

Theory and Advanced Simulation

The Reversed-Field Pinch case

Helical Self-Organization processes

Susanna Cappello susanna.cappello@igi.cnr.it

Theory and Simulation physics group of Consorzio RFX

*Consiglio Nazionale delle Ricerche – CNR – ISTP (Istitute for Plasma Science and Technology)
CONSORZIO RFX*

*Associazione Euratom-ENEA sulla Fusione - PADOVA - ITALY
partnership of CNR, ENEA, INFN, Padova University and Acciaierie Venete spa*



Preliminary considerations, a few slides:

RFP and RFX in Italy,
Theory-Simulation EUROFusion context.

“Palazzo della Ragione”



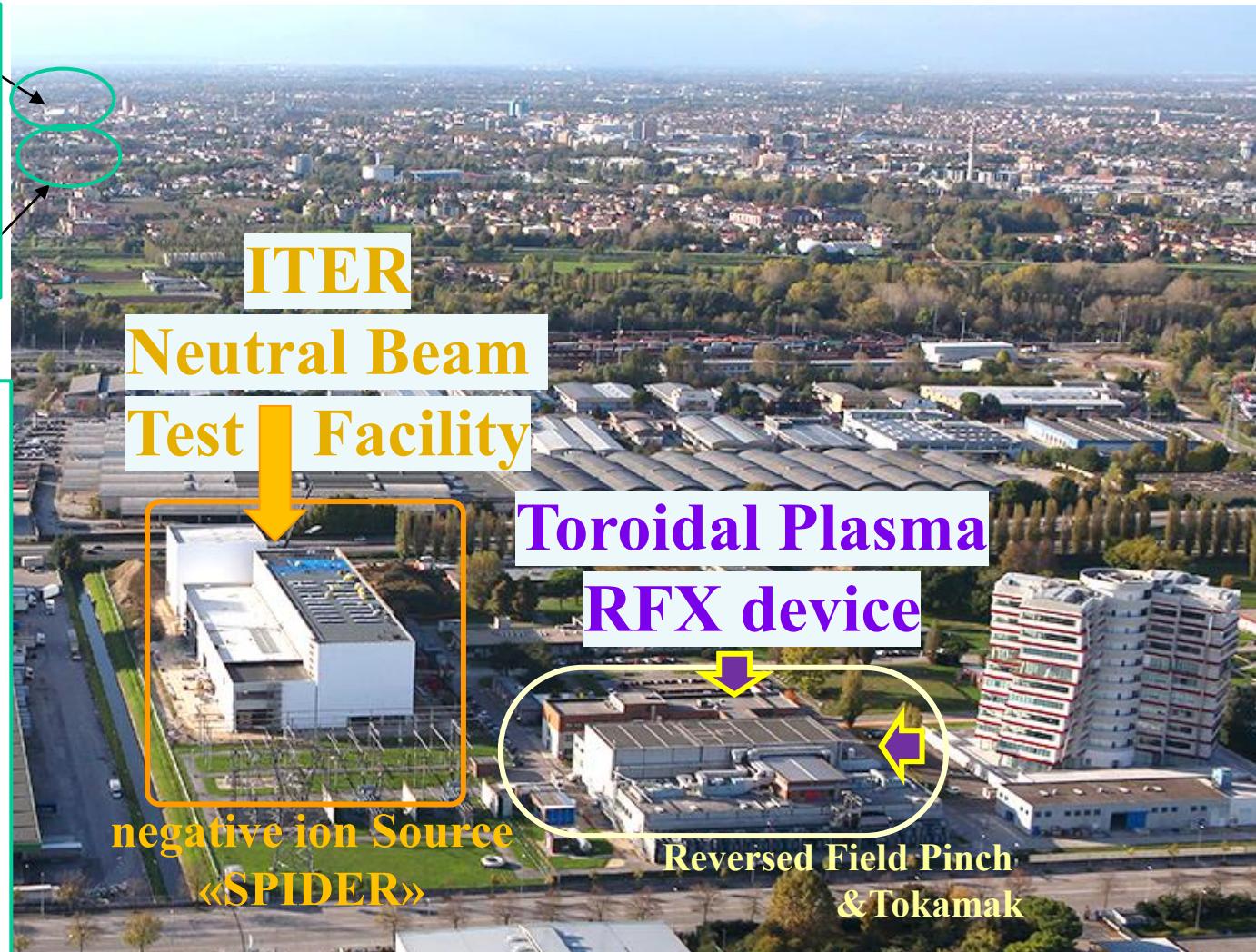
From the web

https://en.wikipedia.org/wiki/Palazzo_della_Ragione,_Padua

Padova University historical site



From the web



https://en.wikipedia.org/wiki/University_of_Padua

Reversed Field Pinch, RFP, partners:
USA - Sweden - Japan – China

High priorities infrastructures in Italy (for Fusion): DTT (ENEA) and RFX (CNR)

NRRP (National Recovery and Resilience Plan):

project “**NEFERTARI**” based upon the **RFX** Research_Infrastructure

Project title: ‘**NEFERTARI**’

(**New Equipment for Fusion Experimental Research & Technological Advancements with Rfx Infrastructure**)

Project aim: innovation of **experimental equipment** and **diagnostic systems** for RFX-mod2

Duration: 30 months (**2022 – 2025**) *with a perspective scientific exploitation for the next 10 years*

EUROfusion welcomes alternative approaches and intellectual diversity

The Reversed Field Pinch research is an example

The Reversed Field Pinch research is an example

EUROPEAN RESEARCH ROADMAP

https://euro-fusion.org/wp-content/uploads/2022/10/2018_Research_roadmap_long_version_01.pdf

(2018 revision, FP9: 2021-27,
after first release in 2013, FP8: 2014-20)

Preface by T. Donnè & W. Morris - page 3:

“ The strategy of the fusion roadmap is built on three main pillars:

- the international ITER tokamak
- a fusion neutron source facility for materials development and qualification
- demonstration power plant DEMO

In addition, a strong **research and innovation programme is needed** supporting these and looking towards commercial fusion power plants.

Parallel research and innovation programmes ... include **alternative approaches**, notably the stellarator.

In pursuing this goal, Europe should seek all the opportunities for international collaborations for mutual benefit from the **intellectual diversity** of the whole fusion community and from the sharing of resources and facilities.”

Magnetic Configurations for fusion energy

The RFP magnetic configuration is produced mainly by plasma current itself
In principle, no additional heating system appears necessary

Stellarator

Tokamak

RFP

Increasing plasma current



Steady state



Coils Complexity

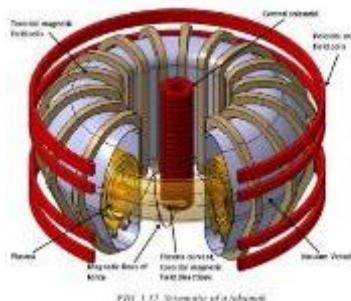


[*]

FIG. 1.14. Schematic of stellarator magnetic field coils and plasma configuration (Ref. [1.62]).

$R = 5.5 \text{ m }$ W7-X
($R = 3.9 \text{ m }$ LHD)

$R = 1.65 \text{ m }$ AUG
 $R = 3 \text{ m }$ JET
 $(R = 6.21 \text{ m })$ ITER



Light Tech expected

Confinement

RFP

Global Helical self-organization



$R = 2.0 \text{ m }$ RFX
(1.5 m MST USA
1.4 m KTX Hefei China)

<https://doi.org/10.1088/1741-4326/abc06c>

[*] Fusion Physics IAEA 2012

[**] Marrelli et al 2021 Nuclear Fusion

Magnetic configurations for fusion energy despite the differences
display several **common physics issues**

Transition low–high confinement regimes

Transport barrier formation

Magnetic relaxation

RFP dynamo/Flux pumping effect

Density limit

Isotopic effect

“Anomalous” ion heating (like in Solar Corona?)

...

proficuous **challenge** for theories, models, understanding !

theories, models, understanding ... in EUROfusion

EUROfusion E-TASC groups **TSVV & ACH** aim at “validated predictive capability”

Eurofusion Theory and Advanced Simulation Coordination effort (E-TASC):

<https://iopscience.iop.org/article/10.1088/1361-6587/ac44e4>

X. Litaudon et al PPCF (2022)

“ Therefore, it is timely to prepare this transition with a **coordinated, comprehensive: Theory, Simulation, Verification and Validation programme**

TSVV

to maximize the benefit delivered from investment in large facilities.

This aspect is recognized in the revised version of the Research Roadmap for the Realisation of Fusion Energy (Donné et al 2017, European Research Roadmap to the Realisation of Fusion Energy 2018) which states

'For all the missions, a **theory and modelling effort integrated tightly with the experimental programme will be crucial in providing the capability of extrapolating the available results to ITER, DEMO and commercial fusion power plants through carefully validated models and codes**'. An empirical approach will not be sufficient to bridge the gap between an experimental facility like ITER and a demonstration facility-like DEMO as stated in the EUROfusion 25 Research Roadmap '

It has become clear that a strong theory and modelling programme is essential because empirically-based predictions are uncertain in unexplored environments like ITER and particularly DEMO, and this will be a stronger focus than foreseen earlier.

It will make use of **Advanced Computational techniques and High performance computers.** ”

AC-Hubs

EUROfusion E-TASC groups: TSVV & ACH



TSVV

Develop state-of-the-art codes for the WPs to also be used for ITER and DEMO

ACH

Support the TSVVs in code development

TSVV:

Theory, Simulation, Verification and Validation

ACH:

Advanced Computing Hubs

E-TASC KOM: Introduction | April 23, 2021

https://indico.euro-fusion.org/category/279/attachments/1700/3352/ETASC-KOM-Intro_Naulin_Jenko.pdf

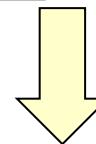
On a smaller scale, RFP research is a *proficuous* place for training and practicing *TSVV*:

“Theory, Simulation, Verification & Validation”

Verification and validation are defined in the DOE Defense Programs (DOE/DP) program plan for the Strategic Computing & Simulation Validation & Verification Program [1] as:

Verification – The process of determining that a computer simulation correctly represents the conceptual model and its solution.

Validation – The process of determining the degree to which a computer simulation is an accurate representation of the real world.



Am I solving the model correctly?

Am I solving the proper model?

... Benchmarking against
- analytical solutions
- different codes

... Tight connection and comparison with experiments

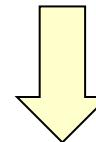
On a smaller scale, RFP research is a *proficuous* place for training and practicing:

“Theory, Simulation, Verification & Validation”

Verification and validation are defined in the DOE Defense Programs (DOE/DP) program plan for the Strategic Computing & Simulation Validation & Verification Program [1] as:

Verification – The process of determining that a computer simulation correctly represents the conceptual model and its solution.

Validation – The process of determining the degree to which a computer simulation is an accurate representation of the real world.



Am I solving the model correctly?

Am I solving the proper model?

... Benchmarking against
- analytical solutions
- different codes

... Tight connection and comparison with experiments

‘Newcomers’,

Uncertainty Quantification (UQ) Sensitivity Analysis (SA)

<https://pmc.ncbi.nlm.nih.gov/articles/PMC9232142/>

While scientific computing has undergone extraordinary increases in sophistication, a fundamental disconnect exists between simulations and practical applications. While most simulations are deterministic, engineering applications have many sources of uncertainty arising from a number of sources such as subject variability, initial conditions or system surroundings.

<https://pmc.ncbi.nlm.nih.gov/articles/PMC7304739/>

<https://www.sciencedirect.com/science/article/pii/S0017931022003957>

VVUQ...

Some links/references (for those who are interested)

2021

https://indico.euro-fusion.org/category/279/attachments/1700/3352/ETASC-KOM-Intro_Naulin_Jenko.pdf

2024

https://finnfusion.fi/app/uploads/2024/06/mantsinen_c.pdf

Advanced Computing Hubs within EUROfusion E-TASC programme

Mervi Mantsinen

ICREA and Barcelona Supercomputing Center (BSC)

FinnFusion Annual Seminar, Helsinki, Finland, 27-28 May 2024

- (2016) https://geodynamics.org/resources/301/download/Oberkampf_Webinar_CIG-2016.pdf

Dr. William L. Oberkampf Sandia National Laboratories (retired)

Verification, Validation, and Predictive Capability: 2021 What's What?

- (2010) M. Greenwald *Verification and validation for magnetic fusion* Phys. Plasmas 17, 058101;
<https://doi.org/10.1063/1.3298884>

- (2008) P. W. Terry, M. Greenwald, J.-N. Leboeuf, G. R. McKee, D. R. Mikkelsen, W. M. Nevins, D. E. Newman, and D. P. Stotler, *Validation in fusion research: Towards guidelines and best practices* Physics of Plasmas 15, 062503
<https://doi.org/10.1063/1.2928909>

- (1998). AIAA. "Guide for the Verification and Validation of Computational Fluid Dynamics Simulations." American Institute of Aeronautics and Astronautics, AIAA-G-077-1998 <https://arc.aiaa.org/doi/book/10.2514/4.472855>

Preliminary considerations summary:

- Consorzio RFX site
- RFX high priority national infrastructure (NEFERTARI project)
- EUROFUSION welcomes:
 - alternative approaches – parallel research – intellectual diversity
- DIFFERENT configurations for Magnetic Confinement Fusion: Stellarator Tokamak RFP
- COMMON PHYSICS issues: challenging for theories models understanding
- Theory, Advanced Simulation, Verification & Validation and EUROFUSION: E-TASC
- RFX-RFP research:
 - Proficuous place for training and practicing Theory, Simulation, V & V ...UQ**

Theory and Advanced Simulation

The Reversed-Field Pinch *case*

Helical Self-Organization processes

tightly integrated to past and future experimental programme:

- RFX / RFX-mod /
- RFX-mod2 device

(1992 – 1999)

RFX

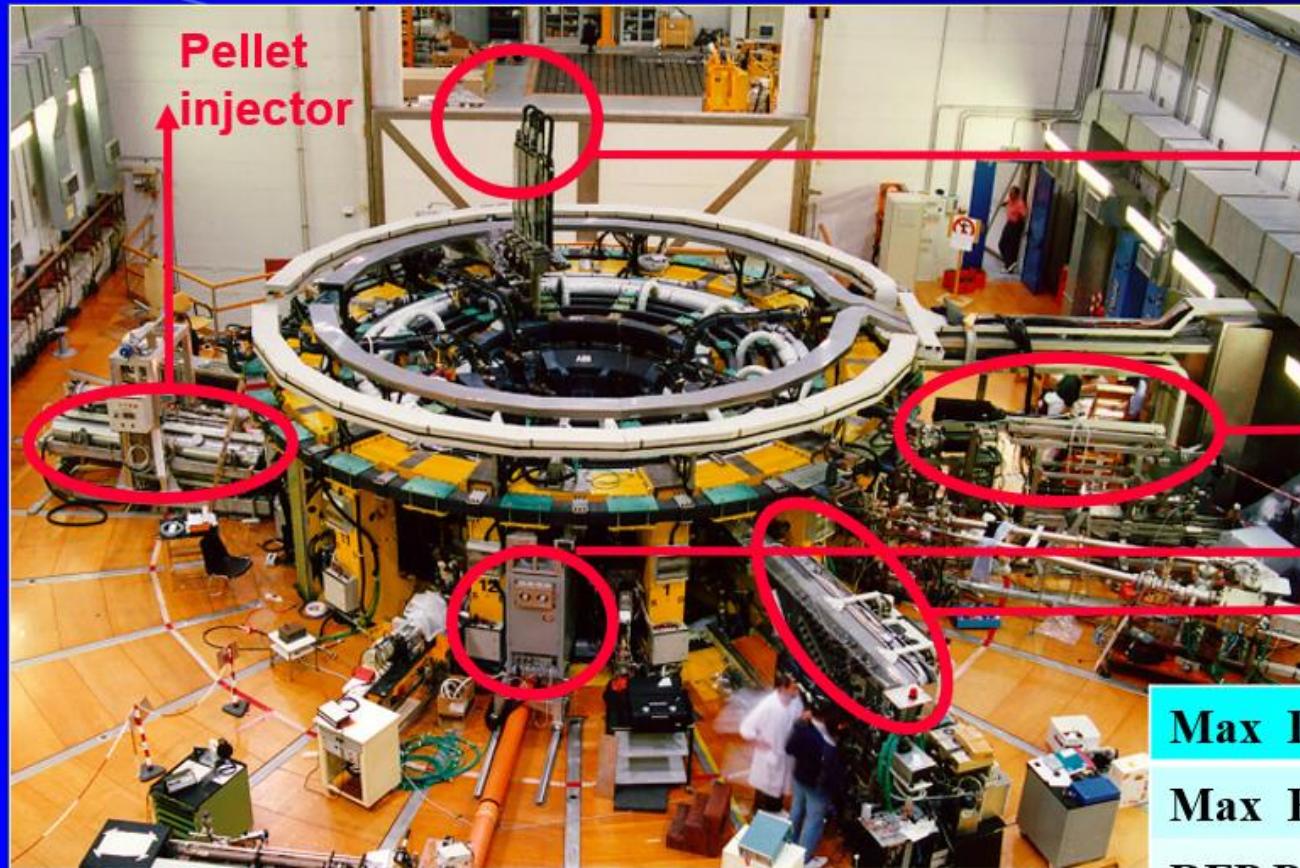
(2004 – 2015)

RFX-mod

(2026 ...)

RFX-mod2

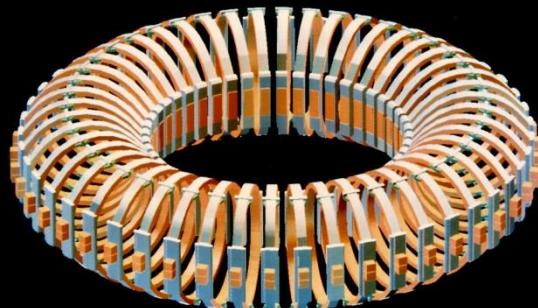
(MIAIVO project
PNRR NEFERTARI project)



Max Ip	2 MA
Max Bz	0.7 T
RFP Pulse duration	0.6 s
Tokamak Pulse	1 s

Pinch device - plasma self-squeezes due to plasma current I

RFX device coils



toroidal magnetic field



poloidal magnetic field

Schematic RFP

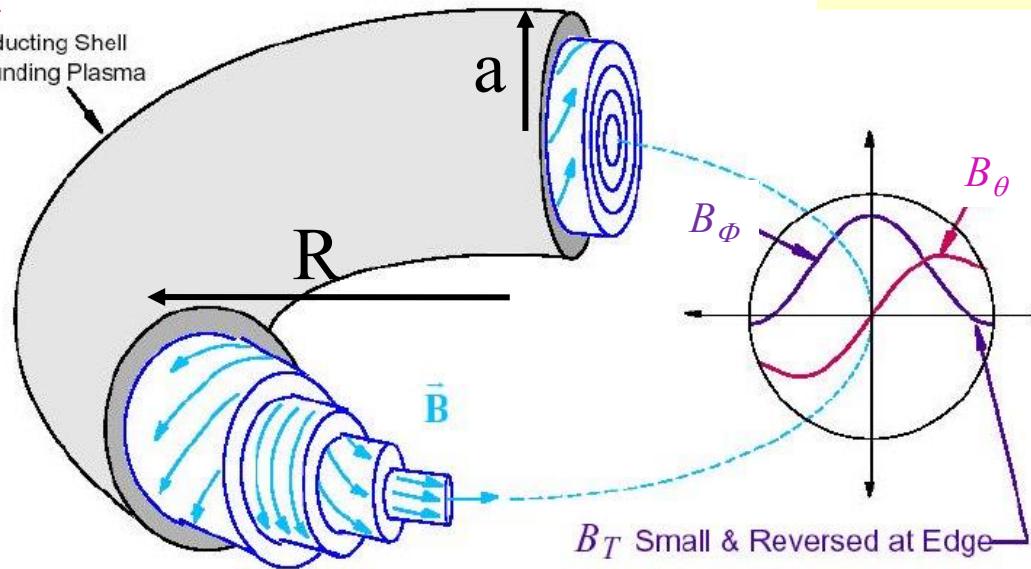
RFX

$R = 2.0\text{m}$

$a = 0.5\text{m}$

MST

Conducting Shell
Surrounding Plasma



induction of
plasma current

mean
magnetic field
radial profiles

Schematic B(r)

axisymmetric components

Tokamak and RFP

given $B_\phi(r=0)$ and plasma radius “a”

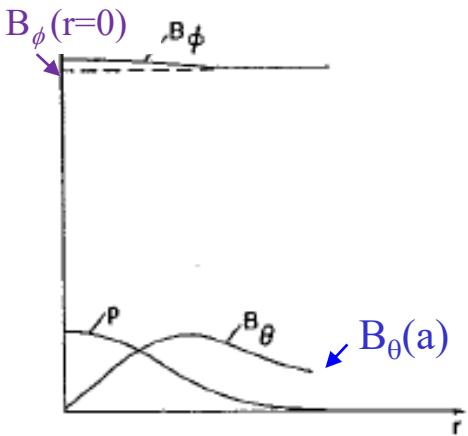


Figure 6.10. Typical radial profiles for an ohmically heated tokamak.

