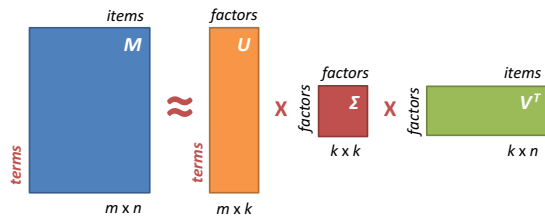
Collaborative filtering



## Latent semantic analysis

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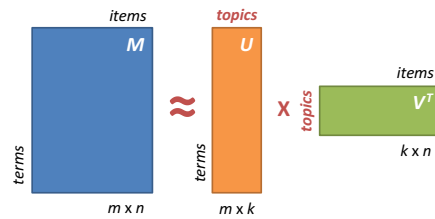
### Content-based filtering



## Latent topic modeling

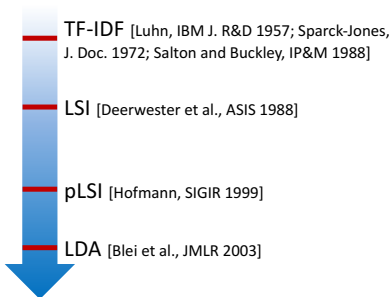
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### Content-based filtering



## Dimensionality reduction

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## Latent Dirichlet allocation (LDA)

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*"Imagine searching and exploring documents based on the themes that run through them. Rather than finding documents through keyword search alone, we might first find the theme that we are interested in, and then examine the documents related to that theme."*

[Blei, CACM 2012]

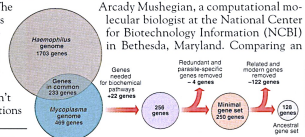
## An example

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### Seeking Life's Bare (Genetic) Necessities

COLD SPRING HARBOR, NEW YORK—How many genes does an organism need to survive? Last week at the genome meeting here,\* two genome researchers with radically different approaches presented complementary views of the basic genes needed for life. One research team, using computer analyses to compare known genomes, concluded that today's organisms can be sustained with just 250 genes, and that the earliest life forms required a mere 128 genes. The other researcher mapped genes in a simple parasite and estimated that for this organism, 800 genes are plenty to do the job—but that anything short of 100 wouldn't be enough. Although the numbers don't match precisely, those predictions

"are not all that far apart," especially comparison to the 75,000 genes in the human genome, notes Siv Andersson of Uppsala University in Sweden, who arrived at the 800 number. But coming up with a consensus answer may be more than just a genetic numbers game, particularly as more and more genomes are completely mapped and sequenced. "It may be a way of organizing any newly sequenced genome," explains Arcady Mushegian, a computational molecular biologist at the National Center for Biotechnology Information (NCBI) in Bethesda, Maryland. Comparing an



\* Genome Mapping and Sequencing, Cold Spring Harbor, New York, May 8 to 12.

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## Latent topics

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human genome	evolution	disease	computer
genome	evolutionary	host	models
dna	species	bacteria	information
genetic	organisms	diseases	data
genes	life	resistance	computers
sequence	origin	bacterial	system
gene	biology	new	network
molecular	groups	strains	systems
sequencing	phylogenetic	control	model
map	living	infectious	parallel
information	diversity	malaria	methods
genetics	group	parasite	networks
mapping	new	parasites	software
project	two	united	new
sequences	common	tuberculosis	simulations
"genetics"	"evolution"	"disease"	"computers"

## Generative modeling



- LDA is a generative model
  - It models the process of generating words
- Say you want a document with  $n$  words
  - Assume there are  $k$  known topics
  - Choose the document's distribution over topics
  - For each of the  $n$  words to be generated
    - Choose a topic from the document's topic distribution
    - Choose a word from the chosen topic

## Generative modeling



- Generating  $n$  words
  - Choose the document's topic distribution
  - For each of the  $n$  words to be generated
    - Choose a topic from the document's distribution
    - Choose a word from the chosen document topic

## Generative modeling



- Generating  $n$  words
  - Choose the document's topic distribution
    - 50% genetics
    - 30% evolution
    - 15% disease
    - 5% computers
  - For each of the  $n$  words to be generated
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"evolution"

evolution  
evolutionary  
species  
organisms  
life  
origin

## Generative modeling



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"genetics"

human  
genome  
dna  
genetic  
genes  
sequence

origin

## Generative modeling

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- Generating  $n$  words
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- Generating  $n$  words
  - Choose the document's topic distribution
  - For each of the  $n$  words to be generated

