

*Joint European Doctorate in Fusion Science
and Engineering*

***Physics of RF Heating and
Current Drive***

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International Joint Doctorate In Fusion Science
And Engineering

FIRST PART

- ❖ Introduction on RF wave in Plasmas
- ❖ Basic theory of wave-plasma interaction
 - ❖ Unmagnetized Plasma
 - ❖ Wave Damping

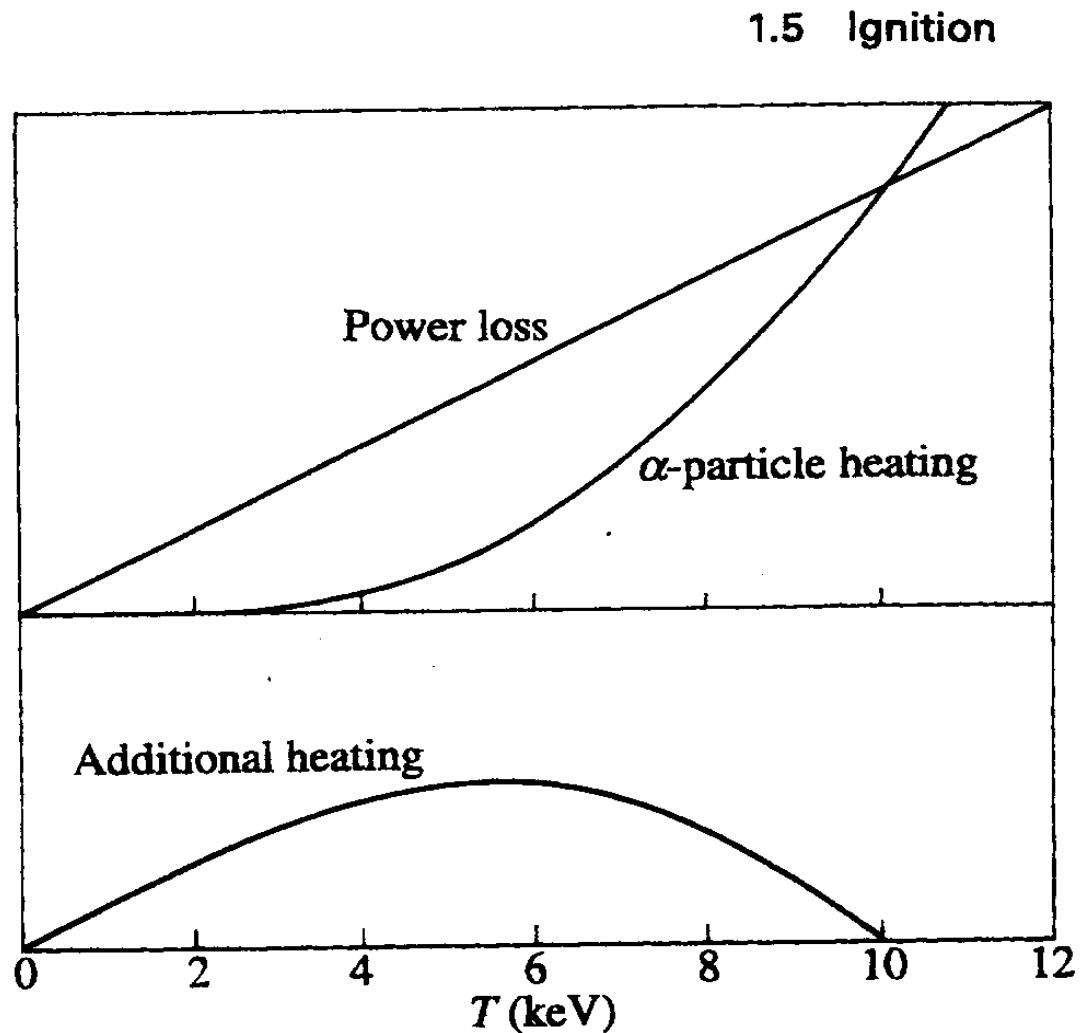
SECOND PART

- ❖ Electron Cyclotron Heating in Fusion Plasmas
 - ❖ ECCD mechanism
 - ❖ Wave Polarization relevance
 - ❖ Propagation and absorption in tokamak
- ❖ Application of ECH waves:
 - ❖ EC assisted start-up
 - ❖ MHD Control

Auxiliary Heating: why?

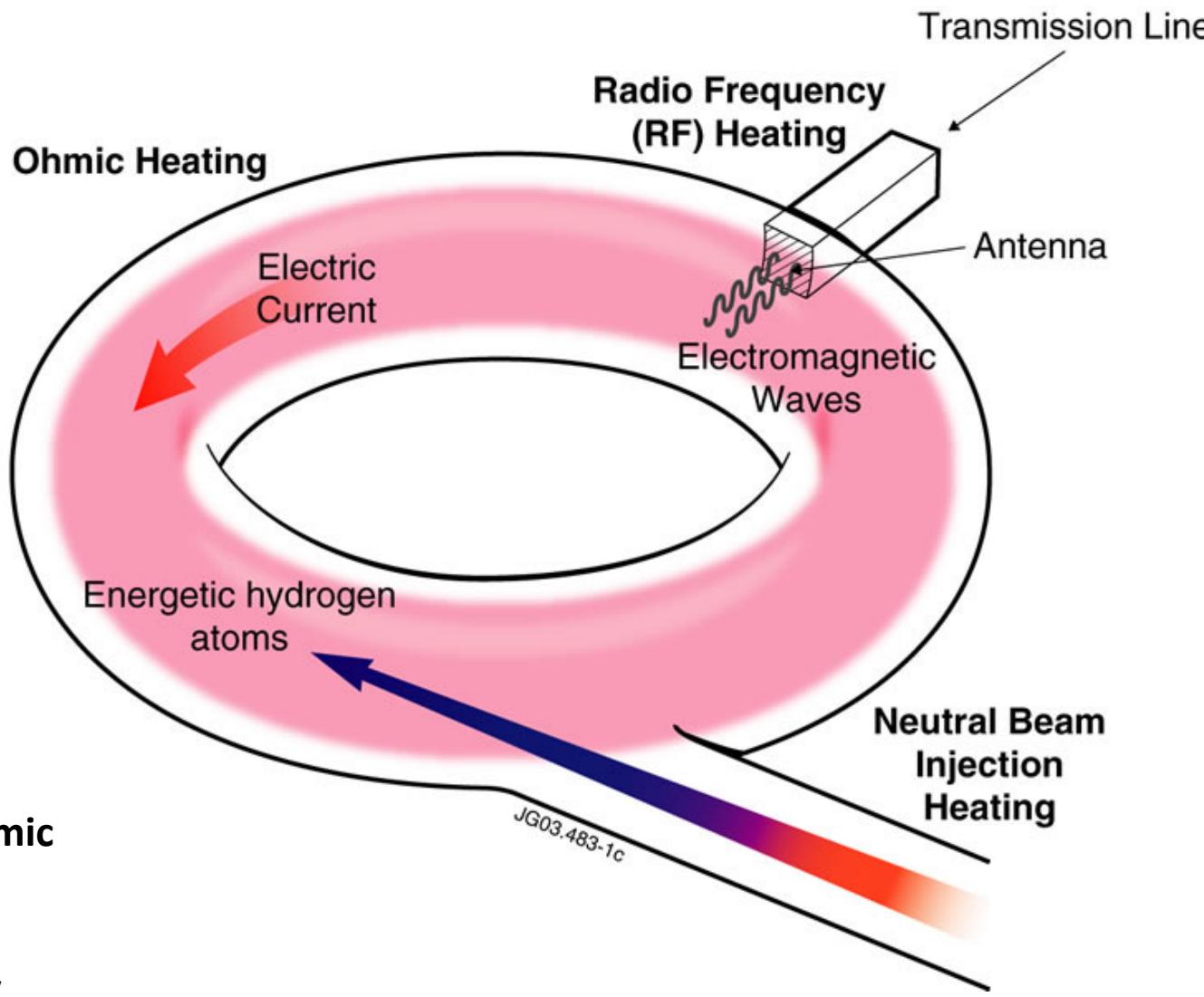
J.Wesson – Tokamaks –
1st Edition – 1987

Additional
or
Fundamental ?



Without external plasma heating temperature for Nuclear Fusion cannot be reached in any magnetic confinement device.

How to heat Plasma



Internal heating : Ohmic

External heatings:

NBI by Kinetic Energy

ICH, ECH, LH, IBW.... by E.M. wave

Main RF Heating waves exploited in Nuclear Fusion devices to heat plasma:

ECW: Electro Cyclotron Waves. Heat Electrons in millimetre wave range (2.45 GHz - 170 GHz)

LH: Lower Hybrid. Heat electrons in centimeter wave range

ICW: Ion Cyclotron Wave. Heat ions in RF wave range (MHz)

IBW: Ion Bernstein wave: Heat Ions in RF wave Range (MHz)

E.M. waves transfers energy to charged particle in plasma in correspondence of resonances, a combination of local conditions between magnetic field, particles energy/temperature and wave frequency.

Heating System in main Experiments

Device	NBI	ECRH	ICRH	LH
JET	<i>32 MW</i>		<i>10 MW</i>	<i>7.2 MW</i>
AUG	20 MW	6 MW	6 MW	
FTU		<i>1.4 MW</i>	<i>0.5 MW of IBW</i>	<i>2.4 MW</i>
D-IIID	20 MW	4 MW	1 MW Helicon FW	
WEST		2 MW	9 MW	7MW
TCV	1MW	5 MW		
JT60-SA	34 MW	7MW		
W7-X	19 MW	10 MW	1.5 MW	
EAST	8 MW	4 MW	12 MW	10 MW
KSTAR	8 MW	0.5 MW	6 MW	

ITER :

NNBI =32 MW

ECRH = 24 MW +24 MW + ?

ICRH= 10 MW

DTT :

NNBI = 10 MW

ECRH = 32 MW

ICRH= 8 MW

SPARC: ICRH for 48 MW

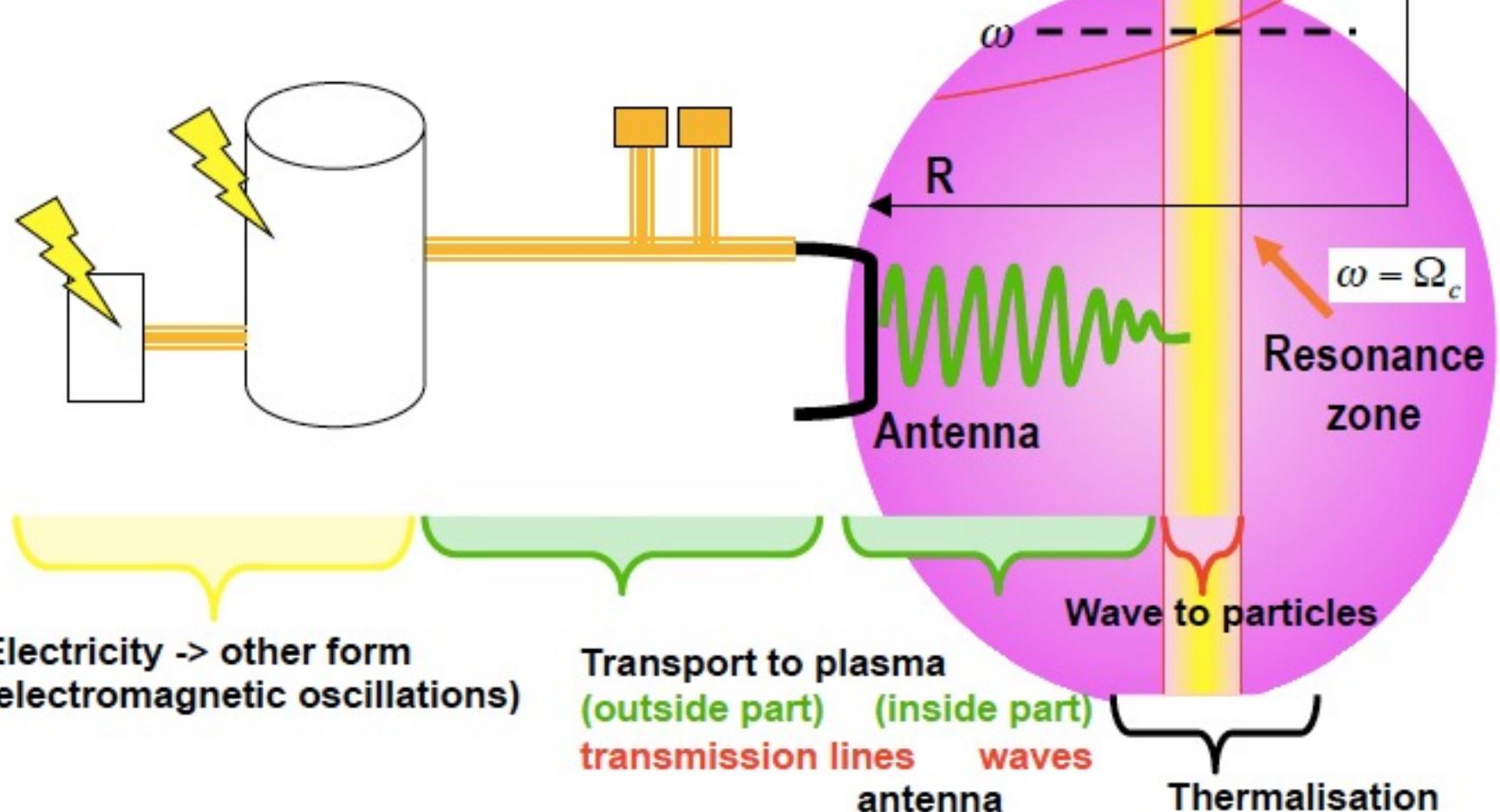
DEMO project is studying an option fully relying on ECRH

RF heating system will play major role in future tokamaks and in perspective for the Reactor

Cyclotronic Wave Heating

$$\Omega_c = \frac{ZeB}{m}$$

IPP



Tasks	ECRH	ICRH	LH
Break down & Plasma start up	X	X	
Plasma Current Ramp up	X	X	X
H-mode access	X	X	X
Electron Heating	X	X	X
Direct Ion Heating		X	
Not Inductive Current drive	X		X
MHD Control	X	X	
Fast Particle Generation		X	
Profiles Control	X	X	X
Impurity Accumulation Avoidance	X	X	
Transport Studies	X		
Diagnostics (heat pulse)	X		
Wall Cleaning	X	X	

Energy transfer from e.m. waves to plasma

When e.m. waves crosses plasma its **Electric field** accelerates charged particles that transfer this energy by collision to plasma

Collisional absorption scales with $T_e^{-3/2}$ and is ineffective (as ohmic ones) to heat a hot plasma (as required to reach the fusion conditions)

Waves can transfer energy to plasma also trough **resonant mechanism** that are **collisionless** and can produce strong direct heating

In a multispecies magnetized plasma there are several of resonances.

The variety of waves existing in a magnetized plasma allows different RF heating schemes, generally at different frequencies.

An RF Heating system based on e.m. waves is composed by 3 main elements:

- **Power generator**
- **Low loss transmission lines**
- **Antenna**

Antenna launches (couples) waves in the plasma

→ waves propagate up to absorption layer and transfer energy (heat or momentum) to plasma

→ The location of the absorption layer should be controlled

The study of the **waves propagation** is at the basis of the selection of the proper RF heating systems (i.e. of the frequency and of the antenna)

E.M. wave propagation in plasma is (can be) quite complex to be treated formally and is outside the scope of this lecture.

Some simplifications are considered to approach the problem of a realistic tokamak plasma.

The most common and valid approach is the:
cold magnetized plasma model

*The model is enough accurate to describe wave propagation in plasma, **except in regions close to resonance and cut-off***

Close to these special regions the **thermal** corrections become important because the wave phase velocity is comparable to the thermal one and the perpendicular wave length (wrt the external magnetic field) is similar to the Larmor radius.

To study energy absorption it is necessary the *warm model*

Cold model -> fluid equations, no temperature effect

Warm Model -> finite Larmor radius plays a role

- **Coupling** cold plasma
 - **Propagation** cold plasma (warm plasma)
 - **Absorption** warm plasma

The mathematical approach is the following:

Maxwell equations + Generalize Ohm's law applied to

Plane waves:

$$\tilde{E}(r,t) = \tilde{E}_0 e^{(-i\omega t + \vec{k} \cdot \vec{r})}$$

where

\mathbf{k} = wave vector = $2\pi/\lambda$

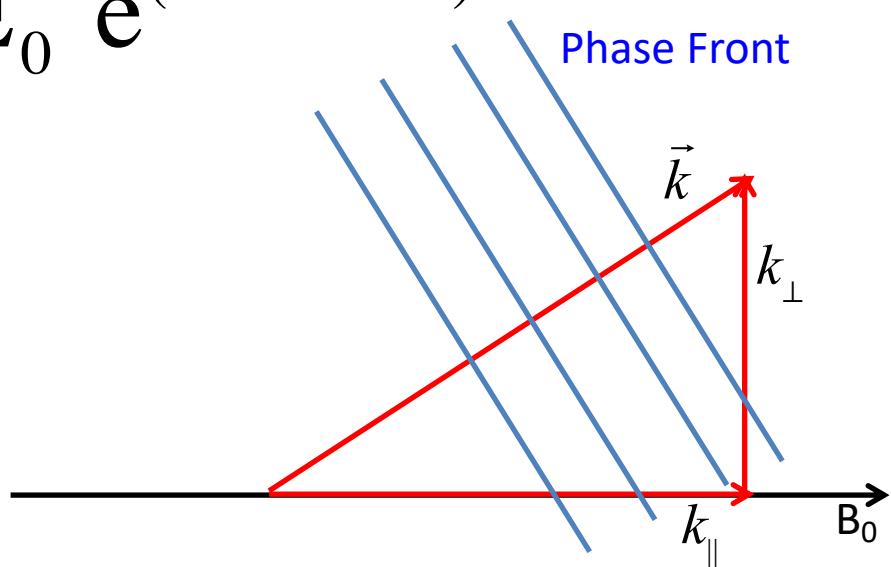
ω = angular frequency = $2\pi f$

Other useful quantities:

v_{ph} = phase velocity = ω/k

v_g = group velocity = $d\omega/dk$

$N = v_{ph}/c$ = refractive index = $k/\omega c$



\vec{k} Response of Plasma

ω Fixed by Generator

Maxwell equations



$$\left. \begin{array}{l} \vec{\nabla} \cdot \vec{B} = 0 \\ \vec{\nabla} \cdot \vec{E} = 4\pi\rho \\ \vec{\nabla} \times \vec{B} = \frac{4\pi}{c} \vec{j} + \frac{1}{c} \frac{\partial \vec{E}}{\partial t} \\ \vec{\nabla} \times \vec{E} = -\frac{1}{c} \frac{\partial \vec{B}}{\partial t} \end{array} \right\}$$

Generalized Ohm's Law



$$\vec{j} = j(\vec{E}, \vec{B}) \rightarrow \vec{j} = \underline{\underline{\sigma}}(\omega, k) \cdot \vec{E}_{\omega, k}$$

Dielectric Tensor

Plane waves:

$$\tilde{E} = E_0 \cos(\vec{k} \cdot \vec{r} - \omega t + \phi) = E_0 e^{i(\vec{k} \cdot \vec{r} - \omega t + \phi)}$$

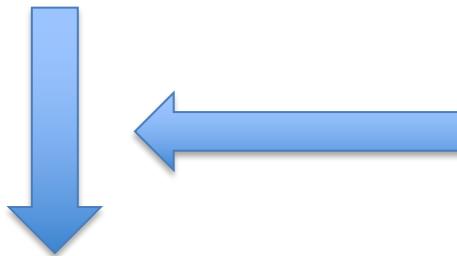


$$\frac{\partial}{\partial t} \rightarrow -i\omega$$

$$\vec{\nabla} \rightarrow i\vec{k}_{15}$$

$$\nabla \times (\vec{\nabla} \times \vec{E}) = -\frac{1}{c} \frac{\partial(\nabla \times \vec{B})}{\partial t}$$

$$\vec{\nabla} \cdot \vec{E} = 4\pi\rho$$



$$\vec{\nabla} \times \vec{B} = \frac{4\pi}{c} \vec{j} + \frac{1}{c} \frac{\partial \vec{E}}{\partial t}$$

$$4\pi\nabla\rho - \nabla^2\vec{E} = -\frac{1}{c} \frac{\partial}{\partial t} \left(\frac{4\pi}{c} \vec{j} + \frac{1}{c} \frac{\partial \vec{E}}{\partial t} \right) + \vec{j} = \underline{\underline{\sigma}}(\omega, k) \cdot \vec{E}_{\omega, k}$$

Wave Equation

$$\underline{k} \times (\underline{k} \times \underline{E}_{\omega, \underline{k}}) + \frac{\omega^2}{c^2} \underline{\underline{K}} \cdot \underline{\underline{\epsilon}}_{\omega, \underline{k}} = 0$$

$$\underline{\underline{K}} = \underline{\underline{1}} + \frac{\underline{\underline{\sigma}}}{i\omega \epsilon_0}$$

Dielectric Tensor

Wave Equation is **exact**, no approximations have been introduced



$$\underline{k} \times (\underline{k} \times \underline{E}_{\omega, \underline{k}}) + \frac{\omega^2}{c^2} \underline{\underline{K}} \cdot \underline{\underline{E}}_{\omega, \underline{k}} = 0$$

Admit solution only if



defining

N = refractive index

$$\underline{N} = \frac{c}{v_{ph}} = \frac{ck}{\omega}$$

$$\det[\underline{N} \times (\underline{N} \times \underline{\underline{1}}) + \underline{\underline{K}}(\omega, \underline{N})] = 0$$

Dispersion Relation

$$\underline{\underline{K}} = \underline{\underline{1}} + \frac{\underline{\sigma}}{i\omega\varepsilon_0}$$

Plasma



Maxwell Equations

Motion Equation

$$n_\alpha m_\alpha \frac{\partial \bar{u}_\alpha}{\partial t} + n_\alpha m_\alpha (\bar{u}_\alpha \cdot \bar{\nabla}) \bar{u}_\alpha = n_\alpha q_\alpha (\bar{E} + \frac{\bar{u}_\alpha}{c} \times \bar{B})$$

Continuity
Equation

$$\frac{\partial n_\alpha}{\partial t} + \bar{\nabla} \cdot (n_\alpha \bar{u}_\alpha) = 0$$

Perturbing Technique

$$f = f_0 + f_1$$

Plasma Model

$$u_0 = E_0 = B_0 = 0$$

$$n_0 \neq 0 \text{ density}$$

Dielectric Tensor



Cold un-magnetized plasma

~~$$\eta_\alpha m_\alpha \frac{\partial \bar{u}_\alpha}{\partial t} + n_\alpha m_\alpha (\bar{u}_\alpha \cdot \bar{\nabla}) \bar{u}_\alpha = n_\alpha q_\alpha (\bar{E} + \frac{\bar{u}_\alpha}{c} \times \bar{B})$$~~

$$-i\omega m_\alpha \bar{u}_{\alpha 1} = q_\alpha \bar{E}_1$$

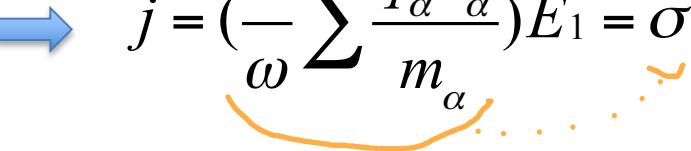
$$\bar{u}_{\alpha 1} = \frac{i}{\omega} \frac{q_\alpha}{m_\alpha} \bar{E}_1$$

$$u = u_0 + u_1 = u_1$$

$$E = E_0 + E_1 = E_1$$

$$B = B_0 + B_1 = B_1$$

Add the current

$$\bar{j} = \sum q_\alpha n_\alpha \bar{u}_\alpha \quad \rightarrow \quad \bar{j} = \left(\frac{i}{\omega} \sum \frac{q_\alpha^2 n_\alpha}{m_\alpha} \right) \bar{E}_1 = \sigma \bar{E}_1$$


$$\bar{j} = \sum_{\alpha} q_{\alpha} n_{0\alpha} \bar{u}_{1\alpha} = \frac{i}{\omega} \left(\sum_{\alpha} \frac{n_{0\alpha} q_{\alpha}^2}{m_{\alpha}} \right) \bar{E}_1$$



Electrical conductivity

From motion equation:
Ohm's Law

- Scalar coefficient
- Independent from k

The dielectric tensor*:

$$K = 1 - \frac{4\pi\sigma(\omega, k)}{i\omega} = 1 - \frac{1}{\omega^2} \sum_{\alpha} \frac{4\pi n_{0\alpha} q_{\alpha}^2}{m_{\alpha}} = 1 - \frac{\omega_p^2}{\omega^2}$$

* Pay attention to different system (SI)

Where $\omega_p^2 = \sum_{\alpha} \frac{4\pi n_{0\alpha} q_{\alpha}^2}{m_{\alpha}}$

Is the Plasma Frequency,
summarized over all the α species

And the Wave Equations is:

$$\left[\frac{k^2 c^2}{\omega^2} \left(\frac{\underline{k}\underline{k}}{\underline{k}^2} - \underline{I} \right) + K \underline{I} \right] : \underline{E} = 0$$



Dielectric tensor

That written in matrix

$$\begin{pmatrix} K - \frac{k^2 c^2}{\omega^2} & 0 & 0 \\ 0 & K - \frac{k^2 c^2}{\omega^2} & 0 \\ 0 & 0 & K \end{pmatrix} \begin{pmatrix} E_x \\ E_y \\ E_z \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$

Admits solution only if $\text{Det}=0$ that leads to:

$$K \left(K - \frac{k^2 c^2}{\omega^2} \right) = 0$$

That has 2 solutions:

- | ➤ $K=0$
- $K= k^2 c^2 / \omega^2$

$\kappa=0$

$$\omega^2 = \omega_p^2$$

Longitudinal

$$k \parallel E$$

From

$$\kappa = k^2 c^2 / \omega^2$$

$$\omega^2 = \omega_p^2 + k^2 c^2$$

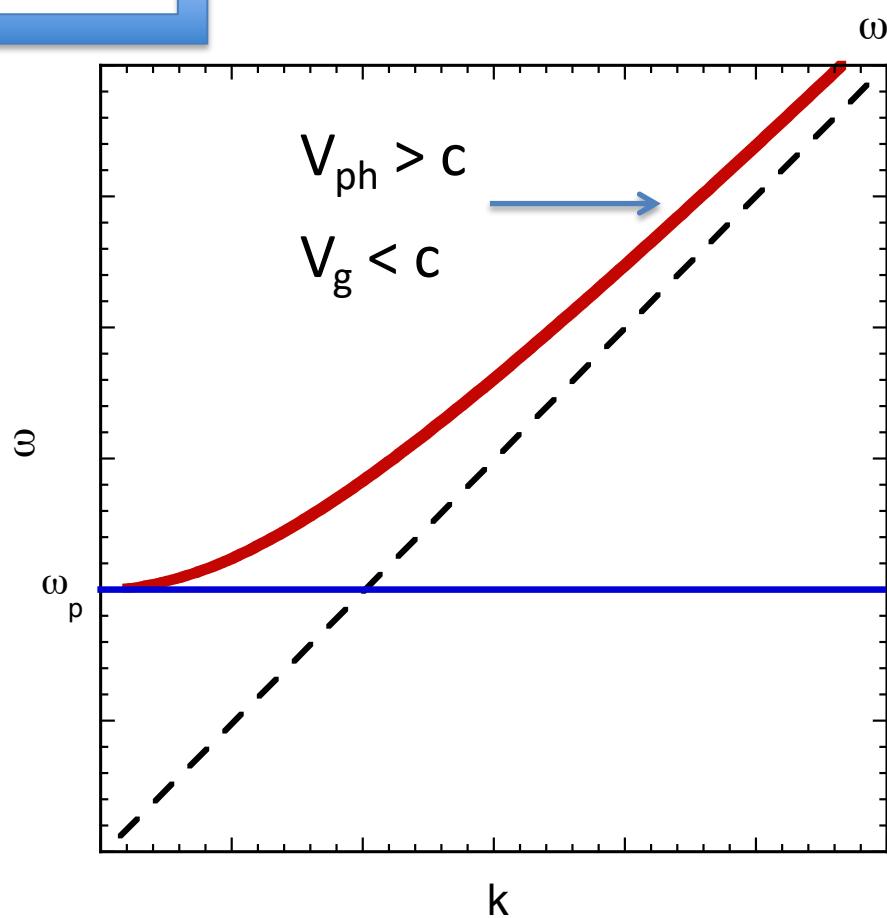
Transverse

$$k \perp E$$

$$K = 1 - \frac{\omega_p^2}{\omega^2}$$

$$v_{ph} = \frac{\omega}{k}$$

$$v_g = \frac{d\omega}{dk}$$



Phase velocity
faster than c

$v_g = 0$

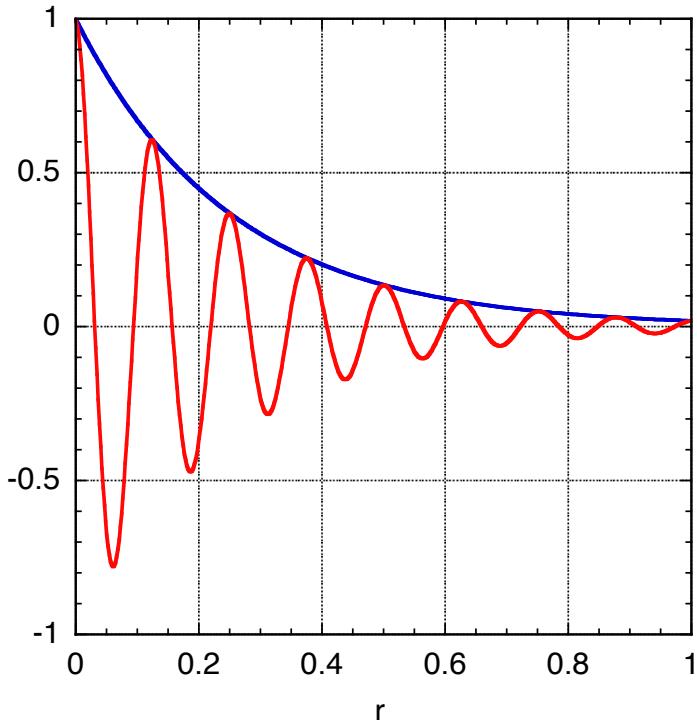
For a transverse wave, extracting k :

cutoff

$$k = \sqrt{(\omega^2 - \omega_p^2) / c^2}$$

The wave can propagate only for

$$\omega > \omega_p$$



if

$$\omega < \omega_p$$



$$k = i |k|$$



$$\tilde{E} = E_0 e^{-kr} \cdot e^{-i(\omega t + \phi)}$$

Wave Damping

Collisionless dissipation of an electromagnetic waves for

- Ion cyclotron
- Electron cyclotron
- Lower hybrid

is governed by the following relationship:

$$\omega - k_{\parallel} v_{\parallel j} - n |\omega_{cj}| = 0$$

Landau Damping

$n=0$ correspond to **Landau damping**:

→ E_{\parallel} accelerates particle in // direction

It is relevant for **Lower Hybrid** and for fast wave in **Ion cyclotron** range of frequency

Basically Landau damping occurs when electron velocity is equal to the phase velocity of the waves

As phase velocity ranges from thermal to light speed the wave can resonate with thermal and suprathermal electrons

Absorption: Collisionless Damping

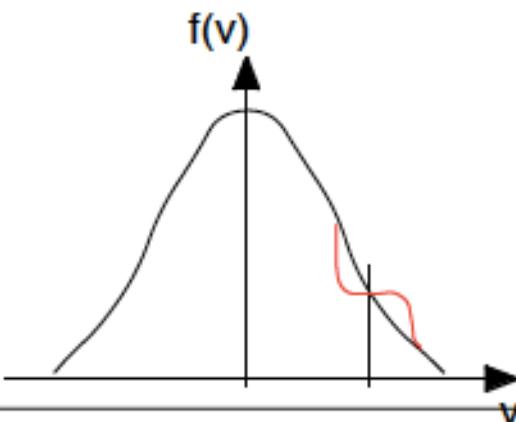
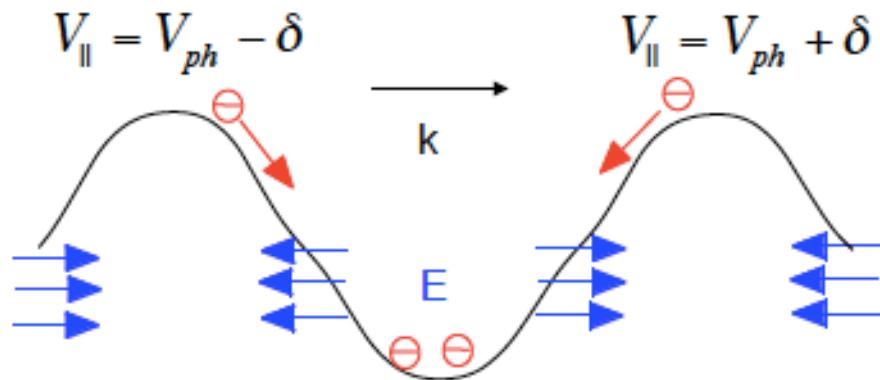
Energy transfer only if

$$\omega - n\omega_c = k_{\parallel}v_{\parallel}$$

$$n = 0$$

Resonance condition:

$$\omega - k_{\parallel}v_{\parallel} = 0$$



$$\frac{\partial f(v)}{\partial v} < 0$$

The deformation of the distribution function increases the energy of the electron system.