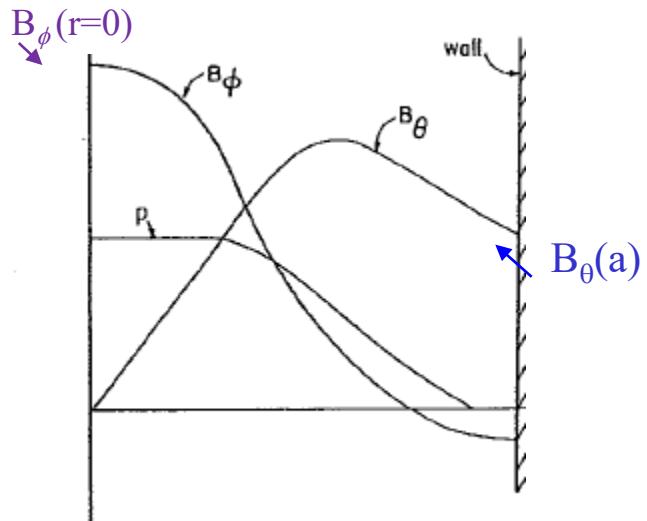
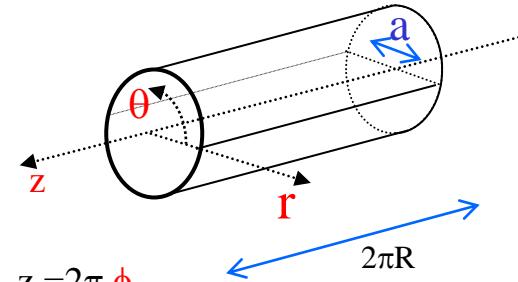


Figure 6.5. Schematic diagram of the B_ϕ , B_θ , and p profiles providing radial pressure balance in an RFP.

Periodic cylinder:
common approximation of the torus.

Usual coordinates:



Poloidal angle θ
and
 z toroidal like, or ϕ

Schematic B(r)

axisymmetric components

Tokamak and RFP

given $B_\phi(r=0)$ and plasma radius “a”

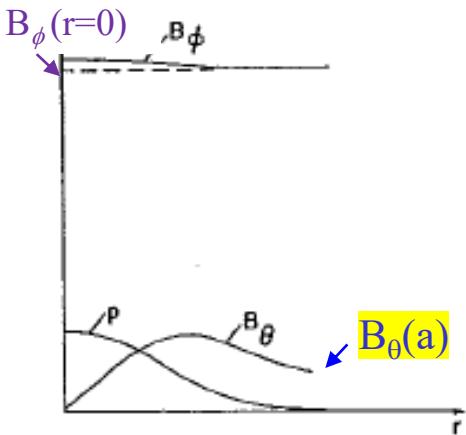


Figure 6.10. Typical radial profiles for an ohmically heated tokamak.

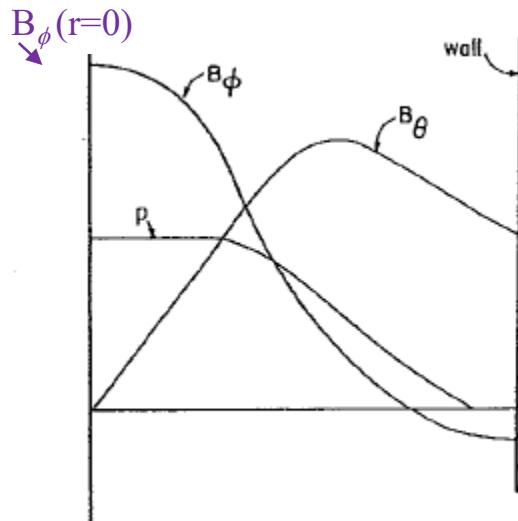
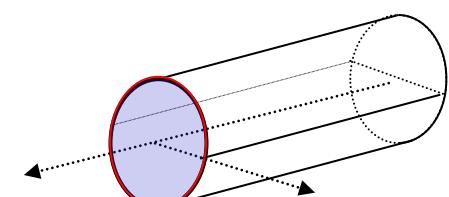


Figure 6.5. Schematic diagram of the B_ϕ , B_θ , and p profiles providing radial pressure balance in an RFP.

RFP much larger plasma current I

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{J}$$

$$\int_S d\mathbf{S} \cdot \nabla \times \mathbf{A} = \oint_C d\mathbf{l} \cdot \mathbf{A}$$



$$aB_\theta(a) \sim I_p$$

Reversal, F, and Pinch, Θ , parameters:

$$F \equiv \frac{\mathbf{B}_z(a)}{\langle \mathbf{B}_z \rangle} \quad \Theta \equiv \frac{\mathbf{B}_g(a)}{\langle \mathbf{B}_z \rangle} \sim \frac{I_p}{\Phi}$$

$$\text{Safety factor: } q(r) = \frac{d\Phi}{d\psi} \sim \frac{r B_z(r)}{R B_\theta(r)}$$

F has a similar relevance as
q(a) in Tokamak “vocabulary”

Let's enter a little bit more into the RFP world

Right from its origin ('50), the RFP placed puzzling issues.

The configuration was discovered in early pinches when pushing plasma current to high enough values

1. B_z self-reversal was **unexpected**,
... associated quiescent regime: **unexpected**
2. Call for an «*RFP dynamo*»

1. Quiescent regimes associated with B_Z field reversal

Historical observations ('50ties several toroidal pinches) ZETA machine (UK):
Pushing plasma current above “threshold” → toroidal B_Z self-reversal

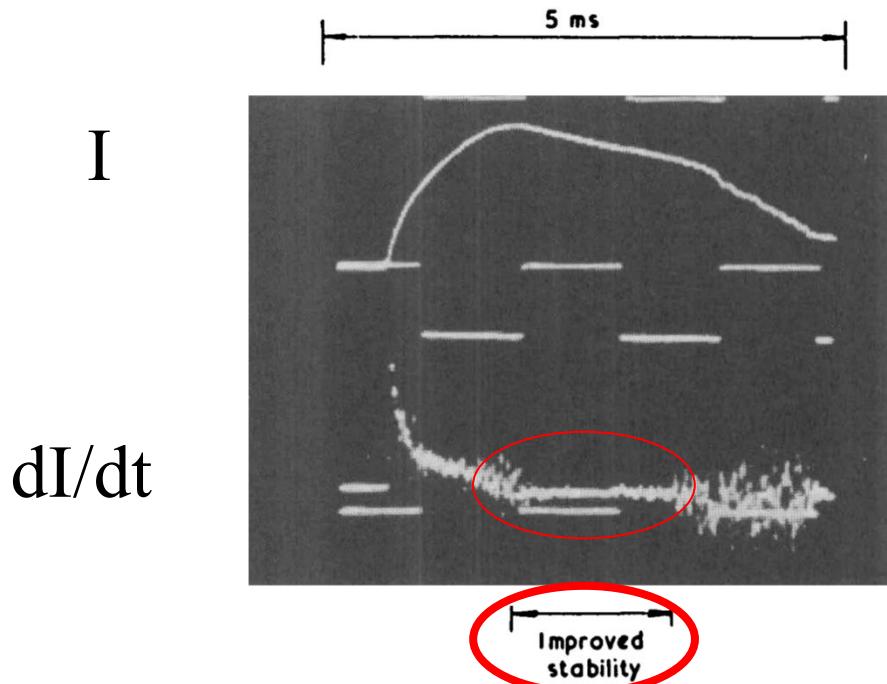


FIG.2. Oscilloscope record of ZETA discharge lasting 5 ms. Top trace is gas current I , reaching a maximum here of 420 kA, while lower trace is rate-of-change of current dI/dt and exhibits period of quiescence subsequently associated with magnetic-field reversal.

1. Quiescent regimes associated with B_Z field reversal

*A few lines about Taylor's relaxation theory for the RFP.
It was inspired by astrophysical dynamo theories*

1. Quiescent regimes associated with B_Z field reversal

*A few lines about Taylor's relaxation theory for the RFP.
It was inspired by astrophysical dynamo theories*

Taylor's relaxation theory for the RFP [*]

boosted the RFP research due to its ability to provide a first understanding...

Taylor's conjecture can be considered a “weak formulation” of Woltjer theorem (1958) proposed to describe astrophysical magnetic fields of celestial bodies:
astrophysical dynamo... in particular ***turbulent dynamo***

It considers a variational principle:

- search for the minimum of magnetic energy,
- compatible with a given conserved topological complexity (magnetic helicity).

(The topological complexity is an ideal invariant, due to the frozen-in law of magnetic field in perfectly conducting fluids... Alfvén theorem).

[*]

J. B. Taylor PRL 1974

J. B. Taylor Rev. Mod Phys. 1986

1. Quiescent regimes associated with B_Z field reversal

By solving the variational problem casted by Taylor's relaxation theory one finds "relaxed states" with **field reversal** for $\Theta \geq 1.2$

The theory gained a great success, providing a first way to understand the experimental observations

... despite quantitative differences, significant in the external region around reversal...



Bessel analytical solutions

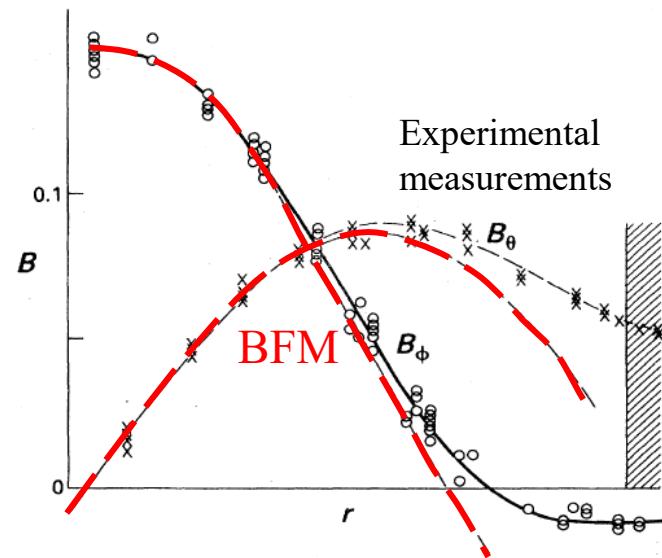


FIG. 2. Experimental and theoretical magnetic field profiles. HBTX-1A (from Bodin, 1984).

Bessel Function Model (BFM)

Rev. Mod. Phys., Vol. 58, No. 3, July 1986

[*]

J. B. Taylor PRL 1974

J. B. Taylor Rev. Mod Phys. 1986

For those interested in the Taylor Relaxation Theory: come to my office.
I can suggest some material.

2. “RFP dynamo effect ” needed ... let's recall **the equations for conducting fluid:**

Ohm's law

$$\mathbf{E} + \mathbf{V} \wedge \mathbf{B} = \eta \mathbf{J}$$

(simple form for conducting fluid)

Induction equation

$$\frac{\partial \mathbf{B}}{\partial t} = -\nabla \wedge \mathbf{E}$$

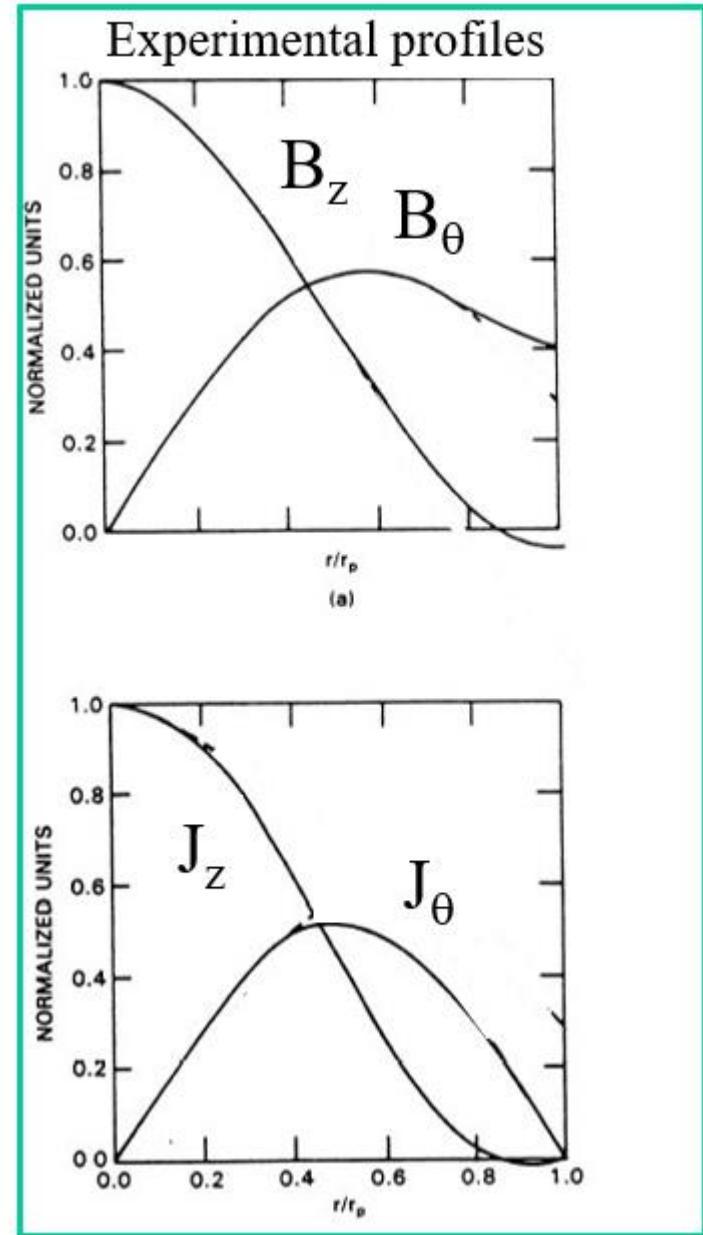
2. “RFP dynamo effect ” needed ... let's recall [the typical B and J profiles](#):

Ohm's law

$$\mathbf{E} + \mathbf{V} \wedge \mathbf{B} = \eta \mathbf{J}$$

Induction equation

$$\frac{\partial \mathbf{B}}{\partial t} = -\nabla \wedge \mathbf{E}$$



2. “RFP dynamo effect ” needed ... let's recall the typical B and J profiles:

Ohm's law

$$\mathbf{E} + \mathbf{V} \wedge \mathbf{B} = \eta \mathbf{J}$$

Induction equation

$$\frac{\partial \mathbf{B}}{\partial t} = -\nabla \wedge \mathbf{E}$$

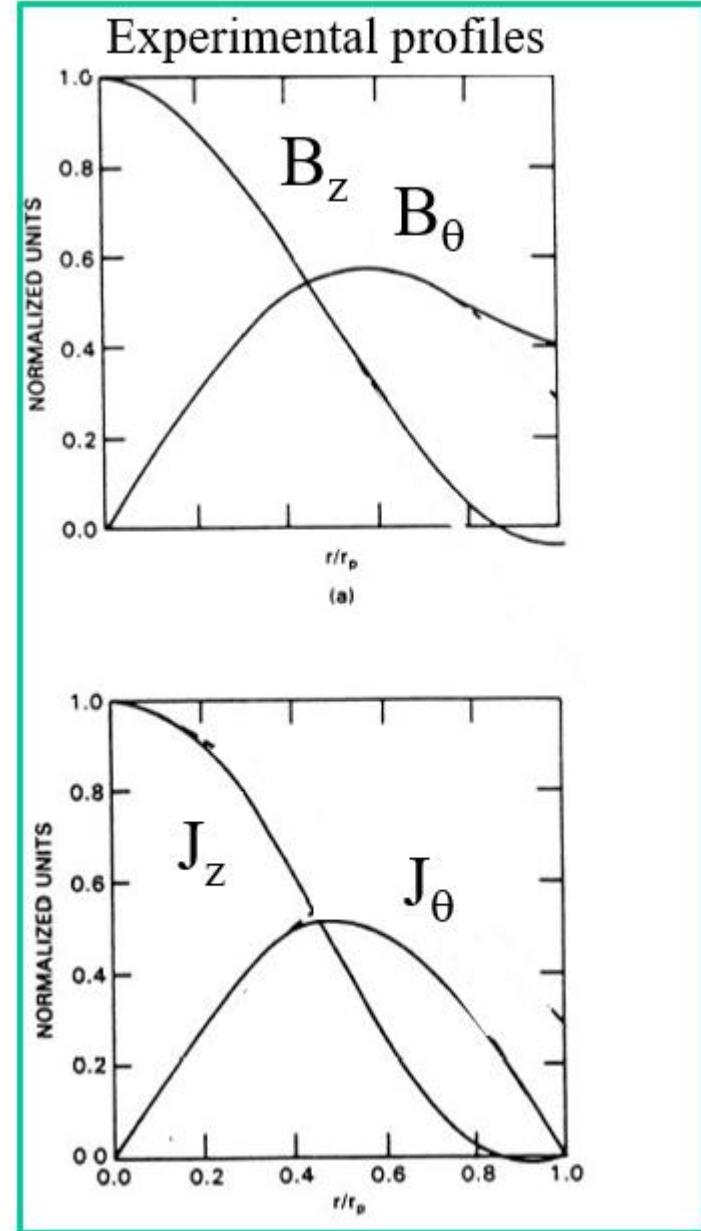
stationarity $\frac{\partial}{\partial t} = 0 \rightarrow$

Consider stationary fields

$$E_\theta(r) \equiv 0$$

$$E_Z(r) \equiv E_o$$

(Applied Voltage)



2. “RFP dynamo effect” needed

!! Inconsistency

Project along poloidal coordinate

→ Ohm's law

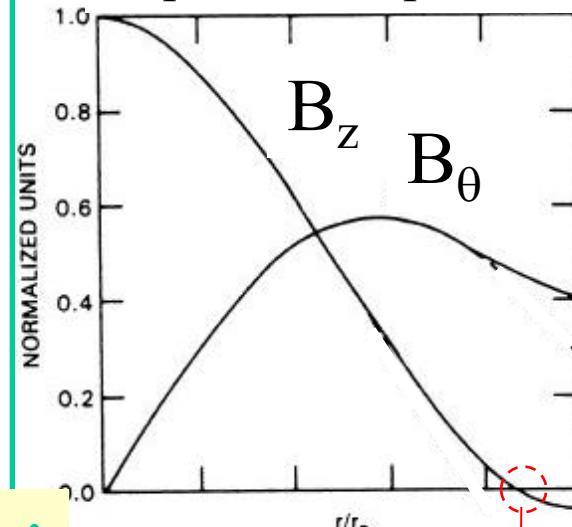
$$\mathbf{E} + \mathbf{V} \wedge \mathbf{B} = \eta \mathbf{J}$$

at reversal $B_z=0$

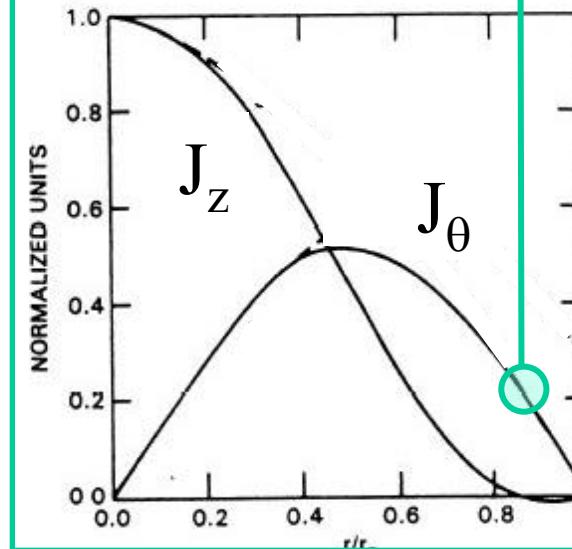
$$E_\theta(r) = \eta J_\theta + Vr B_z$$

$$J_\vartheta(r) = 0 !$$

Experimental profiles



$$J_\vartheta(r) \neq 0$$



$$\frac{\partial \mathbf{B}}{\partial t} = -\nabla \wedge \mathbf{E}$$

stationarity $\frac{\partial}{\partial t} = 0 \rightarrow$

$$E_\theta(r) \equiv 0$$

$$E_z(r) \equiv E_o$$

(Applied Voltage)

2. “RFP dynamo effect” needed

an additional “**dynamo**” electric field is needed with respect to the one provided by axisymmetric B and v fields in order to balance Ohm’s law if a finite J_θ is present at reversal radius:

within resistive MHD such a contribution comes through a
coherent modulations V^1, B^1 on top of the axisymmetric components V, B

$$E_\theta(r) = \eta J_\theta + Vr B_z \langle V^1 \wedge B^1 \rangle_\theta$$

E_{dynamo}

Thus, inspired by astrophysical studies, and supported by Taylor Relaxation Theory, a small scale turbulence has been deemed as necessary to get RFP dynamo effect ...

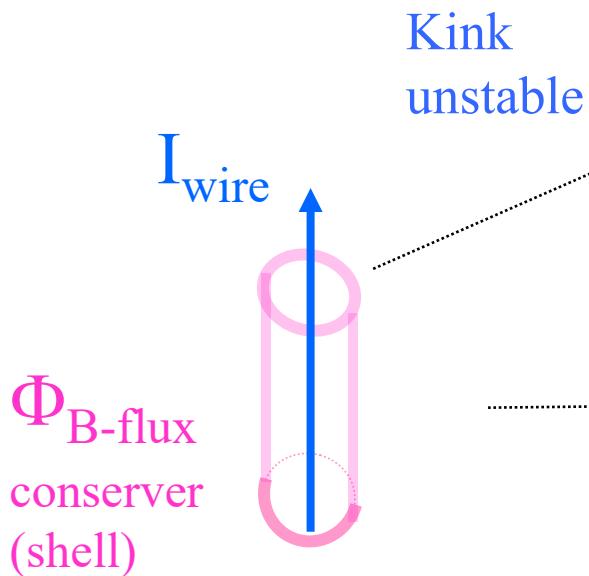
*We shall see that a laminar –steady- macroscopic helical dynamo can also be a solution of **3D nonlinear MHD** simulations for cylindrical RFP.*

Toy model

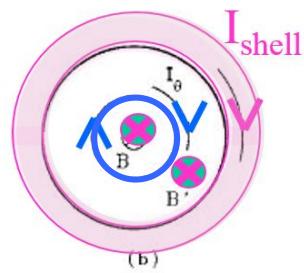
The toy model:
intuitive and simplified understanding of self-reversal
(schematic and intuitive RFP)
... and of the global helical self-organization

Toy model (1): a kink deformation of the current “path” pumps toroidal B-flux

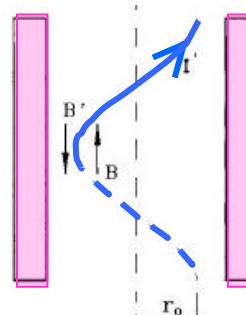
Think of a **current carrying wire** in a **flux conserver**:



Kink
unstable

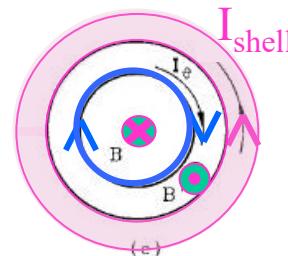


$I_{\text{wire}} & I_{\text{shell}}$ attract each other



solenoidal effect
by the wire itself:
- core B increase

by flux conservation:
- edge B decreases ..



