# Mathematical Optimization Algorithms

Lab 1: Linear Programming





#### Scenario:

- You are the Operations Manager at a tea production company, **Namaste Ikigai**, which specializes in producing and selling various types of teas across Europe.
- Your goal is to maximize the company's operating income for the upcoming fiscal year 2025.
- To achieve this, you need to determine the optimal production and distribution plan for different types
  and sizes of tea boxes to various countries, while considering production capacities, costs, and market
  demand.

### Objective:

 Formulate and solve a Linear Programming problem to maximize Namaste Ikigai operating income by determining the optimal quantities of each tea product to produce and distribute to each country.



### Selling Price:

- Green Tea: 50g box (GT50) at 6 USD per box, 100g box (GT100) at 10 USD per box
- Black Tea: 50g box (BT50) at 7 USD per box, 100g box (BT100) at 12 USD per box
- White Tea:50g box (WT50) at 9 USD per box, 100g box (WT100) at 16 USD per box
- Red Tea: 50g box (RT50) at 8 USD per box, 100g box (RT100) at 14 USD per box

### Buying Price:

- Green Tea 100g 3.5 USD
- Black Tea: 100g 4.5 USD
- White Tea:100g 5.5 USD
- Red Tea 100g 5 USD



### Markets:

- The products are sold in the following countries through their main cities:
- Portugal, Spain, France, Italy, Germany, Poland

### **Distribution Cost**

#### **Demand Forecast:**

USD/box	Country	GT50	GT100	BT50	BT100	WT50	WT100	RT50	RT100
0.5	Portugal	100	80	90	70	50	40	60	50
0.4	Spain	150	120	130	110	80	60	100	90
0.6	France	200	170	180	160	100	90	120	110
0.7	Italy	130	110	120	100	70	60	90	80
0.8	Germany	180	160	170	150	90	80	110	100
1.0	Poland	120	100	110	90	60	50	80	70
	0.5 0.4 0.6 0.7 0.8	<ul> <li>0.5</li> <li>0.4</li> <li>Spain</li> <li>0.6</li> <li>France</li> <li>0.7</li> <li>Italy</li> <li>Germany</li> </ul>	0.5       Portugal       100         0.4       Spain       150         0.6       France       200         0.7       Italy       130         0.8       Germany       180	0.5       Portugal       100       80         0.4       Spain       150       120         0.6       France       200       170         0.7       Italy       130       110         0.8       Germany       180       160	0.5       Portugal       100       80       90         0.4       Spain       150       120       130         0.6       France       200       170       180         0.7       Italy       130       110       120         0.8       Germany       180       160       170	0.5       Portugal       100       80       90       70         0.4       Spain       150       120       130       110         0.6       France       200       170       180       160         0.7       Italy       130       110       120       100         0.8       Germany       180       160       170       150	0.5       Portugal       100       80       90       70       50         0.4       Spain       150       120       130       110       80         0.6       France       200       170       180       160       100         0.7       Italy       130       110       120       100       70         0.8       Germany       180       160       170       150       90	0.5       Portugal       100       80       90       70       50       40         0.4       Spain       150       120       130       110       80       60         0.6       France       200       170       180       160       100       90         0.7       Italy       130       110       120       100       70       60         0.8       Germany       180       160       170       150       90       80	0.5       Portugal       100       80       90       70       50       40       60         0.4       Spain       150       120       130       110       80       60       100         0.6       France       200       170       180       160       100       90       120         0.7       Italy       130       110       120       100       70       60       90         0.8       Germany       180       160       170       150       90       80       110



#### **Additional Information:**

- Production Cost is 1 USD per box (regardless of type and size)
- Marketing Cost is Fixed annual cost of 400 k USD
- Fixed annual cost of 4 M USD (not dependent on production quantity)
- The factory in Girona can produce a total of 2 million boxes per year.
- Total raw tea available per year is Green Tea: 25,000,000 grams, Black Tea: 30,000,000 grams, White Tea: 15,000,000 grams, Red Tea: 20,000,000 grams,
- The company wants to ensure that at least 10% of the total production is allocated to each type of tea to maintain market presence.



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