Landau damping: Increase of parallel momentum

Cyclotron Resonance



$n \neq 0$ correspond to **cyclotron resonance**

Particles gain energy in perpendicular direction
Only momentum (?)

The condition of resonance can be written

$$\nu_{//j} = \frac{\omega}{k_{//}} - \frac{n|\omega_{cj}|}{k_{//}}$$

3

It is valid for particles with velocity smaller than the wave phase velocity ($n > 0$)

$n=1$ correspond to fundamental resonance:
valid for

Electron cyclotron

Ion cyclotron minority heating

$n=2$ correspond to 2nd harmonic resonance:
valid for

Electron cyclotron

Ion cyclotron

Absorption: Cyclotron Damping

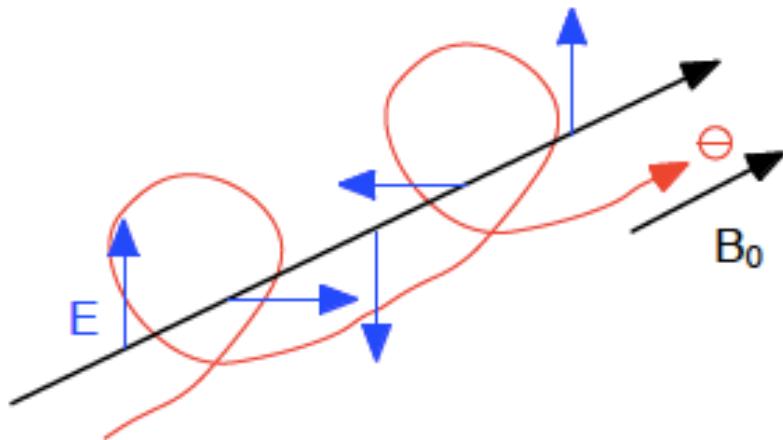
Energy transfer only if

$$\omega - n\omega_c = k_{\parallel}v_{\parallel}$$

$$n = 1$$

Resonance condition:

$$\omega - k_{\parallel}v_{\parallel} = \omega_c$$



Cyclotron Damping: increase of perpendicular momentum

Absorption depends on the temperature: higher absorbs better

3

ICRH: can use both cyclotron or Landau damping, **used to heat ions and generate fast particle and current**

Fast particle from landau

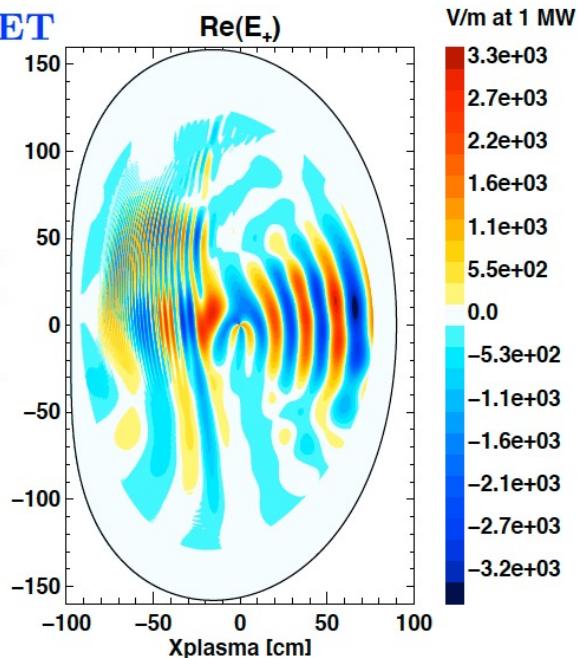
LHCD: only Landau damping, **to generate non inductive current**

Works better at high temps

ECRH: only cyclotron damping, **to heat electrons and generate non inductive current**

f = 42 MHz

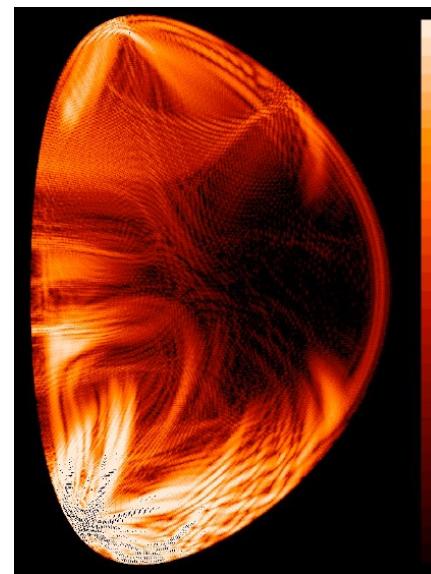
JET



Ion Cyclotron Waves

courtesy R Bilato, MPI- IPP

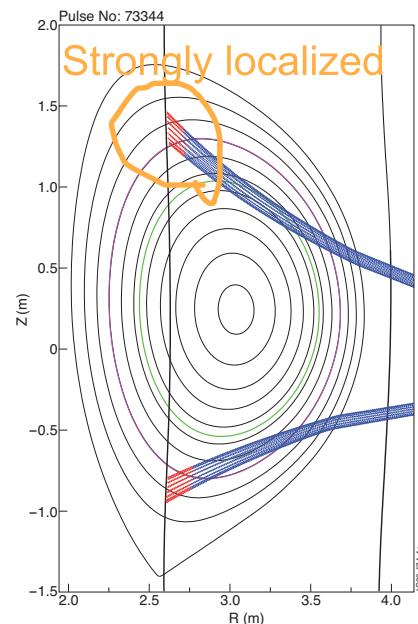
f = 3.7GHz



Lower Hybrid Waves

courtesy R Bilato, MPI- IPP

f = 170 GHz



Electron Cyclotron Waves

D. Farina, IFP-CNR, 2010 proposal

Physics of RF Heating and Current Drive

Part II: Applications of EC waves

SECOND PART

- ❖ Electron Cyclotron Heating in Fusion Plasmas
 - ❖ ECCD mechanism
 - ❖ Wave Polarization relevance
 - ❖ Propagation and absorption in tokamak
- ❖ Application of ECH waves:
 - ❖ EC assisted start-up
 - ❖ MHD Control

ECRH: Electron Cyclotron Resonant Heating

ECCD: Electron Cyclotron Current Drive

*The only Heating System able to deposit power or current in
highly localized and controllable way*

The e.m. wave gives energy to particles rotating at the same frequency around the (toroidal) field B_T .

Resonant with the mode in the plasma

The simplest and quick formula for a specie x is:

$$\omega_0 = n\Omega_{cx} = n \frac{eB}{m_x c}$$

Harmonic

* Maxwellian distribution & perpendicular injection

For electrons:

$$f_0(\text{GHz}) = 28(\text{GHz}) \cdot B_T(T) \cdot n$$

For ions:

$$f_0(\text{MHz}) = 15.2(\text{MHz}) \cdot B_T(T) \cdot \frac{Z}{A} \cdot n$$

Propagation, cut-off & resonances

For ECRH/ECCD application we are considering transversal e.m. waves propagating in vacuum and in the plasma without evanescent region.

Ecrh can go through plasma and be absorbed only
in the region of interest

The waves met cut-off and/or resonances depending by: **wave polarization** & **harmonic**, **plasma density**, **magnetic field** and θ .

Propagation limits are defined by the two limits in the diffraction index

$N=0 \rightarrow k=0 \rightarrow$ no wave propagation: **Cut-off**

At cutoff there is reflection

$N=\infty \rightarrow k=\infty \rightarrow$ wave absorption: **Resonance**

Cut-off $\rightarrow N=0 \quad \epsilon_R \epsilon_L \epsilon_3 = 0$

Resonance $\rightarrow N=\infty$

$$N^2 = \frac{\epsilon_L \epsilon_R}{\epsilon_1}$$

$$\omega = \Omega_{ce}$$

Electron Cyclotron

$$\omega = \omega_p$$

Density

cutoff (more stuff,
watch video)

Right and Left

$$\omega = \omega_{R/L} \cong \frac{1}{2} (\pm |\Omega_e| + \sqrt{\Omega_e^2 + 4\omega_p^2})$$

5

$$\omega_{UH}^2 = \Omega_e^2 + \omega_{pe}^2$$

Upper Hybrid

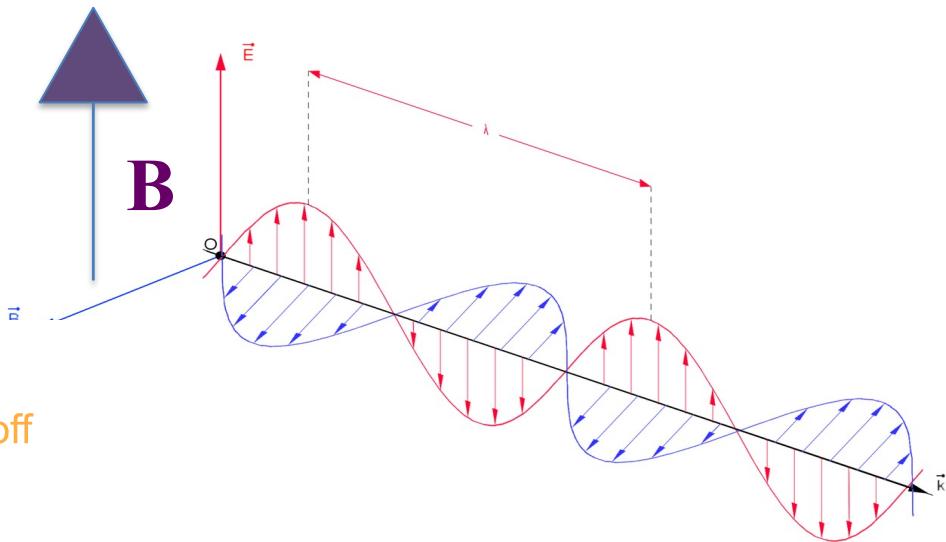
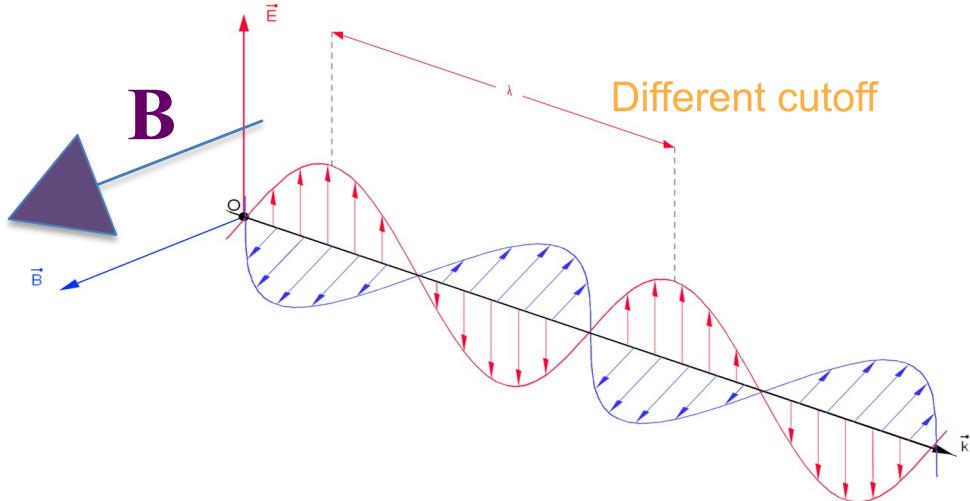
$$\omega_{LH}^2 \approx \Omega_e \Omega_i \frac{1 + \frac{\Omega_i^2}{\omega_{pi}^2}}{1 + \frac{\Omega_e^2}{\omega_{pe}^2}}$$

Lower Hybrid

Wave polarization

The polarization of e.m. wave in magnetised plasma is defined as the direction of the Wave Electric Field respect to external Magnetic Field direction:

O-Mode (ordinary) when Electric field is parallel to B_0



X-Mode (extraordinary) when Electric field is perpendicular to B_0

- The modes exist only in plasma
- Propagation depends on plasma parameter and N_{\parallel}
- The propagating wave is a mixture of the two (elliptic polarization)

Cut-off & polarization

An e.m. wave propagating in plasma can meet **resonances** and **cut-off**:

At a cut-off surface the waves is reflected backward.

Cut-off (and some resonance) can depend on the polarization

Density Cut-off

$$\omega = \omega_p$$



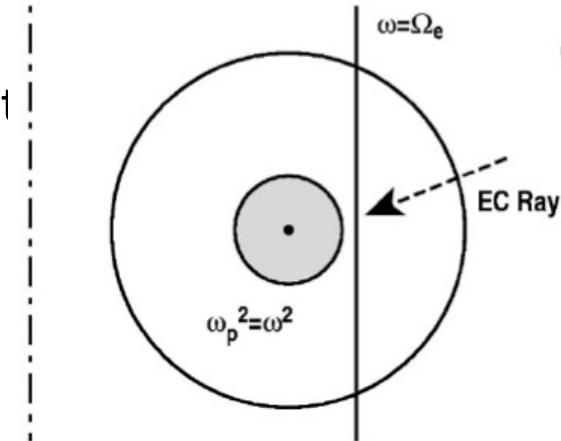
Ordinary Mode

$$n_e < n_c = \frac{m_e \omega_o^2}{4\pi e^2} = \frac{B_{\perp}^2(T)}{10.3} l^2 [10^{20} m^{-3}]$$



Extraordinary Mode

$$n_e < l(l-1)n_c \quad l > 1$$



$$f = 140 \text{ GHz}$$

$$\text{O1}_{\text{FTU}} \quad n_c = 2.4 \cdot 10^{20} \text{ m}^{-3}$$

$$\text{X2}_{\text{AUG}} \quad n_c = 1.21 \cdot 10^{20} \text{ m}^{-3}$$

$$\text{X3}_{\text{TCV}} \quad n_c = 1.61 \cdot 10^{20} \text{ m}^{-3}$$

XM propagation & Cut-off

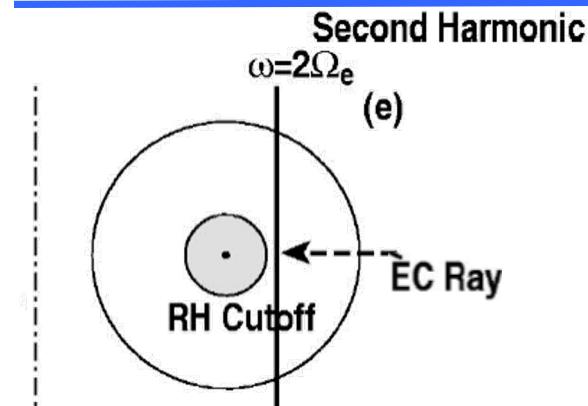
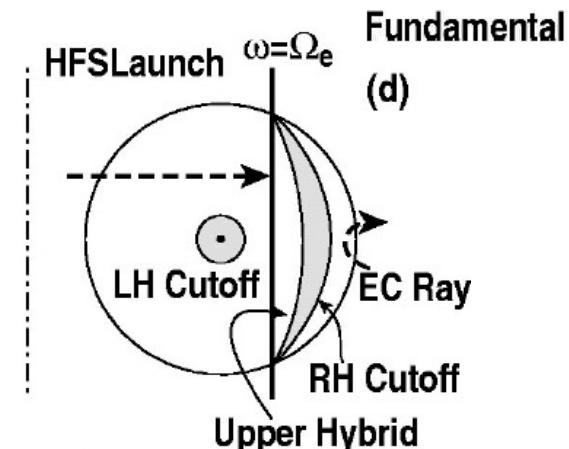
1st Harmonic XM has 2 additional cut-off, the right and left hand cut-off.

$$\omega = \omega_{R/L} \approx \frac{1}{2} (\pm |\Omega_e| + \sqrt{\Omega_e^2 + 4\omega_p^2})$$

The RH cut-off shield the Upper Hybrid and the cyclotron resonance for a wave coming from LFS.

For this reason the XM can be used only with second harmonic.

The LH cut-off is equivalent to a density cut-off.



$$P_{abs} = P_0(1 - e^{-\tau}) \quad \text{where} \quad \tau = \int \alpha \cdot dl$$

α = local absorption coefficient in m⁻¹

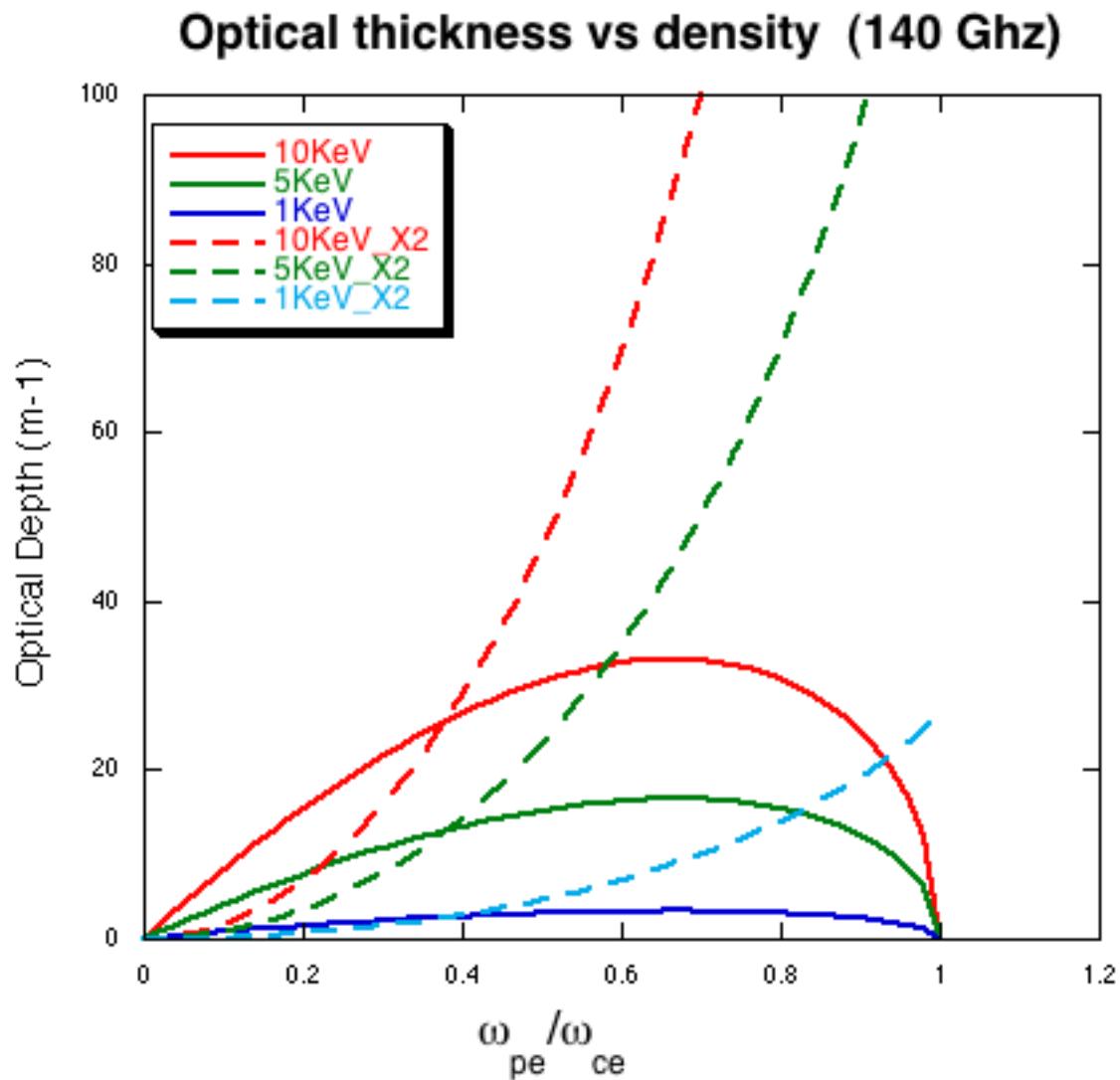
Optical thickness τ changes with polarization, $N_{//}$ and harmonic number. In case of fundamental OM with $N_{//}=0$:

$$\tau_{OM1} = \pi^2 \frac{\omega_{pe}^2}{\omega_{ce}^2} \left(1 - \frac{\omega_{pe}^2}{\omega_{ce}^2}\right)^{1/2} \frac{v_{Te}^2}{c^2} \frac{R}{\lambda}$$

Absorption depends
on Te and n_e

$$\tau_{OX2} = 2\pi^2 \frac{\omega_{pe}^2}{\omega_{ce}^2} \frac{\left(6 - \frac{\omega_{pe}^2}{\omega_{ce}^2}\right)^2}{\left(6 - 2\frac{\omega_{pe}^2}{\omega_{ce}^2}\right)^2} \frac{v_{Te}^2}{c^2} \frac{R}{\lambda}$$

Optical thickness



$$f_o = 140 \text{ GHz}$$

$$N_{||} = 0$$

with $\tau > 3$: $P_{abs} \sim 95\%$

Absorption depends on Te and ne
XM2 is stronger absorbed approaching cut-off

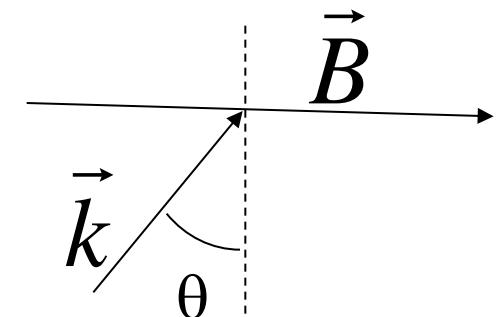
A more complete resonance condition is:

$$\frac{1}{\gamma} \cdot n\Omega_{ce} = \omega_o - \vec{k} \cdot \vec{v} = \omega_o - k v_{\parallel} \cos \theta$$

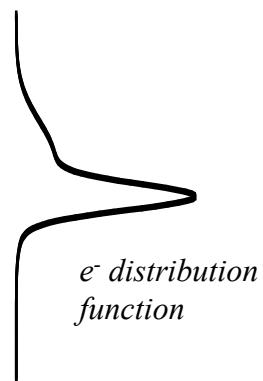
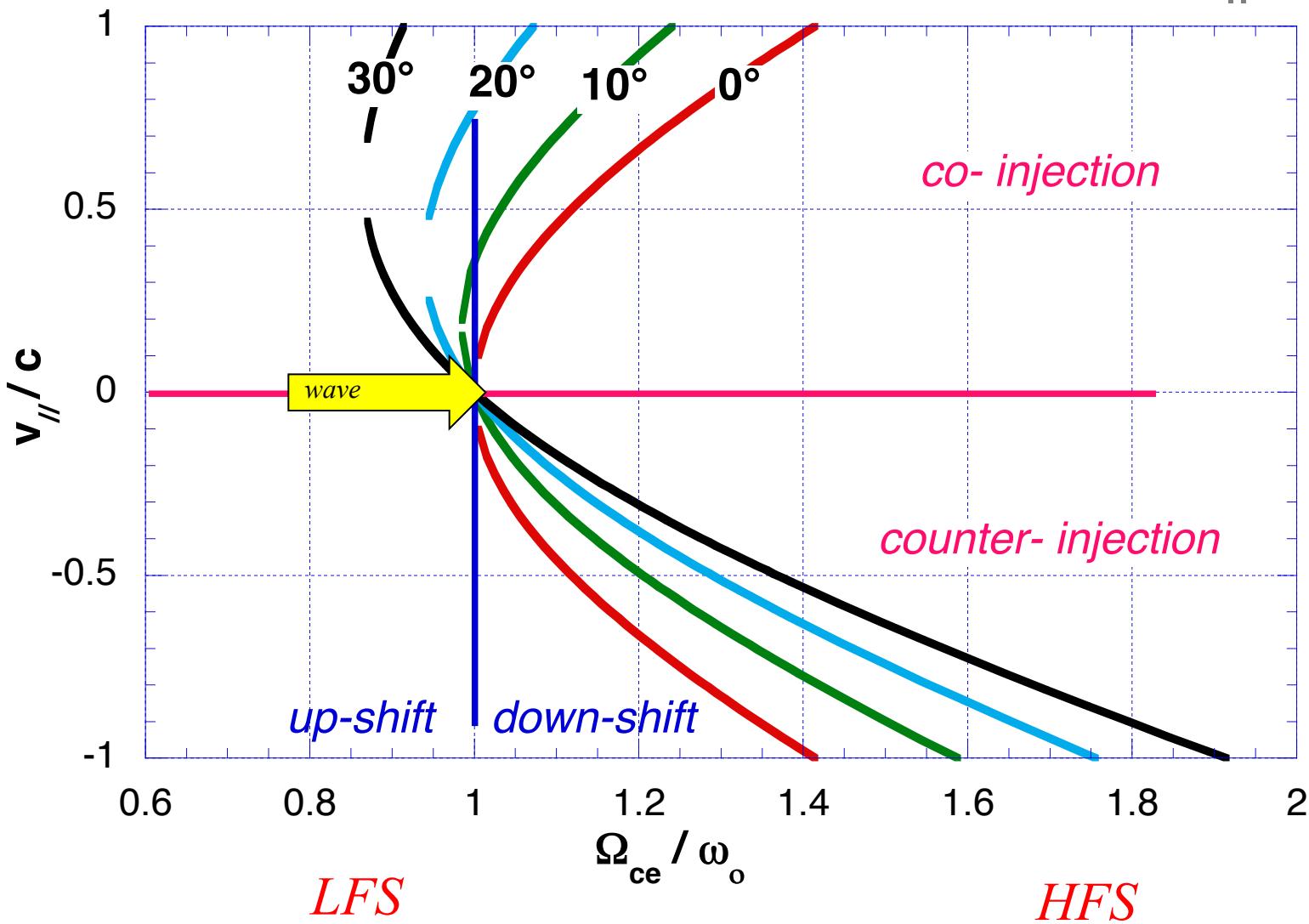
Relativistic Gamma *Electron velocity* *Angle between wave propagation and the perpendicular to the magnetic field*

$$\gamma = \frac{1}{\sqrt{1 - \frac{v_{\parallel}^2}{c^2}}}$$

$$\frac{\Omega_{ec}}{\omega_o} = \frac{c/v_{\parallel}}{\sqrt{c/v_{\parallel}^2 - 1}} \left(1 - \frac{N_{\parallel}^{EC}}{c/v_{\parallel}} \right)$$



The Graphic Solution of Resonance Equation at different $N_{||}$



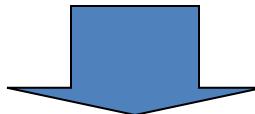
EC waves gives only **perpendicular energy** to electrons:
no net longitudinal momentum transfer

The EC wave can produce non inductive current drive exploiting two different and opposite effects:

- **Fisch&Boozer effects** (effect on collisionality)
- **Ohkawa effects** (trapped particles balance)

ECCD **efficiency** is **low**, but the high **localization** can be exploited for **current profile control** aiming to **MHD stability** or q profile shaping.