Kink saturates when/if
reversal of edge field
is achieved

Elaborated in:

Benisti Escande EFTC 1998

Escande et al. PPCF 2000

See also Cappello et al Varenna 2008

$r_0 \rightarrow 1$ (disruption) for too small $\frac{I_{\text{wire}}}{\Phi}$
(Tokamak case)

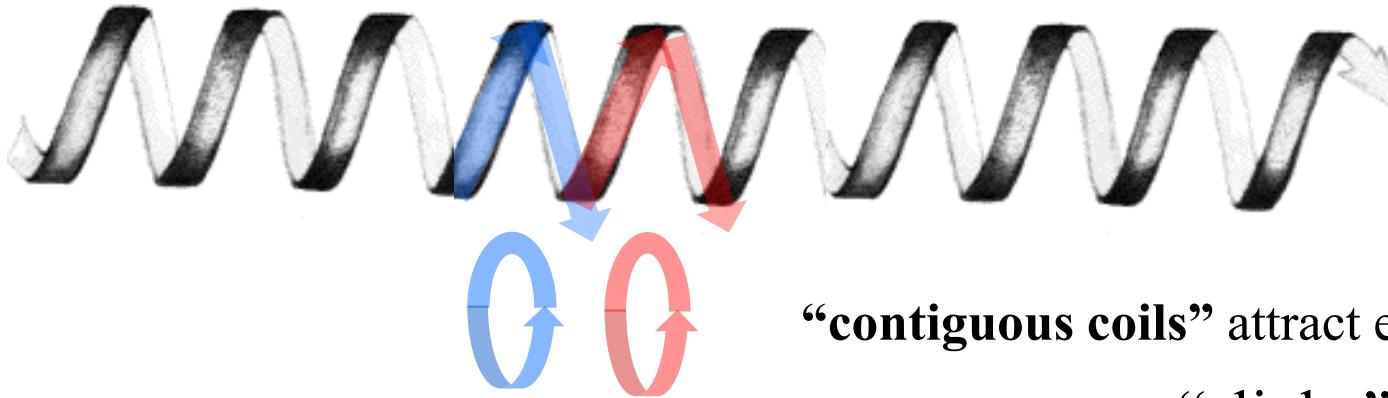
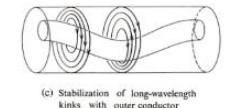
Early elements:

Verhage-Furzer-Robinson NF 1978

Kadomtsev 1992 (Sawer PoF 1959)

Toy model (2): the kink deformation is subject to a secondary instability

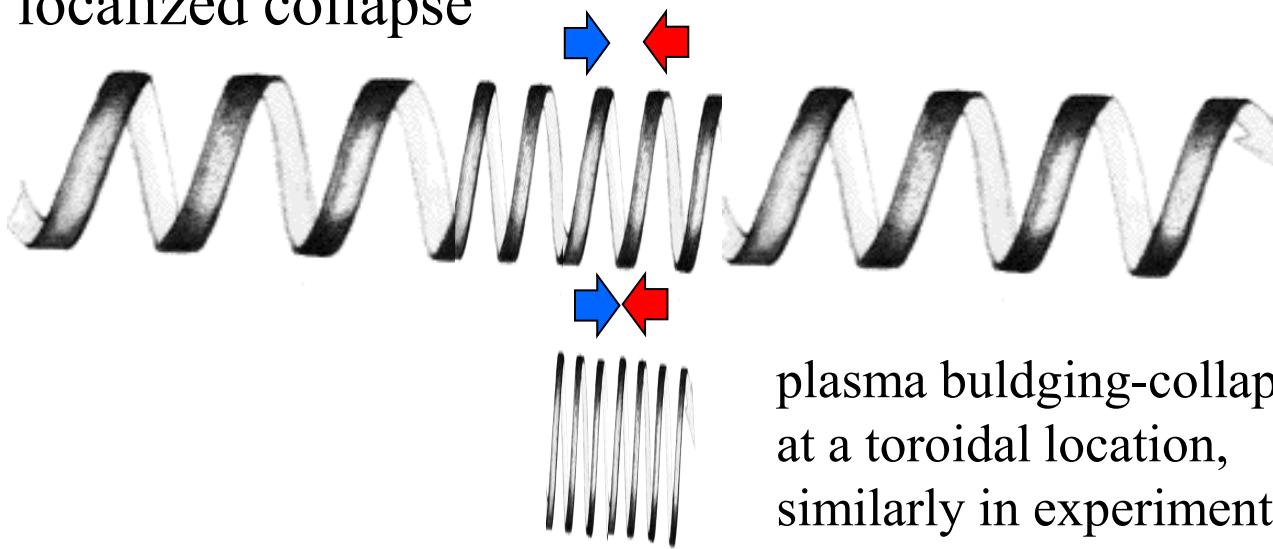
After kinking ...



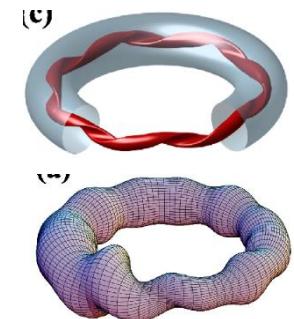
“contiguous coils” attract each other ...

... “slinky” instability

... localized collapse



plasma bulging-collapse
at a toroidal location,
similarly in experiments
and nonlinear modeling...



Summary of first steps in RFP theory, modeling and understanding :

- ZETA experiment puzzling: quiescent regime & reversal of magnetic field ('60)
- Taylor relaxation theory ('70):
 - analytical «relaxed» solutions with B_z reversal
 - need for additional dynamo Electric field (small scale turbulence deemed necessary)
- Toy model schematic intuitive description of reversal effect (flux pumping by global kink)

Modern era - Helical self-organization processes

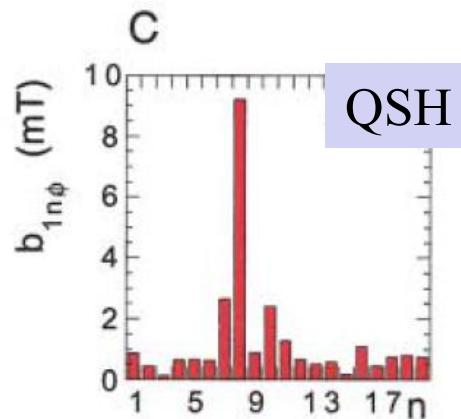
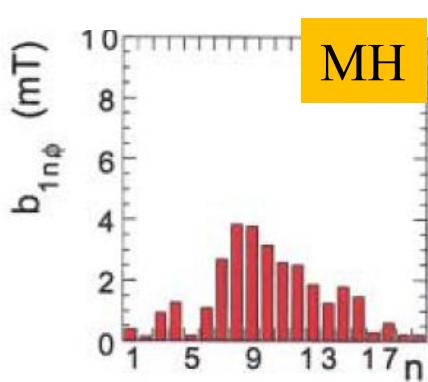
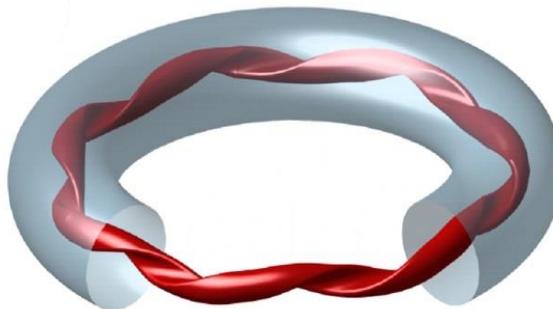
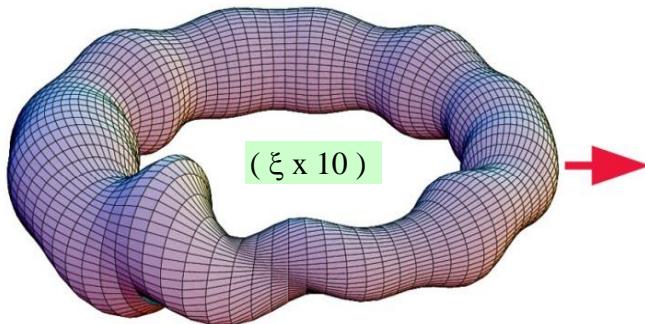
- Overview of RFX observations
- Description from **nonlinear MHD model:**
3D Numerical Simulation

RFP self-organization in brief

RFX

RFP \leftrightarrow saturated KINKED plasma

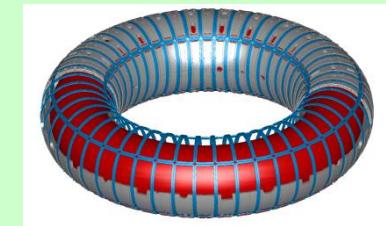
for I_p above ~ 1 MA



MHD spectrum: resistive kink-tearing modes

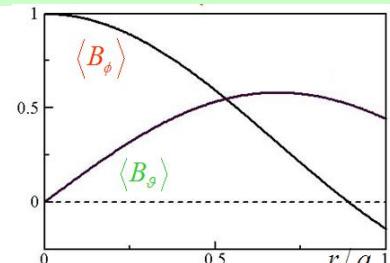
Advanced operation required in RFX-mod

CLEAN MODE CONTROL
and/or
NON-CONVENTIONAL SCENARIOS (PPCD-OPCD)



192 independent coils

Feedback coils system
Typical operation:
 $I_p \sim 1.7$ MA
 T_e up to 1.2 keV

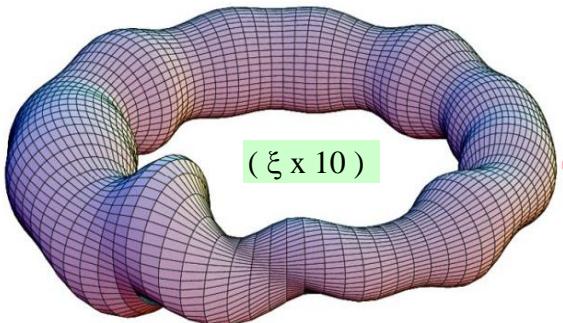


RFP self-organization in brief

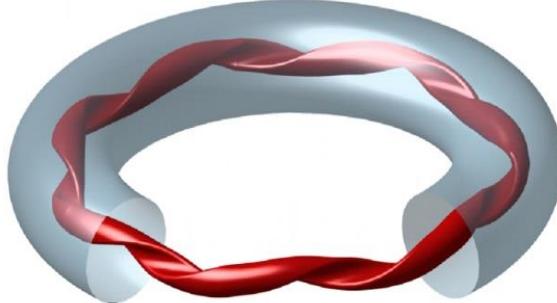
RFX

RFP \leftrightarrow saturated KINKED plasma

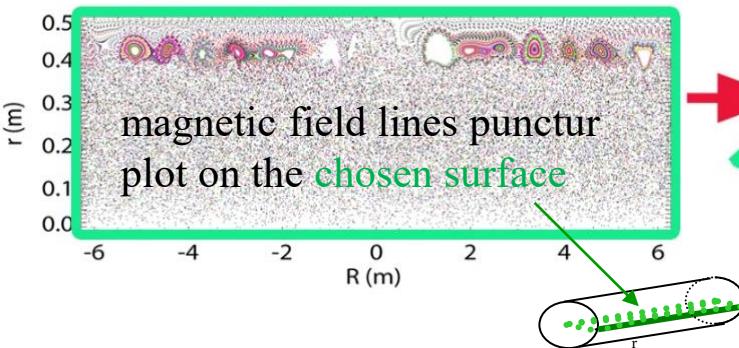
for I_p above ~ 1 MA



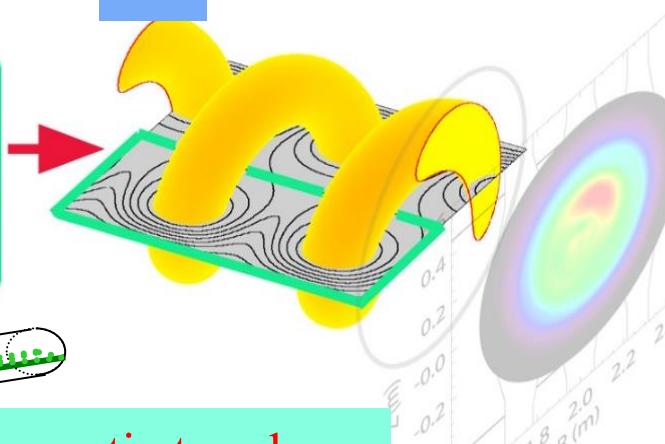
MH



SH



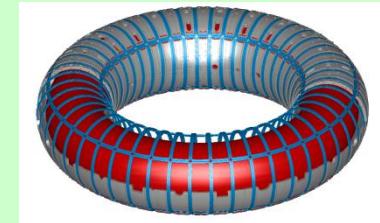
MHD spectrum impact on magnetic topology
Believed to rule transport properties in RFP



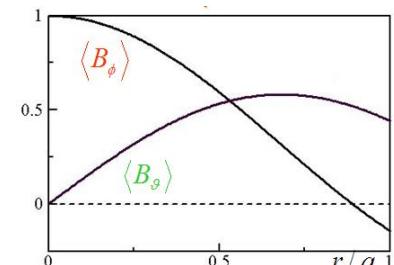
Advanced operation required in RFX-mod

CLEAN MODE CONTROL
and/or
NON-CONVENTIONAL SCENARIOS (PPCD-OPCD)

RFX-mod



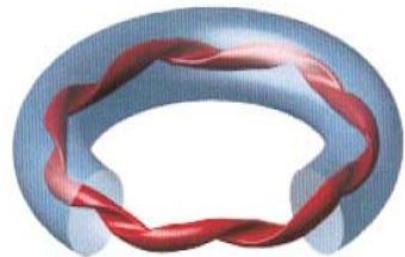
Feedback coils system
Typical operation:
 $I_p \sim 1.7$ MA
 T_e up to 1.2 keV



RFP helical self-organization – Experimental overview

- **First observations: one single MHD mode emerging**
- **Statistical robustness of the helical self-organization**
- **Electron Temperature (and density) Internal Transport barrier – eITB**
 - Relation with safety factor profile
 - Temporal behavior
- Impurity screening effect
- Isotopic effect: better performances when running Deuterium discharges

RFP helical self-organization: several experiments RFX – TPE – MST –T2R



RFX

FIG. 3 (color). Schematic view of a $n = 7$ helical structure inside the RFX vessel.

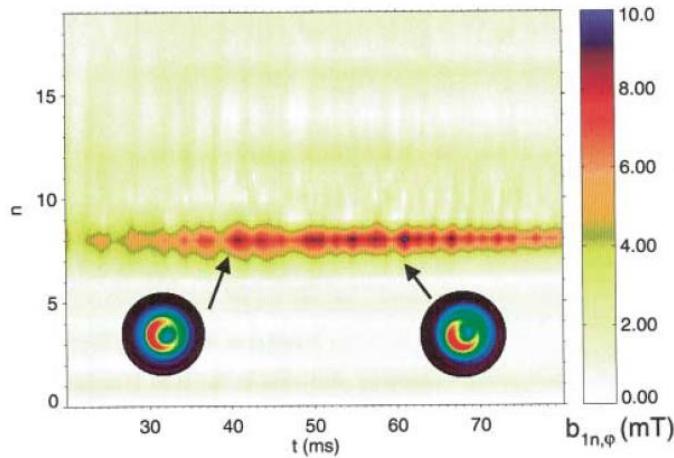
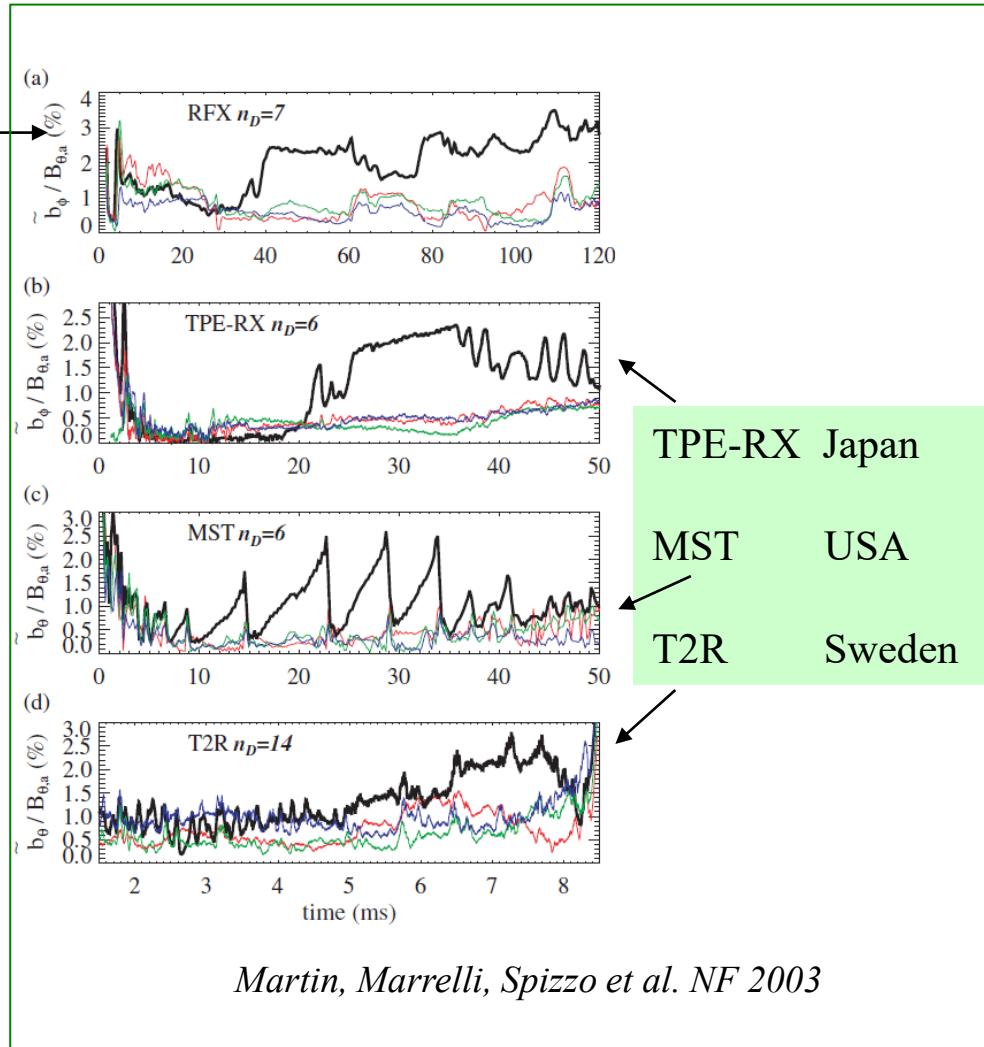


FIG. 5 (color). $m = 1$ modes n -spectrum vs time and SXR emissivity patterns at selected times ($t = 40$ ms and $t = 60$ ms) in a plasma (No. 11336) where the QSH state is permanent. The dominant mode in this case is $n = 8$.

