

The steady state under given conditions can be expressed with following equations:

$$(C_{Cl\_in} - C_{Na\_in} - C_{K\_in})V_i = -\frac{EC}{F},$$

$$(C_{Cl\_out} - C_{Na\_out} - C_{K\_out})V_o = \frac{EC}{F},$$

$$C_{K\_in} + C_{Na\_in} + C_{Cl\_in} = C_{K\_out} + C_{Na\_out} + C_{Cl\_out},$$

$$E = \frac{RT}{F} \ln \frac{C_{Cl\_in}}{C_{Cl\_out}}.$$

After some mathematical transformations of these equations, following formula can be written:

$$E = \frac{RT}{F} \ln \frac{1}{C_{Cl\_out}} \left[ C_{Cl\_out} - \frac{EC}{2F} \left( \frac{1}{V_i} + \frac{1}{V_o} \right) \right]$$

This can be transformed to a less complicated form:

$$\ln E_2 = \left( -\frac{m}{np} \right) E_2 + \left( \frac{m}{np} \right),$$

$$m = C_{Cl\_out} > 0,$$

$$n = \frac{RT}{F} > 0,$$

$$p = \frac{C}{2F} \left( \frac{1}{V_i} + \frac{1}{V_o} \right) > 0,$$

$$E_2 = \frac{m - pE}{m}.$$

Now, it can be easily conceived that there is only one solution for this equation, i.e.  $E_2 = 1$ , which yields further:  $E = (m - mE_2)/p = 0$ .