Co-injection: power absorption on co-current electrons



⊥ Energy increase



Collisionality reduction



Not-symmetric losses (co electrons lost less than cnt electrons)



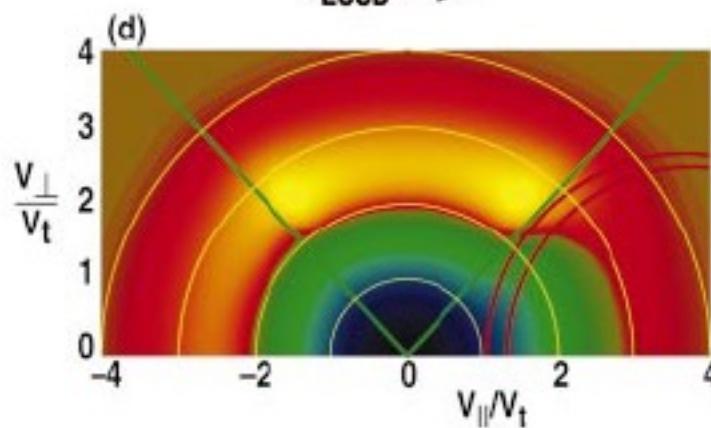
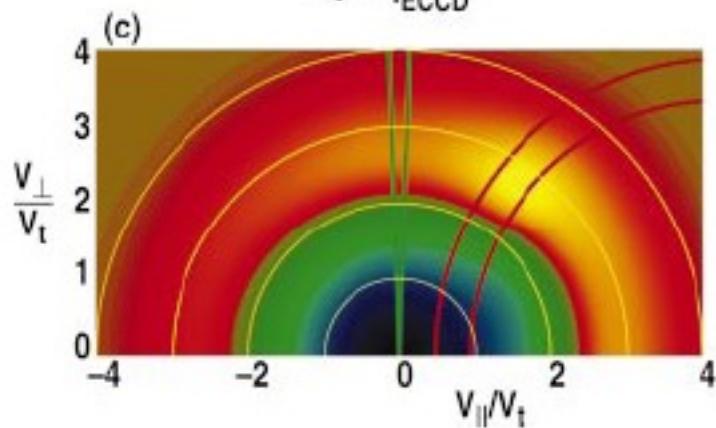
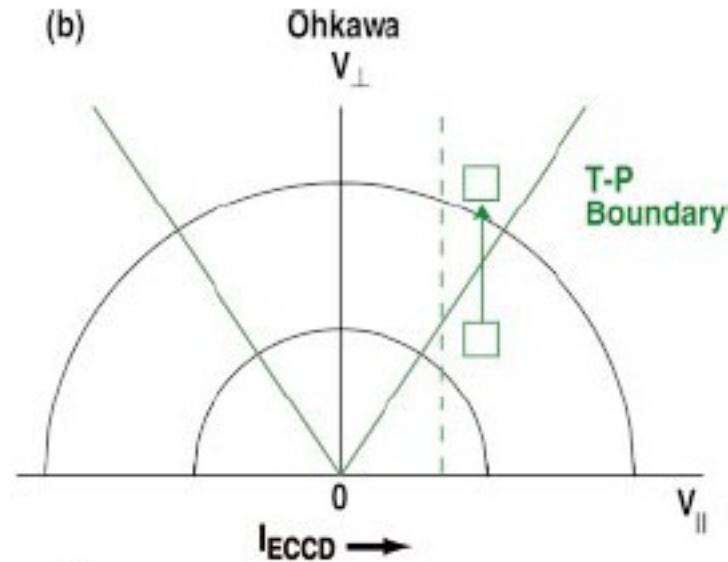
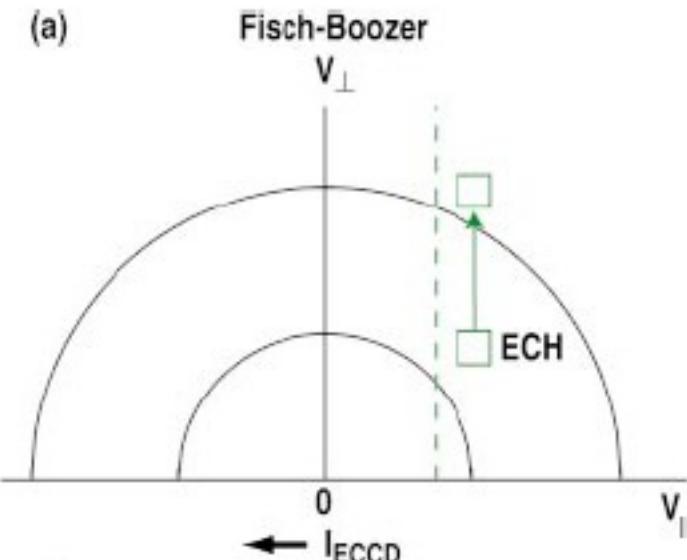
Net co-current generation

In toroidal geometry the presence of trapped particle is at the basis of Okhawa ECCD effect.

Electrons, gaining E_{\perp} from EC wave, can enter in the **trapped cone**, and stops to drive current (due to the bouncing of such particle in the trapped *banana*).

This create an **asymmetry** for the particles going in the opposite direction than does not absorb EC wave and continue to circulate.

This asymmetry produce a net current drive term in the **opposite** direction with respect to the resonant electrons absorbing the wave.



EC Power Deposition

EC wave is usually fully absorbed at 1st pass (if $T_e > 2$ KeV and $n_e \sim 0.1 n_{\text{cutoff}}$)

The deposited power is strongly localized, depending on the beam intersection with the resonant layer

The profile of power deposition is calculated (in all experiments) using Ray Tracing and/or Beam Tracing codes well consolidates and benchmarked. Result depends on accuracy of equilibrium, T_e and n_e profiles, being known the mirrors steering.

Main Codes used: **TORBEAM**, **ECGWB**, **GRAY**, **TORAY-GA**, **BANDIT-3D** (*beam tracing*, ray-tracing)

The amount of CD driven by EC wave is a function of :

Local Temperature

Local Zeff

Wave frequency

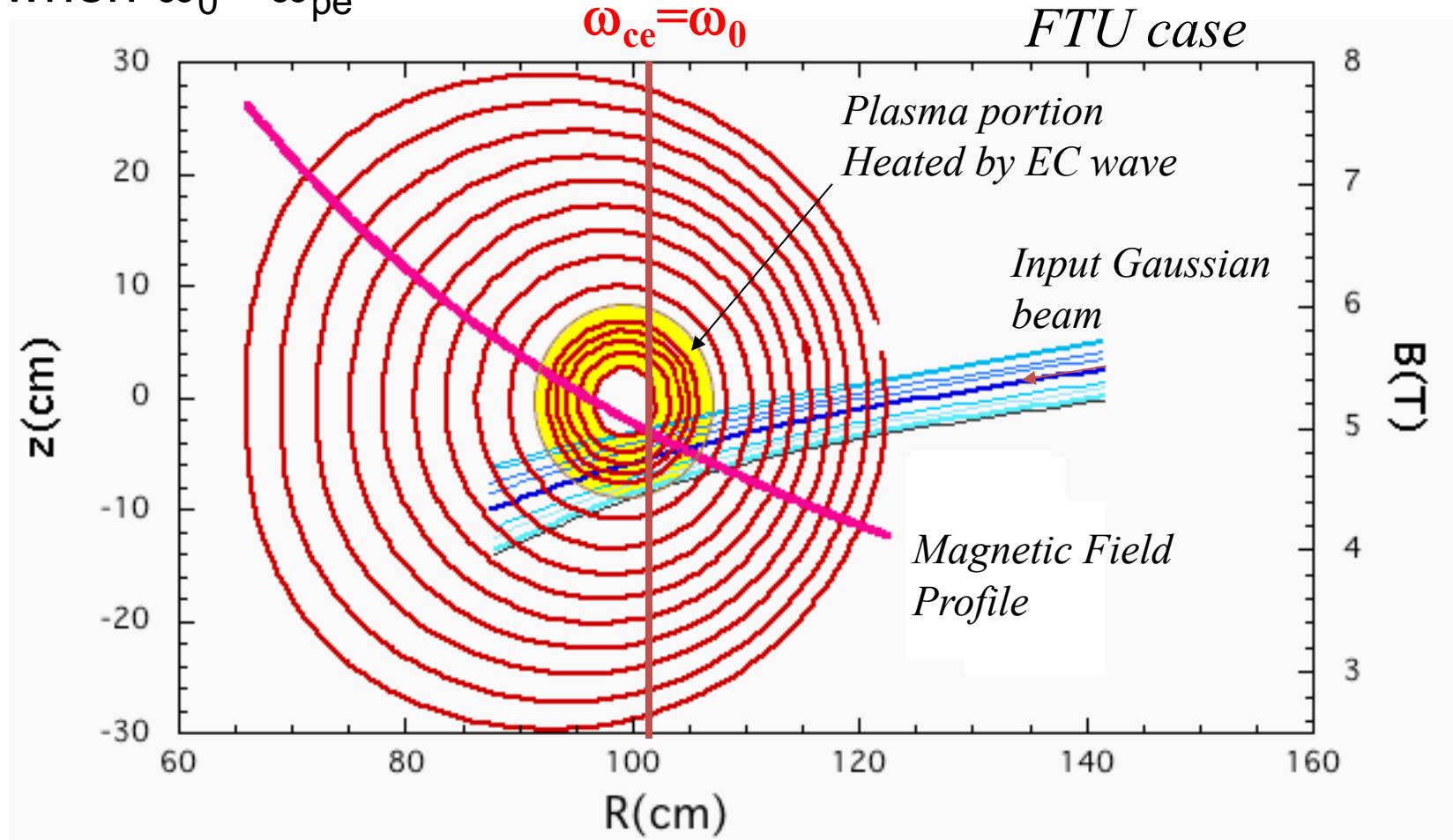
Local plasma density

Injection angle

Geometrical Effects

Beam Propagation

The beam suffers of plasma refraction (when it crosses high density regions) up to a full bending (reflection) when $\omega_0 = \omega_{pe}$



Beam Propagation

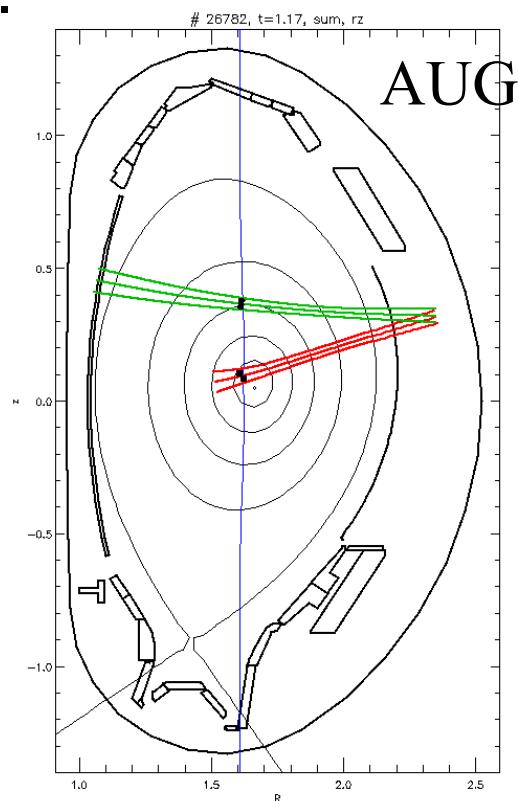
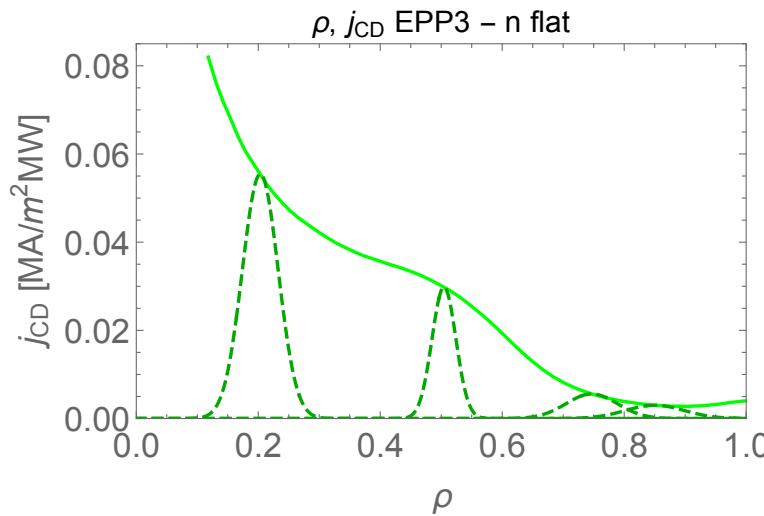
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Main Codes used:

TORBEAM, GRAY

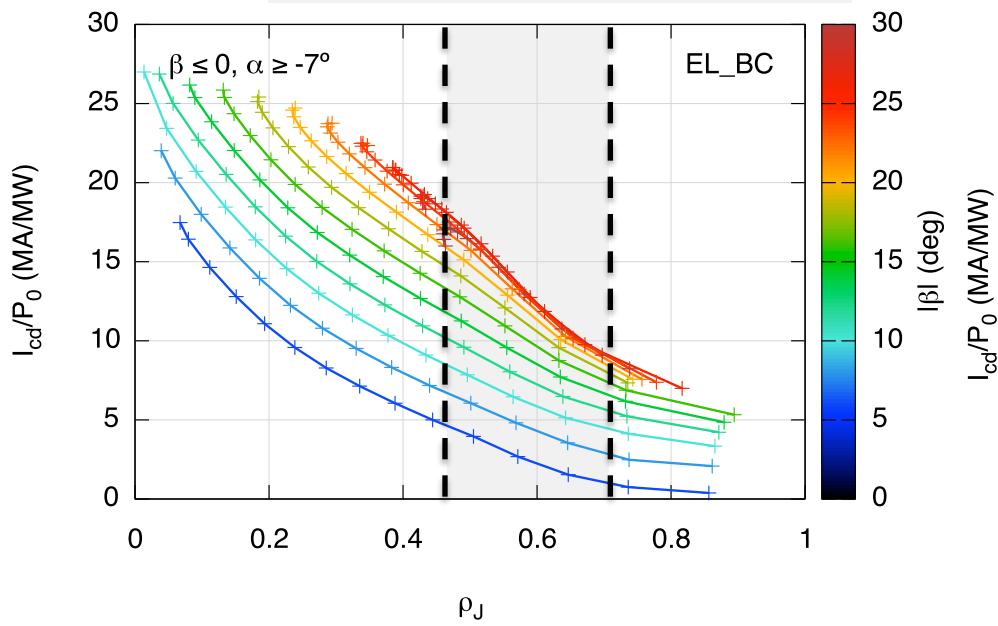
TORAY-GA, BANDIT-3D



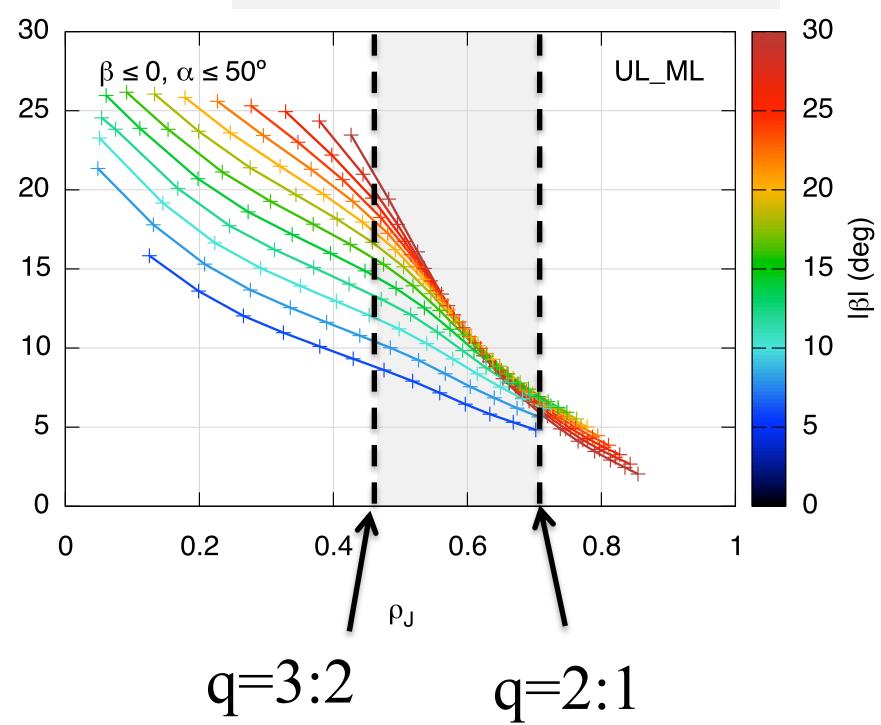
Current drive $I_{CD}/P_0 (\rho)$

DTT case

Equatorial Launcher



Upper Launcher



Current drive efficiency depends on two parameters:
 Local electron temperature
 Toroidal angle (beta)

Application of EC power in experiments for Plasma operation and RT control

Introduction

Which are the characteristics of EC wave that make it a suitable tool for plasma control to be used in closed loops?

Easily predictable power deposition localization

→ geometrical ray tracing and beam tracing

Highly localized power deposition (strong local effect)

→ the EC wave can be launched as TEM00:

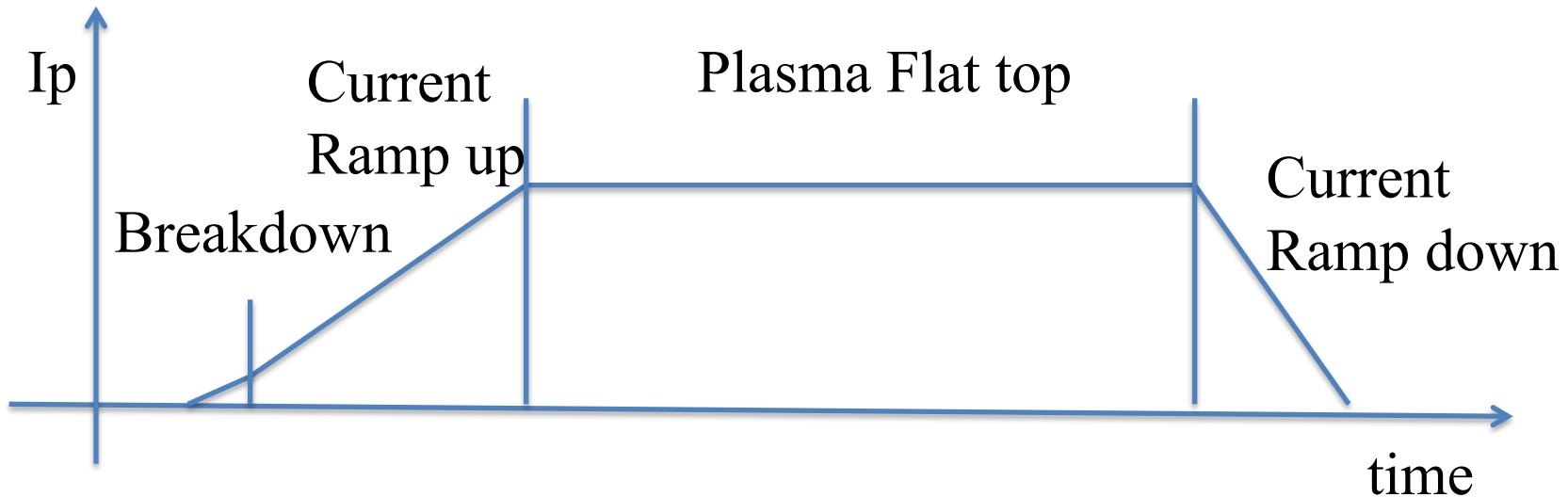
Gaussian beam with $w_o \geq 2\lambda/\pi$ (100 GHz: $w_o > 1.9$ mm!)

Easy control of deposition localization (radius)

→ use of steerable mirrors due to the possibility od Q.O. approach

Fast switch on/off time

power rise time limited by HVPS capability ($\sim 100\mu s$). Modulation up to 10KHz demonstrated (5 KHz required for ITER)



Breakdown: pre-ionization, burn-through

Ramp up: lower internal inductance, save transformer flux for longer pulses

Flat top: profiles control, **MHD Control** (NTM and ST), Impurity accumulation, localized CD

Ramp-down: avoid temperature collapse, **disruption avoidance**/control

EC wave in presence of resonant magnetic field is able to accelerate electron up to ionization energy, starting the avalanche and sustaining a low temperature (20 eV) and low density (10^{18} m^{-3}) plasma.

This technique is used in stellarator to sustain plasma and in tokamak to initiate plasma and (applying electric field) ramp-up current.

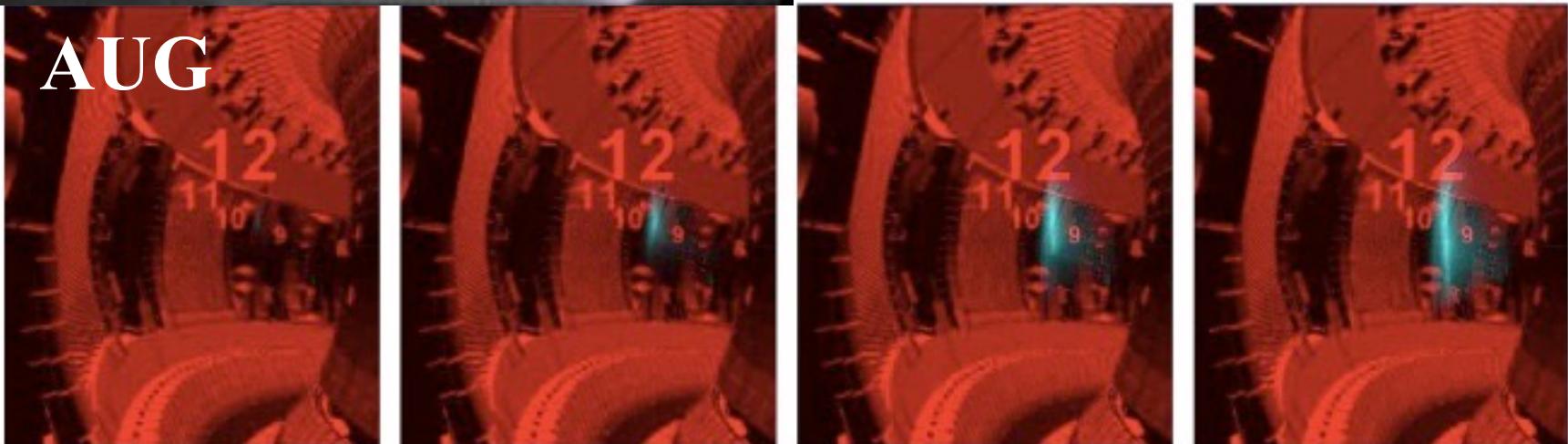
FTU

5 T resonance

The plasma is ionized where the RF beam crosses the resonance cylinder.

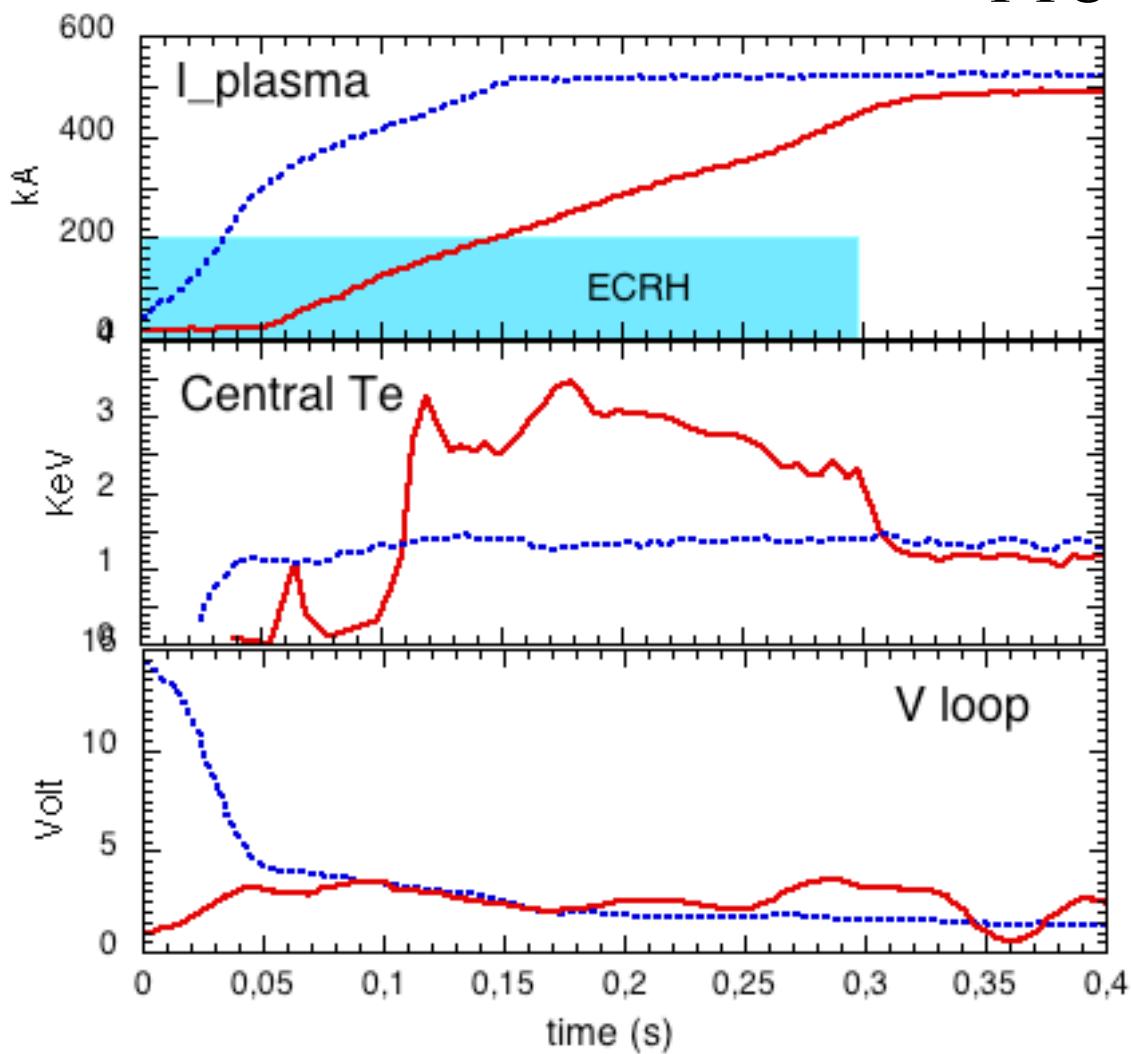
The plasma drift in vertical and outer direction, until the current starts the confinement

AUG



EC Assisted Break-down vs ohmic

FTU

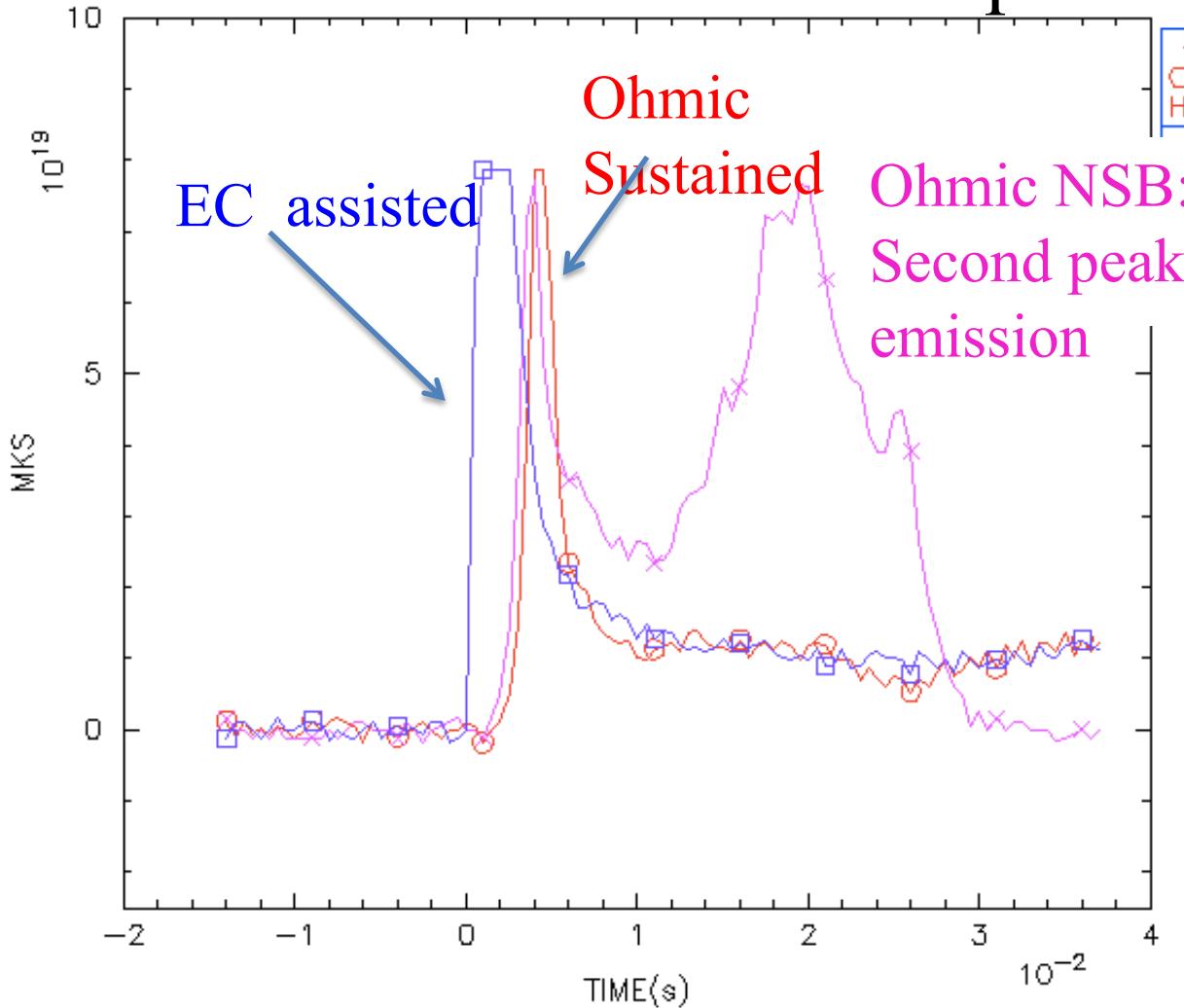


EC power is applied at $t=0\text{s}$ and maintained for all the current ramp

With ECH assistance it is possible to start-up tokamak current at low V_{loop}

High Temperature after initial phase at low absorption

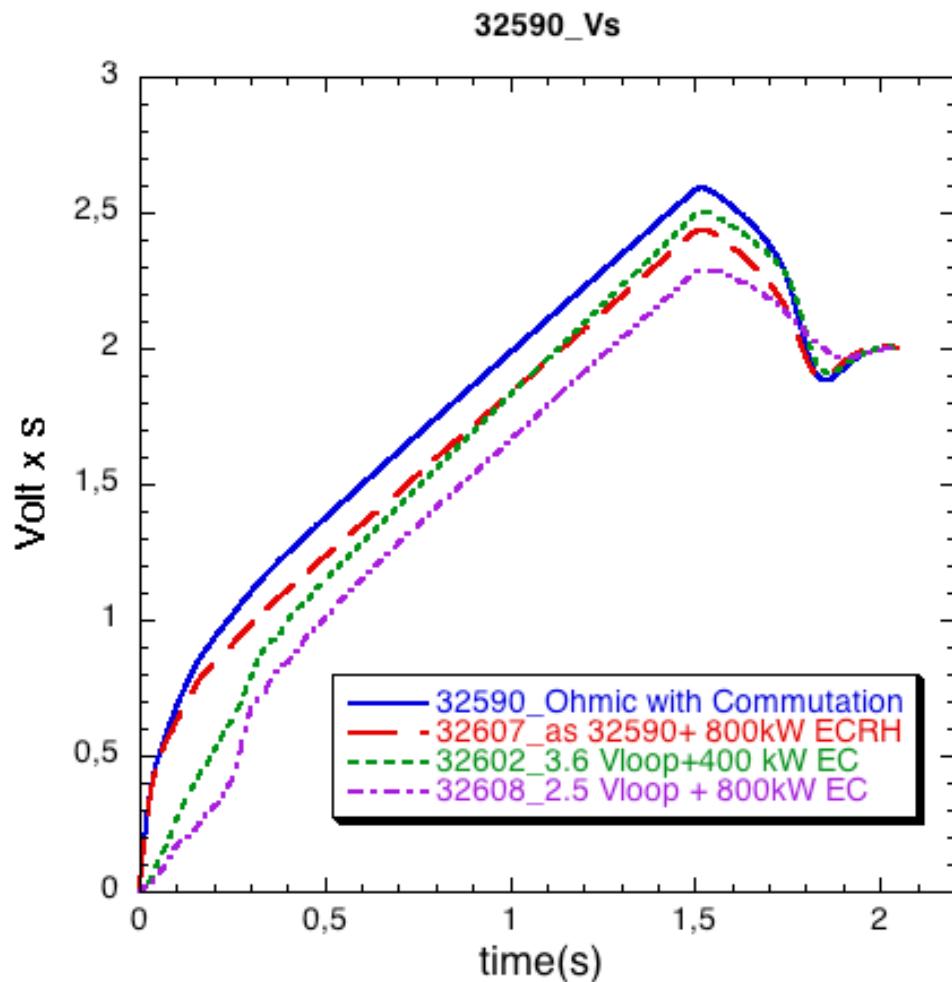
D-alfa emission at start-up



In case of low V_{loop} (or high impurity content) the hydrogen plasma cannot overcome the condition of H-alfa peak (at 20-100eV).