Escande, Martin, Ortolani et al. PRL 2000

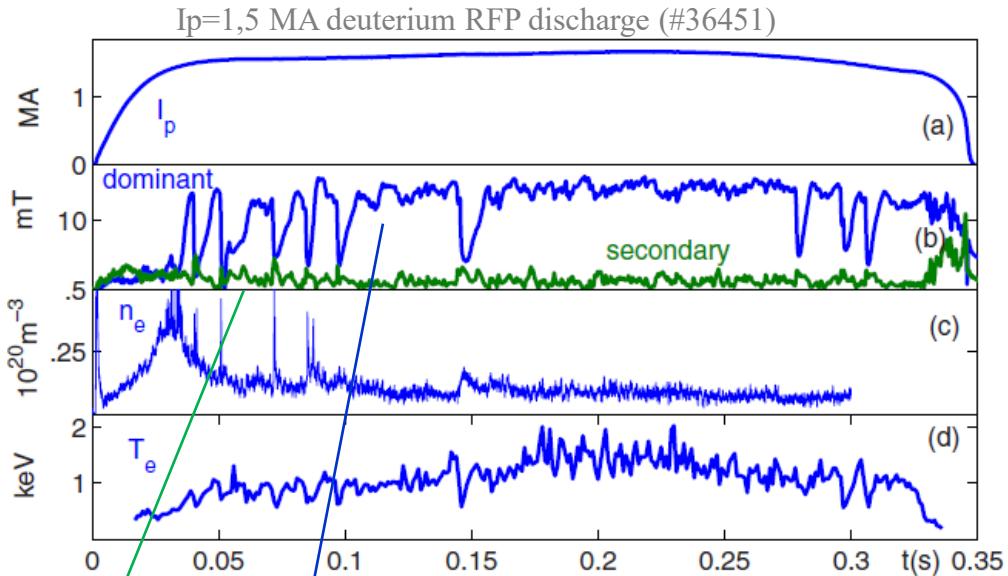


More recently also:
RELAX (Japan), KTX (Hefei- China)

RFP helical self-organization: a robust process

RFX -mod

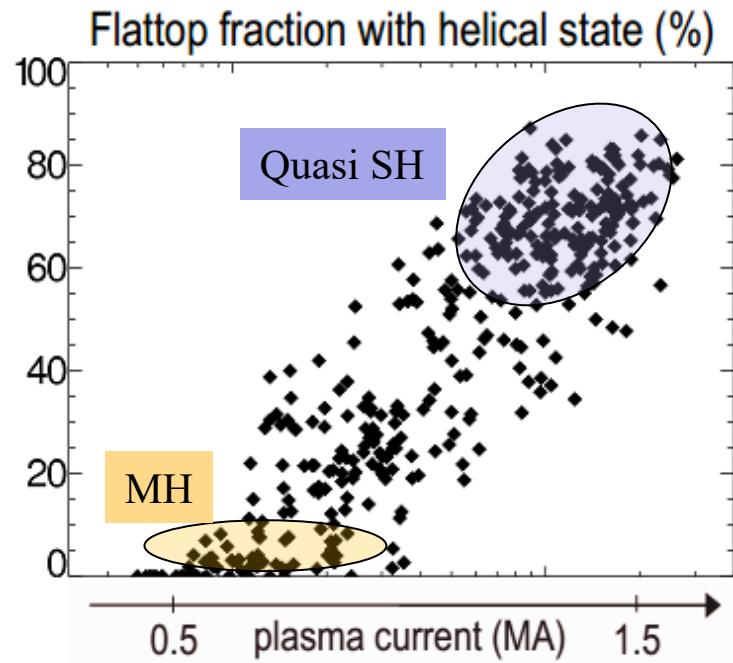
HELICAL persistency increases with current - up to > 85% of flat top



Dominant mode (internal)

ave secondary modes

Puiatti, Dal Bello, Marrelli et al. NF 2015



(hydrogen RFP discharges)

Piovesan, Zuin et al NuclFus 2009

Similar behavior in MST experiment:

- Chapman et al IAEA EX/P6-01 (2012)
- Sarff et al Nucl Fus (2013)

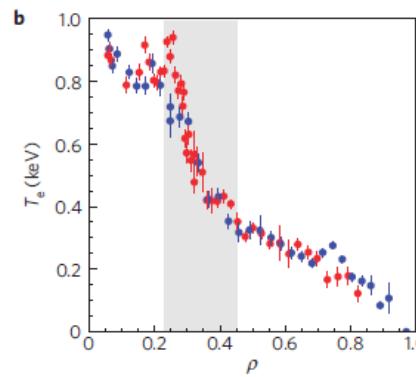
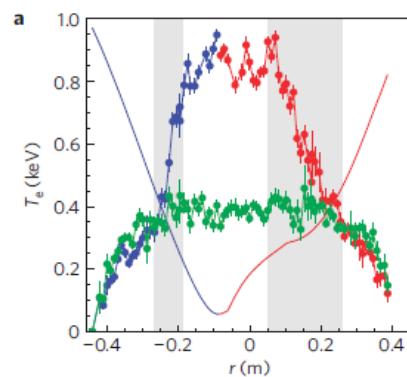
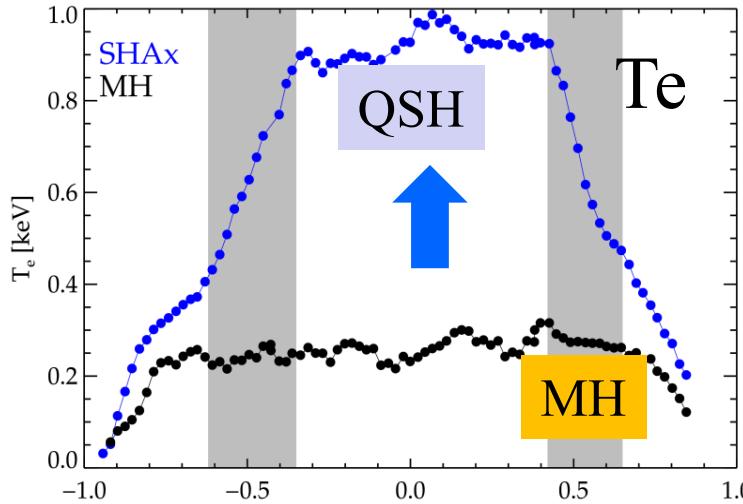
RFP helical self-organization: barriers formation

RFX -mod

Formation of e-Internal Transport Barriers

24598, 117ms
 $I_p=1.3\text{MA}$
 $n/n_G=0.20$

22201, 35ms
 $I_p=0.7\text{MA}$
 $n/n_G=0.22$



Barrier formation
believed to be
provided by
magnetic chaos
healing effect

Lorenzini, Martines, Piovesan et al NatPhys 2009

Piovesan, Zuin, Alfier et al NF 2009

Cappello et al Theory of Fusion Plasmas, 2008

Joint Varenna-Lausanne International Workshop



RFP helical self-organization – 3D nonlinear MHD modeling

- SpeCyl code
- Verification benchmark vs PIXIE3D (LANL code)
- Relevant dimensionless parameters in governing dynamical regime transition
Resistivity η , Viscosity ν , and the Hartman number $(\eta\nu)^{-1/2}$
- Role of non-ideal Boundary Condition:
Magnetic Perturbation (Resonant MP / Non-Resonant MP) and sawtooth pacing
- ...
- Sensitivity Analysis vs viscosity profiles
- Magnetic chaos healing, Lagrangian Coherent Structures detection

3D nonlinear MHD modeling

$B(r,\theta,z,t)$, $v(r,\theta,z,t)$

The “minimum” visco resistive 3D MHD approximation:

Induction equation: Faraday + Ohm's law

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \wedge (\mathbf{v} \wedge \mathbf{B}) - \nabla \wedge (\eta \mathbf{J})$$

Momentum equation

more or less *Navier Stokes* (*-pressure + Lorentz*)

$$\frac{d\mathbf{v}}{dt} = \mathbf{J} \wedge \mathbf{B} + \nu \nabla^2 \mathbf{v}$$

Implemented in the
SpeCyl numerical code

3D nonlinear MHD

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \wedge (\mathbf{v} \wedge \mathbf{B}) - \nabla \wedge (\eta \mathbf{J})$$

$$\frac{d\mathbf{v}}{dt} = \mathbf{J} \wedge \mathbf{B} + \nu \nabla^2 \mathbf{v}$$

$$\rho \equiv 1, \quad \nabla p \equiv 0$$

$$\nabla \cdot \mathbf{B} \equiv 0 \quad \nabla \wedge \mathbf{B} \equiv \mathbf{J}$$

SpeCyl code - simple visco-resistive approx.

Cappello & Biskamp Nucl. Fus. 1996

$$\eta = \tau_A / \tau_R$$

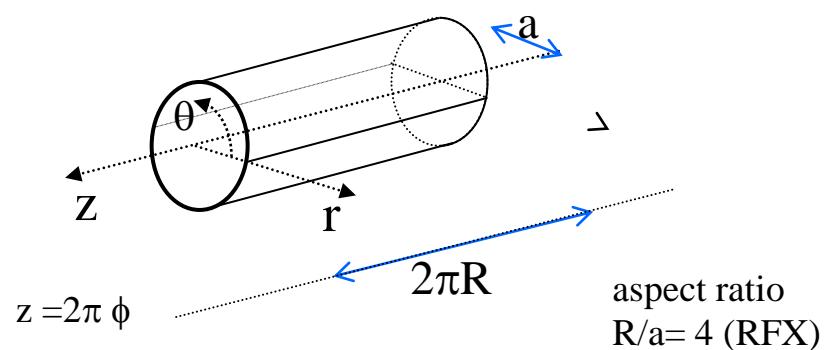
two dimensionless parameters
with assigned radial profiles

$$\nu = \tau_A / \tau_v$$

$$\begin{cases} \text{Lundquist: } & \mathbf{S} = 1 / \eta \\ \text{Viscous Lundquist } & \mathbf{M} = 1 / \nu \end{cases}$$

r	Finite difference
θ, ϕ	Spectral formulation
t	Predictor-corrector + semi-implicit

Geometry: periodic cylinder



3D nonlinear MHD

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \wedge (\mathbf{v} \wedge \mathbf{B}) - \nabla \wedge (\eta \mathbf{J})$$

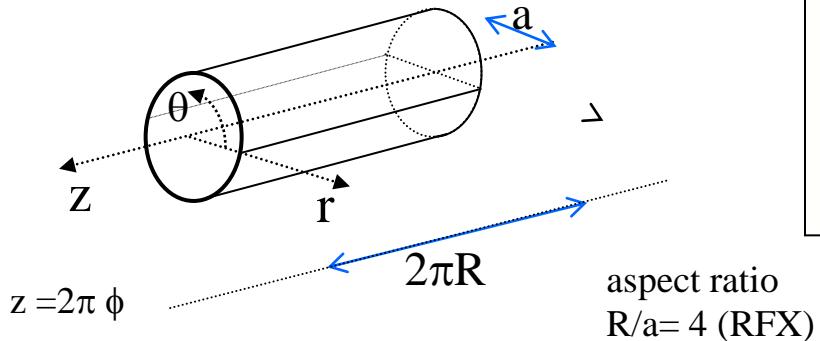
$$\frac{d\mathbf{v}}{dt} = \mathbf{J} \wedge \mathbf{B} + \nu \nabla^2 \mathbf{v}$$

$$\rho \equiv 1, \quad \nabla p \equiv 0$$

$$\nabla \cdot \mathbf{B} \equiv 0 \quad \nabla \wedge \mathbf{B} \equiv \mathbf{J}$$

r	Finite difference
θ, ϕ	Spectral formulation
t	Predictor-corrector + semi-implicit

Geometry: periodic cylinder



SpeCyl code - simple visco-resistive approx.

Cappello & Biskamp Nucl. Fus. 1996

$$\eta = \tau_A / \tau_R$$

two dimensionless parameters
with assigned radial profiles

$$\nu = \tau_A / \tau_v$$

Lundquist: $S = 1 / \eta$
Viscous Lundquist $M = 1 / \nu$

“typical” boundary conditions:

- $B'_z = 0$ (**constant magnetic flux Φ**)
- Constant E_z (or constant I_p)
 - m,n {
 - Ideal boundary
 - MP on $B_{r m,n}$ ($\sim 1\%, 2\%, 4\% \dots$)
 - Thin shell + vacuum layer +ideal wall
- velocity field: no slip/self consistent.

initial conditions define Φ, I_z

Nonlinear **verification** benchmark SpeCyl – PIXIE3D

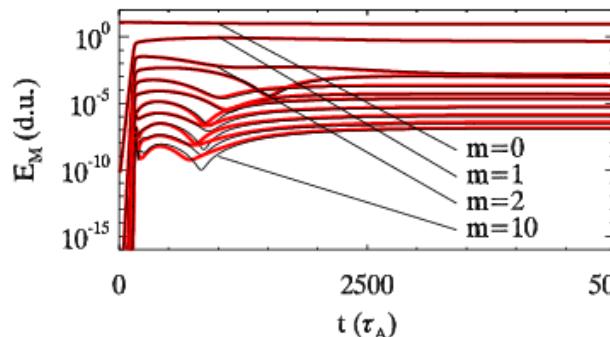
PIXIE3D is a massively parallel code in arbitrary curvilinear geometry
 conservative, solenoidal finite-volume discretization in space,
 fully implicit temporal advance.

PIXIE3D: Chacón CPC 2004, PoP 2008, Los Alamos NL -NM USA

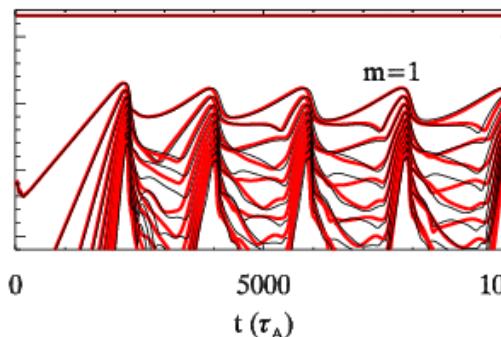
*Bonfiglio, Chacón, Cappello POP 2010
 Spinicci, Bonfiglio, Chacón, et al, AIP Advances 2023*

2D

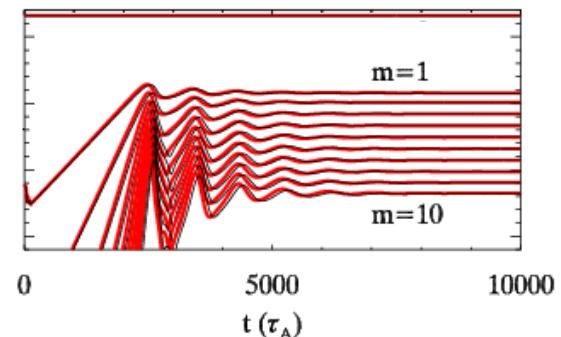
2D: single helicity (SH) RFP



2D: Tokamak sawtooth

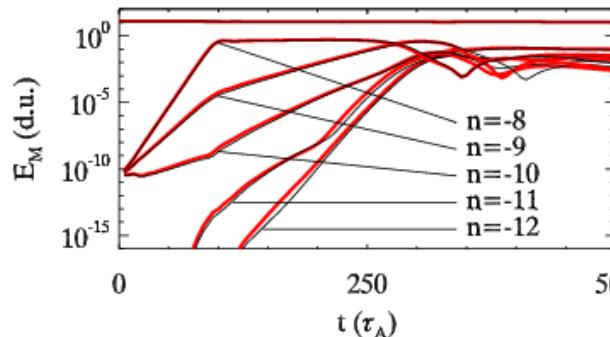


2D: Tokamak snake

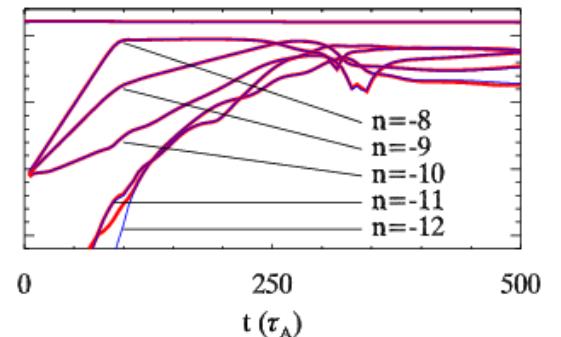
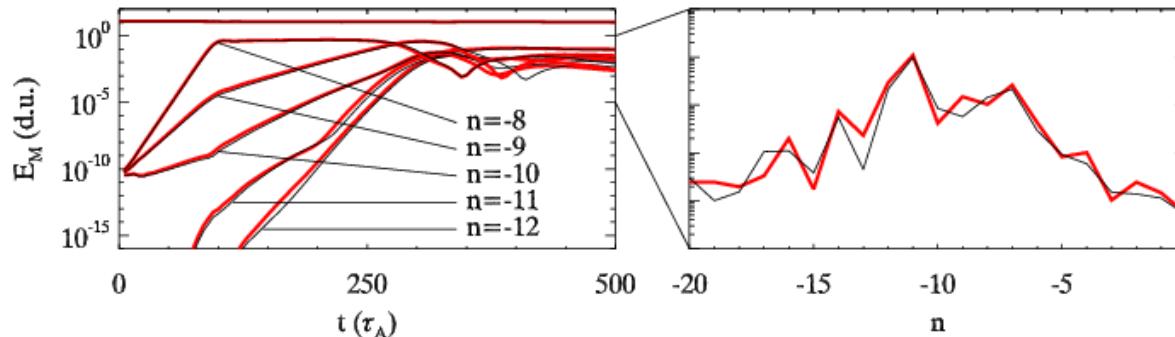


3D

3D: multiple helicity (MH) RFP



PIXIE3D: $\Delta t = 1.0 \tau_A$



Magnetic energy evolution from SpeCyl and PIXIE3D (black and red curves respectively).

Top panels 2D) RFP and Tokamak.

Bottom 3D) left) RFP case, right) PIXIE3D with different time steps (red $\Delta t = 5 \times 10^{-3}$ blue $\Delta t = 1 \tau_A$)

Model equations transformation

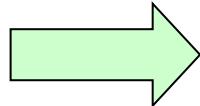
... re-scaling :

$$t \rightarrow \bar{t} = \sqrt{\frac{\eta}{\nu}} t$$

$$v \rightarrow \bar{v} = \sqrt{\frac{\nu}{\eta}} v$$

(S, M)

(η, v)



(H, P)

Magnetic Prandtl $P = \nu/\eta = S/M$
Hartmann number $H = (\nu\eta)^{-1/2}$

Hartmann: $H = (\nu\eta)^{-1/2}$

highlighted in

D. Montgomery et al. PPCF 92-93 (applied to linearized equations)

magnetic Prandtl: $P = \nu / \eta$

Whenever inertia is negligible and/or magnetic Prandtl is large:
the H number alone governs the solutions of the model equations

$$\frac{\partial \bar{B}}{\partial \bar{t}} = \nabla \wedge (\bar{v} \wedge \bar{B}) - \nabla \wedge (\bar{H}^{-1} \bar{J})$$

$$\frac{1}{P} \frac{d\bar{v}}{d\bar{t}} = \bar{J} \wedge \bar{B} + \nabla^2 (\bar{H}^{-1} \bar{v})$$

$$\rho \equiv 1, p \equiv 0$$

3D nonlinear MHD

Some examples of different regimes decided by H

Spectrum of MHD modes: $m=1$ resistive kink/tearing modes

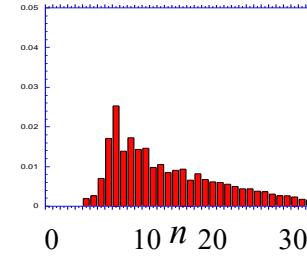
$m=1$ modes

$\delta B_{m=1, n}$

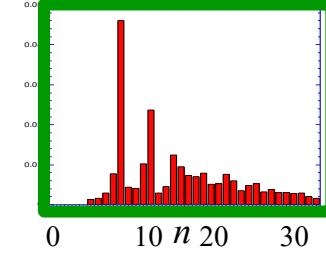
$m=1$ modes
nonlinearly drive
 $m=0$ modes

$m = 0$ modes:
signature of the dynamical regime

MH

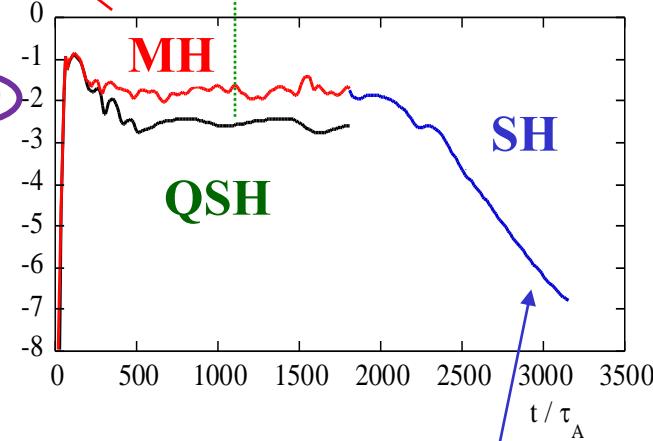


QSH



$m=1, n=1, 2, \dots$

Log $W_{m=0}$



$m=0, \sum_n$

Low H : SH Single Helicity regime

$m=1$ ONE single $m=1$ mode survives (and its harmonics)
 $m=0$ modes decrease to vanishing values

3D nonlinear MHD

The transition to helical regimes

- is a continuous one ruled by: Hartmann number, H , $(\eta v)^{-1/2}$

$m = 0$ modes:
signature of the dynamical regime

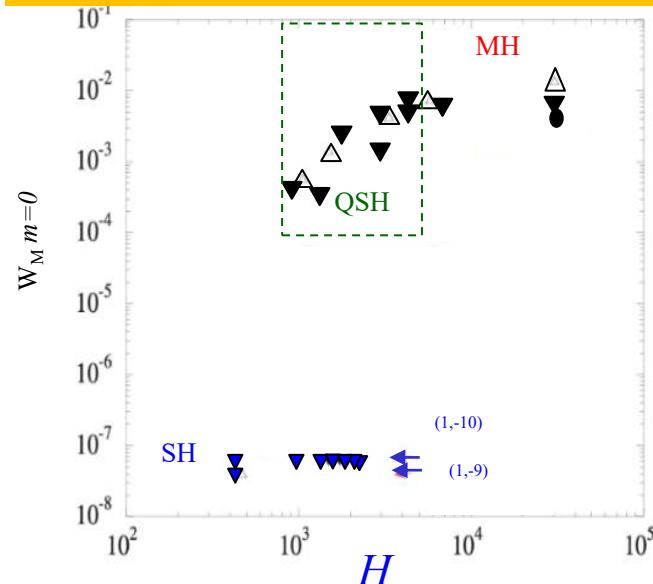
$\Delta S = 3.3 \times 10^3$ (P: 2/3-10)
 $\nabla S = 3.0 \times 10^4$ (P: 1-5000)
 $\bullet S = 10^5$ (P = 10)

SH

$W_{m=0}$ exponentially decaying: \longrightarrow
conventional finite value assigned in the plot

Pinch Parameter $\Theta = 1,6$

A transition diagram can be drawn in terms of:
- **$W_{m=0}$ mode** -time averaged- energy (order parameter)
vs
- **Hartmann number**



Solutions with different values of the couple (S, P) lie on a single curve when plotted against H