50% genetics  
30% evolution  
15% disease  
5% computers

"computers"  
computer  
models  
information  
data  
computers  
system

origin human

- Choose a topic from the document's distribution
- Choose a word from the chosen document topic

## Generative modeling

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- Generating  $n$  words
  - Choose the document's topic distribution
  - For each of the  $n$  words to be generated

50% genetics  
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5% computers

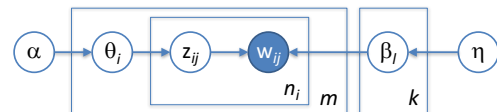
"computers"  
computer  
models  
information  
data  
computers  
system

origin human models

- Choose a topic from the document's distribution
- Choose a word from the chosen document topic

## In plate notation

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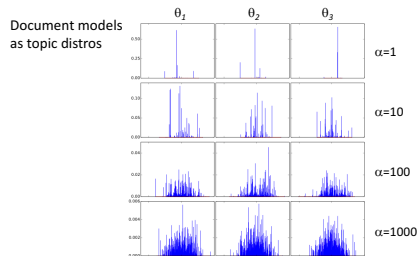


- $\theta_i$ : topic distribution of document  $i$  (of  $m$  documents)
  - $\alpha$ : parameter of the Dirichlet prior
- $\beta_l$ : word distribution of topic  $l$  (of  $k$  topics)
  - $\eta$ : parameter of the Dirichlet prior
- $w_{ij}$ :  $j$ -th word in document  $i$
- $z_{ij}$ : chosen topic of word  $w_{ij}$

## Dirichlet distribution

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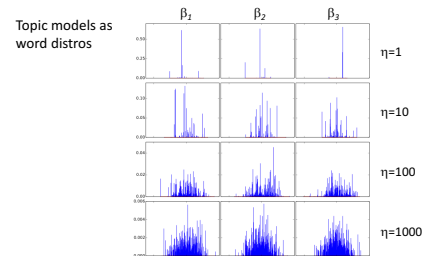
- A "distribution of distributions" with concentration parameter  $\alpha$



## Dirichlet distribution

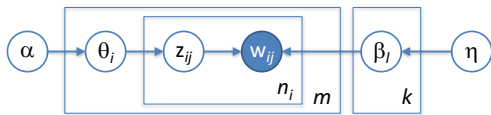
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- A "distribution of distributions" with concentration parameter  $\beta$



## In plate notation

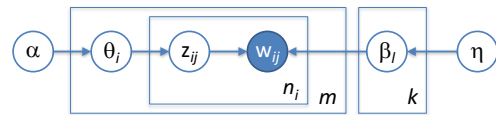
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- Choose  $\theta_i \sim \text{Dir}(\alpha)$  for  $i \in \{1, \dots, m\}$
- Choose  $\beta_l \sim \text{Dir}(\eta)$  for  $l \in \{1, \dots, k\}$
- For each document  $i \in \{1, \dots, m\}$ 
  - For each position  $j \in \{1, \dots, n_i\}$ 
    - Choose a topic  $z_{ij} \sim \text{Mult}(\theta_i)$
    - Choose a word  $w_{ij} \sim \text{Mult}(\beta_{z_{ij}})$

## Mathematically

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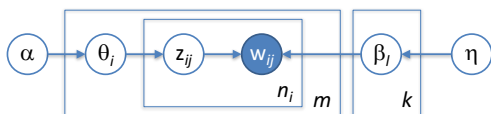


- Equivalent to the following joint distribution

$$p(\beta_{1:k}, \theta_{1:m}, z_{1:m}, w_{1:m}) = \prod_{l=1}^k p(\beta_l | \eta) \prod_{i=1}^m p(\theta_i | \alpha) \left( \prod_{j=1}^{n_i} p(z_{ij} | \theta_i) p(w_{ij} | \beta_{z_{ij}}) \right)$$

## Reversing the logic

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- In reality, we don't know the topics
  - Or, equivalently, the  $\theta_i$  and  $\beta_l$  distributions
- We actually know the documents
  - *How to uncover the hidden topic structure?*