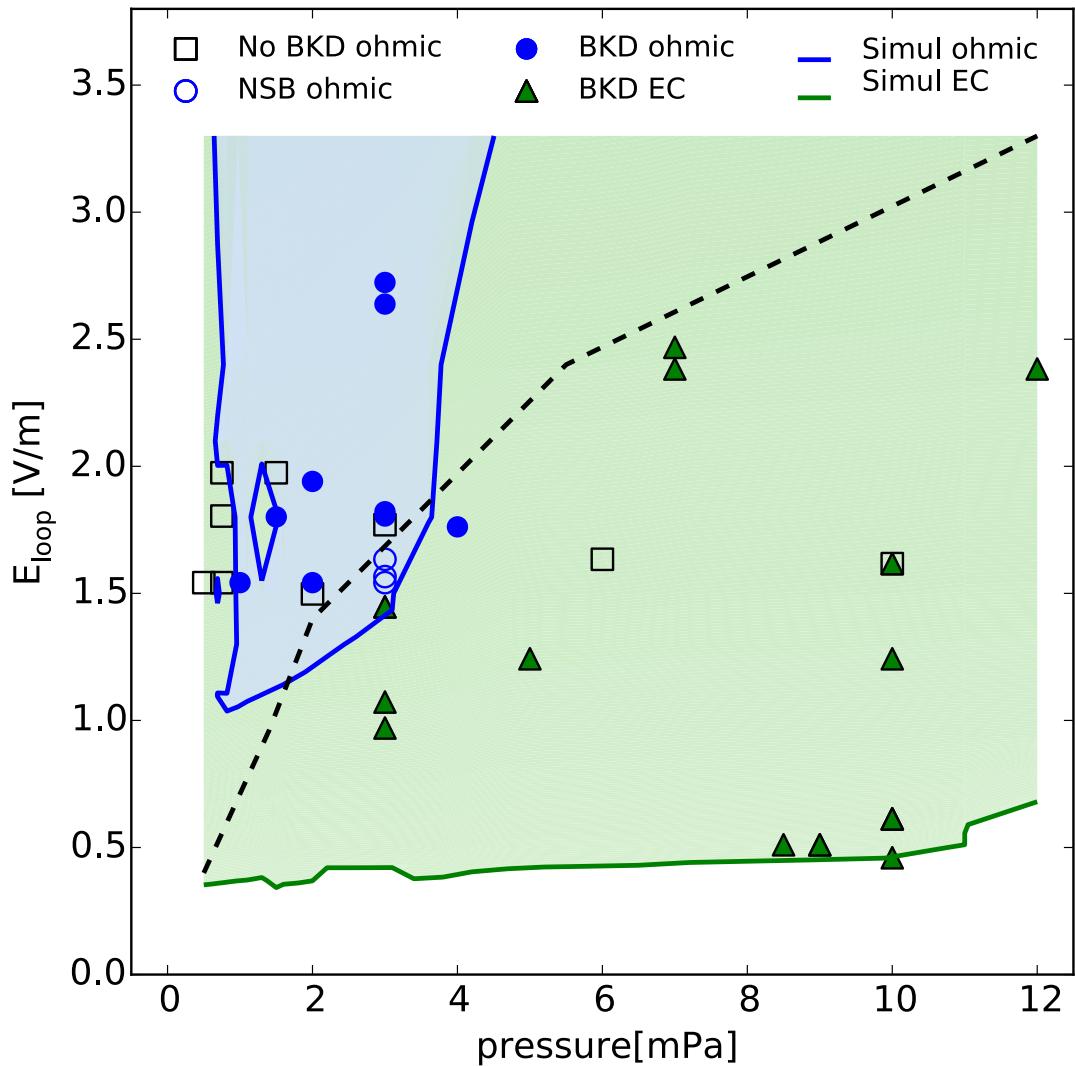
EC power gives energy to compensate radiation losses in the low temperature plasma, allowing to increase of temperature ($>200\text{eV}$) necessary to ramp-up the plasma current

Transformer flux saving



Application of EC power to start-up plasma current leads to flux saving for two main reasons:

- 1- Breakdown at low Vloop (a fast drop of I_{trafo} is not required)
- 2- Higher temperature during current ramp reduce plasma resistivity

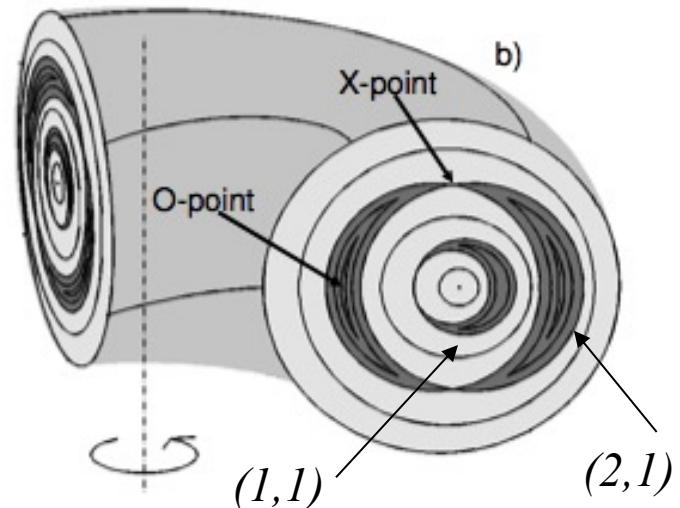


Use of EC power in the start up phase allows wider operational window in term of Electric field and Pressure

Here the FTU results together with simulation from BKD0 code.

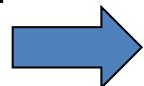
In a large scale machine (like reactor) the automatic **control** for plasma stability and **performance** is one of the main challenge.

Instabilities of Magnetic Hydrodynamic type (**MHD**) can produce a deformation in the magnetic configuration reducing **energy confinement** and increasing the risk of **plasma disruption**.



The control requires correct physic models and proper actuator. One of tool to perform plasma control is the Radio Frequency used as auxiliary heating as **Electron Cyclotron Resonance Heating** (ECRH).

Island width evolution



$$g_1 \frac{\tau_R}{r_s^2} \frac{dW}{dt} = \pm \Delta'_0 + a_1 \Delta'_{BS} - a_4 \Delta'_{cd}$$

$$\Delta'_0(W) = \Delta' - \alpha W = \lim_{\varepsilon \rightarrow 0} \frac{1}{\psi} \left[\left(\frac{d\psi}{dr} \right)_{r_s+\varepsilon} - \left(\frac{d\psi}{dr} \right)_{r_s-\varepsilon} \right] - \alpha W$$

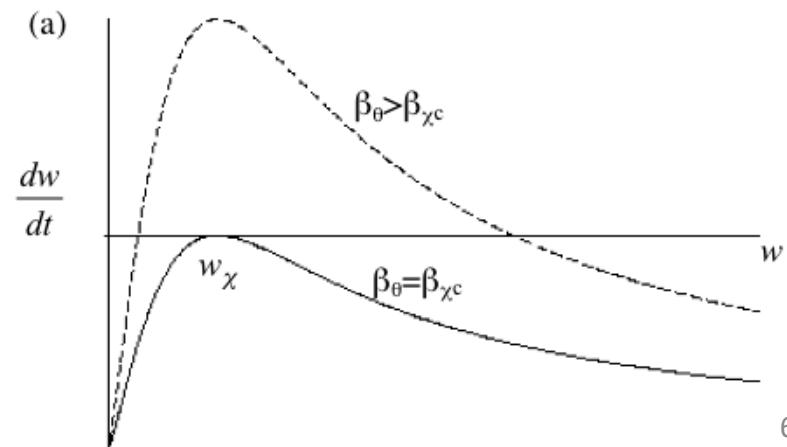
stabiliz./destab.
depending on the $\nabla_r J_{\parallel}$

$$\Delta'_{bs} \propto \beta_p \frac{q'}{q} \frac{p'}{p} \frac{W}{W^2 + W_s^2}$$

significant for large plasma pressure

$$\Delta'_{cd} \propto \frac{I_{CD}}{I_p} \eta(W / \delta_{CD}) \frac{1}{W^2}$$

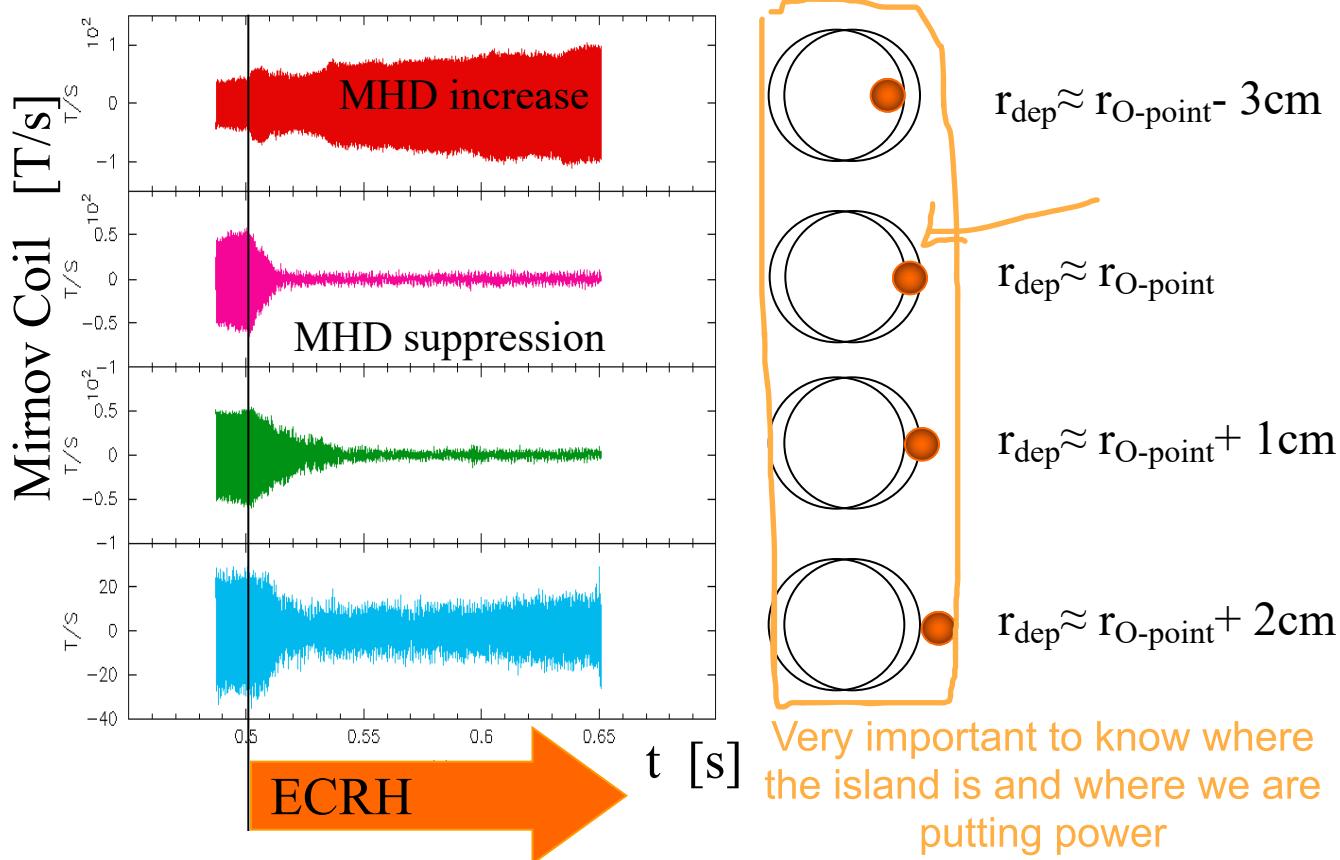
stabiliz./destab. depending on island radial centering



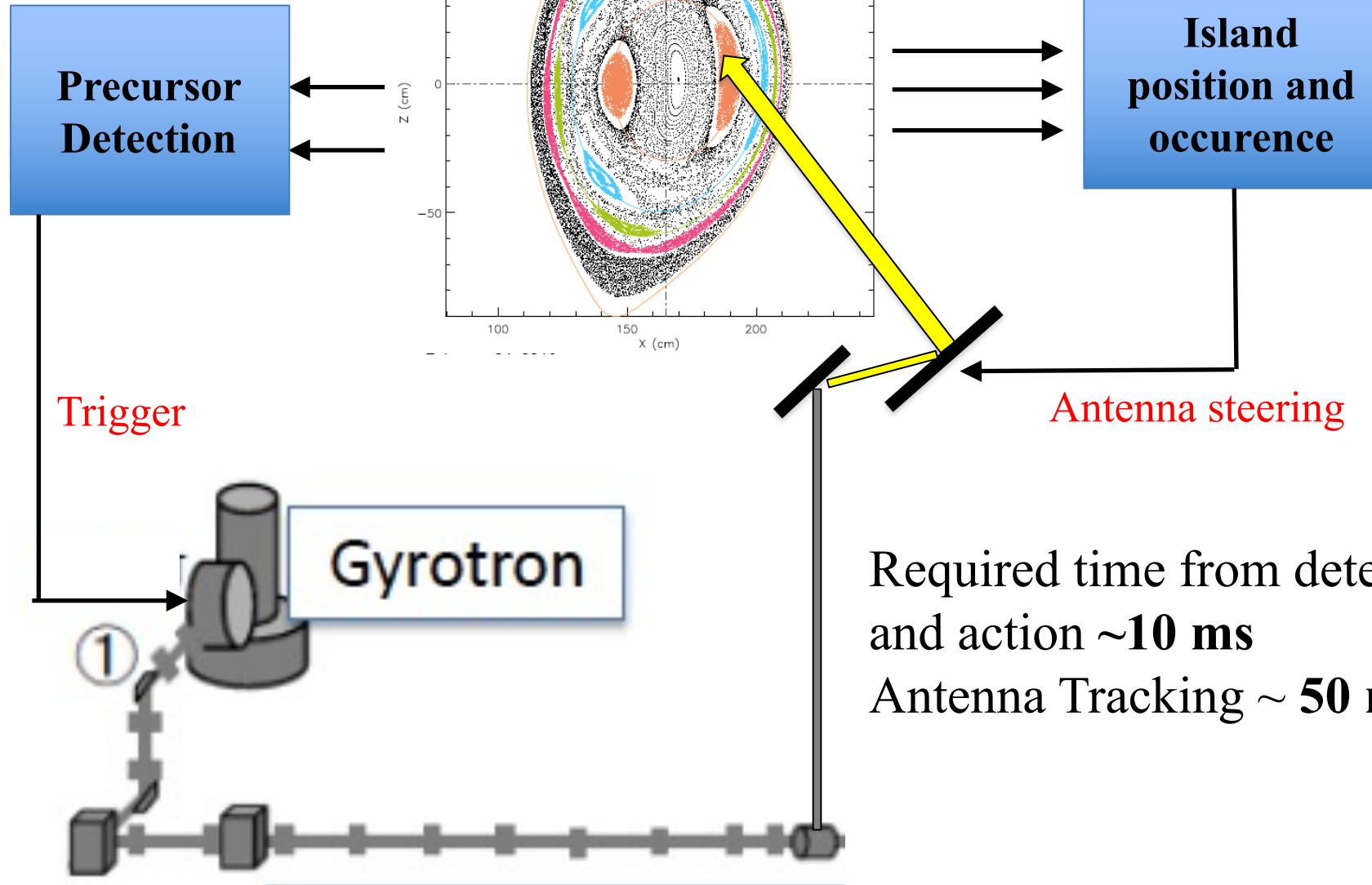
First Demonstrative Experiment

S.Cirant et al. IAEA
Sorrento 2000

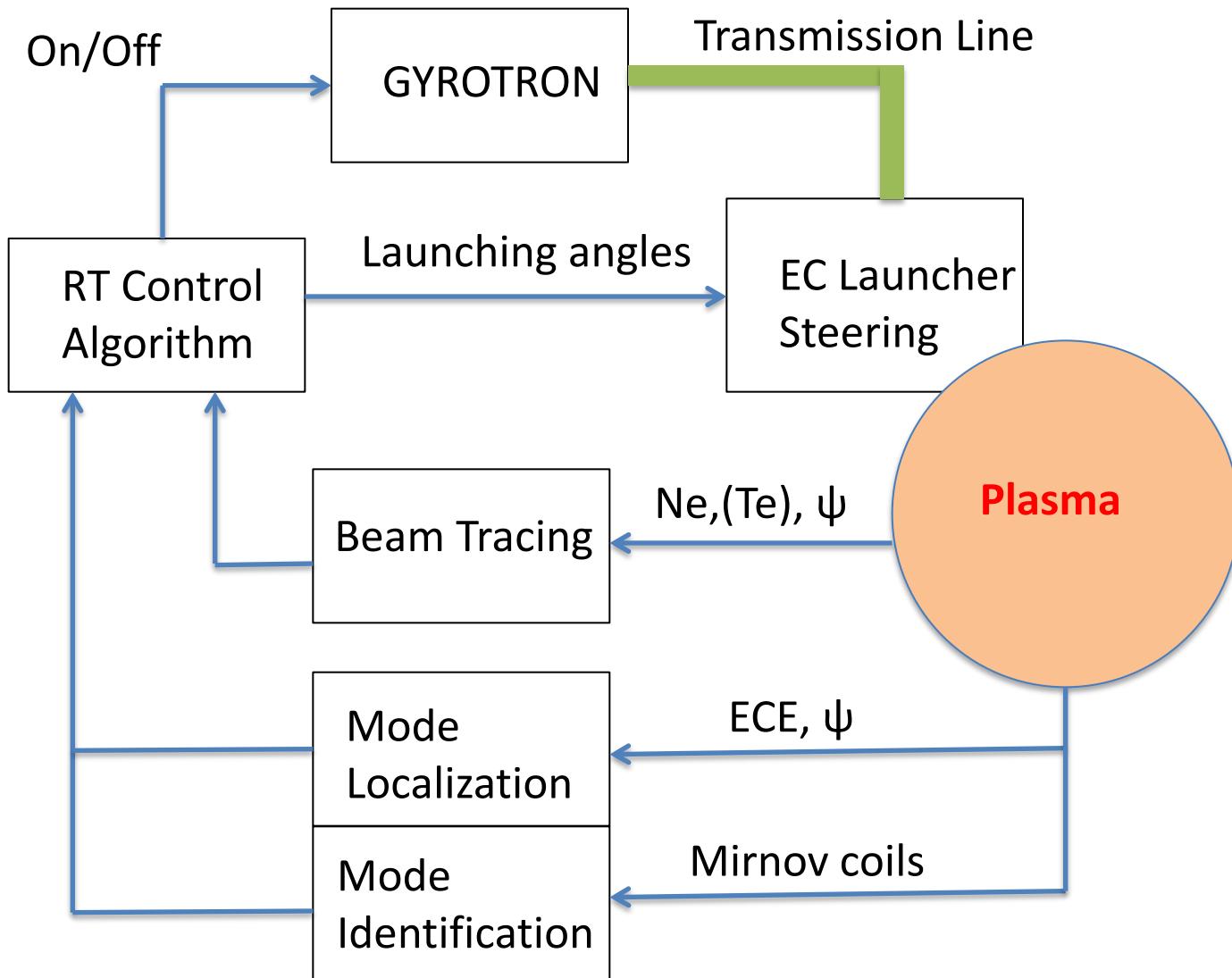
MHD instabilities are monitored by external magnetic signals with Mirnov coil



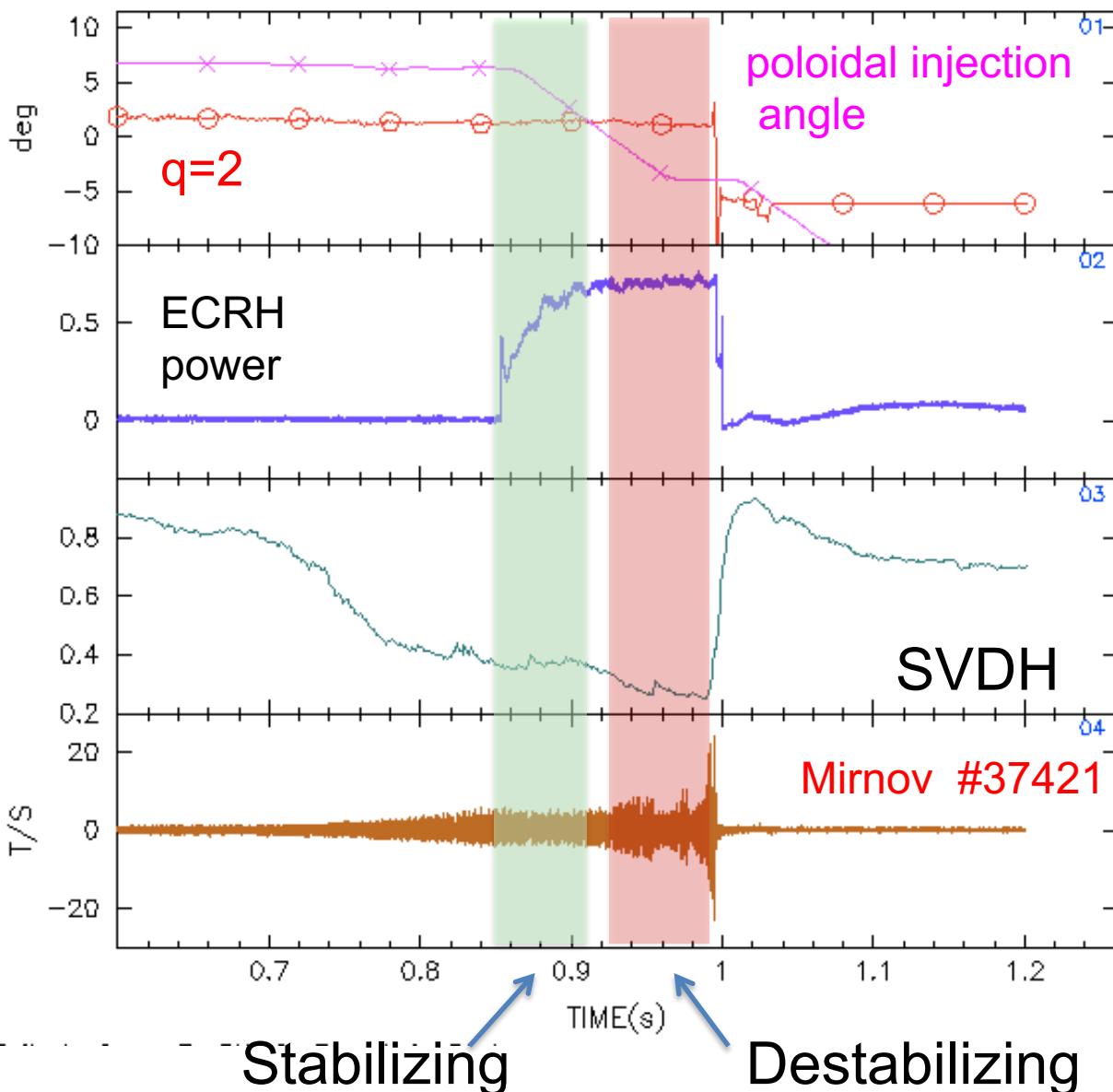
The **islands** can be reduced in width or completely **suppressed** by a **current driven** (also resistively) by absorption of electron cyclotron waves (EC) **accurately located within the island**.



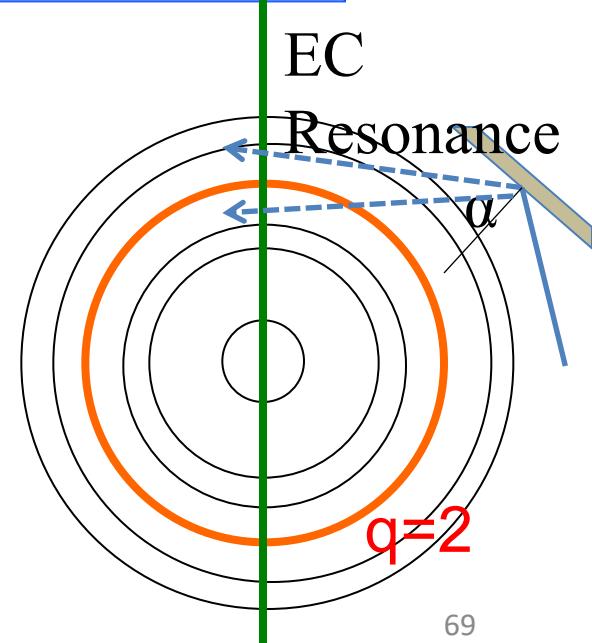
The ideal MHD control Loop



Stabilization/destabilization depends on the ECRH absorption radius



37421	01/A
	MECRH.EQFQLOALPHA2
37421	01/B
	X ECRHL.ALFA2_Po
	ALFA L0 MIS.
37421	02/D
	MECRH.ADDGY4PWR
37421	03/E
	MECRH.svdh
37421	04/F
	%e.mhdfst(4)
	9D021PO

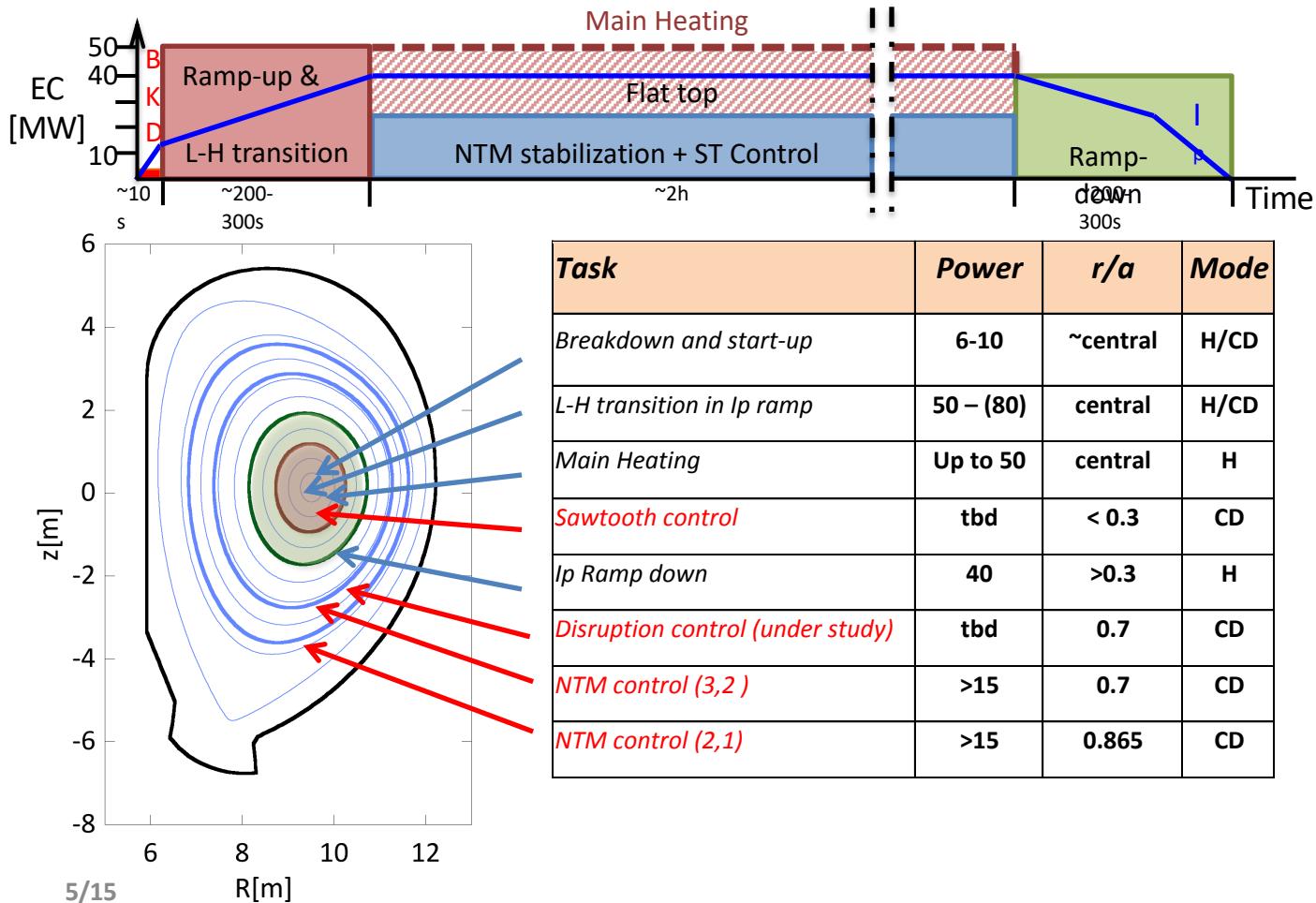


Basic for a Design of an ECRH System

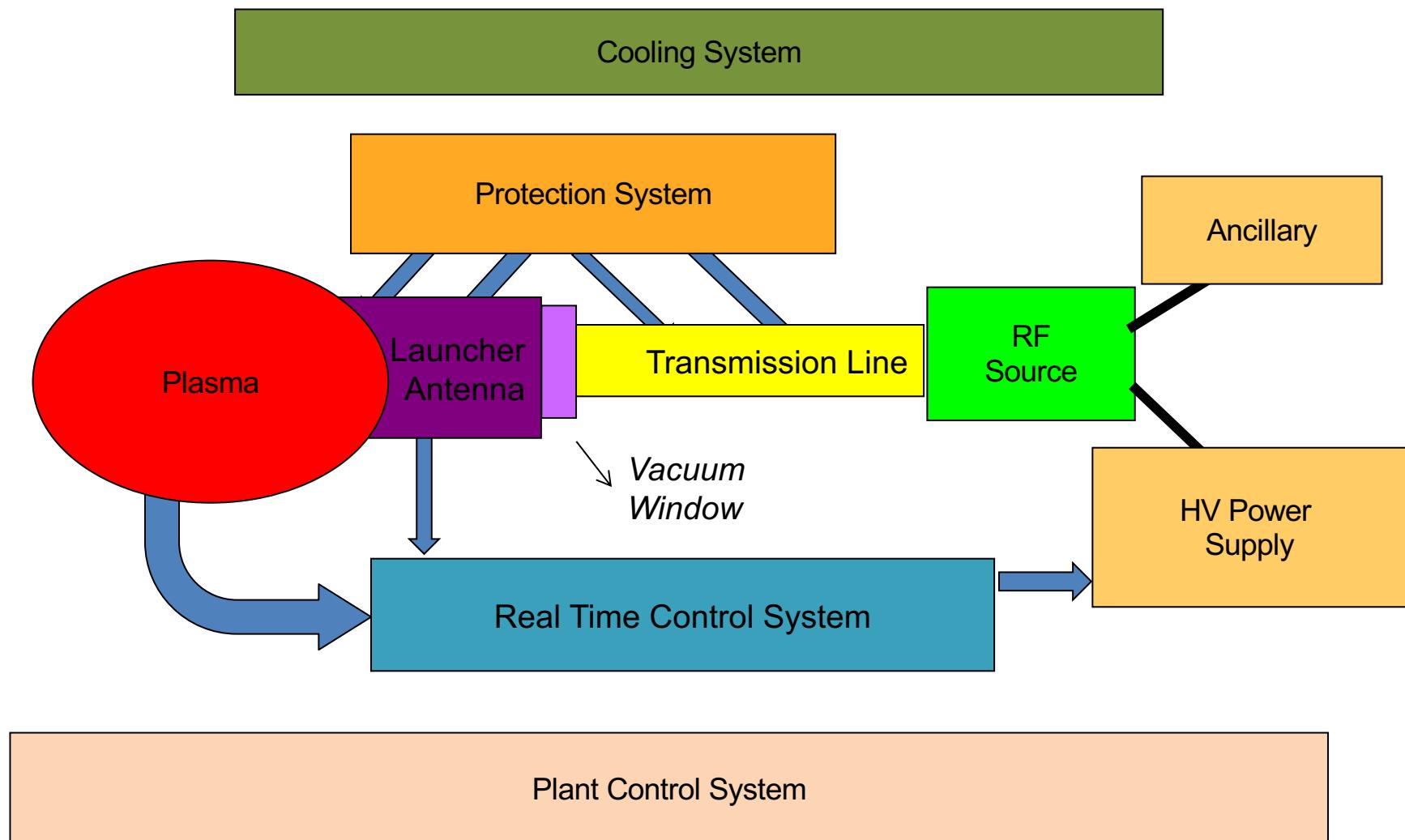
Outline

- Main Physic requirement for ECRH system
- ECRH System General Overview
- RF Power Source
- Gyrotron Power Supply
- Transmission Line
- Polarizer
- Coupling EC power to plasma: Launcher
- Control System