3D nonlinear MHD

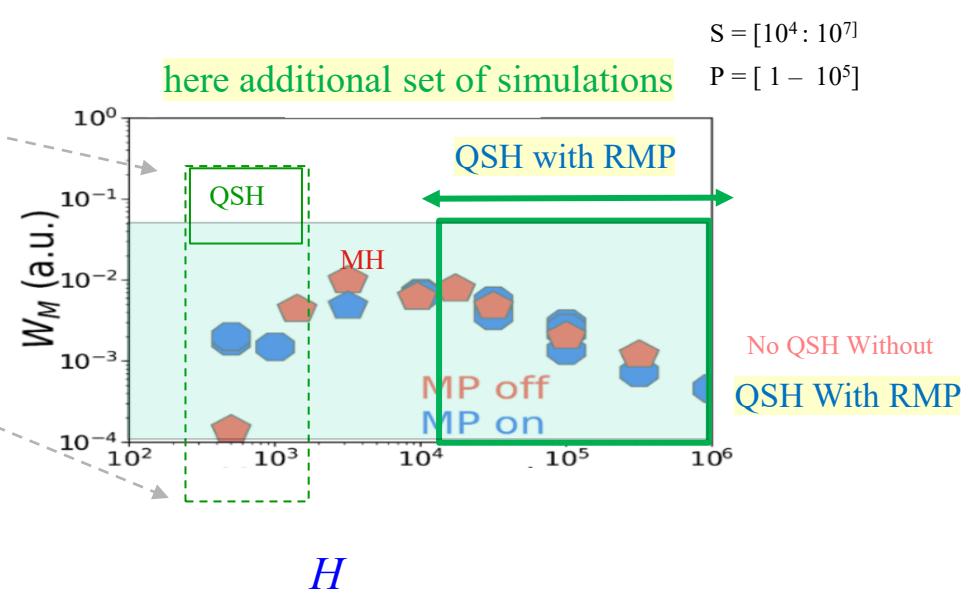
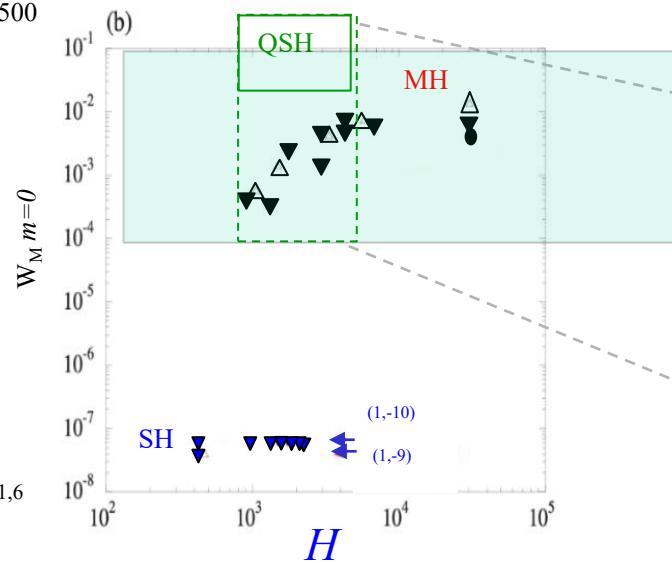
The transition to helical regimes

- is a continuous one ruled by: Hartmann number, H , $(\eta v)^{-1/2}$
- is significantly favored by **seed** edge **Magnetic Perturbation**

$\Delta S = 3.3 \times 10^3$ (P: 2/3-10)

$\blacktriangledown S = 3.0 \times 10^4$ (P: 1-500)

$\bullet S = 10^5$ (P = 10)

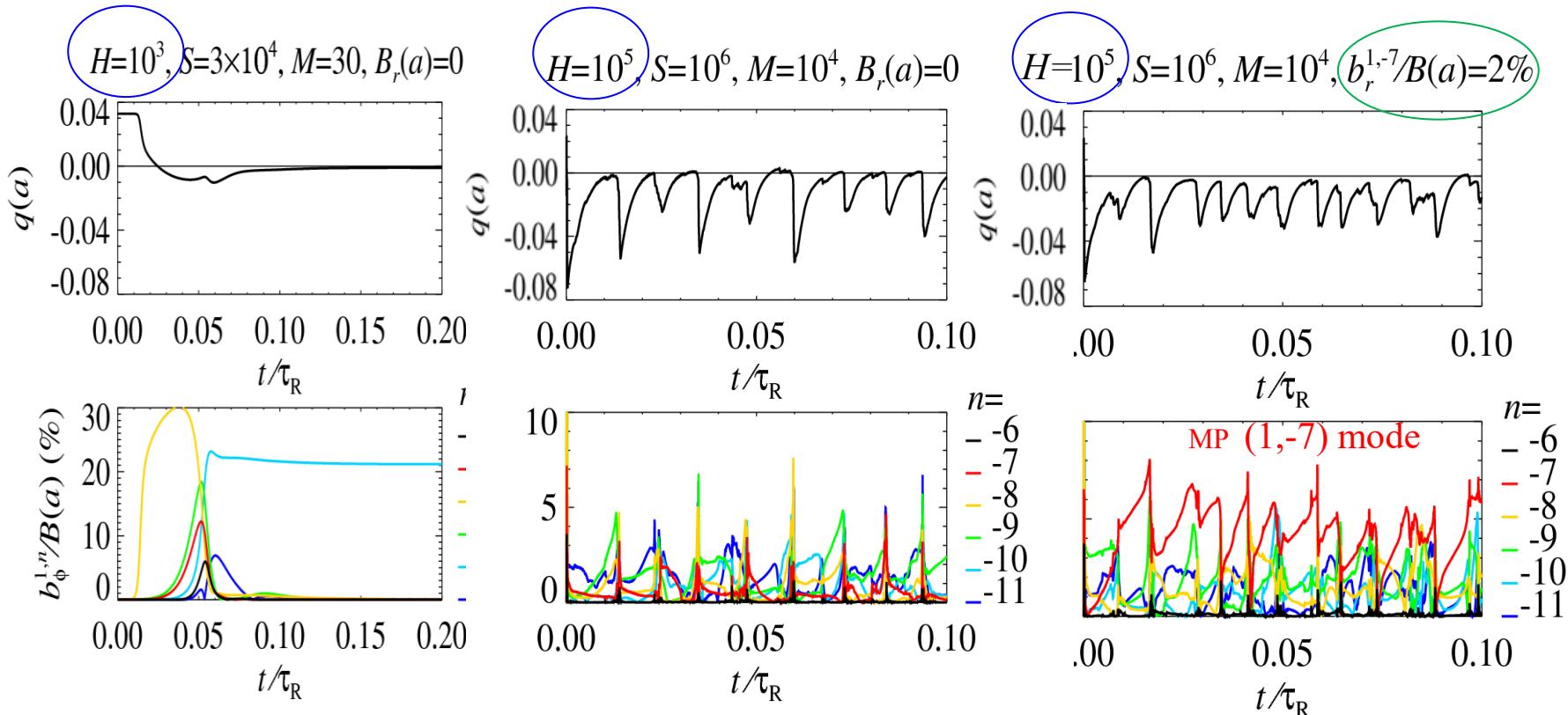


The higher H (lower dissipation)
the smaller the MP required to
excite QSH regimes

Trend with increasing H and applying MP

RFP “sawtooth” cycle excitation

“sawtooth” cycle pacing and QSH excitation



Similar to RFX-mod at
“intermediate” values of
plasma current

Circular tokamak in viscoresistive SpeCyl simulations: + MP $(1,1)$

Snake like (high dissipation) \rightarrow periodic sawtoothing (low dissipation)

approaching snake (**same dissipation but MP applied**)

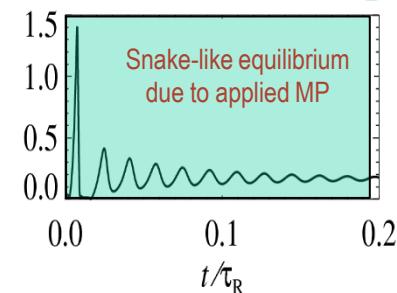
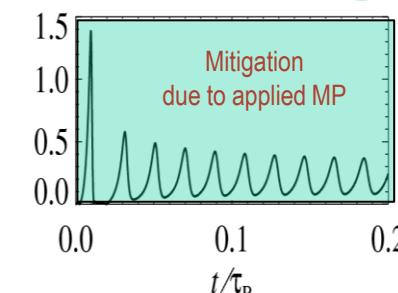
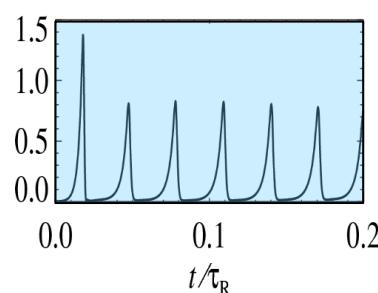
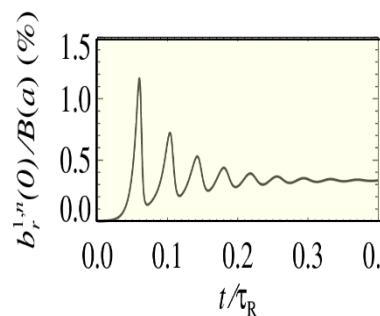
Trend with increasing H and applying MP

$$H=5.7 \times 10^3, S=10^6, M=33, B_r(a)=0$$

$$H=1.8 \times 10^4, S=10^6, M=330, B_r(a)=0$$

$$H=1.8 \times 10^4, S=10^6, M=330, b_r^{1,1}/B(a)=0.1\%$$

$$H=1.8 \times 10^4, S=10^6, M=330, b_r^{1,1}/B(a)=0.3\%$$



H & MP produce similar dynamical effects as in RFP

Bonfiglio, Chacon, Cappello PoP 2010

Bonfiglio, Escande , Zanca, Cappello NF 2011

Veranda, Bonfiglio Cappello et al EPS 2012

Bonfiglio, Veranda , Cappello et al PPCF 2015

Remarks:

- 3D nonlinear MHD simulations at realistic values of Lundquist parameters remain beyond present capabilities,
- indeed, the estimate of a realistic viscous Lundquist, i.e. theory of momentum transport, is still an open issue,
- Uncertainty in the estimate of Lundquist number appears less problematic, yet some debate still pop up here and there;

3D nonlinear MHD

Summary of the presented hints from viscoresistive approximation of RFP description:

Large and medium scale resistive-kink/tearing modes yield field reversal (dynamo effect);

Resitivity and viscosity (the product of them - η) govern:

- the transition from magnetic chaos dominated to reduced chaos (QSH) regimes,
- the amplitude and frequency of sawtooting,

Magnetic Perturbations (MP):

- are capable of pacing sawtooth amplitude and frequency,
- favors the transition to QSH;

Summary and Concluding remarks

J. B. Taylor theory of RFP relaxation ('70ties).

- Variational principle: provides analytical solutions of magnetic profiles similar to experimental measurements.

Toy model ('60ties and modern *revival*).

- Schematic model provides intuitive description of macroscopic helical self-organization.

3D nonlinear MHD numerical simulations.

- Despite the simple approximation adopted in SpeCyl code implementation, several characteristic features observed in experiments find a useful description and inspires directions to be studied.

It still remains challenging to achieve a quantitative predictive capability, needed for fusion research.

Additional hints are available from viscoresistive approximation of RFP description, and are briefly presented in the following slides:

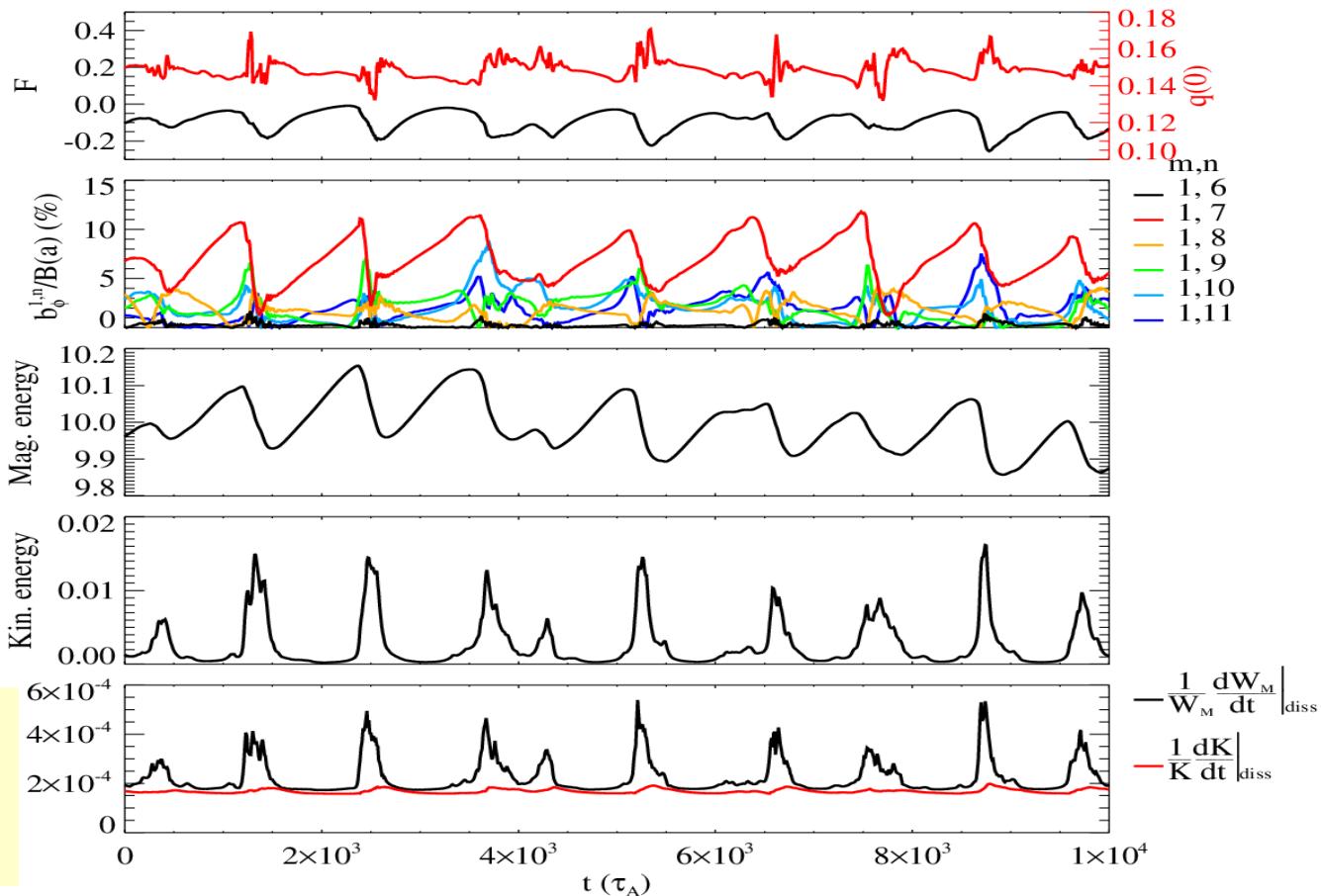
- Relaxation-reconnection events at sawtooth cycle
 - Magnetic into Kinetic energy conversion (possible ion heating?)
 - Current sheets formation – magnetic reconnection,
 - Mode phase locking, (toroidal collapse of the helix)
 - Excitation of Alfvén waves
- Transport Barrier formation and Magnetic chaos healing
- Some open issues

next slides: relaxation-reconnection cycles features (only mention)

- Magnetic into Kinetic energy conversion (possible ion heating?)
- Current sheets formation – magnetic reconnection,
- Mode phase locking, (toroidal collapse of the helix)
- Excitation of Alfvén waves

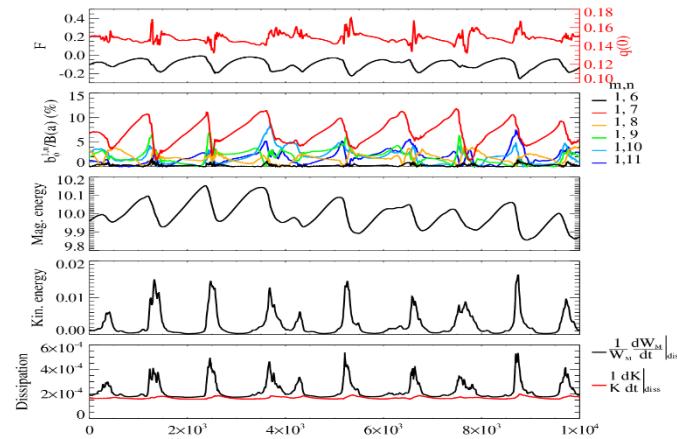
- Magnetic into Kinetic energy conversion

RFP “sawtooth” cycle

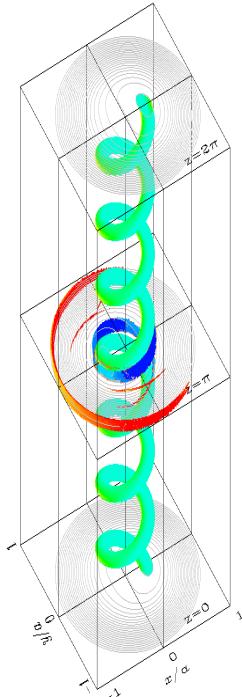


current sheets formation mode phase locking and excitation of Alfvén waves

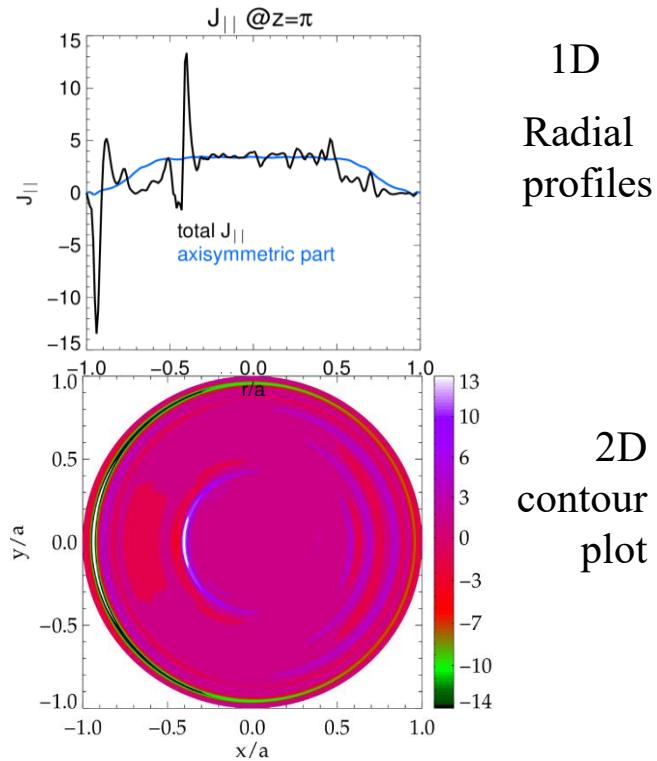
RFP S=10⁵, P=10



$J \cdot B$



3D

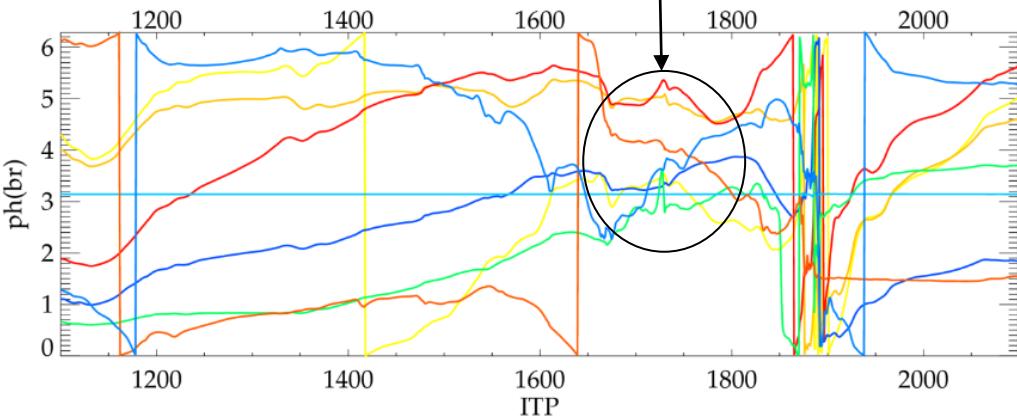
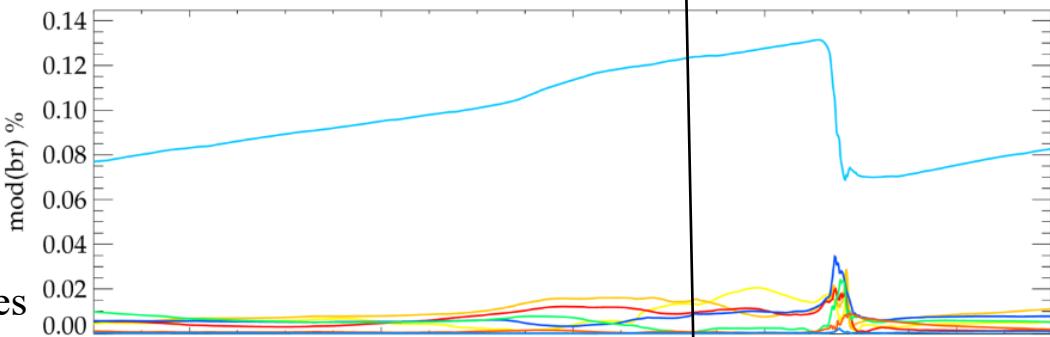
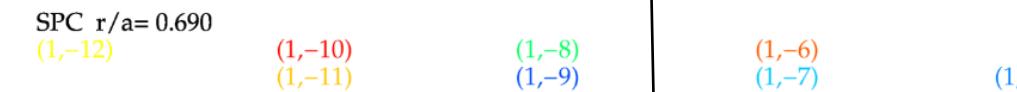
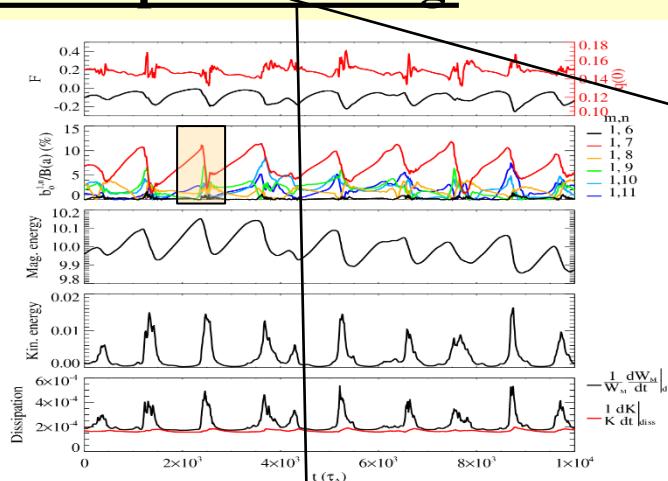


