

Matemática Casabueno

$$N \rightarrow S: 5 \quad N \rightarrow L: 4 \quad S \rightarrow L: 2 \quad L \rightarrow S: 1 \quad L \rightarrow O: 3$$

$$\cancel{N \rightarrow O: 1} \quad O \rightarrow N: 1 \quad O \rightarrow S: 2 \quad O \rightarrow L: 2$$

$$Q = \begin{bmatrix} -9 & 5 & 4 & 0 \\ 0 & -2 & 2 & 0 \\ 0 & 1 & -4 & 3 \\ 1 & 2 & 2 & -5 \end{bmatrix} \quad \begin{cases} -9\pi_N + \pi_O = 0 \\ 5\pi_N - 2\pi_S + \pi_L + 2\pi_O = 0 \\ 4\pi_N + 2\pi_S - 4\pi_L + 2\pi_O = 0 \\ 3\pi_L - 5\pi_O = 0 \\ \pi_N + \pi_S + \pi_L + \pi_O = 1 \end{cases}$$

$$-9\pi_N + \pi_O = 0 \Rightarrow \pi_O = 9\pi_N$$

$$\pi_O = 9\pi_N$$

$$5\pi_N - 2\pi_S + \pi_L + 2\pi_O = 0$$

$$4\pi_N + 2\pi_S - 4\pi_L + 2\pi_O = 0$$

$$3\pi_L - 5\pi_O = 0 \Rightarrow \pi_L = \frac{5}{3}\pi_O$$

$$\pi_L = \frac{5}{3} \cdot 9\pi_N = 15\pi_N$$

$$\pi_N + \pi_S + \pi_L + \pi_O = 1$$

$$5\pi_N - 2\pi_S + 15\pi_N + 2 \cdot 9\pi_N = 0 \Rightarrow 5\pi_N + 15\pi_N + 18\pi_N - 2\pi_S = 0 \Rightarrow$$

$$38\pi_N - 2\pi_S = 0 \quad \Rightarrow \pi_S = 19\pi_N$$

$$\pi_N = \pi_N$$

$$\pi_N = \frac{1}{44}$$

$$\pi_S = 19\pi_N$$

$$\pi_S = 19 \cdot \frac{1}{44} = \frac{19}{44}$$

$$\pi_L = 15\pi_N$$

$$\pi_L = 15/44$$

$$\pi_O = 9\pi_N$$

$$\pi_O = 9/44$$

$$\pi_N + 19\pi_N + 15\pi_N + 9\pi_N = 1$$

$$\pi_N = 1/44$$

Estado	Prob. exata	Aprox.
N	1/44	2,27%
S	19/44	43,18%
L	15/44	34,09%
O	9/44	20,45%