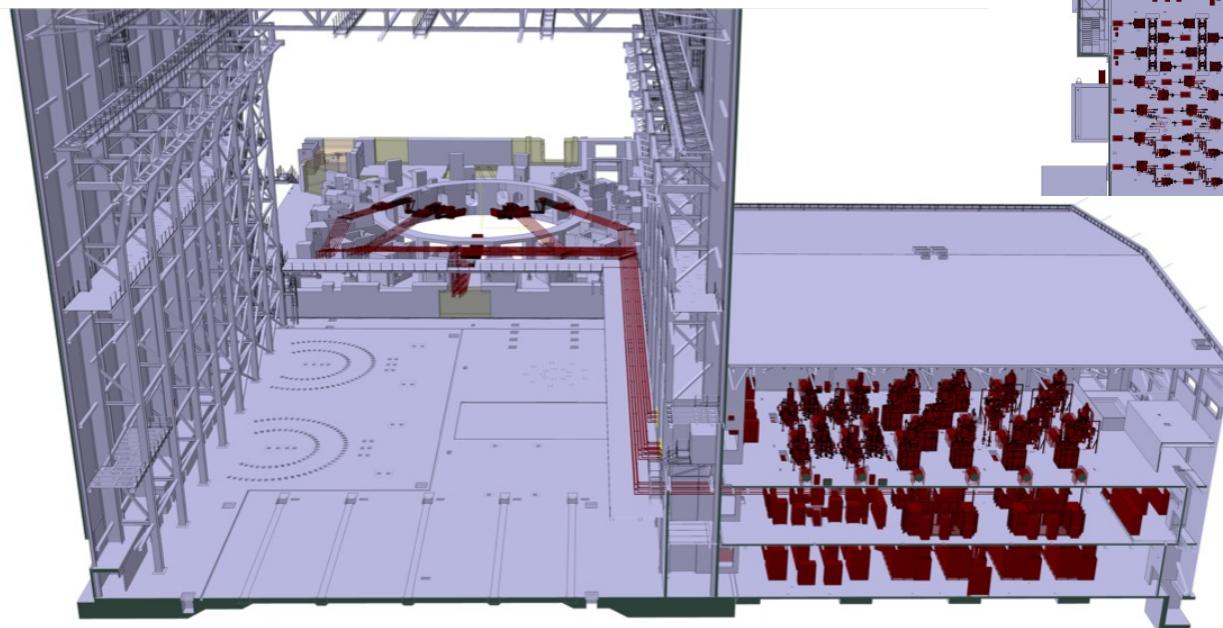
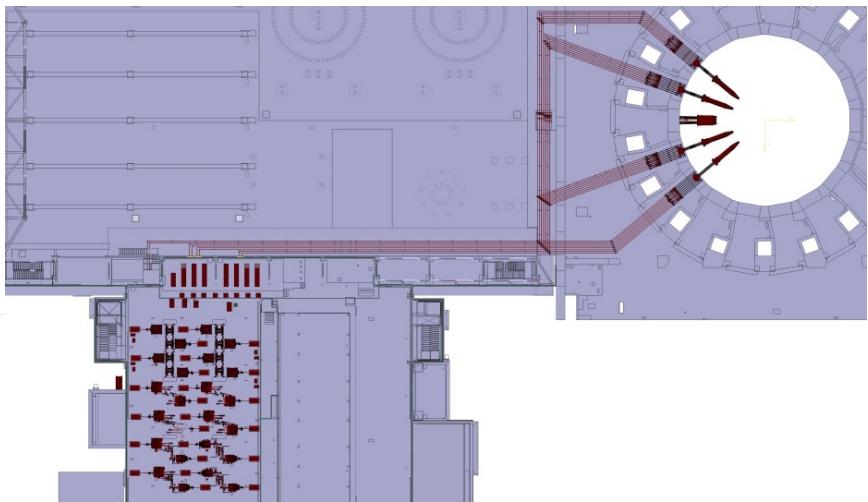
EC System Physical Requirements



ECRH system in blocks



- ✓ EC system will inject 24 beams of 0.83 MW (20 MW total)
- ✓ Corresponding to **24 MW installed**

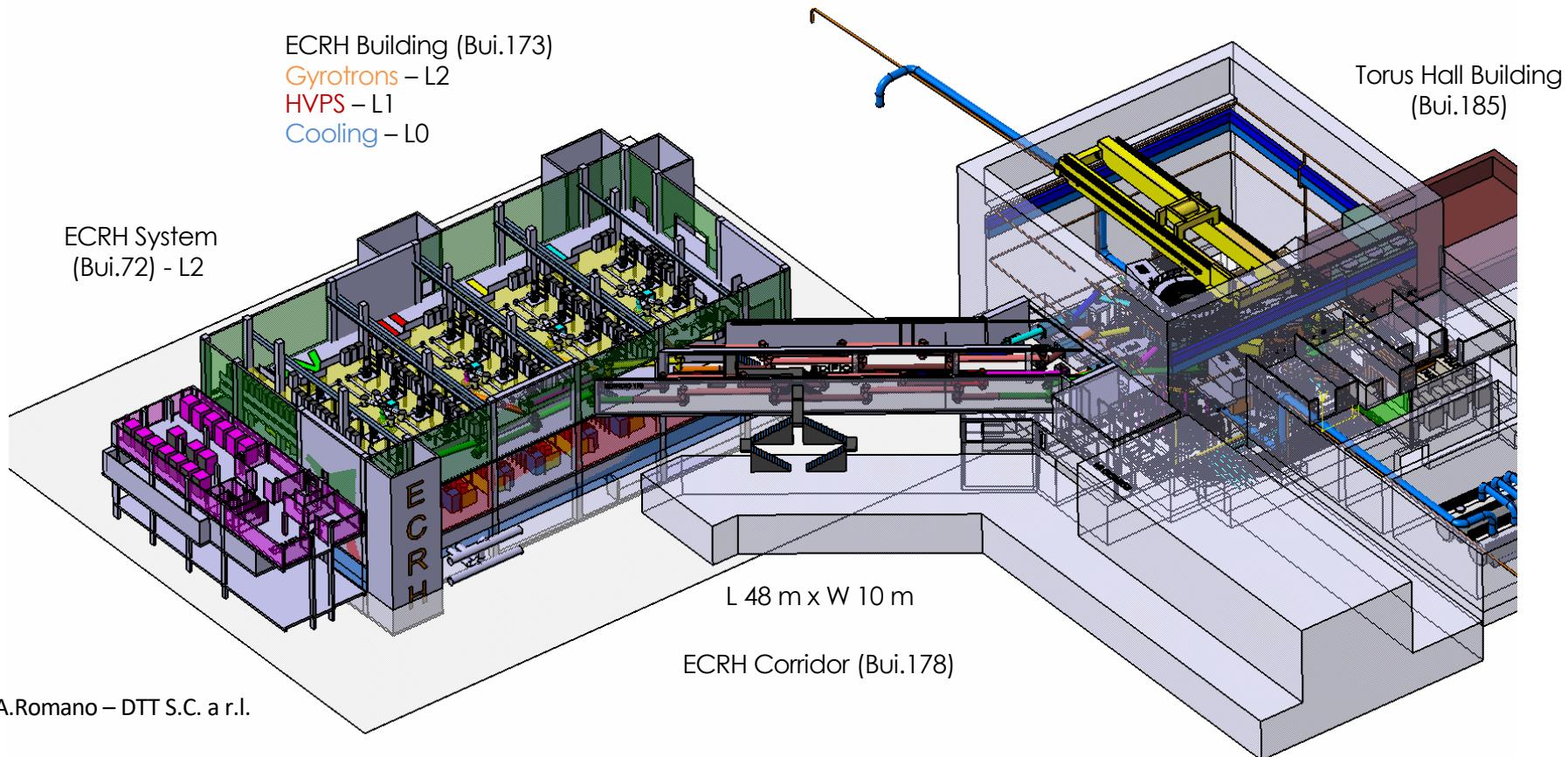


Courtesy from F.Gandini – EC-20 - 2018

12 HVPS sets
24 Auxiliaries set
24 Gyrotrons
24 Transmission Line
4 Upper Launcher
1 Equatorial Launcher
1 Control system

iST^{DTT} - ECH System: General Layout

Consiglio Nazionale delle Ricerche



A.Romano – DTT S.C. a r.l.

RF Source

- *High Frequency (up to 170GHz)*
- *High Power (1 MW class)*
- *Pulse length: ~1000 s -> cw*
- *Gaussian output: 98%*
- *Reliability: > 94%*

- Klystron (for high frequency power decreases)
- Magnetron (i.e. 2.45 GHz : microwave oven)
- BWO (few watts, only for signal measurements)
- **Gyrotron : cw, up to 240GHz, 1-2 MW**
- FEM (Free Electron Maser): high frequency, only prototype study
- CARM: high frequency, high power: under consideration at Enea Lab

In a Gyrotron an electron beam (emitted by a hot cathode) is accelerated in strong magnetic field crossing a cavity shaped for a specific mode. The electrons emit power at frequency:

Effective frequency

$$\omega_c = n \frac{\Omega_{c0}}{\gamma}$$

$$\gamma = \left[1 - \left(\frac{v}{c} \right)^2 \right]^{1/2} = 1 + \frac{eV_0}{m_o c^2} = 1 + \frac{V(kV)}{511}$$

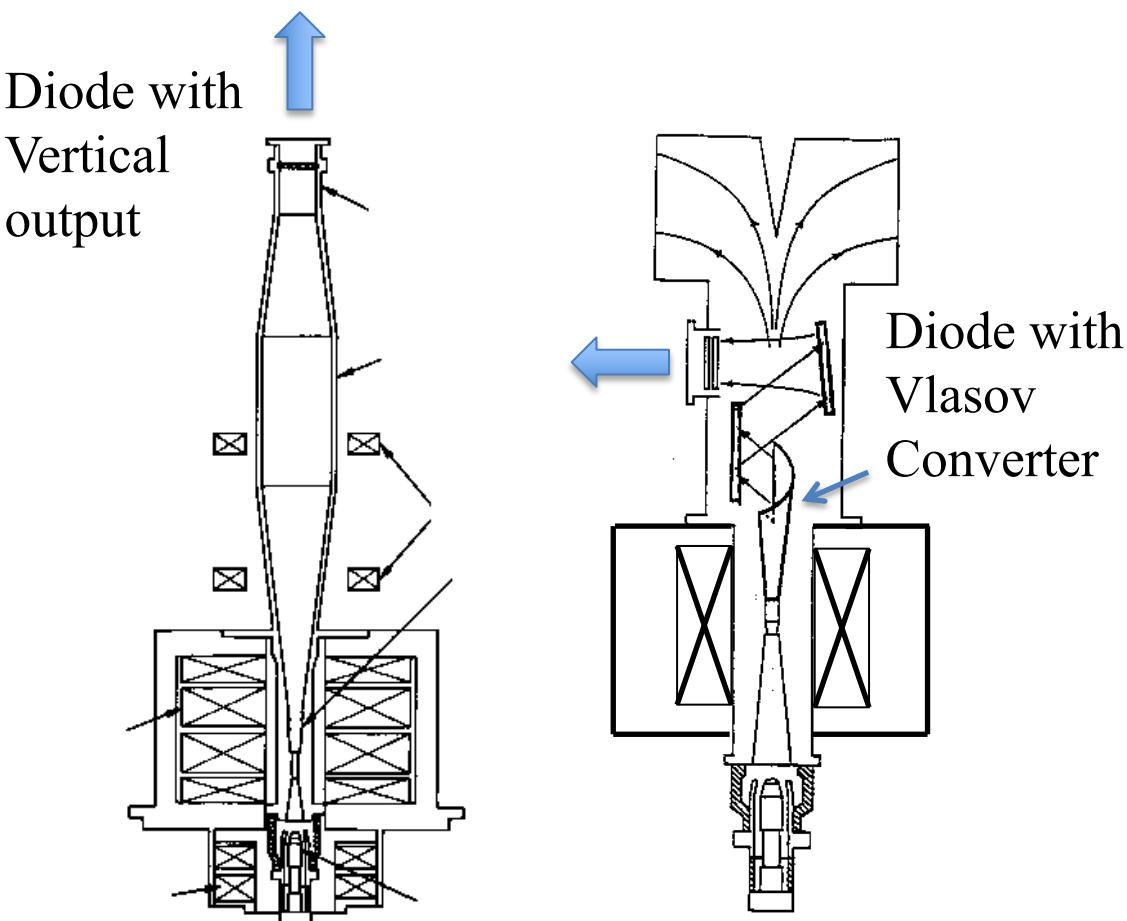
Relativistic term

Gyrotron is an oscillating tube: not an amplifier

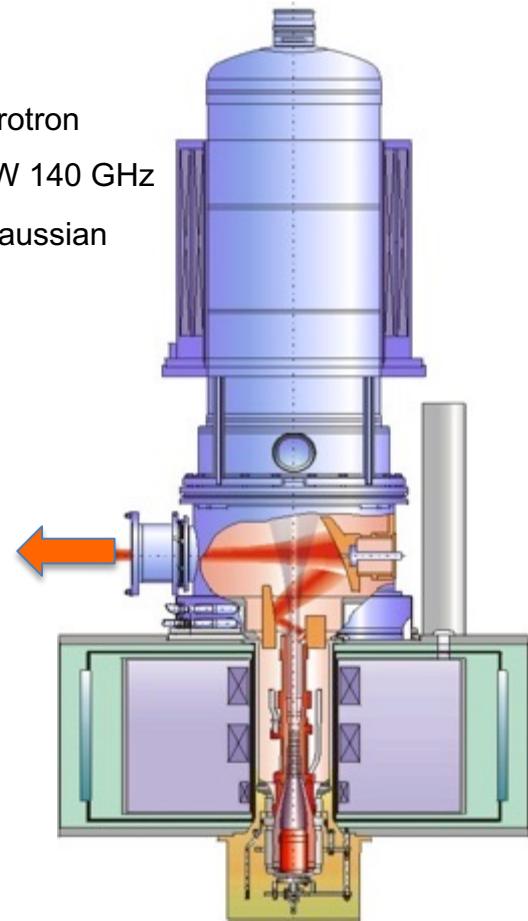
Main Gyrotron Types

Diode, Triode or SPD (Depressed Collector efficiency ~50%)

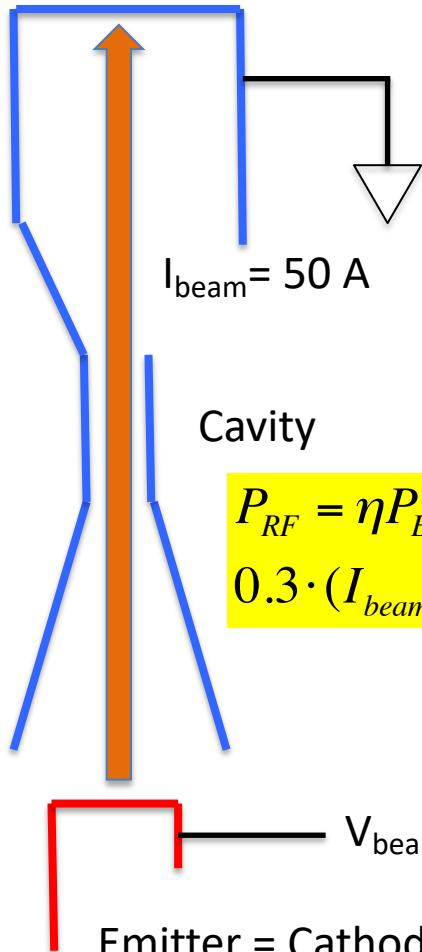
Vertical output or transversal gaussian output



W7-X gyrotron
1 MW CW 140 GHz
Radial Gaussian Output



Collector = Anode



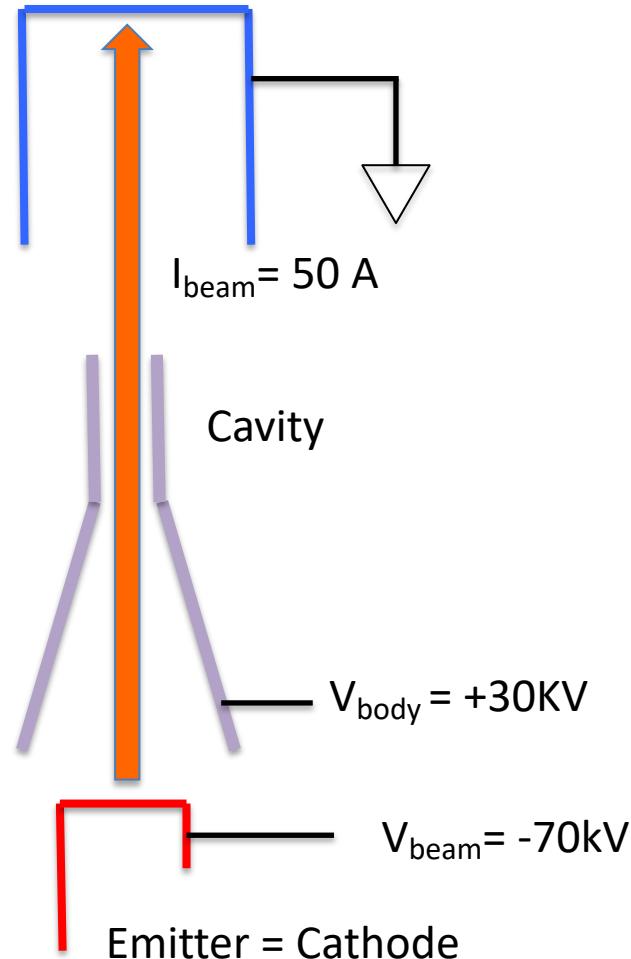
Cavity

$$P_{RF} = \eta P_{EL} = \\ 0.3 \cdot (I_{beam} \cdot V_{beam}) = 1.05MW$$

Emitter = Cathode

$$P_{RF} = \eta P_{EL} = \\ 0.3 \cdot (I_{beam} \cdot V_{Cath-Body}) = 1.50MW$$

Collector = Anode



$$\eta = \frac{P_{RF}}{P_{EL}} = \frac{1.5MW}{3.5MW} \sim 42\%$$

The Gyrotron RF output



The gyrotron RF output is not a pure gaussian beam. 10-15% of **spurious modes** are usually present. **Future goal < 2 - 5%**

The output beam is modified by the use of two shaped mirrors (elliptic or phase corrected): Matching Optics Unit (**MOU**)

The output **polarization** is **linear and horizontal** (with respect to the tube vertical axis) in the last generation tube (with Vlasov Converter)

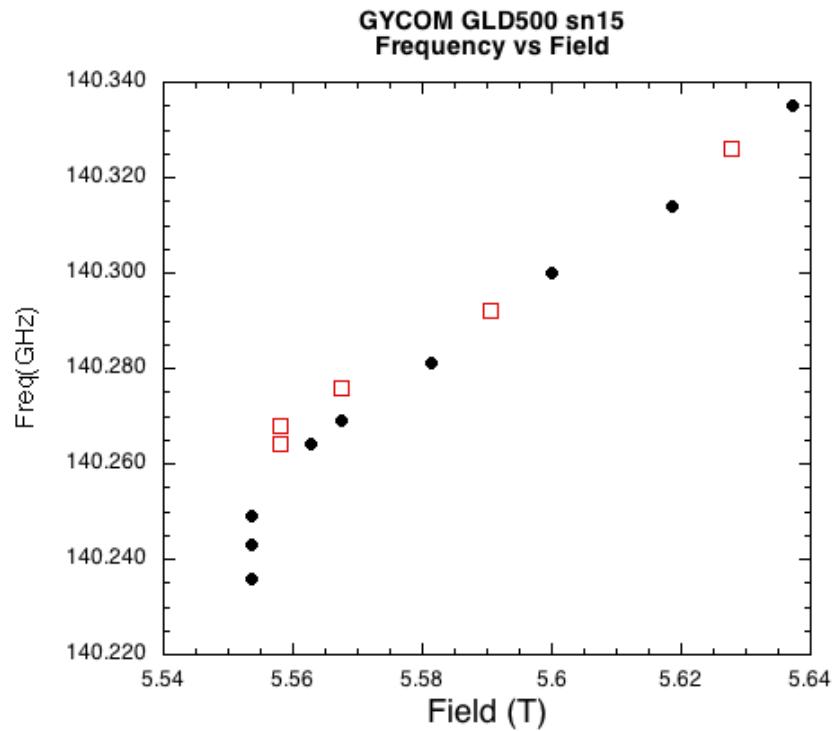
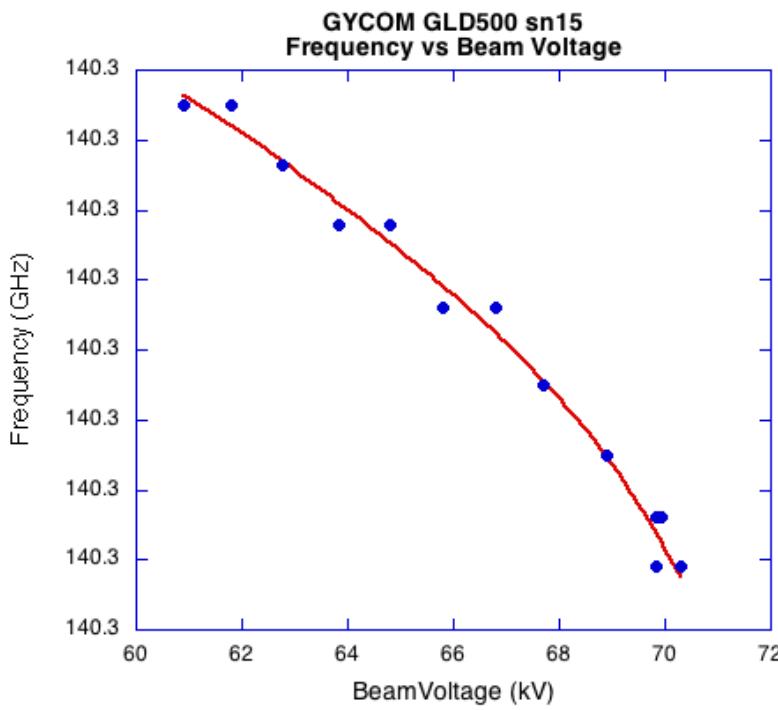
The beam must be matched with the Transmission Line minimizing the **conversion losses**.

*The lost power **MUST** be absorbed in some way therefore **MUST** be minimized*

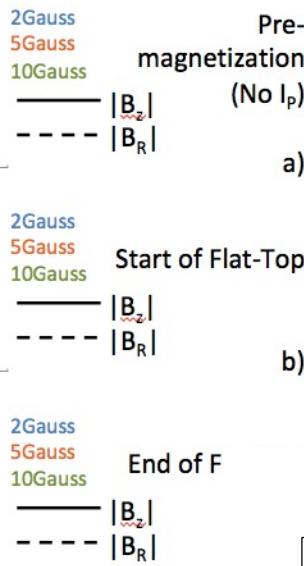
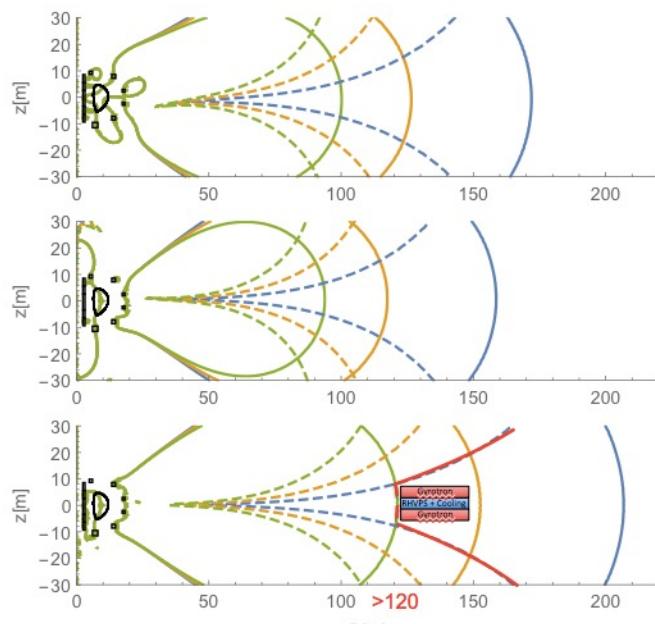
$$\omega_c = n \frac{\Omega_{c0}}{\gamma}$$

$$\gamma = \left[1 - \left(\frac{v}{c} \right)^2 \right]^{1/2} = 1 + \frac{eV_0}{m_o c^2} = 1 + \frac{V(kV)}{511}$$

Frequency depends on **magnetic field** and accelerating voltage (**beam voltage**)

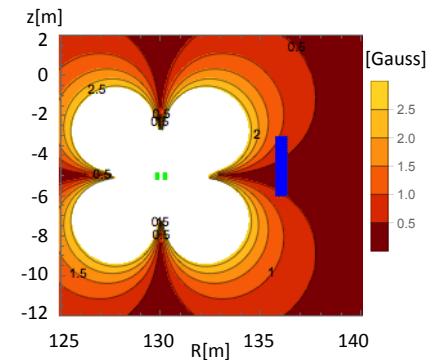
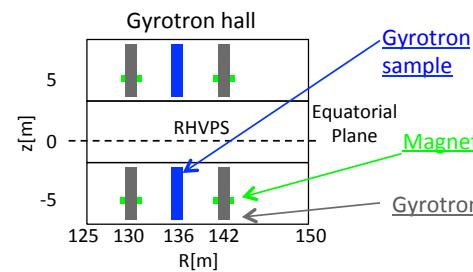


Dependency on magnetic field is linear but too slow (high impedance) to be used



The stray field is generated by:

Plasma Current + Poloidal coils + Central Solenoid
neighbour gyrotrons

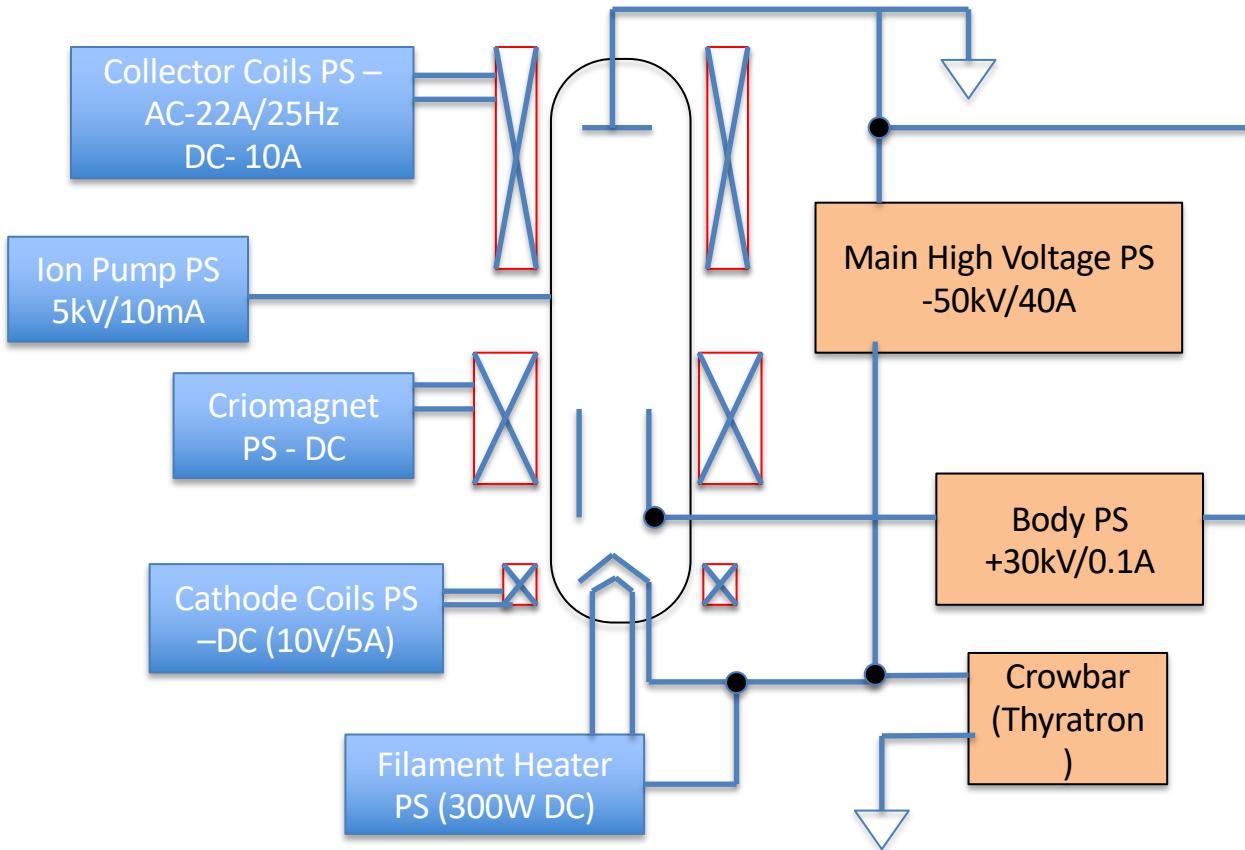


Gyrotron can be damaged by a stray magnetic field at level of collector.