1D
Radial
profiles

2D
contour
plot

current sheets formation **mode phase locking** and excitation of Alfvén waves

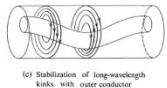
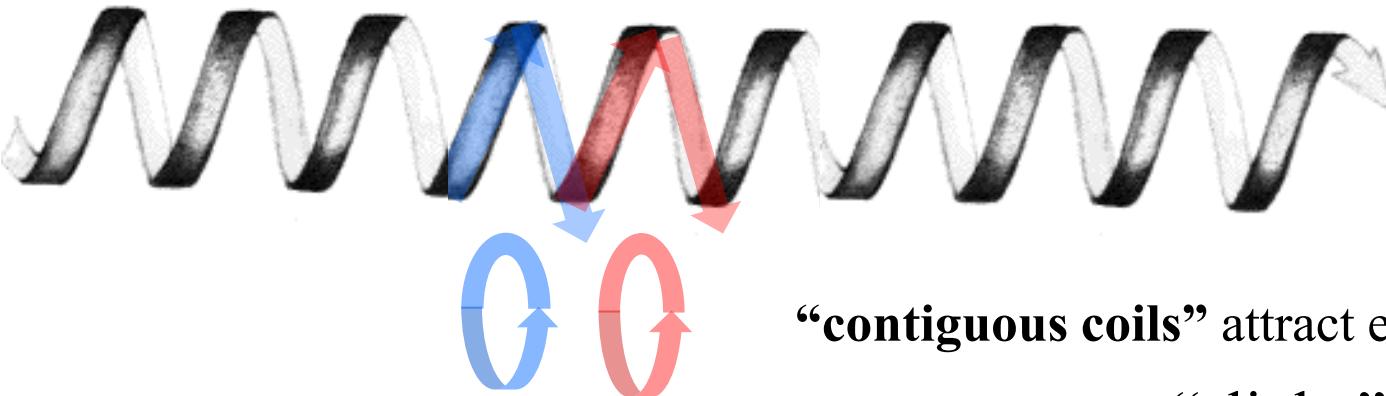
RFP S=10⁵, P=10



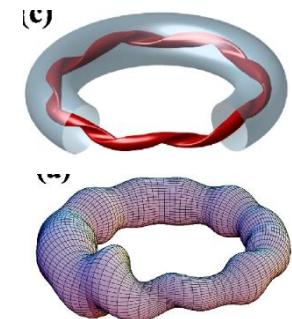
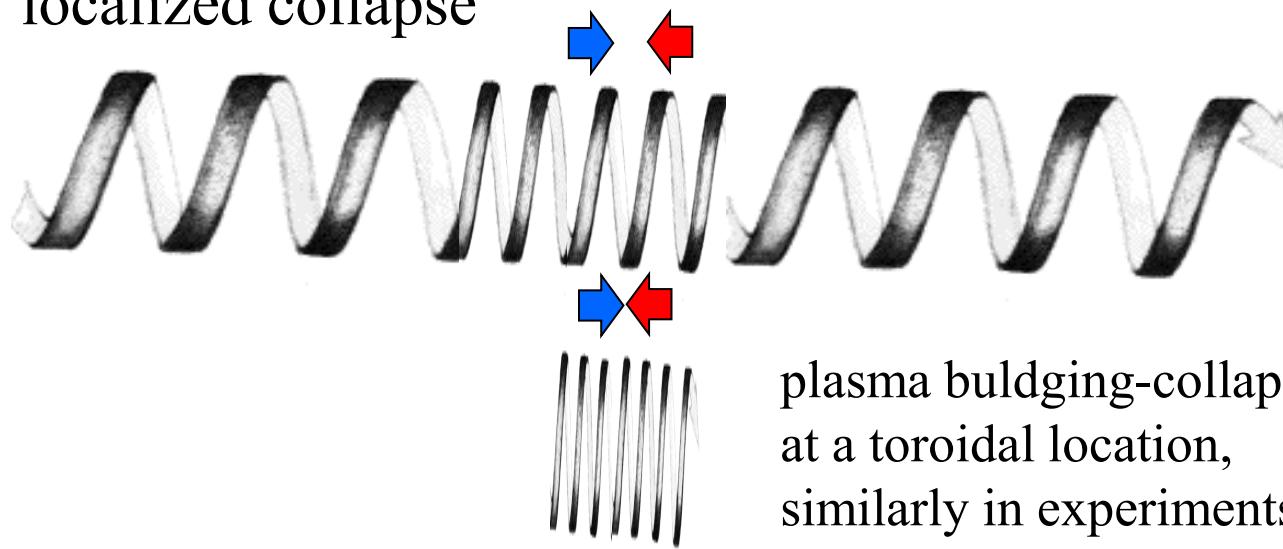
J// contours

RFP Toy model: useful to describe the “slinky -phase locking- effect”

After kinking ...



... localized collapse

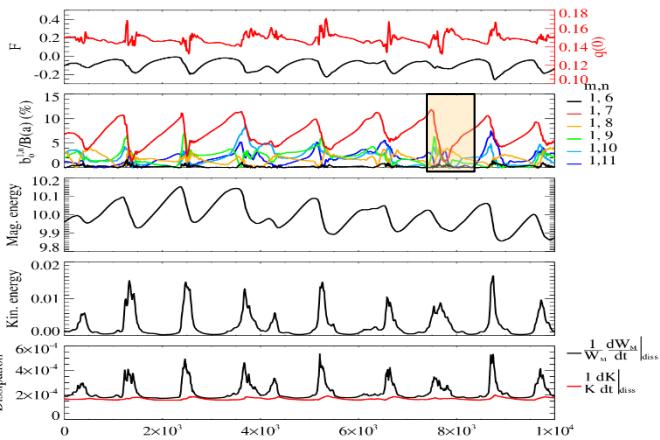
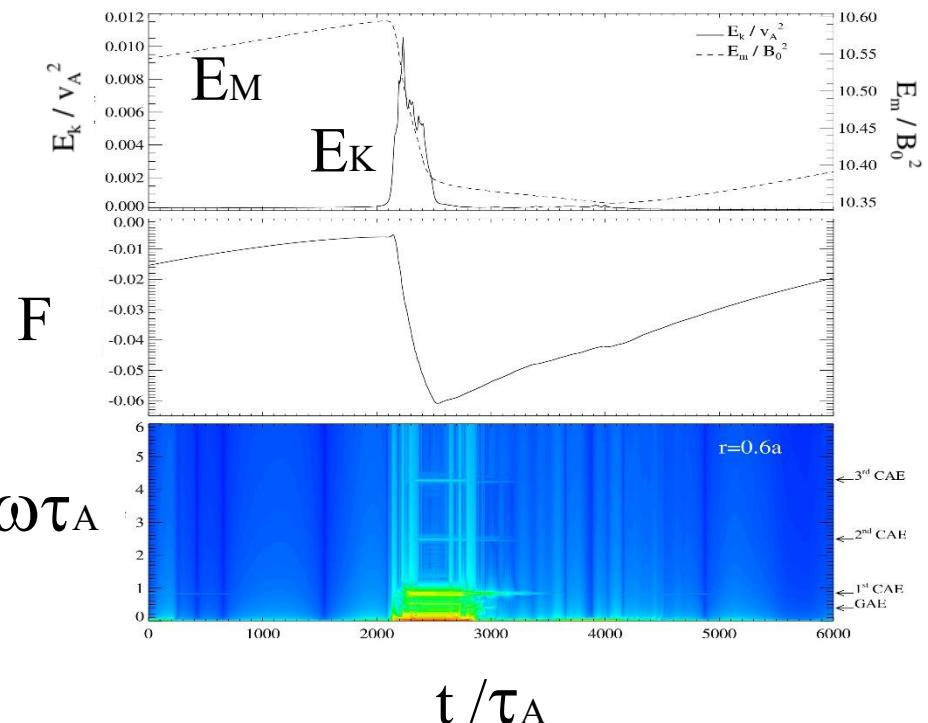


current sheets formation mode phase locking and excitation of Alfvén waves

RFP S=10⁵, P=10

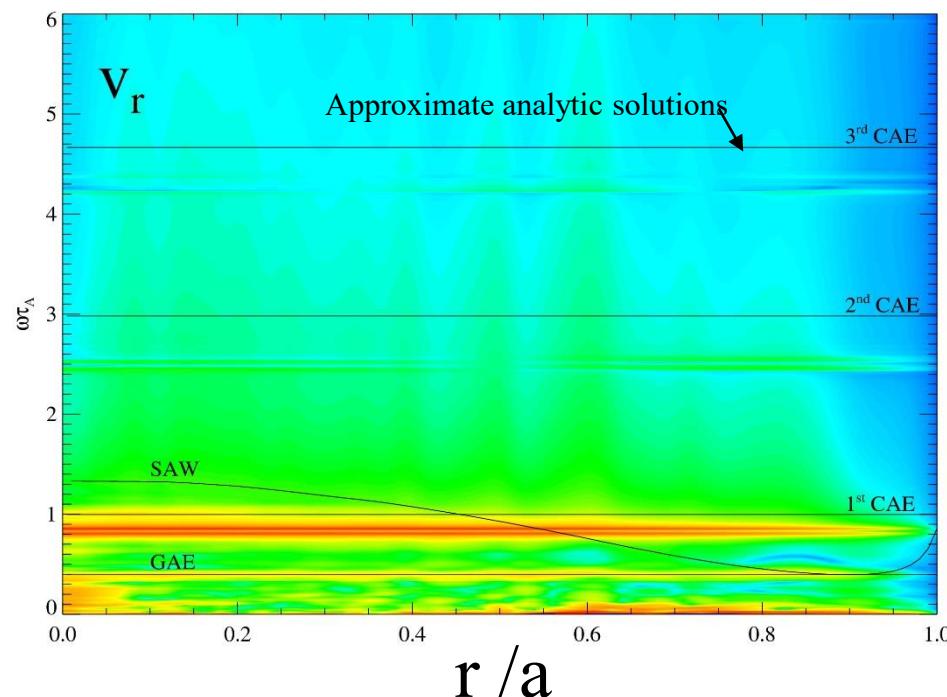
RFX-mod like density profile assigned

Alfvén waves spectrum
($m=1, n=0$) $r = 0.6a$



Kryzhanovskyy et al NF 2022

Alfvén Eigenmodes
(in particular the GAE and the
1st CAE) are excited by
magnetic reconnection event.



Experimentally observed in RFPs:
Spagnolo NF 2011 and therein refs, Koliner PRL 2012

Transport in RFP is believed to be ruled by **magnetic topology properties**:

Typical tool for topology inspection:

Poincarè surface of section approximated by **magnetic field lines punctur plot**:

Trace magnetic Field Line and mark intersection in chosen surface.

Chaotic magnetic field emerge in several conditions in RFP, Tokamak and Stellarator.

Magnetic Field line integration, numerical tools available at Consorzio RFX:

NEMATO [1]

benchmarked vs ORBIT code [2]

[1] Finn, Chacòn **PoP** 2005

[2] Ciaccio, Veranda, Bonfiglio, Cappello, Spizzo, White **PoP** (2013)

Magnetic field lines and magnetic surfaces

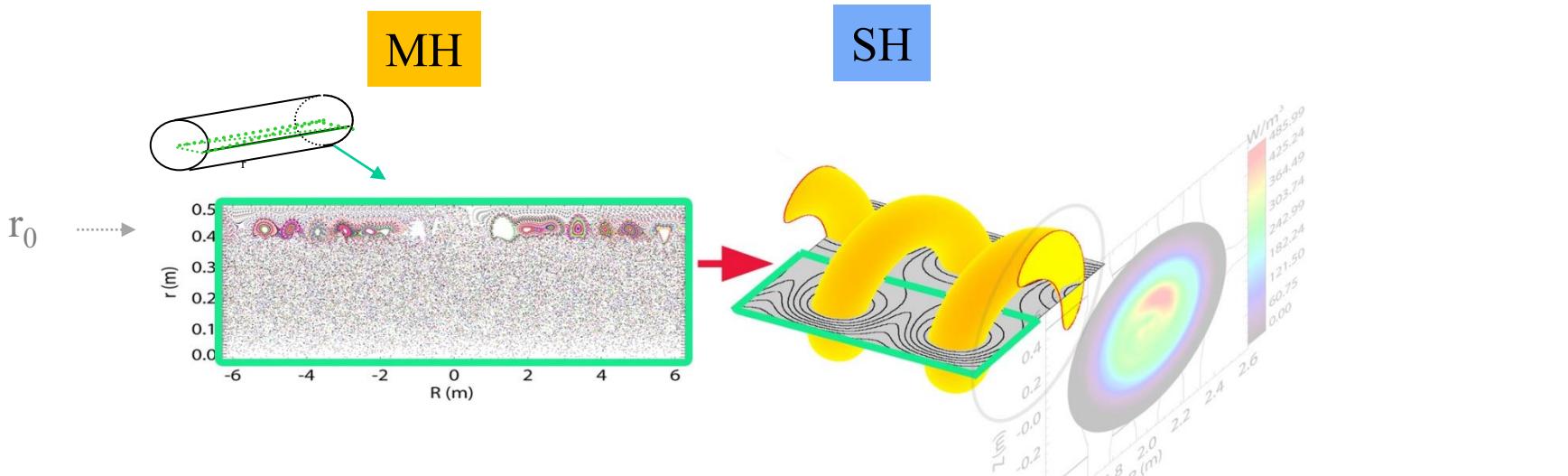
The two extreme dynamical regimes:
MH and SH (exist only in cylinder)

Magnetic field lines punctur plot:

- Magnetic chaos spreads in the core of the domain
- A chain of magnetic islands exist at reversal radius: magnetic lines lie on that surfaces, do not move from them.

Magnetic flux surfaces perfectly conserved

In helical symmetry you can find a helical flux function, the isosurfaces are magnetic flux surfaces:
Magnetic field lines lie on flux surfaces.



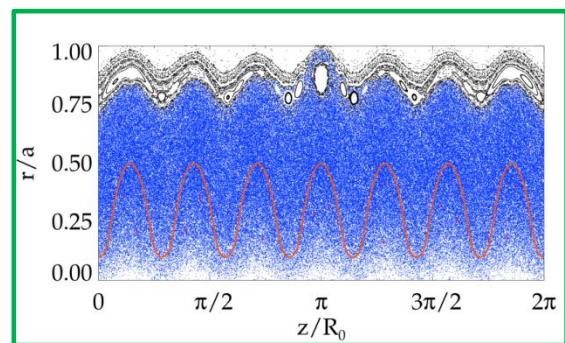
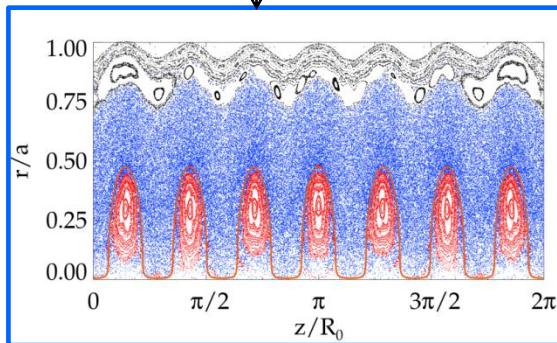
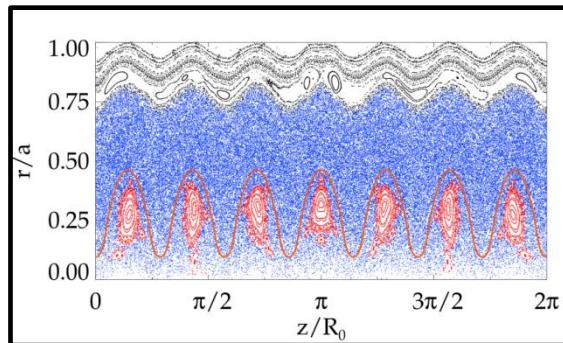
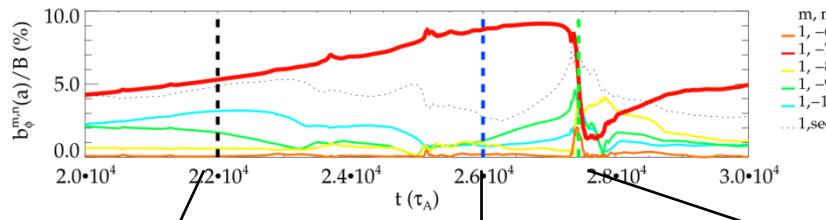
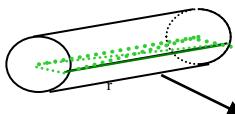
Chaos healing effect thanks to helical structure

By inspection of magnetic topology during a typical QSH sawtooth cycle in simulations we find an intermediate situation in between MH and SH: partial chaos healing

Chaos healing effect thanks to helical structure

[Dominant mode
separatrix expulsion
Escande et al PRL (2000)]

The width of conserved helical core evolves

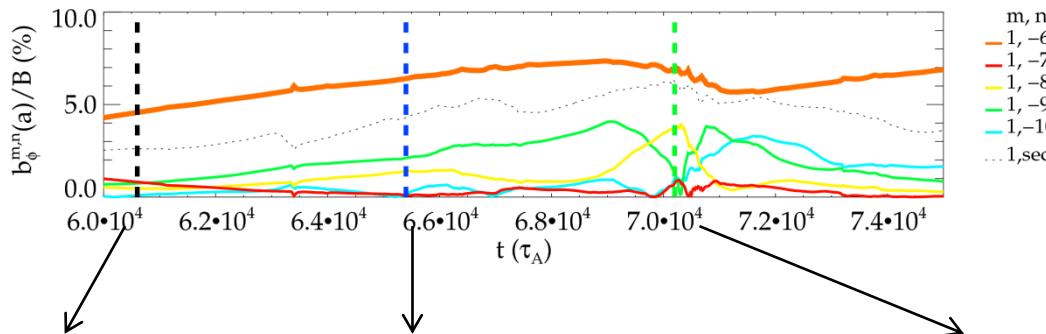


Core conserved
surfaces are lost at
slinky collapse

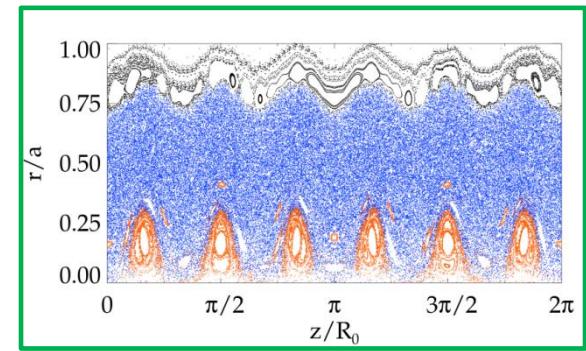
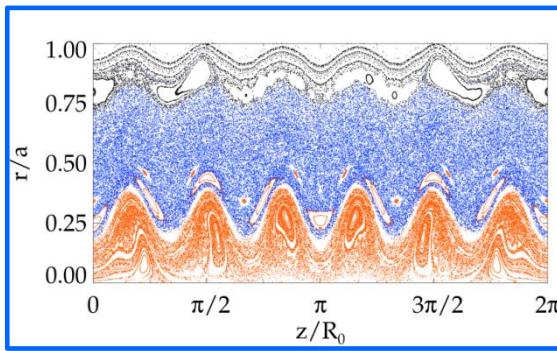
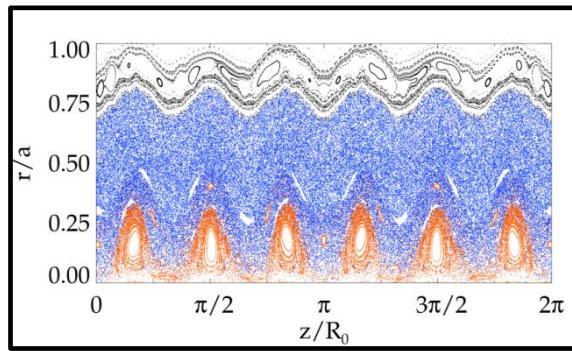


Inspired by indications obtained in topology studies of numerical simulations we studied a Non-Resonant helical regimes

More efficient chaos healing by stimulating n=6 (Non Resonant)



Conserved surfaces
are never lost



Poincare plots: secondary modes divided by 5 to match experimental amplitudes (as scaled to $S = 10^7$)

Lagrangian Coherent Structures, LCS, detected in simulation cases:

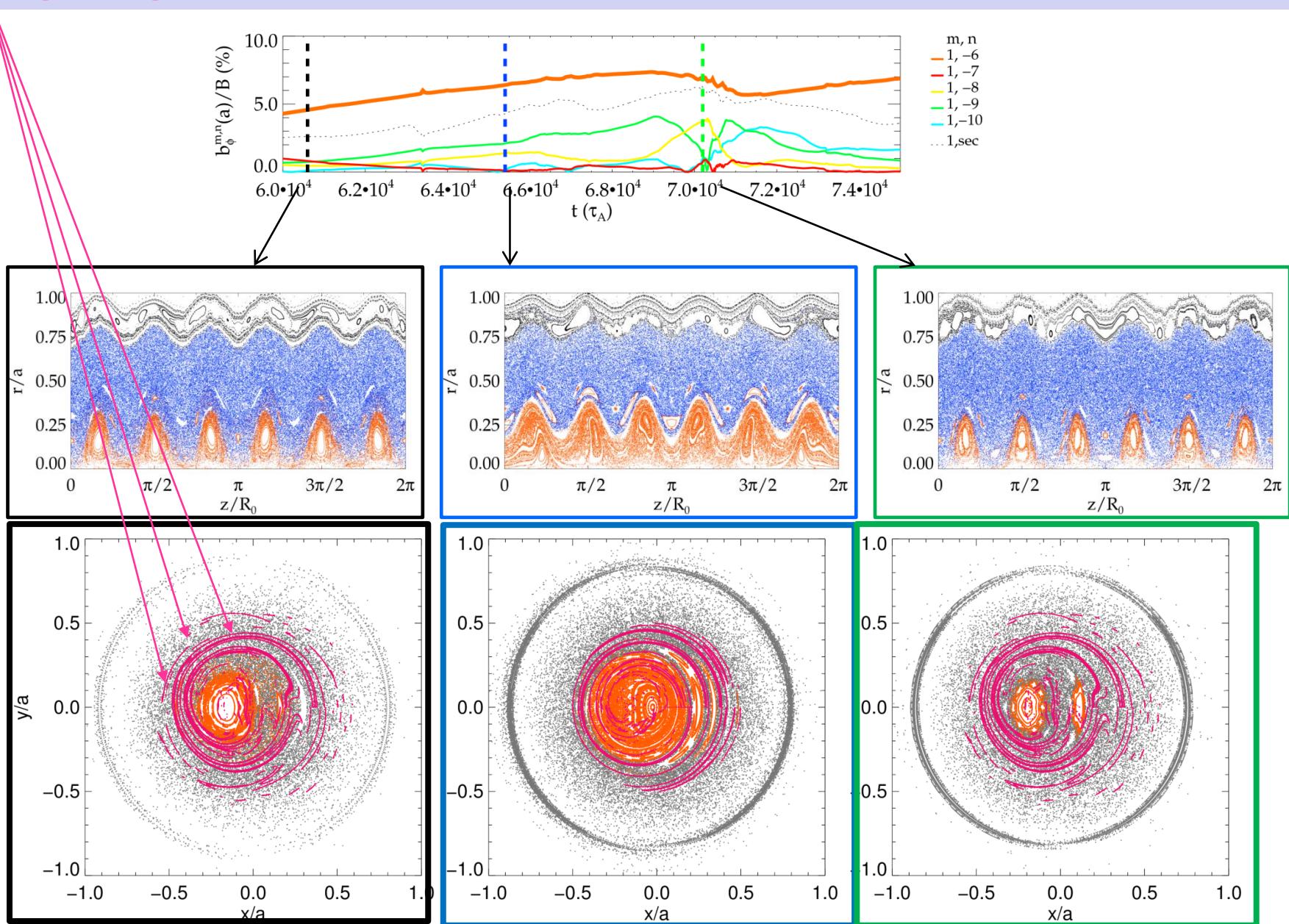
Barriers to the wandering magnetic field lines *embedded in chaotic domains*

- Di Giannatale, Bonfiglio, Cappello, Chacòn, Veranda NF (2021)
- Veranda, Bonfiglio, Cappello, Di Giannatale, Escande NF (2020)
- Pegoraro *, PPCF (2019)
- Di Giannatale, et al POP a,b (2019)
- Rubino °, Borgogno°, Veranda, Bonfiglio, Cappello, Grasso°, PPCF (2015)

Collaboration with

- ° ISC (Institute for Complex Systems) - CNR Torino Italy – Politecnico Torino
- * University of Pisa - Italy

Lagrangian Coherent Structures nearby conserved surfaces

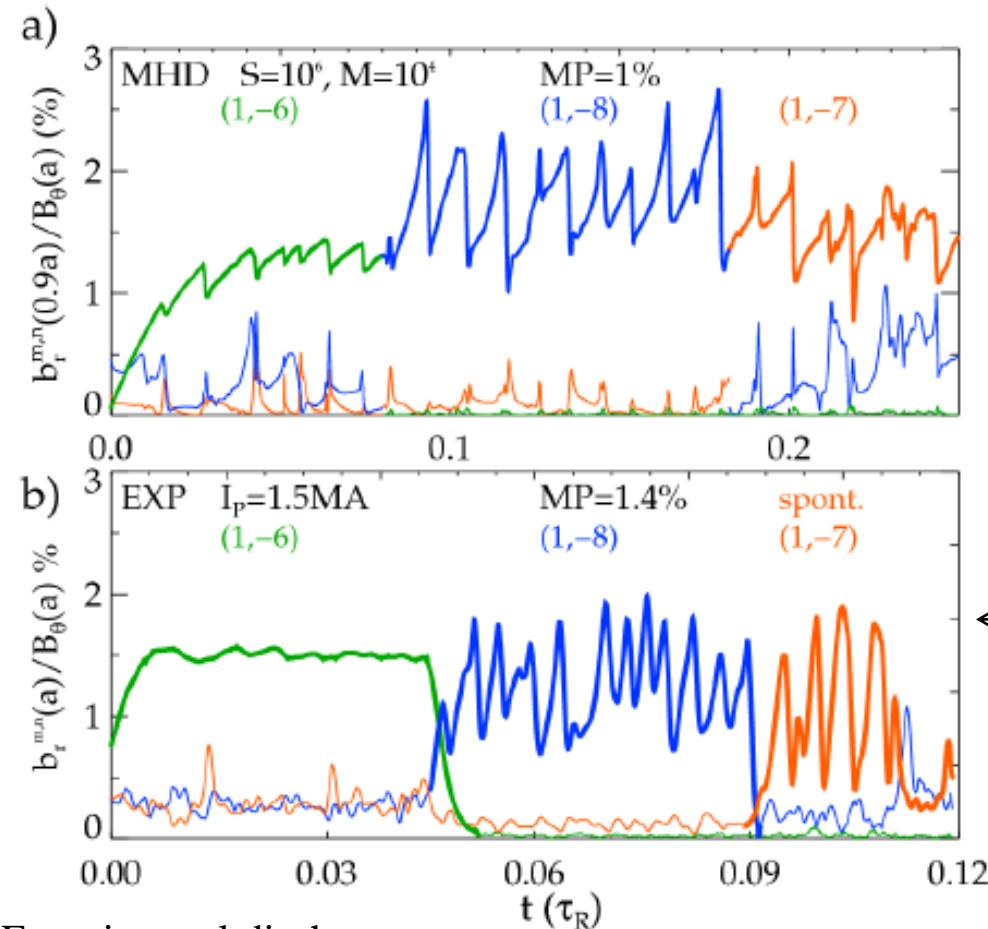


The possibility to convey the experimental discharge toward a “new” helical solution, in particular, low n non-resonant helix, has been tested in RFX-mod by applying suitable MP.

Dynamics successfully confirmed in RFX-mod experiment

Small edge Magnetic Perturbations (MP) can drive new helical regimes, with different pitch:

Validation example



Experimental discharge
#30932 RFX-mod

simulation

Successful RFX-mod experiments:
alternative ns
stimulated by seed MP

Some open issues, Ongoing work:

Implementation of more **realistic Boundary Conditions**

Verification SpeCyl – PIXIE3D (Chacòn-LosAlamos)

Spinicci (PhD), Bonfiglio et al, EPS 2022

Addressing **estimate of experimental effective Hartmann**

Heuristic approach (momentum transport in plasmas is a long standing open issue)

Vivenzi (PhD) Veranda et al, EPS 2022 ; Vivenzi Veranda et al, Theory Fusion Plasmas 2022 submitted JPCS

Assessing **magnetic LCS validation on experimental eITB**

follow up of Veranda et al, NF 2017

Further develop **analogies RFP – Tokamak - ...**

- **Alfven waves excitation at sawtoothing (ohmic)**

Kryzhanovskyy (PostDoc), Bonfiglio et al, Nuclear Fusion 2022 <https://doi.org/10.1088/1741-4326/ac6ad3>

Kryzhanovskyy (PostDoc), Bonfiglio et al, paper under revision

- **What is the role of visco-resistive “quality” in determining MHD mode coupling in Tokamak ?**

Possible impact on density limit processes (both RFP and Tokamak) under discussion

What is the mechanism of “anomalous” ion heating in RFPs (observed at sawtoothing) ?

non resonant Alfvèn wave particle interaction

spare slides

Theory and Simulation Group at Consorzio RFX:

Susanna Cappello

[3D nonlinear MHD (head of the group)]

nome.cognome@igi.cnr.it

Fabio Sattin

[particle statistics and wave-particle]

Daniele Bonfiglio

[3D nonlinear MHD]

Italo Predebon

[gyrokinetics, MHD]

Marco Veranda

[3D nonlinear MHD, magnetic topology]

Emanuele Spada

[high voltage holding (MITICA-NBTF) / theoretical studies]

+ 2 Post Doc (Kryzhanovskyy, Spinicci)

+ 1 PhD student (Calcagno)

+ international collaborators

Main NUMERICAL TOOLS involved on the modeling side

- **3D nonlinear MHD** – viscoresistive approximation:
SpeCyl ^[a] - PIXIE3D ^[b] (benchmarked codes) ^[c]
- **Magnetic Field line integration:**
NEMATO ^[d] (benchmarked vs ORBIT code ^[e])
- **Lagrangian Coherent Structures** detection ^[f, g]

[a] Cappello, Biskamp **NF** 1996

[b] Chacòn **CPC** 2004, Chacòn **PoP** 2008

[c] Bonfiglio, Chacon, Cappello **PoP** 2010

[d] Finn, Chacòn **PoP** 2005

[e] Ciaccio, Veranda, Bonfiglio, Cappello, Spizzo, White **PoP** (2013)

Recent collaboration with Borgogno (CNRS-Nice), Rubino and Grasso (CNR – ISC Torino, PoliTO) :

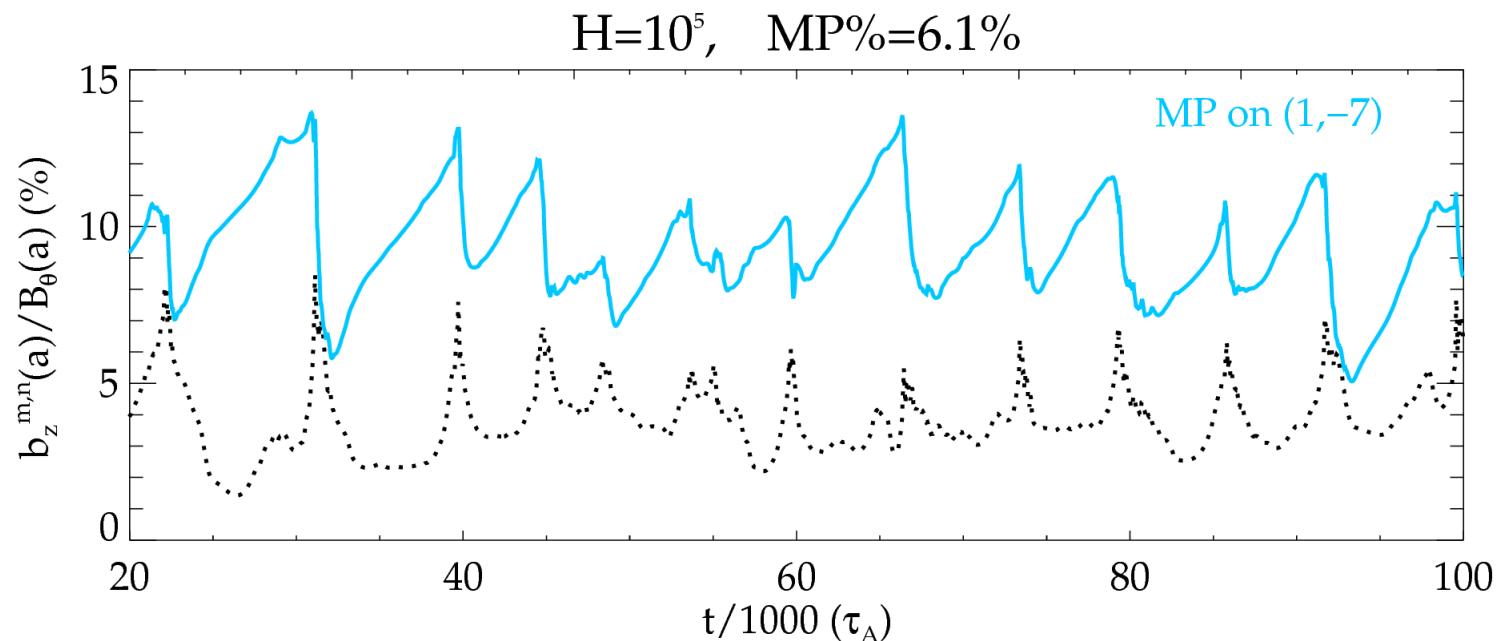
[f] Rubino, Borgogno, Veranda, Bonfiglio, Cappello, Grasso **PPCF** (2015)

[f] Di Giannatale, et al **POP** a,b (2019)

[f] Pegoraro, **PPCF** (2019)

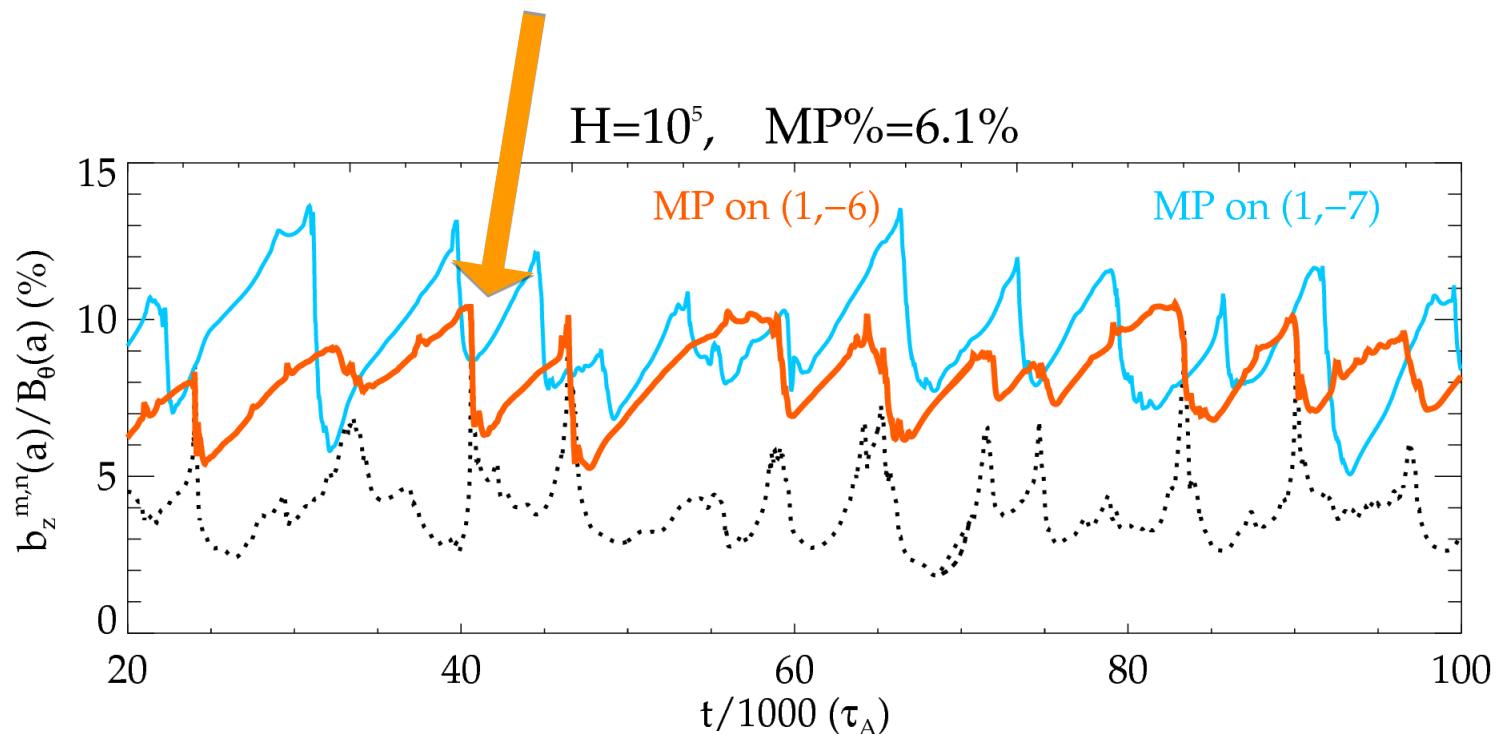
Possible to excite different ns

Dominant $(1,-7)$ and sum of secondary modes



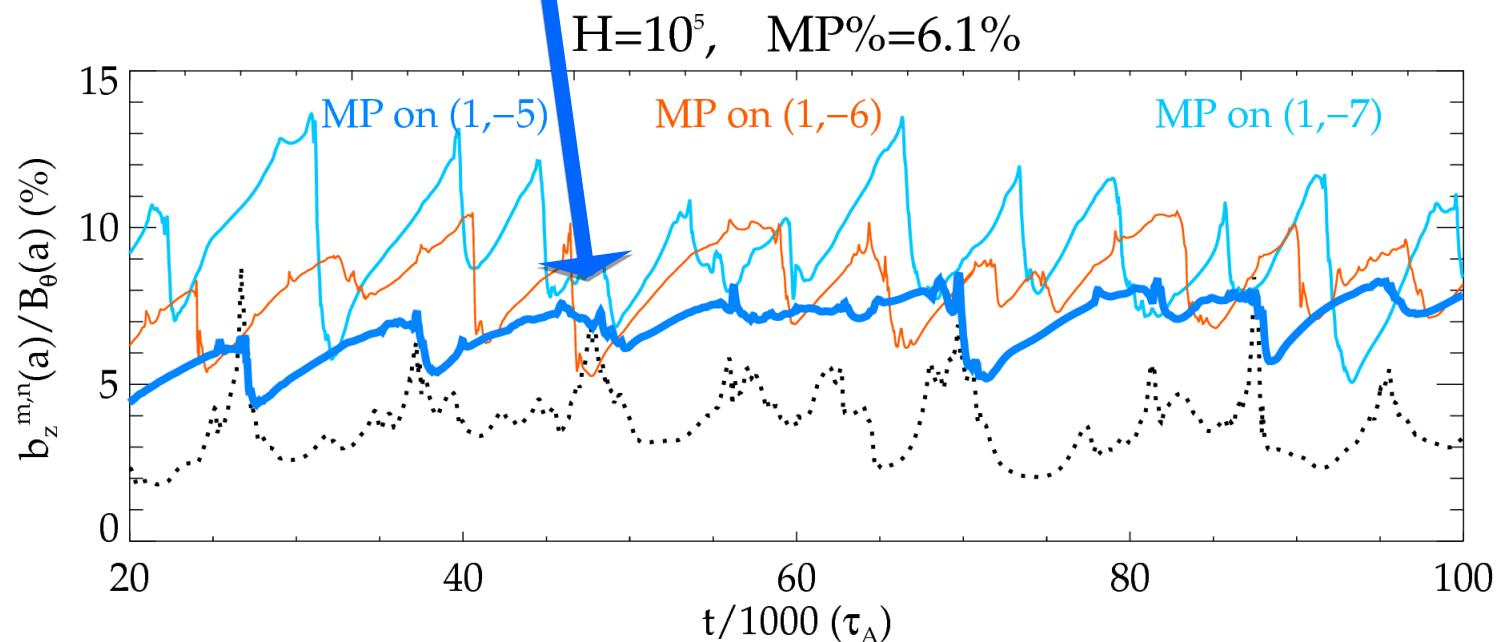
Response to different MPs : comparison

Dominant (1,-6) less reactive than -7



Response to different MPs : comparison

Dominant (1,-5) even less reactive

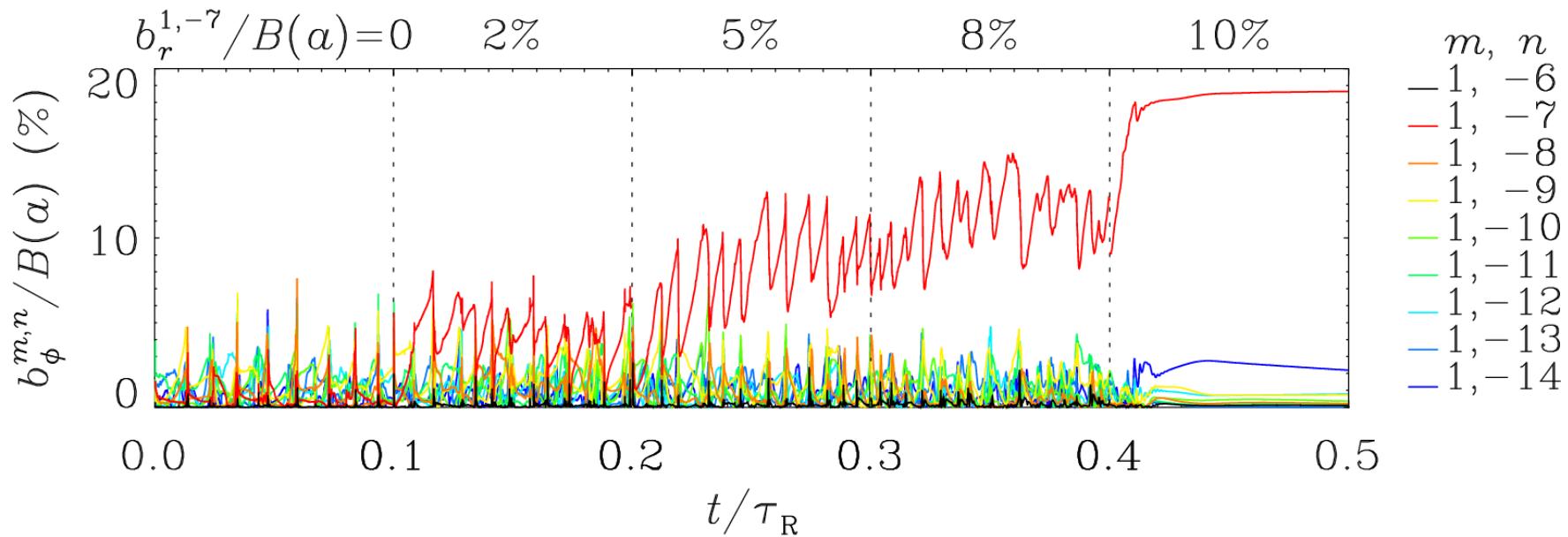


NOTE: the lower the n_{MP} -> the smaller the **Frequency&Amplitude** of cyclic oscillations