## Posterior inference

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- How to compute the distribution of the topic structure given the observed documents?
  - Aka the posterior distribution

$$p(\beta_{1:k}, \theta_{1:m}, z_{1:m} | w_{1:m}) = \frac{p(\beta_{1:k}, \theta_{1:m}, z_{1:m}, w_{1:m})}{p(w_{1:m})}$$

- Problem: computing the marginal  $p(w_{1:m})$ 
  - *Intractable*: would require examining every possible instantiation of the hidden variables

## Approximate inference

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- Sampling algorithms
  - Iteratively collect samples from the posterior
    - e.g., Gibbs sampling
- Variational algorithms
  - Posit a parameterized family of distributions over the hidden structure, search for the best one
    - Easily handle millions of documents
    - Can accommodate streaming textual collections

## More on this?

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- Related courses
  - Probabilistic graphical models
  - Bayesian inference

## How to leverage topics?

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- Vector space model
  - $p(i|u) = \cos(\theta_u, \theta_i)$
- Item likelihood model
  - $p(i|u) = \prod_{w \in i} p(w|\theta_u)^{\text{tf}_{wu}}$
- Unified likelihood model
  - $p(i|u) = -KL(\theta_u || \theta_i)$ 

$$= -p(w|\theta_u) \log \frac{p(w|\theta_u)}{p(w|\theta_i)}$$

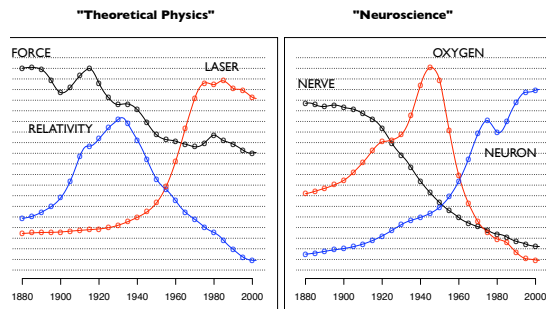
## LDA variants

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- Syntactic topic model
  - A word or its topic is influenced by syntax
- Correlated topic model, hierarchical topic model
  - Some topics resemble other topics
- Polylingual topic model
  - Different languages, same topic mixtures
- Relational topic model
  - Exploiting link structure
- Dynamic topic model
  - Topics are time-dependent

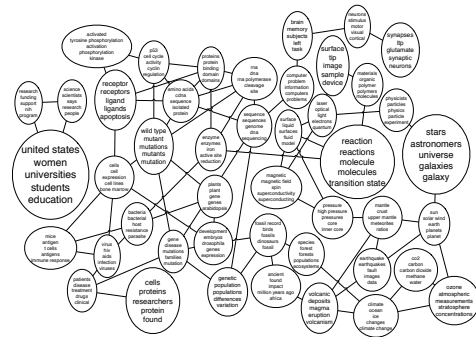
## Modeling evolution

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## Modeling correlations

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## Summary

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- Content-based recommender systems are effective in many difficult scenarios
  - Cold-start items, basket analysis
- Build upon a history of research in IR
  - How to represent users and items
  - How to match users and items
- Still an active research area
  - How to go beyond a raw content representation?

## A word of caution

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### Recommending New Movies: Even a Few Ratings Are More Valuable Than Metadata

István Pilászy  
Dept. of Measurement and Information Systems  
Budapest University of Technology and Economics  
Magyar Tudósok krt. 2.  
Budapest, Hungary  
pilas@mit.bme.hu

Domenkos Tikk  
Dept. of Telecom. and Media Informatics  
Budapest University of Technology and Economics  
Magyar Tudósok krt. 2.  
Budapest, Hungary  
tikk@mit.bme.hu

#### ABSTRACT

The Netflix Prize (NP) competition gave much attention to collaborative filtering (CF) approaches. Matrix factorization (MF) has been the most successful approach in this competition. We show that even 10 ratings of a new movie are more valuable than its metadata for predicting user ratings.

#### 1. INTRODUCTION

The goal of recommender systems is to give personalized recommendation on items to users. Typically the recommendation is based on the former and current activity of users. When a user rates a movie, this rating is a valuable information for the system. We show that even 10 ratings of a new movie are more valuable than its metadata for predicting user ratings.

*We show that even 10 ratings of a new movie are more valuable than its metadata for predicting user ratings.*