The MW level gyrotrons require:

2 G for radial component
10 G for vertical component

Gyrotron Auxiliaries



High stability: $\pm 0.2\%$

Fast voltage ramp: ~ 1 ms

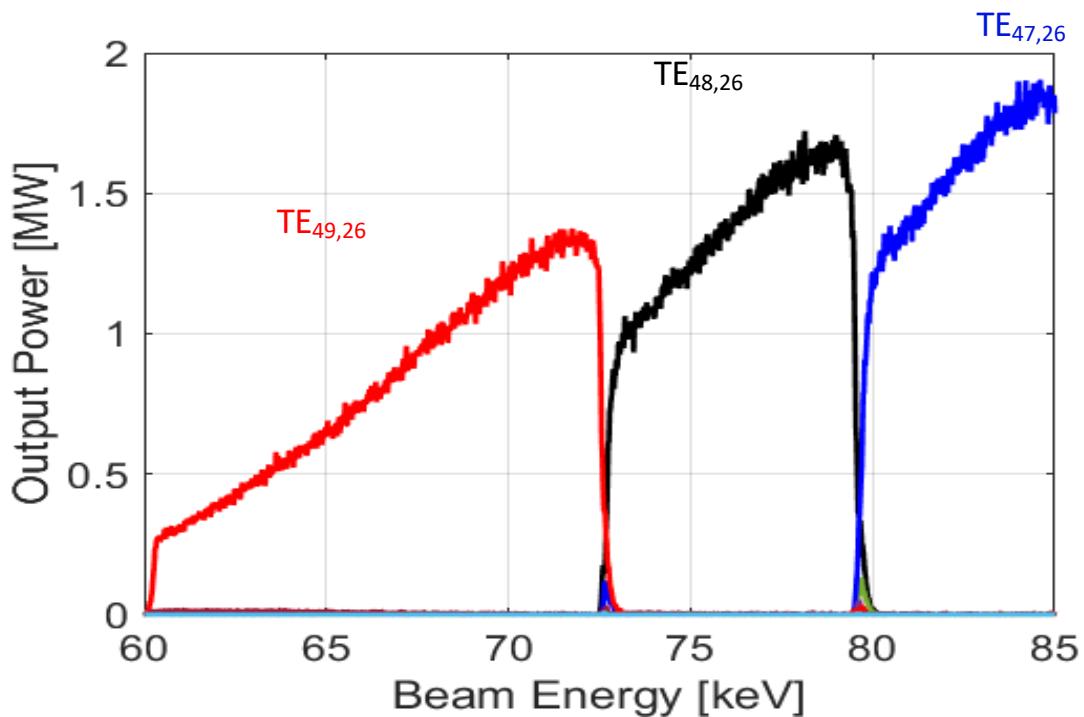
Fast protection time: 5-10 μ s (max energy in the fault = 10J)

Up to 5 KHz full modulation (for MHD control)

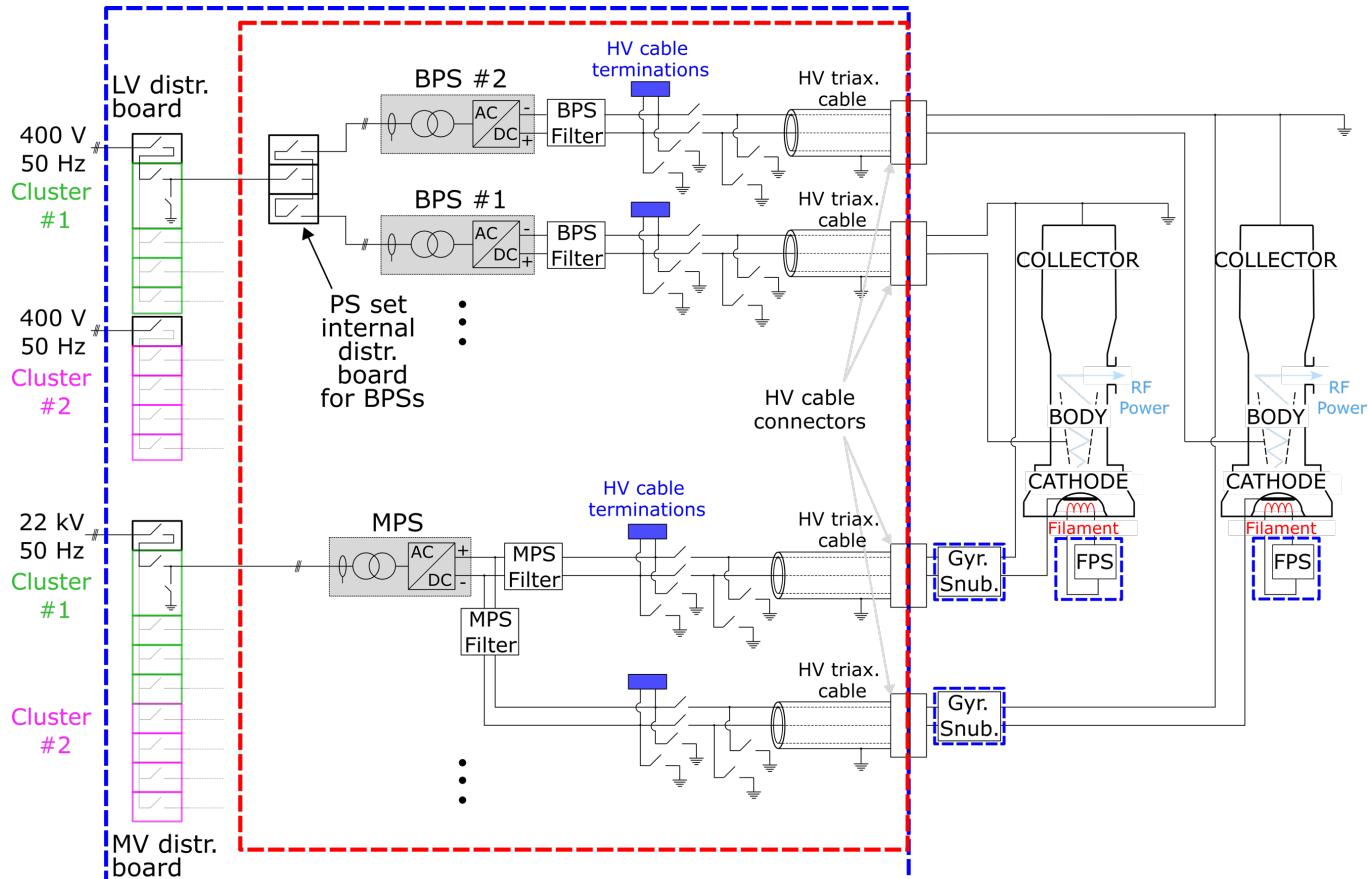
Short distance between PS and gyrotron (low parasitic capacity)

Stabilization using Body PS in feedback on the whole accelerating voltage ($V_c + V_b$).

Fast Rise time avoid competitive mode oscillation



The HV Power Supplies for CPD Gyrotron



Several IGBT Modules
Digitally controlled
Feed by a multi-
secondary
transformer



Objective of a Transmission System

To transmit the power with the lower losses

To assure safe and stable operation for the source

To measure the delivered power

To control polarization

To match the delivered power with the plasma

To guarantee a friendly and effective control by operator

Main Transmission Lines Type

Wave guide: metallic structure (cylindrical or rectangular) capable to transmit power at long distance with reduced attenuation

Mirrors: the microwave wavelengths allow a quasi-optical approach. The RF field can be treated as an electromagnetic wave. A set of focussing mirrors can be used to transmit power.

Closed system: over-moded waveguide

ITER (evacuated)

AUG (in air)

TCV (evacuated)

FTU (in air)

WEST (evacuated)

DIII-D (evacuated)

Open system: quasi-optical approach using reflecting mirror:

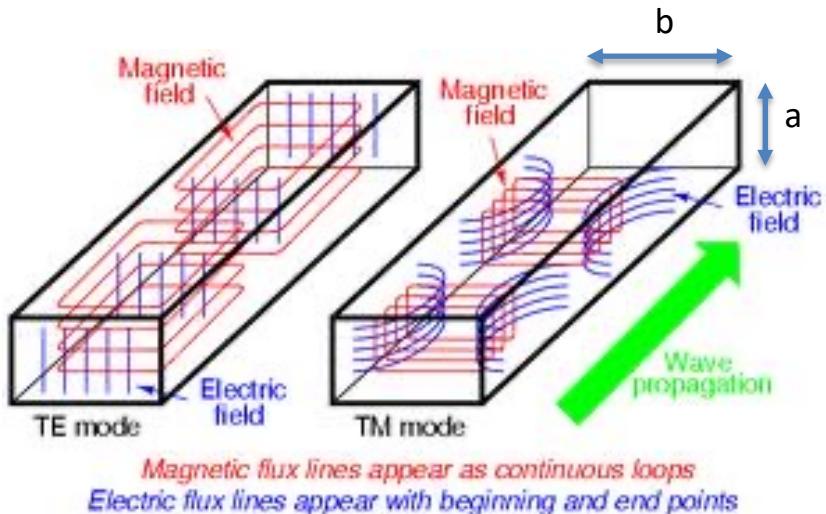
W7-X (in air)

DTT (evacuated)

DEMO (evacuated)

Wave Guide concept

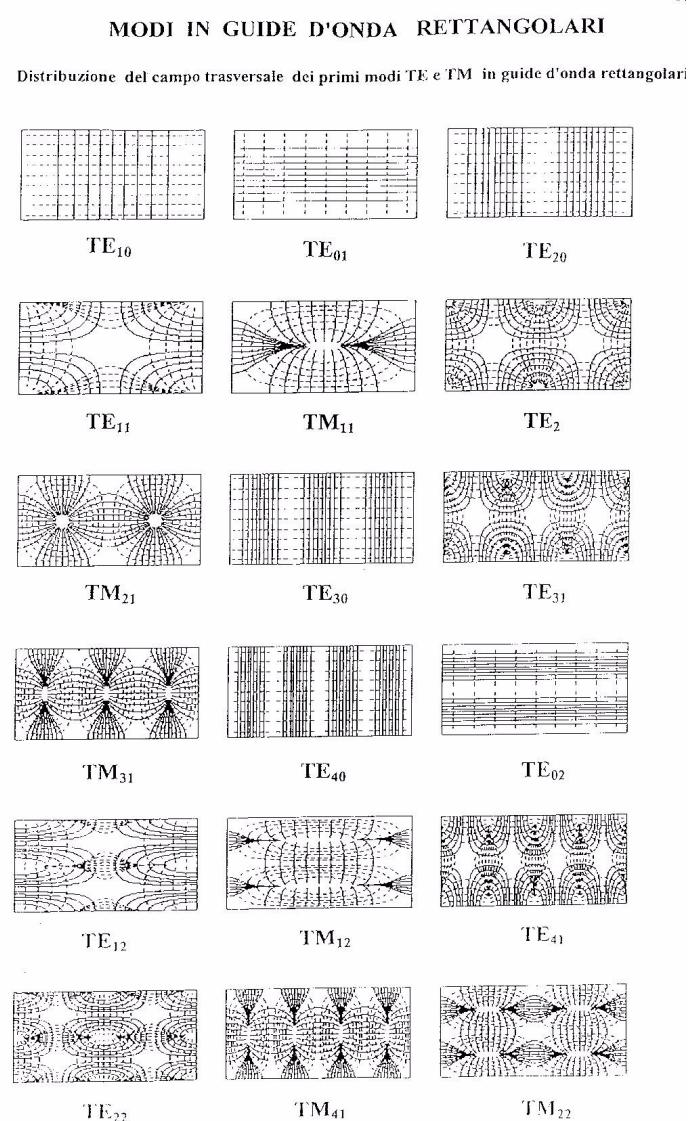
Propagation of e.m field is sustained by induced current in the metallic wall of the waveguide.



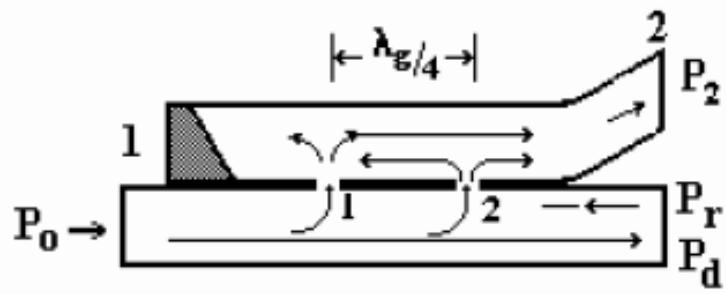
The propagating mode is based on the solution of the telegraphist equation, which is a combination of Bessel functions.

$$\lambda_c = \frac{2}{\sqrt{\left(\frac{m}{a}\right)^2 + \left(\frac{n}{b}\right)^2}}$$

For a given dimension (a,b) a cut-off lambda is defined: only waves with lower lambda can propagate or being excited



Directional Coupler



This is used to pick-up part of the wave travelling in a wave guide.

It is used to measure forward (and reflected) power

The power is transmitted across a series of holes at a distance of $\lambda_g/4$.

The power depends on the holes dimension, the coupled wave maintain the propagation direction.

It can be used ONLY in a mono-modal waveguide.

The circular over-mode WG

Transmission of high power requires enough power handling.

In dry air the break down electric field is **15 kV/cm**, from the mode choice and the power delivered is possible to fix the minimum i.d. of the waveguide:

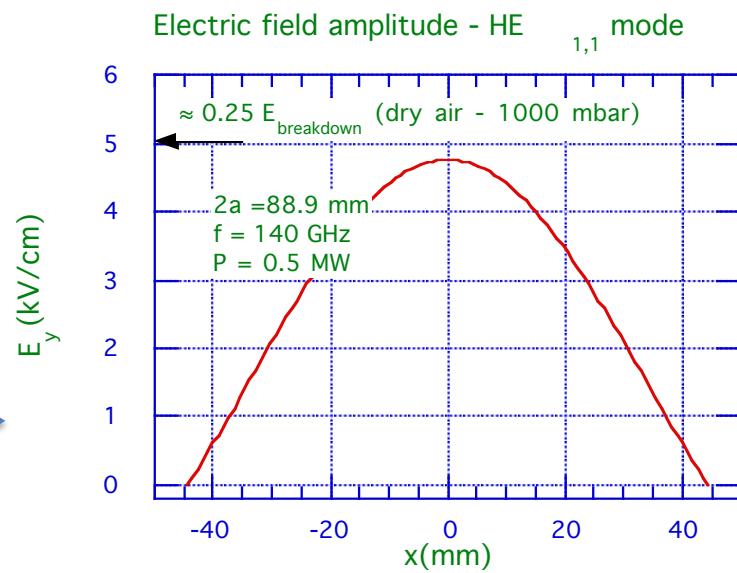
$$P = E_{\max}^2 1.99 \cdot 10^{-3} a^2 \frac{\lambda}{\lambda_g} \quad \text{TE1,1 in circular wg}$$

For $P = 1\text{MW}$

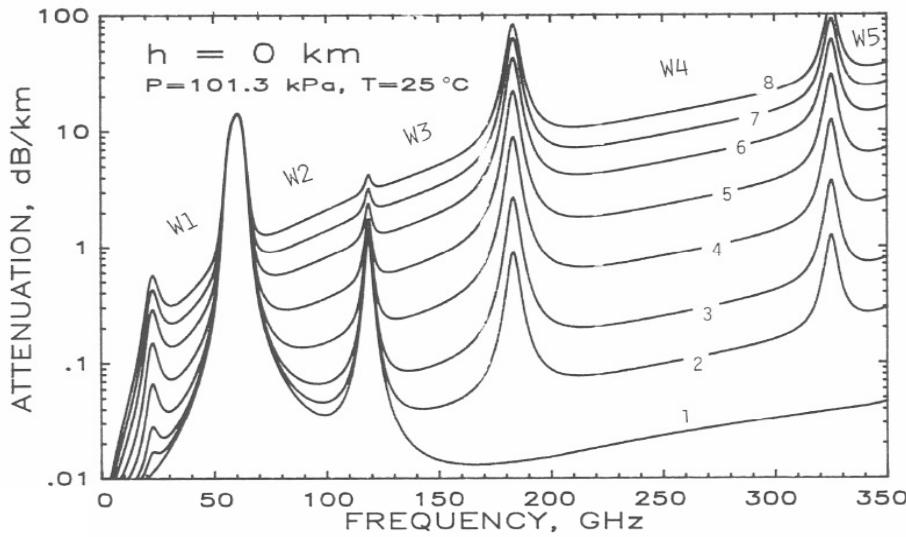
$E_{\max} = 7 \text{ kV/cm}$ (in case of reflection at mitre bend)

which requires a diameter of $\sim 10 \text{ cm}$

HE1,1 in corrugated over-mode wg



- 1- Breakdown: transmission of high power wave is limited by air breakdown that gives a limit to the electric field
- 2- Losses: the air can absorb high frequencies (losses) depending on humidity, as a consequence it is necessary to cool down the heated.



Propagation in Vacuum reduces the risk of arc (only on metallic surfaces) and eliminates the air losses.

To keep under vacuum a transmission line required a specific design and additional cost.

Under vacuum lines exhibits less problem with the RF leakage

Corrugated waveguide

A small corrugation on the wall of the wg produces a non zero impedance along wg axis (z), in this way a so called **hybrid modes** can propagate (combination of TE_{0N} and TM_{0N}).

When the wg i.d. $2a \gg \lambda > p$ (period of corrugation) the wg wall begin to look like a surface with an anisotropic reactance:



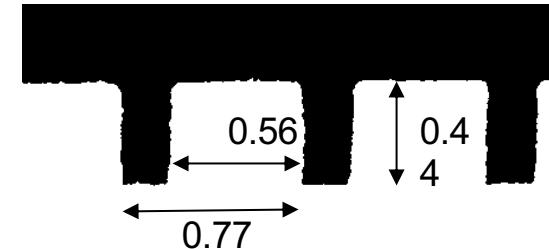
$$Z_\phi = \left. \frac{E_\phi}{H_z} \right|_a = 0$$

Internal diameter 88.9 mm

$$Z_z = -\left. \frac{E_z}{H_\phi} \right|_a \cong jZZ_0$$

$$Z = \frac{w}{p} \tan(kd)$$

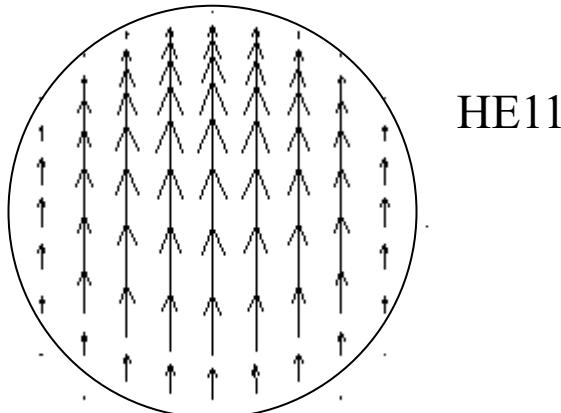
$$Z_0 = \sqrt{\mu_0 / \epsilon_0}$$



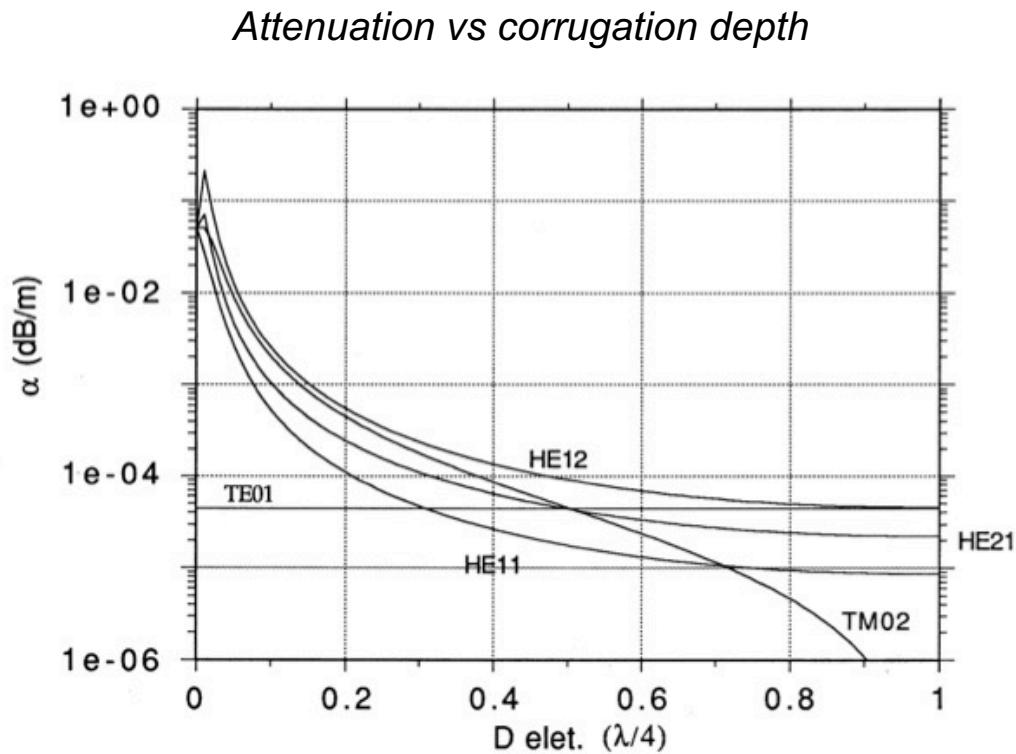
Detail of the wg wall section for ECRH-FTU TL system at 140 GHz

Attenuation of Hybrid Mode

The different attenuation can be exploited as modal filtering



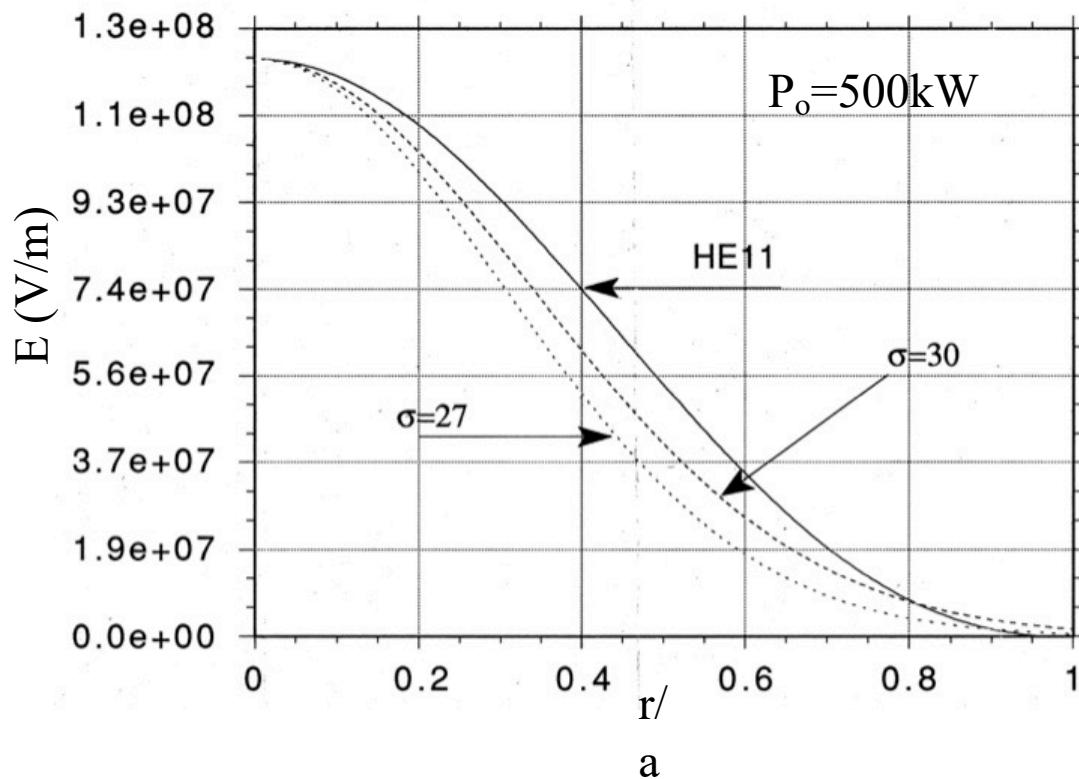
HE11 is the basic mode chosen in fusion application:
 It has a **low attenuation**, it is **linearly polarized** and propagate in free space as a **gaussian mode** (TEM00)



The electric field is close to zero at the wall, with consequent low ohmic attenuation

Hybrid Mode Field Profile vs Gaussian mode

Comparison with Gaussian Distribution (TEM00) with different waist (σ in mm for $a = 44.45$ mm)

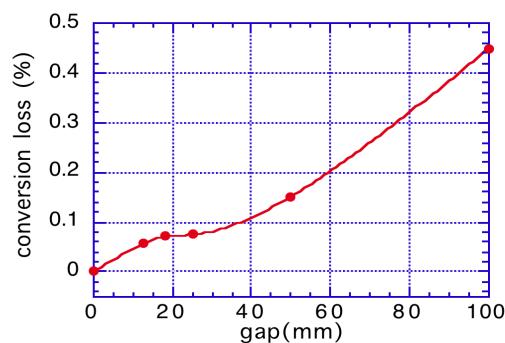
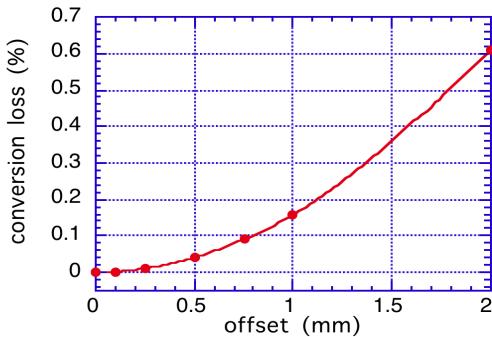
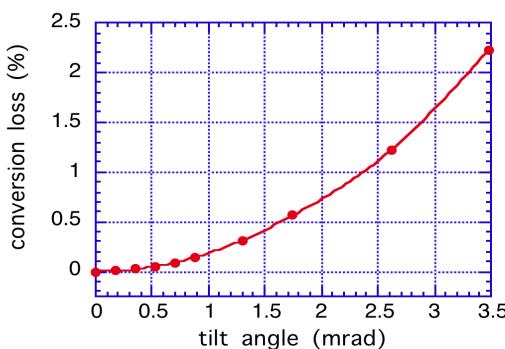


In the conversion from TEM00 to HE11 and vice versa the 2.5% of power is lost

Alignment Issues

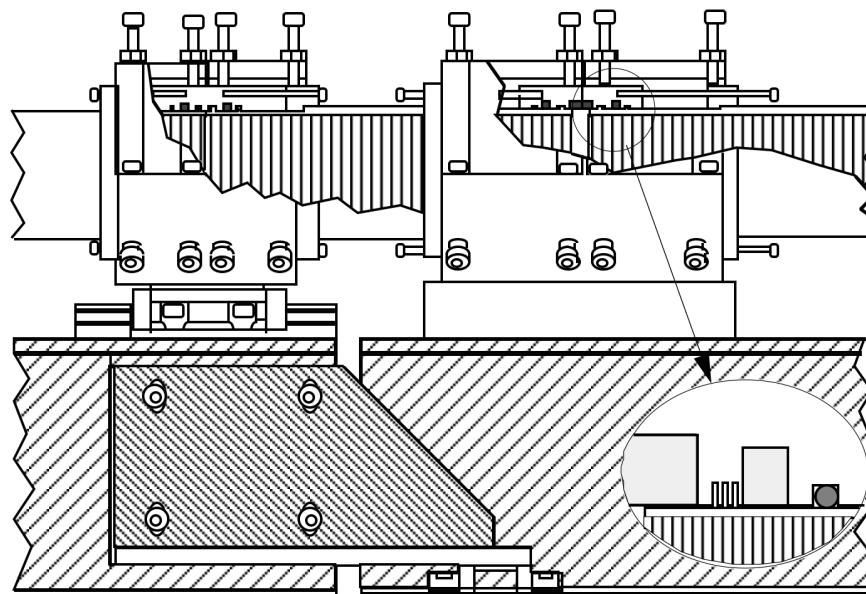


Conversion Losses due to alignment errors



Errors (tilt and/or offset) produce conversion to high order modes.

