

1 Diferencialni operatorji

Obravnavamo polje potenciala $\varphi = |\vec{A} \times \vec{r}|$, kjer je \vec{A} konstanten vektor.

$$E(r) = -\nabla\varphi = A \left(\frac{x}{\sqrt{x^2 + y^2}}, \frac{y}{\sqrt{x^2 + y^2}}, 0 \right)$$

Brez koordinat:

$$\begin{aligned}\varphi &= \sqrt{A^2 r^2 - (\vec{A} \cdot \vec{r})^2} \\ E(r) &= -\nabla\varphi(r) = -\frac{\nabla(A^2 r^2 - (\vec{A} \cdot \vec{r})^2)}{2\sqrt{A^2 r^2 - (\vec{A} \cdot \vec{r})^2}} \\ \nabla r^2 &= 2r\nabla r\end{aligned}$$

V cilindričnih koordinatah je $\nabla r = \hat{e}_r$.

$$\nabla(\vec{A} \cdot \vec{r})^2 = 2(\vec{A} \cdot \vec{r})\nabla(\vec{A} \cdot \vec{r}) = 2(\vec{A} \cdot \vec{r})\vec{A}$$

Definiramo vektor $\vec{\rho} = \vec{r} - \text{pr}_{\vec{A}}^{\perp}(\vec{r})$, kar nam da $E(r) = -\frac{\vec{\rho}}{\rho}$.