

Fourierjeva transformacija. Če je $f: \mathbb{R} \rightarrow \mathbb{C}$, je njena Fourierjeva transformiranka definirana kot

$$\widehat{f}(\xi) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} f(x) e^{-ix\xi} dx$$

Ima sledeče lastnosti:

$$\widehat{f(x)e^{itx}}(\xi) = \widehat{f}(\xi - t)$$

$$\widehat{f(ax)} = \frac{1}{a} \widehat{f}\left(\frac{\xi}{a}\right)$$

$$\widehat{f(x-t)}(\xi) = \widehat{f}(\xi) e^{-it\xi}$$

Inverzna Fourierjeva transformacija:

$$f(x) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \widehat{f}(\xi) e^{-ix\xi} d\xi$$

Velja $\widehat{\widehat{f}}(x) = f(-x)$

Tabela znanih transformacij. Ravno tako pa prav pride sledeče dejstvo:

$f(x)$	$\widehat{f}(\xi)$
$e^{- x }$	$\sqrt{\frac{1}{\pi}} \frac{1}{1+\xi^2}$
$e^{-a^2 x^2/2}$	$\frac{1}{a} e^{-\xi^2/2a^2} \quad (a > 0)$
$\chi_{[a,a]}(x)$	$\sqrt{\frac{2}{\pi}} \frac{\sin(a\xi)}{\xi}$
$\frac{1}{1+x^2}$	$\sqrt{\frac{\pi}{2}} e^{- \xi }$
e^{-ax^2}	$\frac{1}{\sqrt{2a}} e^{-\xi^2/4a}$

$$\widehat{f'(x)} = i\xi \widehat{f}(\xi)$$

$$\widehat{f''(x)} = -\xi^2 \widehat{f}(\xi)$$