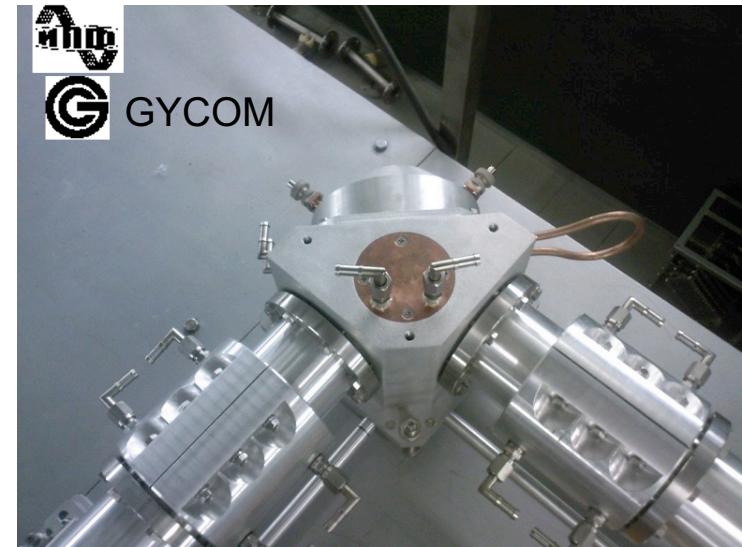
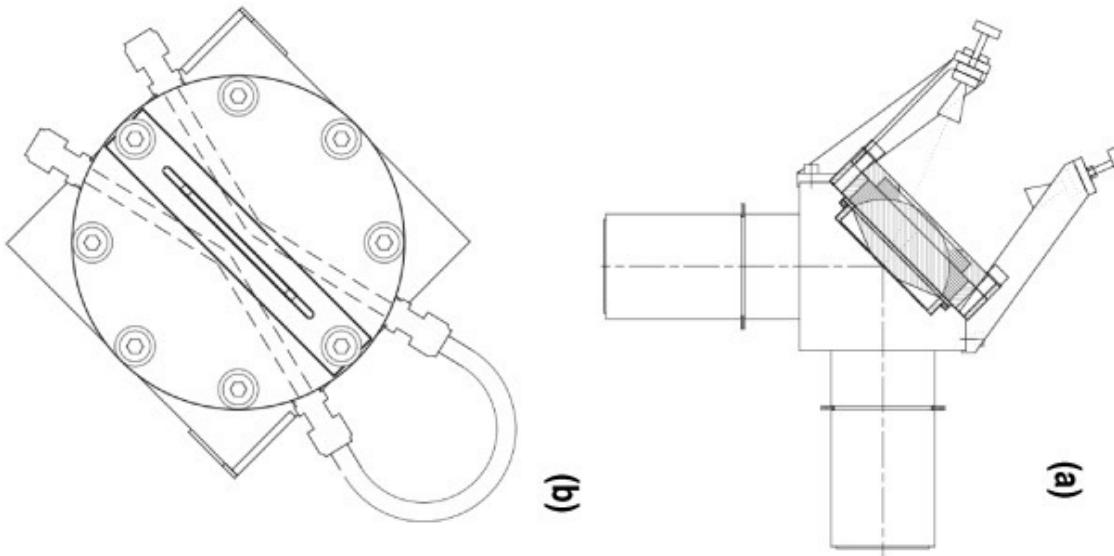
These modes are absorbed by wg requiring a larger cooling or a local increase of electric field (arc risk) .



Expansion Joint for FTU ECH system

In a over modal corrugated wg the change in direction can be done by reflection on flat mirror of the wave propagating after a open-ended wg.

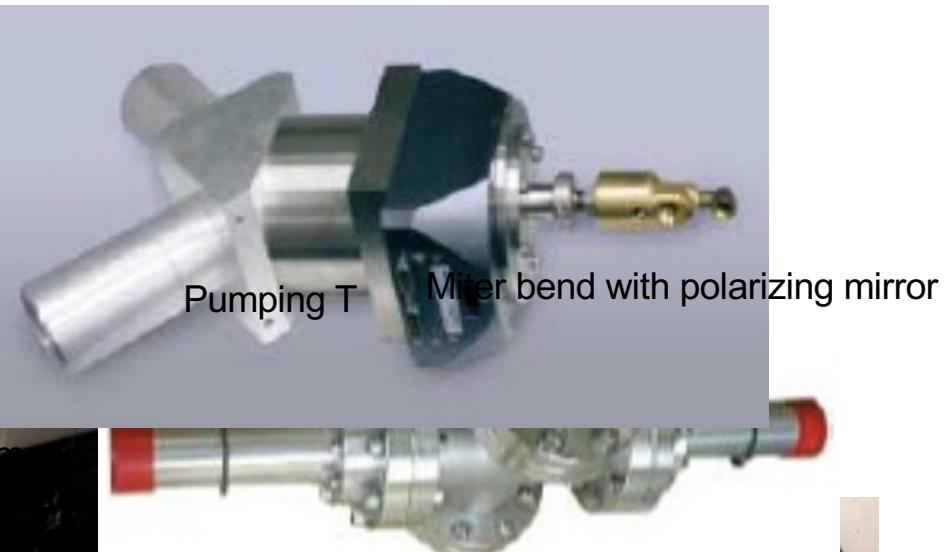
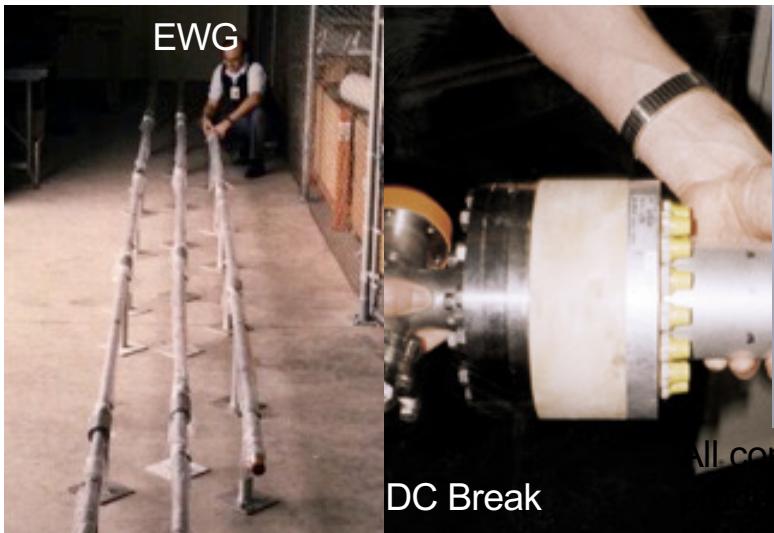
The losses depends on the length of the gap and on the frequency (+ ohmic one on the mirror)



GYCOM 170 GHz mitre bend and clamps for wg cooling

All the component of a cw transmission line must be cooled

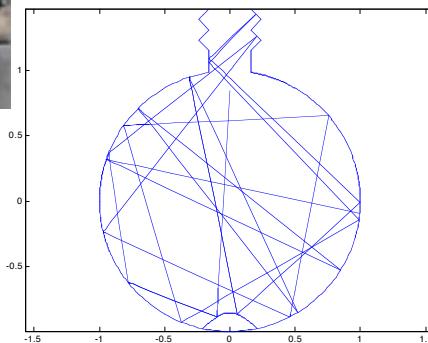
WG evacuated components (GA)



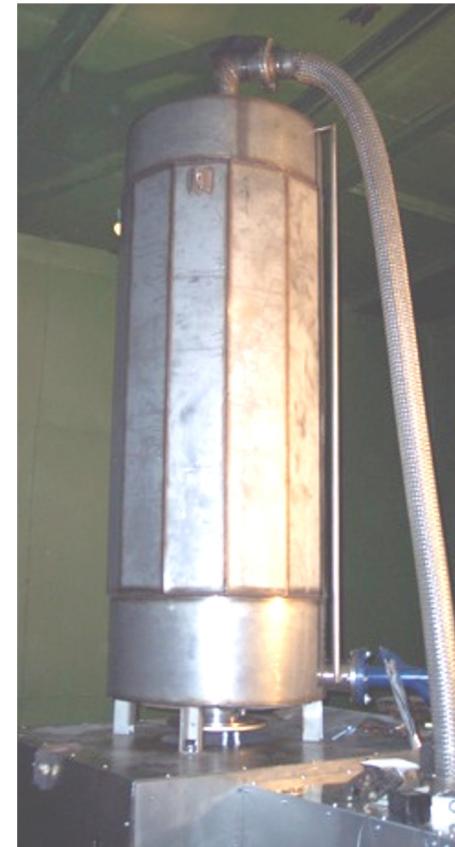
RF loads

The Gyrotron power must be directed on a **dummy load** during commissioning test or **conditioning**.

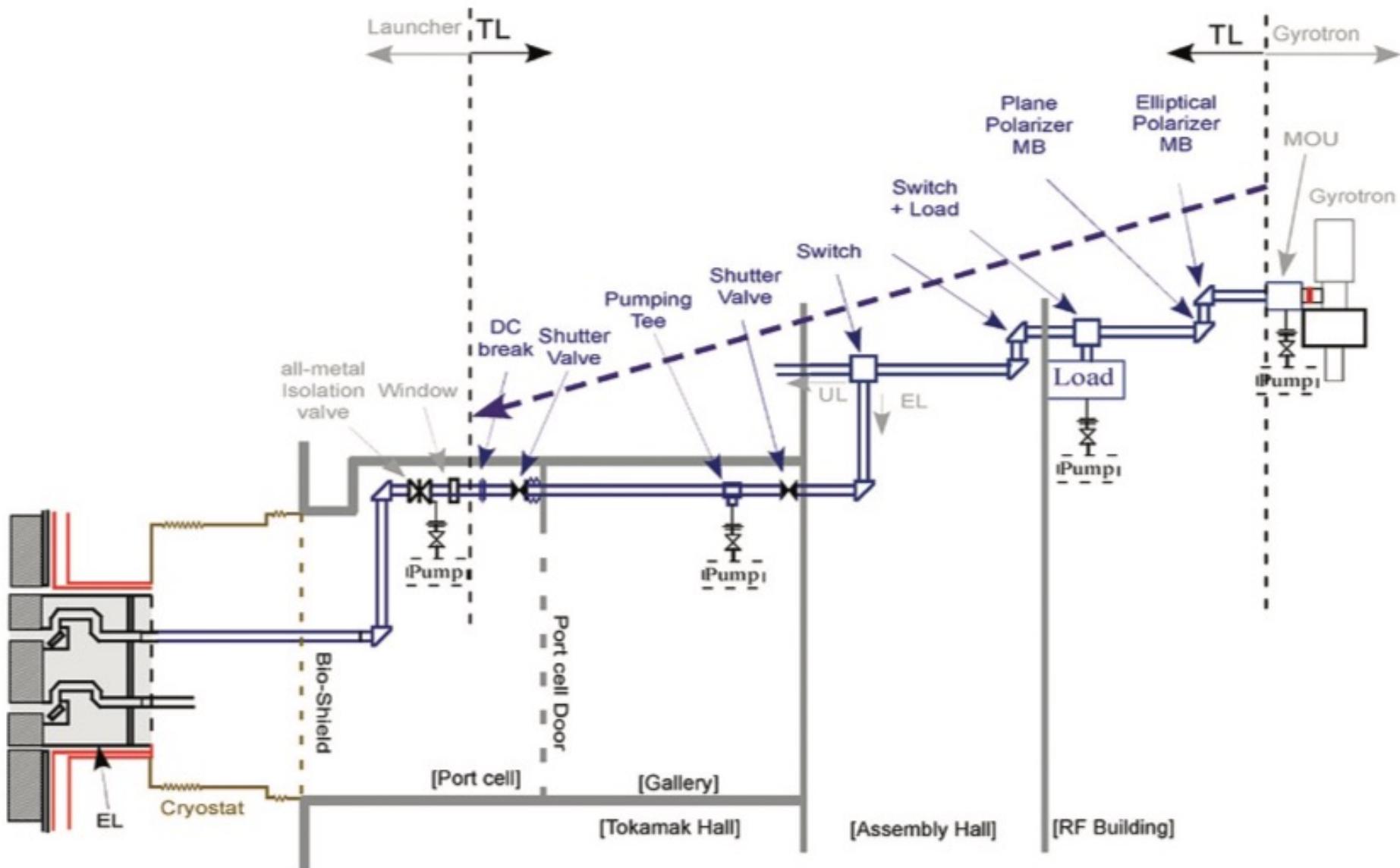
The load must have a low reflection (<4%) and the possibility to measure (bolometer) the absorbed power.



The sphere for FTU and 2MW EU project.



Gycom 2006 version
load. 1MW cw in air



The Quasi Optical Approach

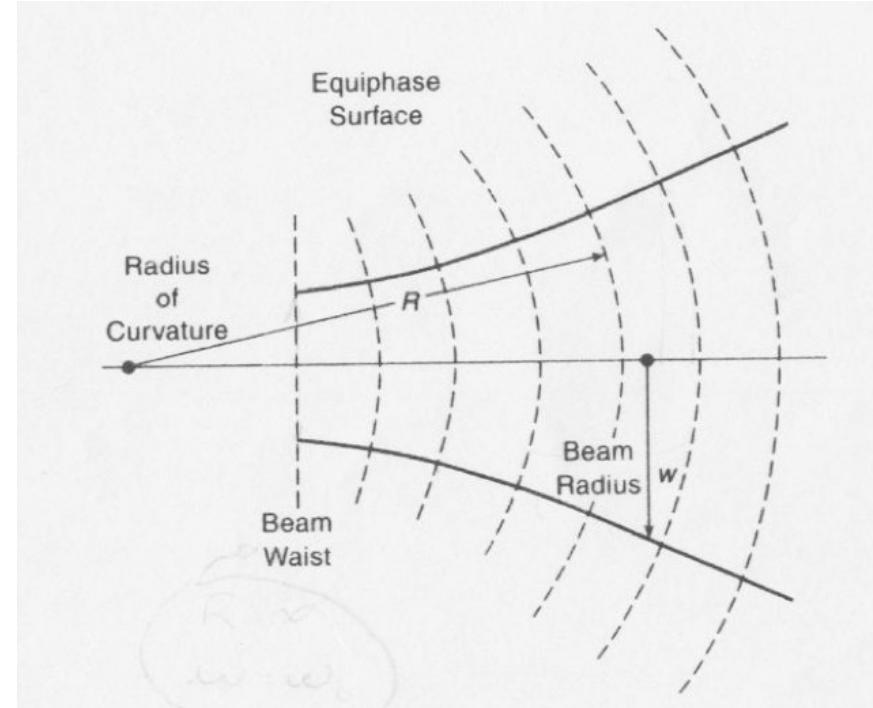
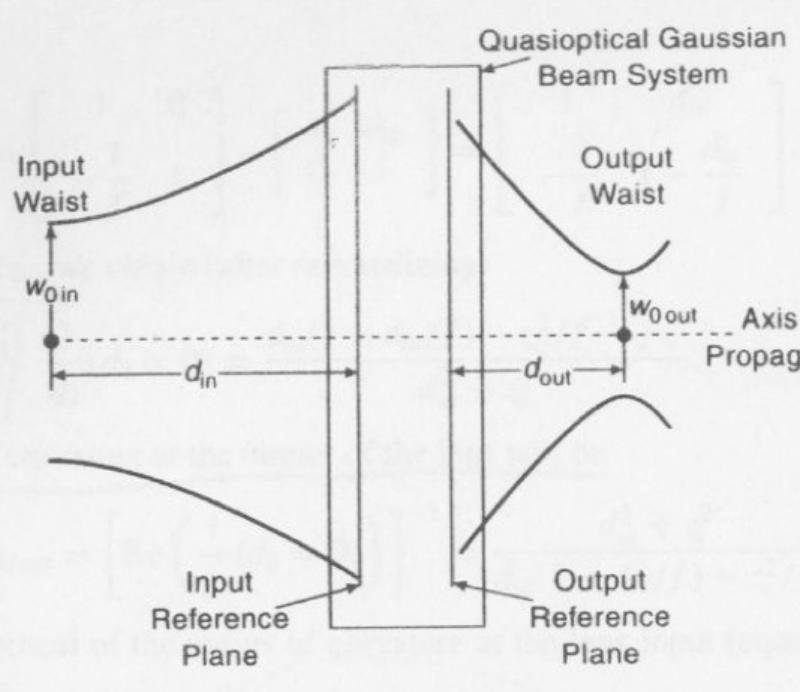
Considering wavelength (mm) the microwave beam can be approached using the optics propagation equations.

Beam diameter

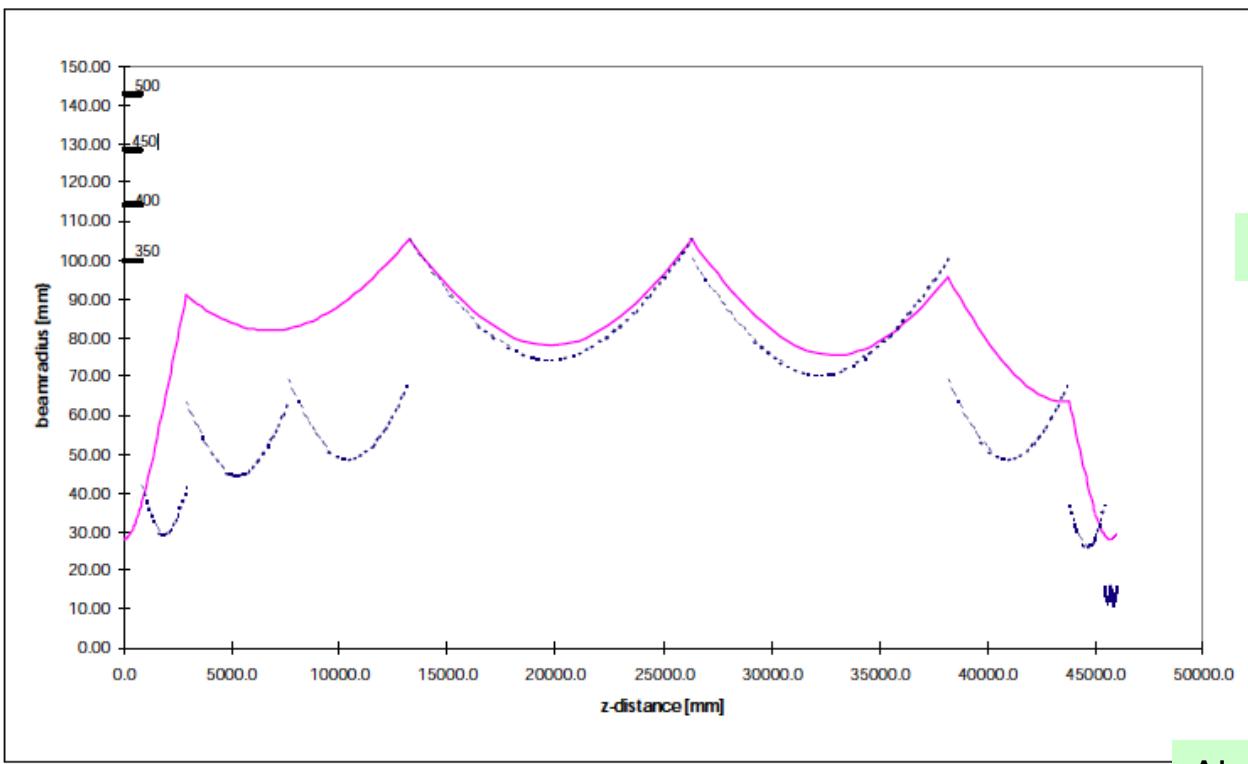
$$w(z) = w_0 \left[1 + \left(\frac{\lambda z}{\pi w_0^2} \right) \right]^{1/2}$$

Curvature of phase front

$$R(z) = z \left[1 + \left(\frac{\pi w_0^2}{\lambda z} \right) \right]$$



The power is reflected by large mirrors from the gyrotron output (MOU) to the vessel window.



Mirrors dimension $\sim 4 w$

High frequency-> less divergence

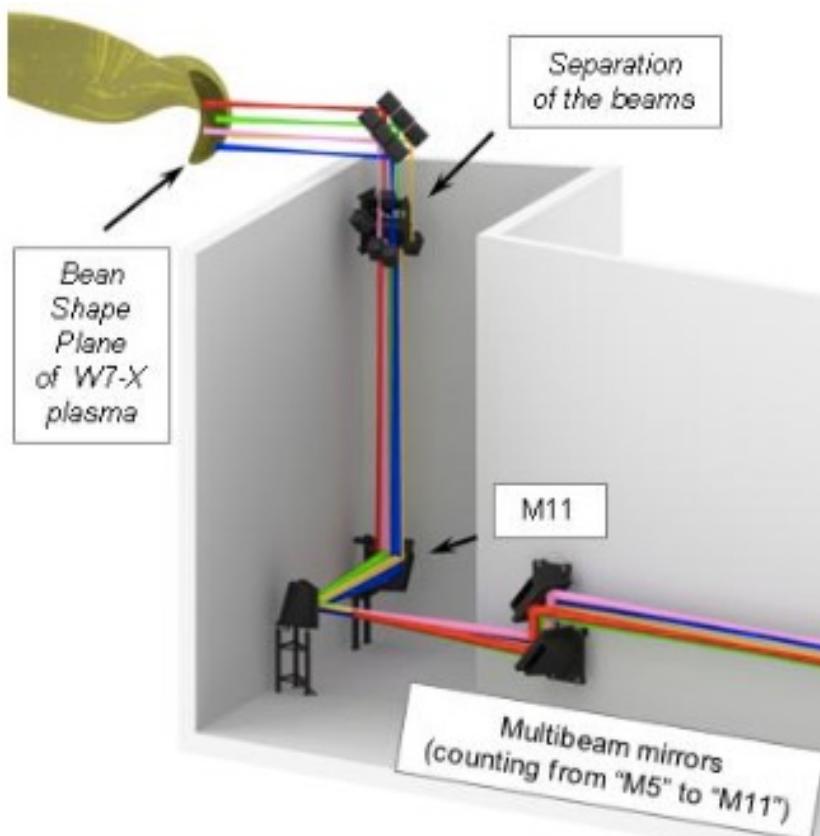
Only Ohmic losses ($\sim 0.25\%$ per reflection)

Multi beam capability

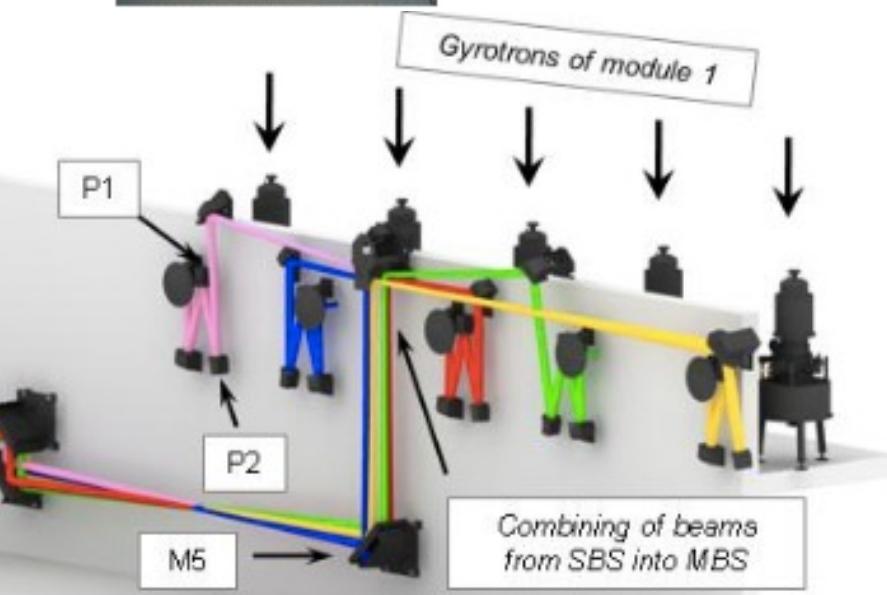
Low mode conversion

Air Conditioning (to dry and to cool)

figure 5. Beam radius (1/e E-field radius) along the Q.O. section of the line



T. Stange et al, EPJ Web of Conferences **157**, 02008 (2017)

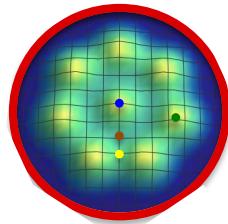
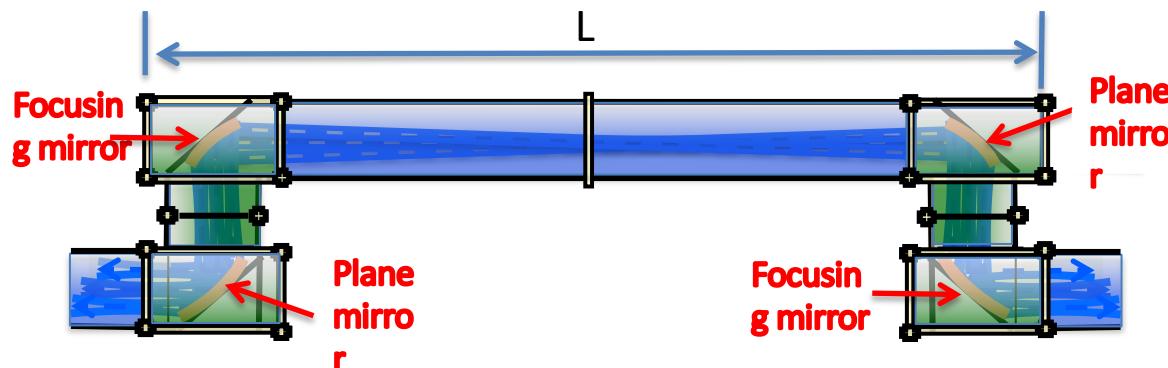


Concept for Multibeam Evacuated QO Transmission Line

Main DEMO TL requirements:

- Efficiency target: 90%
- Power handling: >1MW CW per line
- Multi-frequency (or broadband)
- Tritium compatible
- Large number of beams to be transmitted

The most promising and simple TL considered is a Quasi Optical Multi Beam Evacuated TL

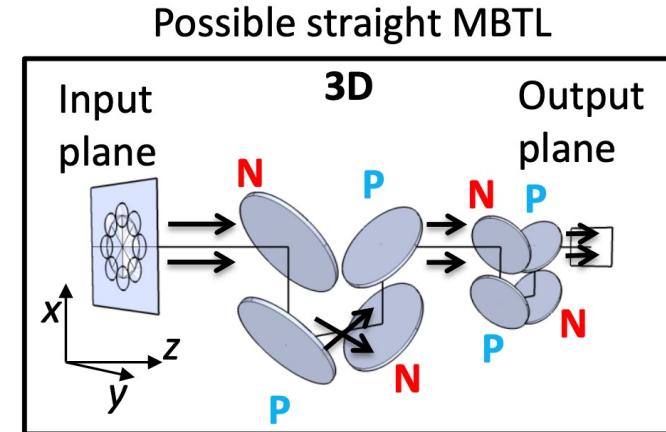
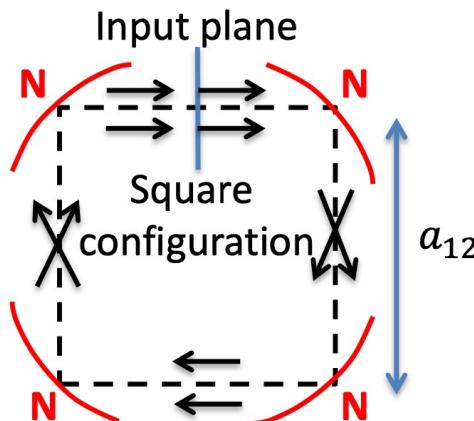
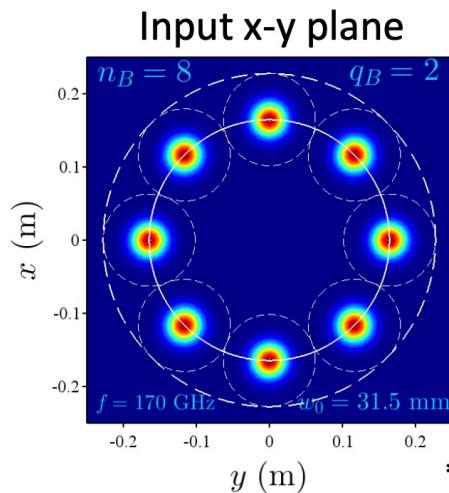


8 beams for each TL with a distance between Focussing units at $L = 8\text{--}10 \text{ m}$ → mirror dimension: 0.6 – 0.8 m

The confocal concept for QO TL



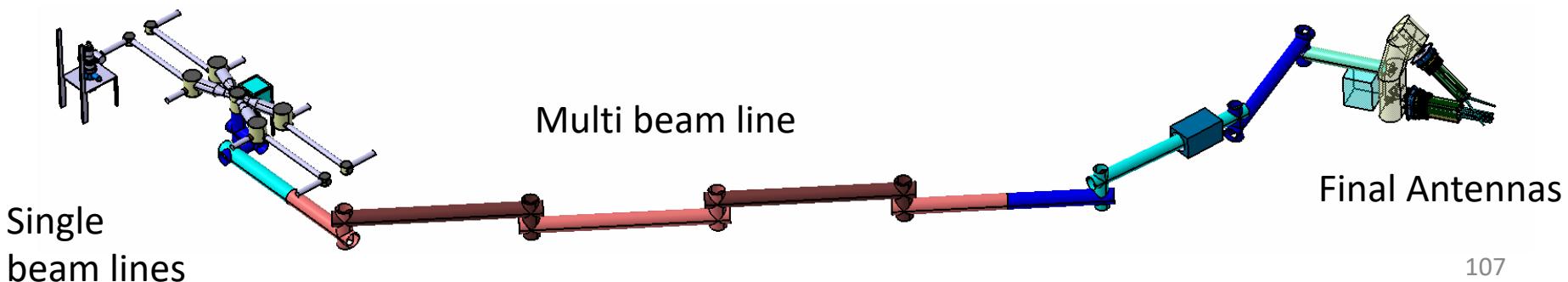
The arrangement with 4 non-plana mirrors allows to produce at the output the same image at the input, this is valid also in case of including 4 planar mirrors.



*L. Empacher and W. Kasperek , *IEEE Transactions on Antennas and Propagation*, **49**, 3 (2001)

gyrotron

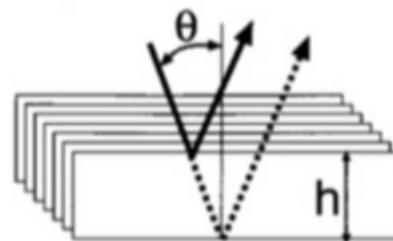
The DTT ECH Evacuated Transmission Line



The linear polarization from the gyrotron must be rotated in order to launch the proper direction with respect the B_T pitch angle. **It is necessary for ECCD.**

Oblique injection requires further rotation in order to compensate the XM or OM components originated by inappropriate angle.

The polarizer are based on corrugated mirrors.



Polarizer Concept

The component E_{\parallel} (with respect to corrugation) is reflected at the bottom

The component E_{\perp} is reflected at the top

A phase shift of $2h/\lambda$ of E_{\parallel} respect to the E_{\perp} (reflected at the top).

This produces a rotation of the electric field.

Using a $\lambda/4$ corrugation depth only linear rotation can be obtained, with $\lambda/8$ one a circular component is introduced to obtain elliptical polarization to be used in case of oblique injection.

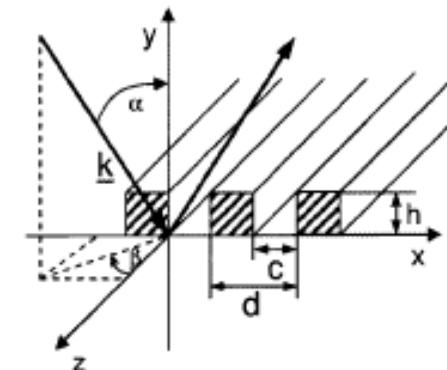
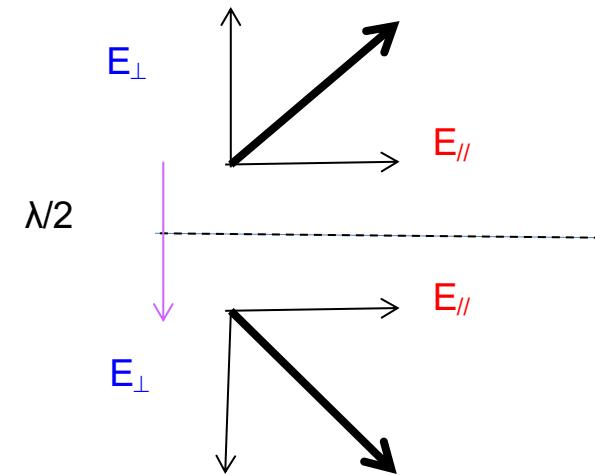
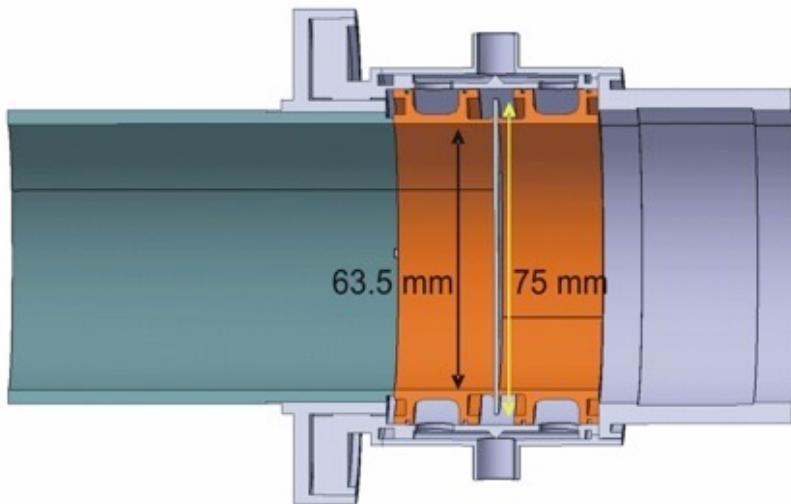


Fig.1 Polarizer corrugation.





Diamond disk Diameter: 75 mm
Thickness: 1.11 mm

Loss measurements at 170 GHz:

$$\operatorname{tg} \delta_{\text{eff}} = 0.9 \times 10^{-5} \text{ (central area)}$$



T. A. Scherer et all 5th IAEA TM
18-20/Feb. 2009 Gandhinagar, India

Launcher

The simpler launcher

At the end of the transmission line the power must be coupled to the plasma. The TL must be connected to an **ANTENNA**. In the EC wave case the antenna becomes a **LAUNCHER**, being the frequency so high that the wave can be thought as propagating light beam.

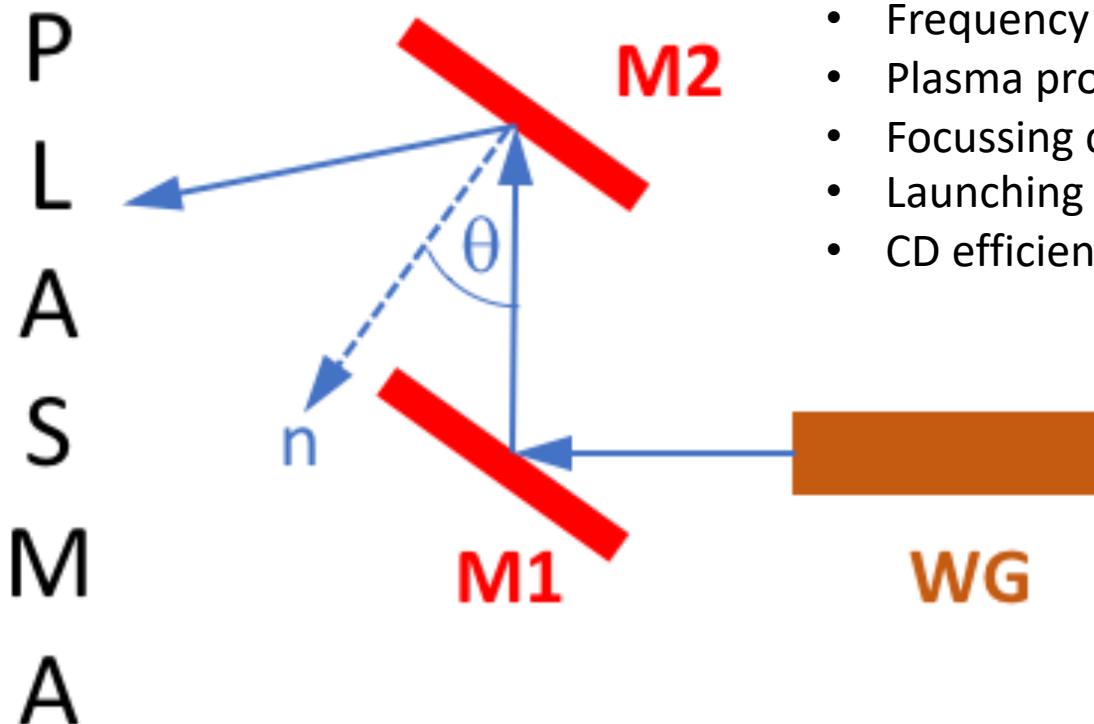
A **truncated waveguide** propagating the delivered mode (TE0,1 or HE1,1) was the main launching antenna used in the pioneering experiments.

The **divergence of the beam** can be reduced increasing the wg diameter and the frequency.

This simple launcher is enough for **heating** experiments but not usable for **ECCD** and **MHD** control.

The front steering concept

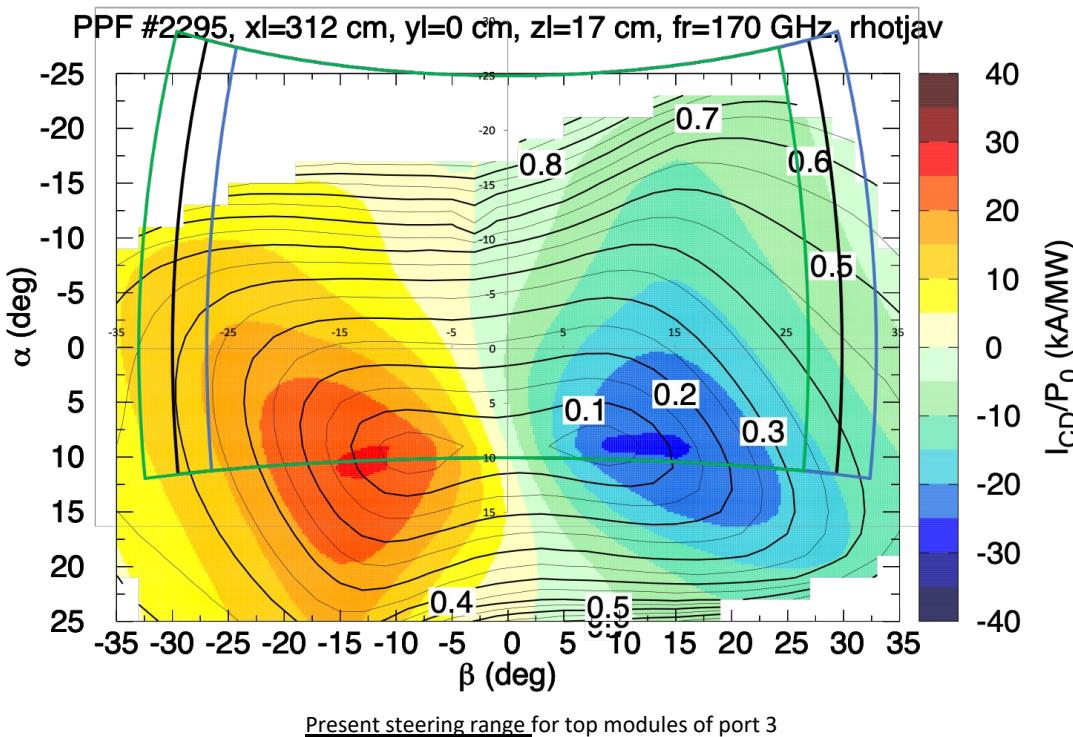
The most popular launcher is a Open Ended Wave Guide, at which is added a mirror to focus and steer the EC beam in plasma



The optics characteristics depend on:

- Frequency
- Plasma profiles
- Focussing distance (q surfaces position)
- Launching points
- CD efficiency required

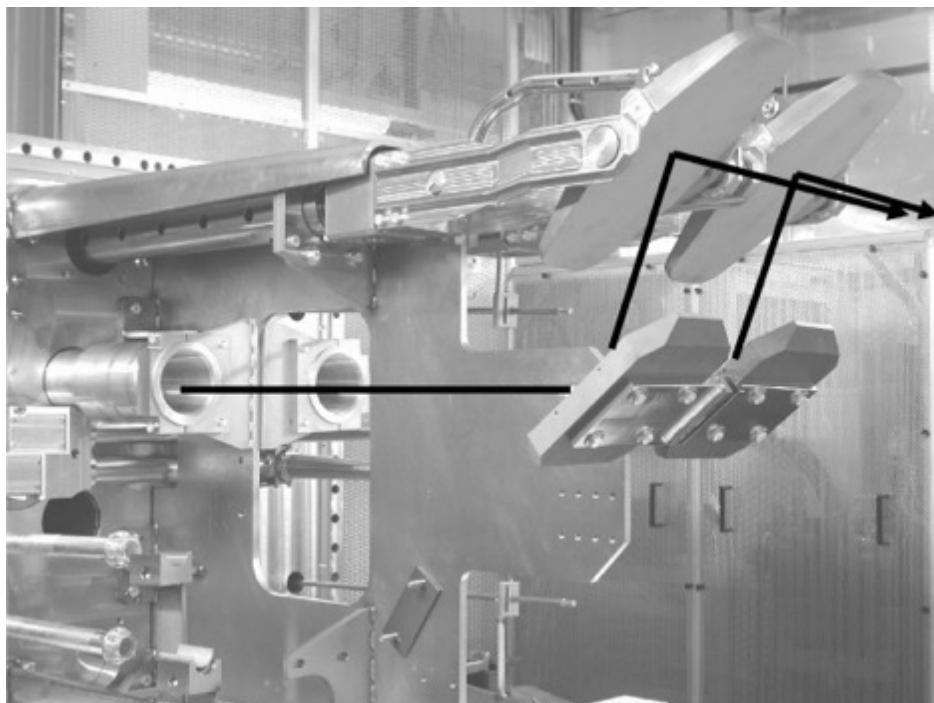
Steering requirements



GRAY code applied to DTT

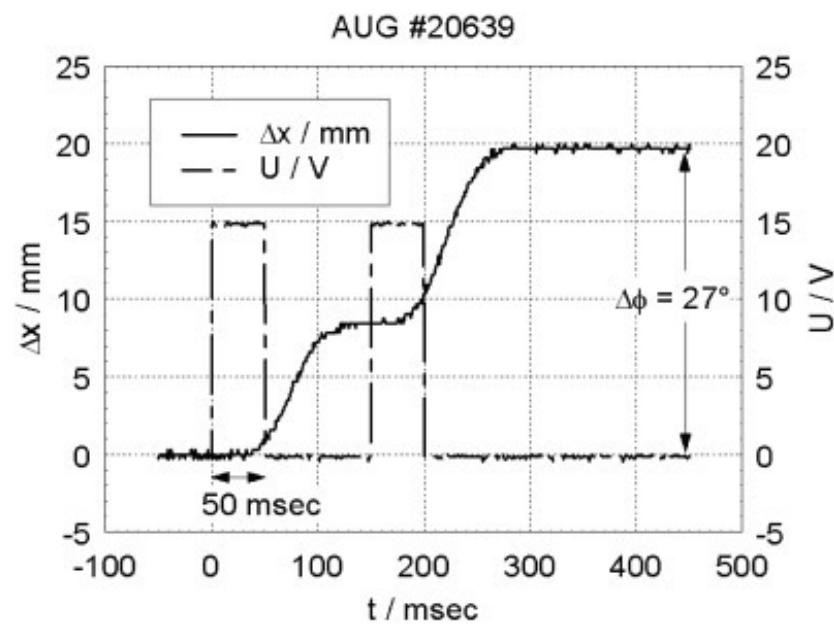
To fix the requirements for the steering ranges of the movable mirror a beam tracing map is usually generated.

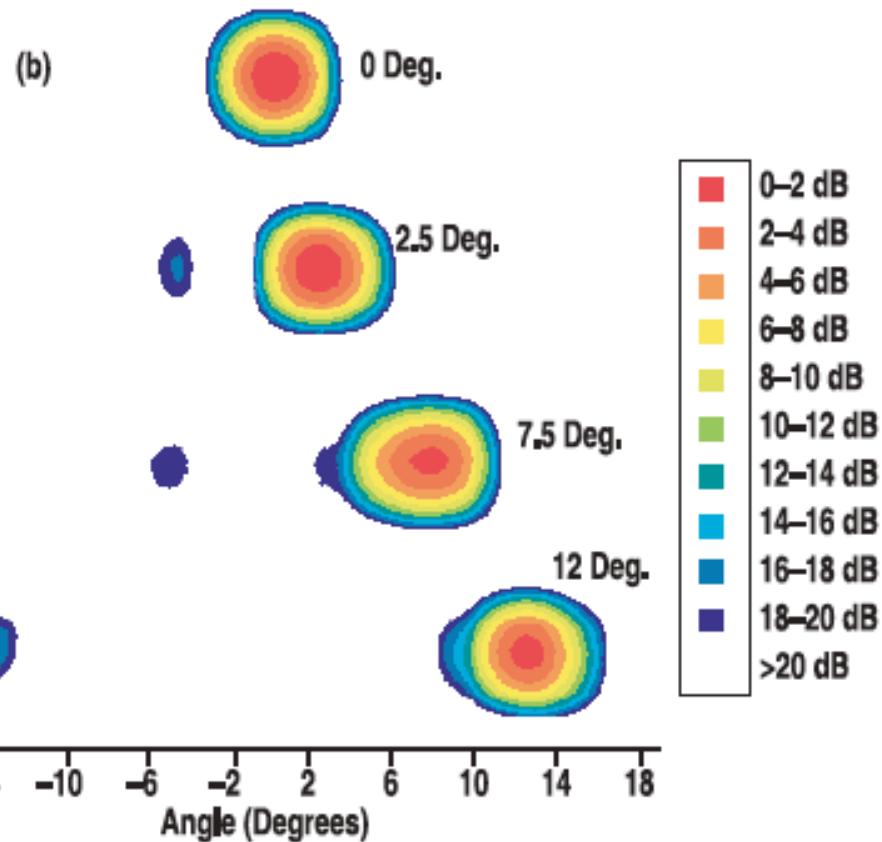
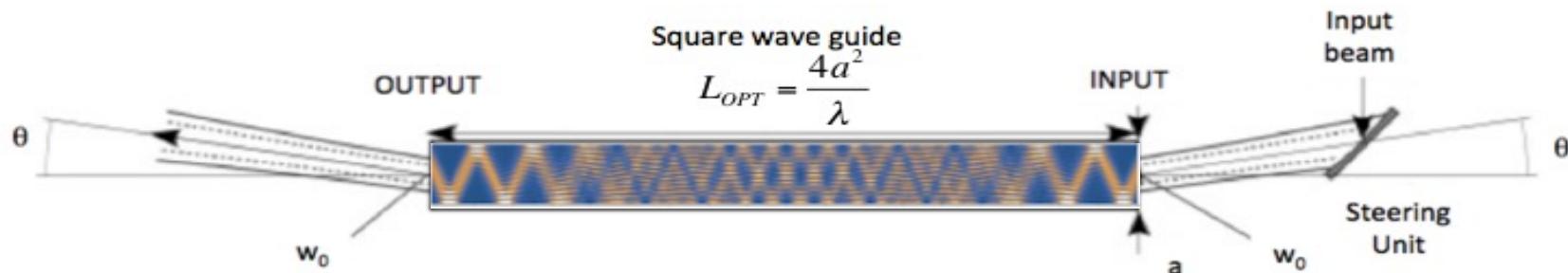
The CD efficiency is calculated as a function of launching angles, and the best range is defined starting from the requirements of the EC system.



Movable mirrors in front of the plasma to steer the beam in the desired point

Real time mirrors steering
(settling time ~ 100 ms)



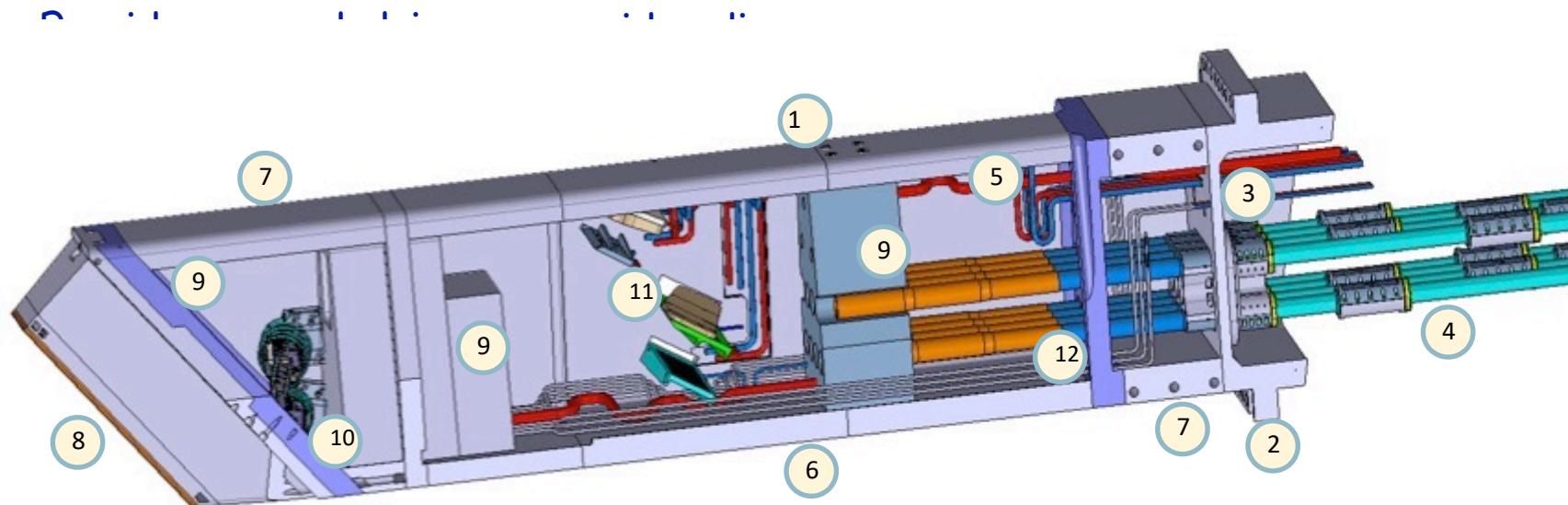


In a corrugated square waveguide the beam propagates decomposed in different modes that recombine after an integer number of coherent distances

Experimental
 Output pattern
 Good but not enough
 oblique angle

Primary Role

- Stabilize MHD activity (Sawtooth and NTM), requiring narrow peaked deposition profile (Deposition width ~4cm)



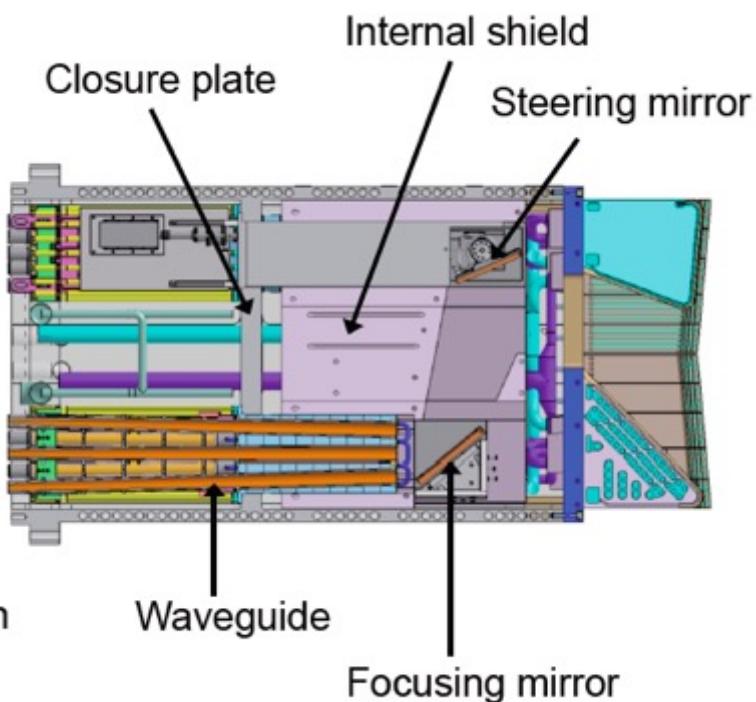
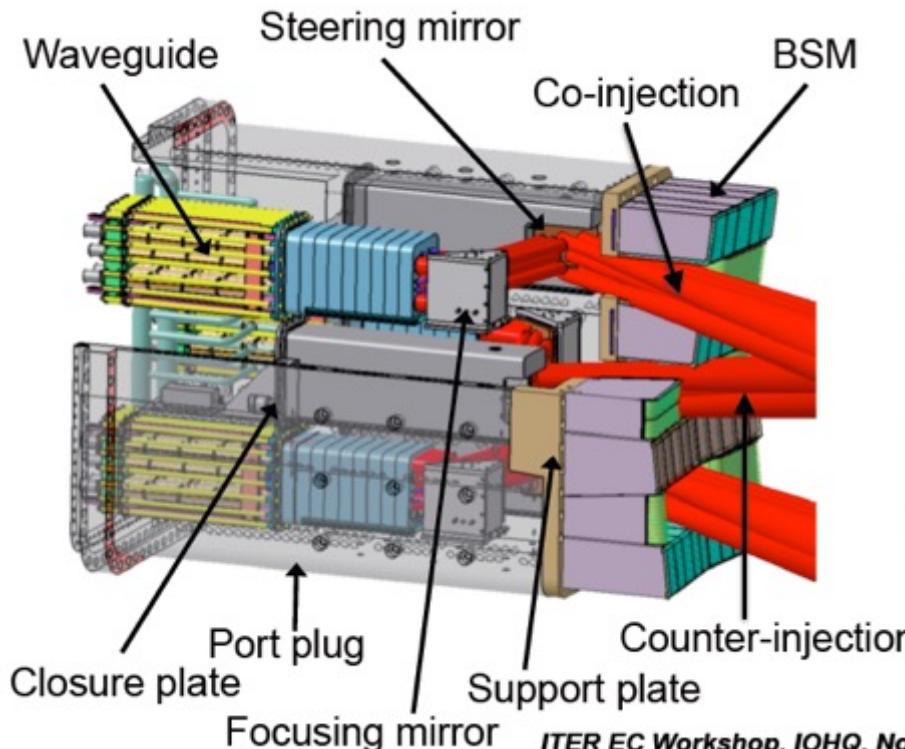
- Overall port plug length ≈ 6m
- Rear flange width ≈ 1.3m
- Wall thickness mid section = 90mm
- Total weight ≈ 18t (no water)
- Internal layout designed to allow guided and free propagation of 8 mm-wave beams

UL components:

1. Port plug body
2. Rear flange
3. Closure plate and feedthroughs
4. Ex-vessel waveguide assembly
5. Services (cooling, gas, etc.)
6. Single wall structure
7. Double wall structure
8. BSM and first wall
9. Neutron shield
10. Steering mechanisms
11. Fixed mirrors
12. In-vessel waveguides

Primary Role

- Central Heating and current drive
- Impurity control
- Breakdown and Burn through
- Current profile tailoring

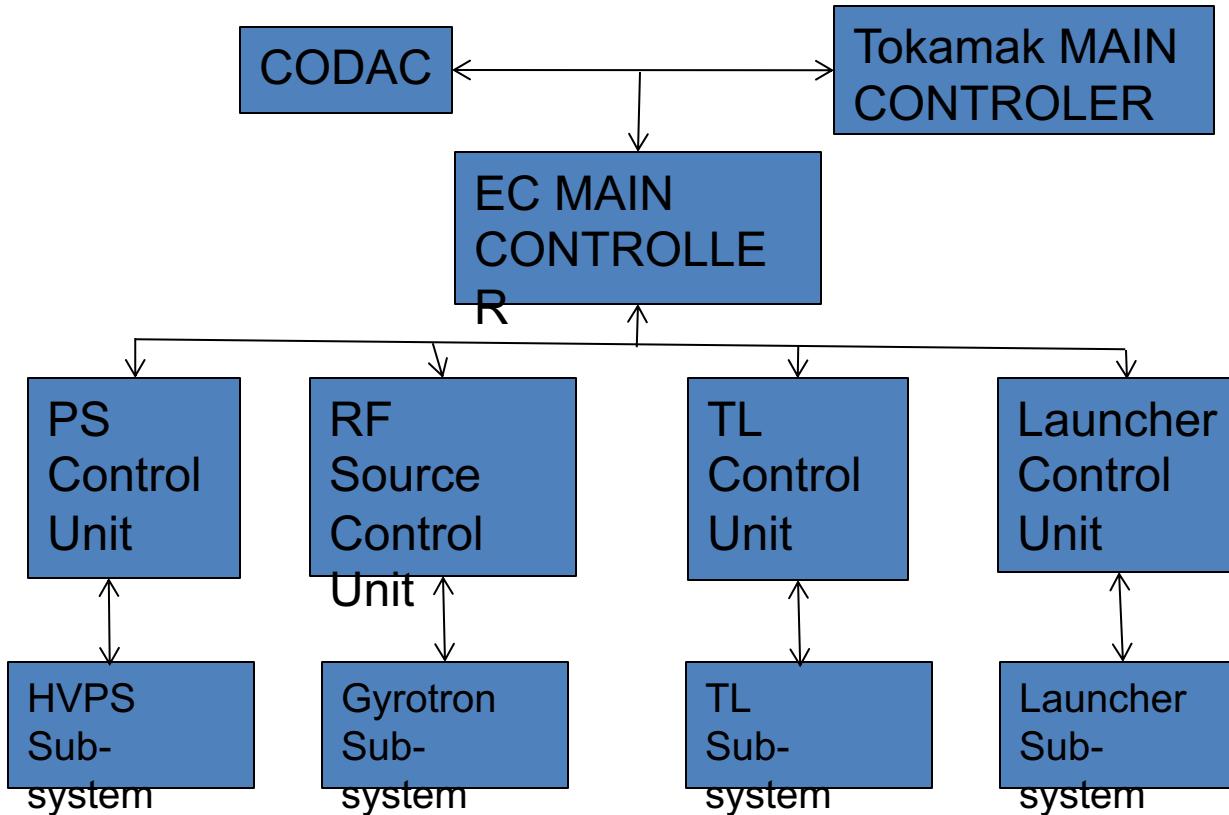


ITER EC Workshop, IOHQ, Nov. 18th – 22nd, 2013

Note that beams now steer in poloidal direction

Control System

The control system



The EC control system

Four different levels of control system:

Fast control: $t < 1\text{ms}$

Fast Sequence Control

Protection system

Real Time Control

Local plant control: $t \sim 100\text{ms}$

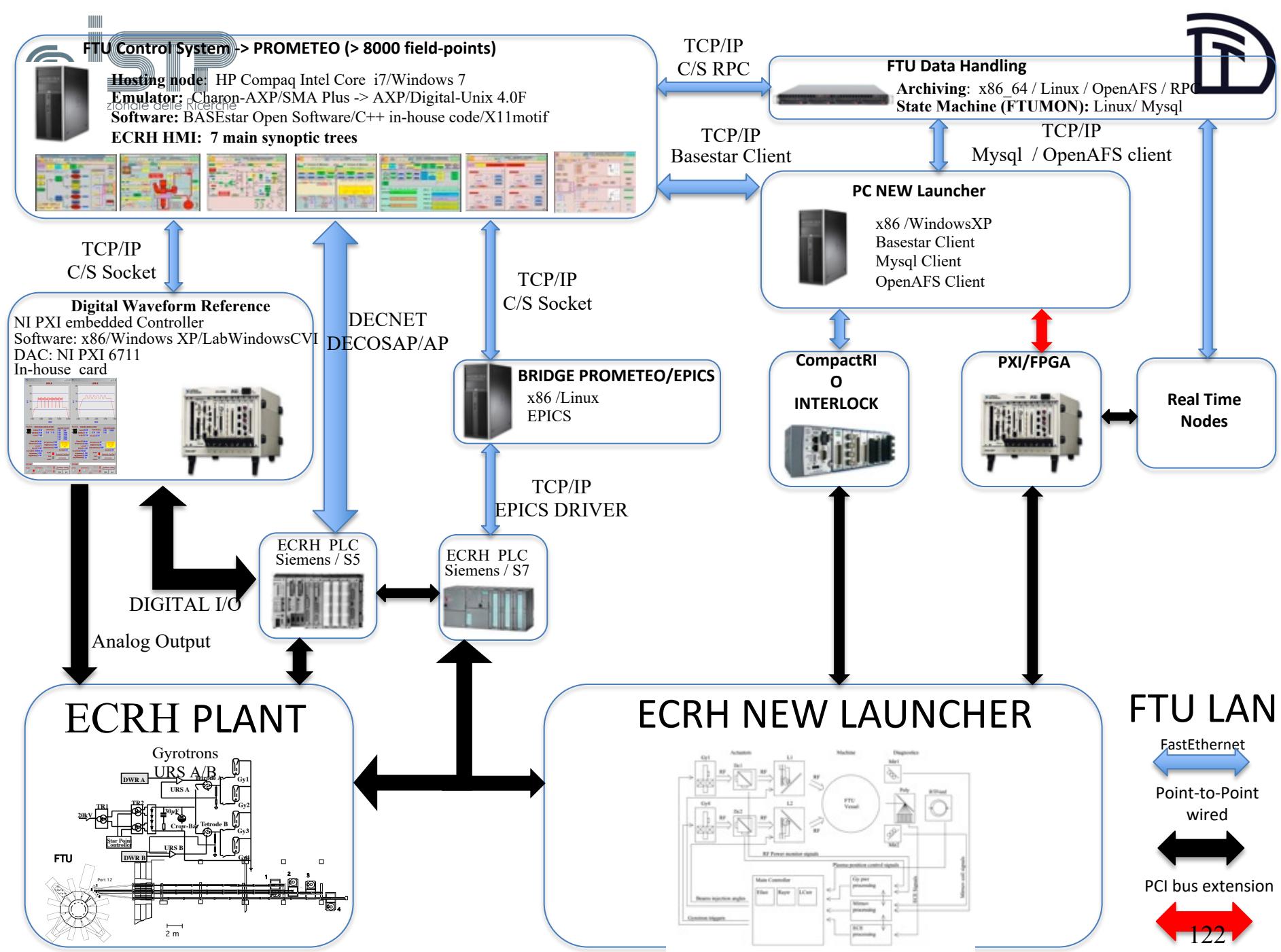
PLC

Field to field connections:

for higher level of safety: $t \sim 10\text{ms}$

Main controller for human interface $t \sim 1\text{s}$

mimic, sequence control:



Final Remarks

EC Systems is nowadays the most promising Heating System for future reactor:

- No component close to plasma
- Remote power generation
- Simple transmission of the power
- Interaction plasma-wave well known
- Modular approach