Larger MPs leads to steady helical saturation

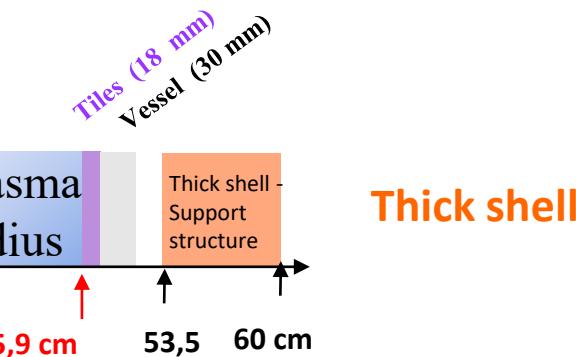
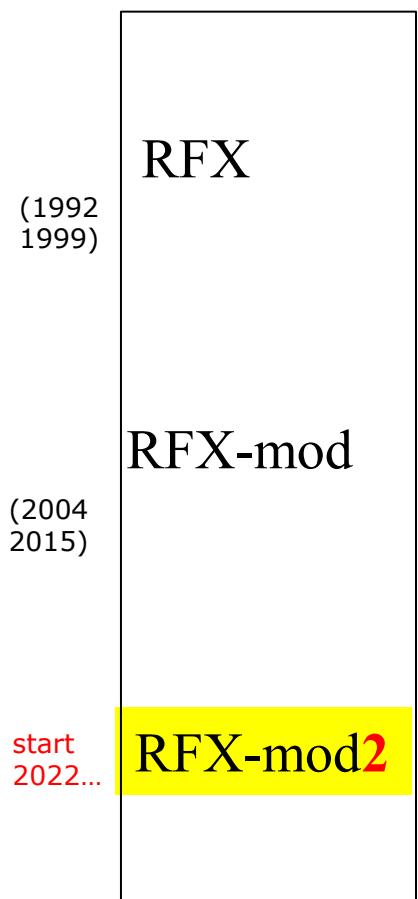
(Similar to the ones obtained at high dissipation)

Veranda PPCF 2013
Bonfiglio PPCF 2015



... to be explored in experiments

RFX device evolution: plasma radius and magnetic front-end

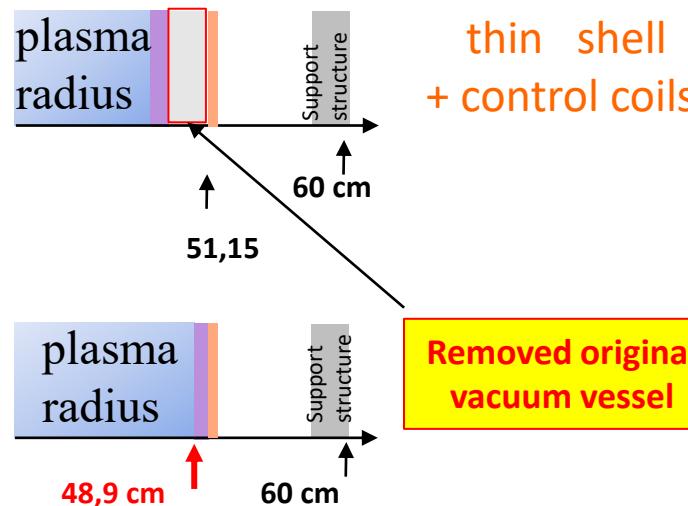


Thick shell

Shell proximity

$$b/a = 1.17$$

RFX-mod
(2004
2015)



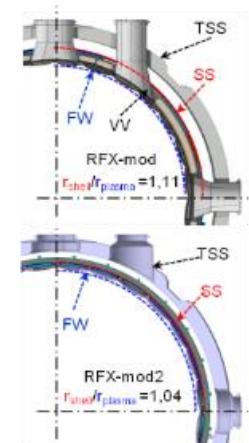
**thin shell
+ control coils**

$$b/a = 1.11$$

$$b/a = \textcolor{red}{1.04}$$

start
2022...

RFX-mod2



$r_{saddle\ sensors} = .5065$



$r_{sadle\ coils} = .5815$



$r_{pick_up\ coils} = .510$



RECONNECTION PROCESSES AND SCALING LAWS IN REVERSED FIELD PINCH MAGNETOHYDRODYNAMICS

S. CAPPELLO

Gruppo di Padova per Ricerche sulla Fusione,
Associazioni Euratom-ENEA-CNR-Univerita' di Padova,
Padova, Italy

D. BISKAMP

Max-Planck-Institut für Plasmaphysik,
Euratom Association, Garching, Germany

ABSTRACT. Reversed field pinch (RFP) sustainment is studied in the framework of three dimensional magnetohydrodynamic (MHD) numerical simulations. The scaling law for the magnetic fluctuation amplitude with Lundquist number S is $\delta B \approx S^{-0.22}$, which can be understood if the basic dynamic processes are governed by current sheet reconnection. Quasi-periodic oscillations are in fact found to be correlated with the presence of localized sheet currents, which for sufficiently large S make the major contribution to the average power dissipated by fluctuations. Special attention is paid to numerical convergence in the simulations. The results are compared with experimental observations.

The $m = 0$ modes are found to contribute directly to the dynamo action. Figure 9 shows the radial profile (time averaged over $3500\tau_A$) of the contributions to the poloidal electric field $E_\theta^D(r) = -(\vec{v} \times \vec{b}_\theta)$ of the

578

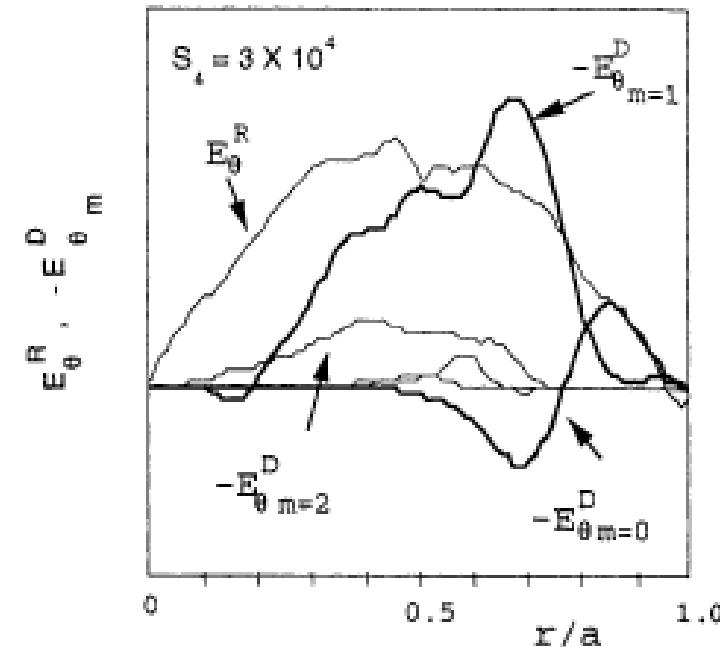
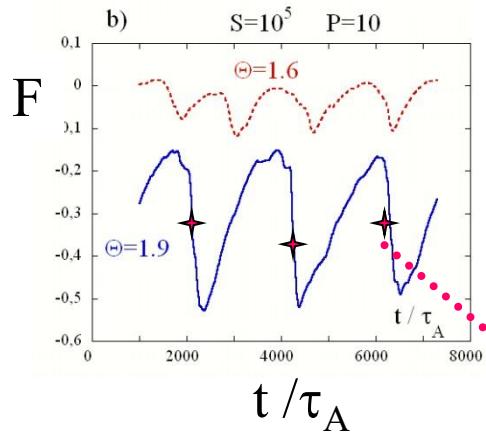


FIG. 9. Poloidal electric field along the radius: resistive and dynamo contributions: $E_\theta^R(r)$ and $-E_{\theta m}^D(r)$.

different m modes in the $S = 3 \times 10^4$ case. E_θ^D balancing the resistive term $E_\theta^R(r) = \eta \bar{J}_\theta$ in Ohm's law. The $m = 1$ modes give the largest contribution to E_θ^D over the major part of the plasma radius, but the $m = 0$ contribution becomes comparable in amplitude in the outer half of the radius and, in particular, by changing sign in the vicinity of the reversal is the

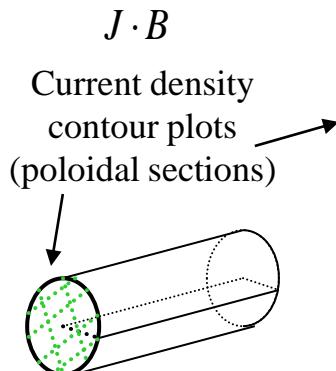
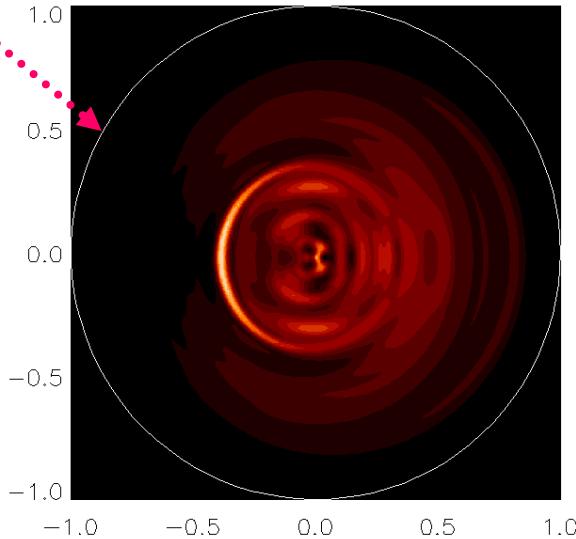
MH regime:

Nearly-periodic relaxation events



(similarly to low current experimental observations)

with formation of current sheets

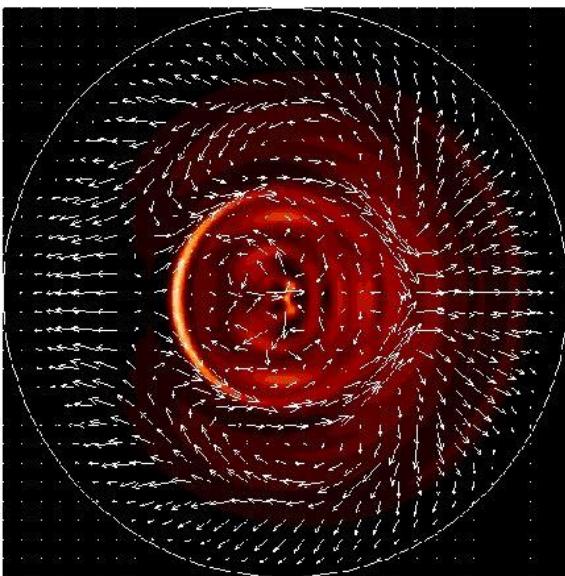


(3D: all of the
modes
contribute)

Bright colour =>
high current

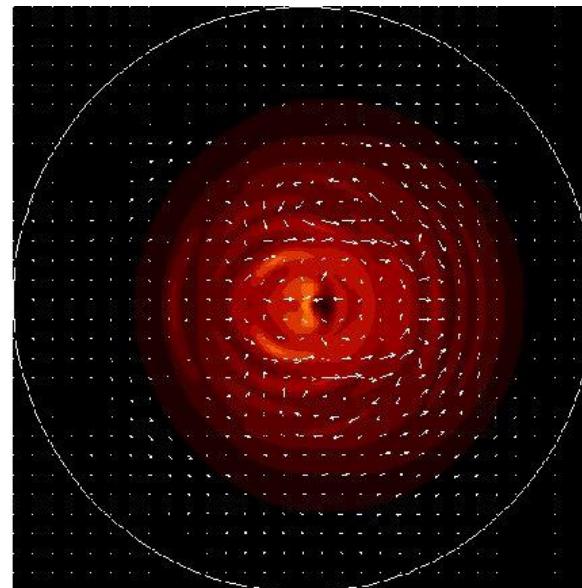
Cappello & Biskamp Nucl Fus 1996

$J \cdot B$ contour plot and flow pattern

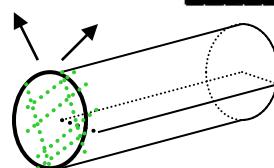


during RFP relaxation event

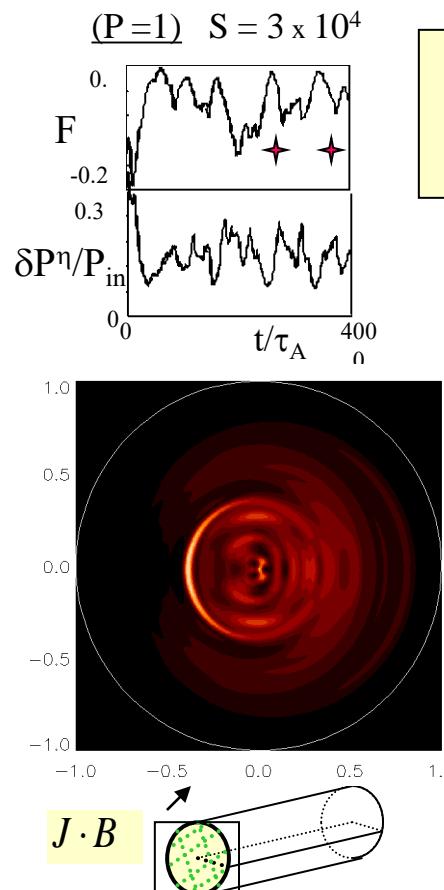
... in between relaxation events



Bright colour => high current



MH regime:



MHD Reconnection and scaling laws

Cappello & Biskamp Nucl Fus 1996

Quasi-periodic relaxation events
with formation of current sheets (3D)

NUMERICAL
scaling law

$$\delta B \sim S^{-0.22} \quad (P=1)$$

$$\delta B \sim S^{-1/4} \quad (= H^{-1/4})$$

(at constant P)

ARGUMENT:

Sweet-Parker reconnection
 $(\delta v_{perp} / \delta B = S^{-1/2})$
dominates RFP dynamics

$$(S^{-1} J_{00} = \langle \delta v \times \delta B \rangle_{0 at reversal})$$

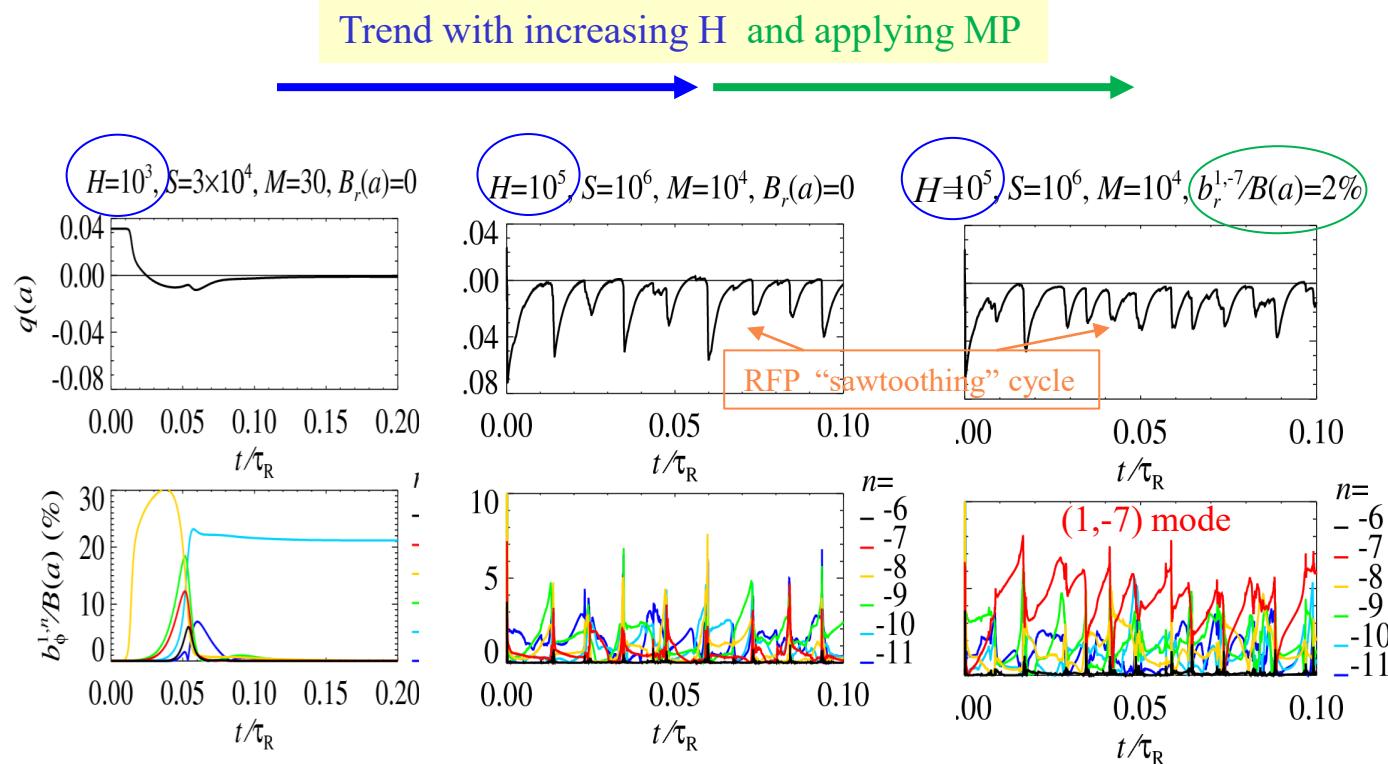
... $P \neq 1$...
+
RFX data

→
ITG turbulent
viscosity may
characterize
the RFPs

Terranova et al. PPCF 2000

3D nonlinear MHD

Reversed Field Pinch in viscoresistive SpeCyl simulations: + MP $(1,-7)$



Similar to RFX-mod discharges at
“intermediate” values of plasma current

3D nonlinear MHD

Circular tokamak in viscoresistive SpeCyl simulations: + MP $(1,1)$

Snake like (high dissipation) \rightarrow periodic sawtoothing (low dissipation)

approaching snake (**same dissipation but MP applied**)

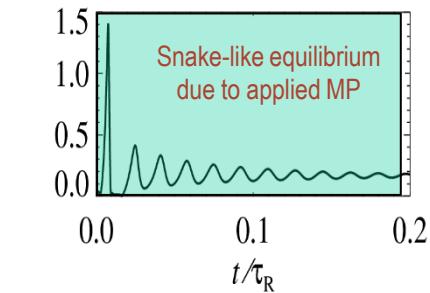
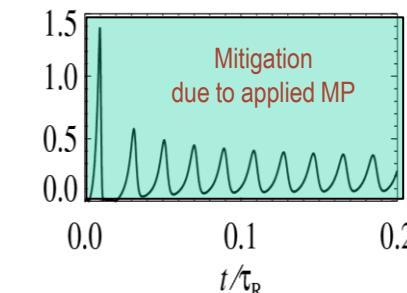
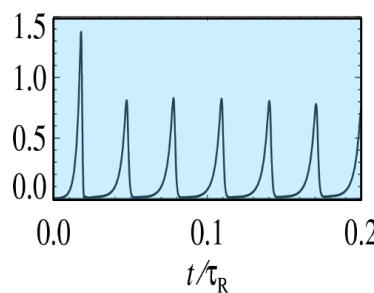
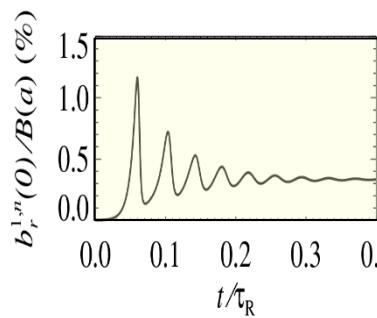
Trend with increasing H and applying MP

$H=5.7\times 10^3, S=10^6, M=33, B_r(a)=0$

$H=1.8\times 10^4, S=10^6, M=330, B_r(a)=0$

$H=1.8\times 10^4, S=10^6, M=330, b_r^{1,1}/B(a)=0.1\%$

$H=1.8\times 10^4, S=10^6, M=330, b_r^{1,1}/B(a)=0.3\%$



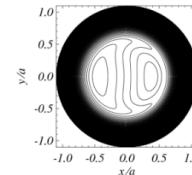
Dissipation & MP produce similar dynamical effects as in RFP

Bonfiglio, Chacon, Cappello PoP 2010

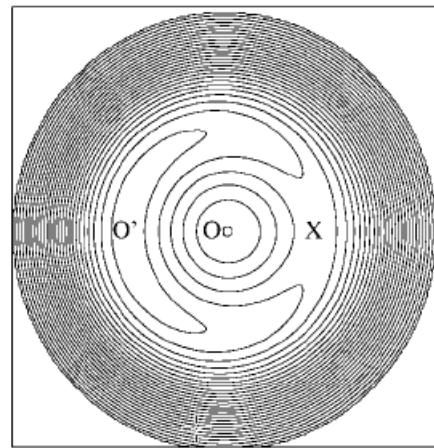
Bonfiglio, Escande , Zanca, Cappello NF 2011

Veranda, Bonfiglio Cappello et al EPS 2012

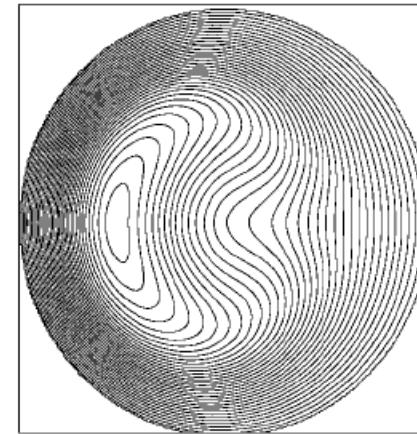
Bonfiglio, Veranda , Cappello et al PPCF 2015



When QSH dominant mode GROWS: separatrix expulsion occurs, and



(a)



(b)

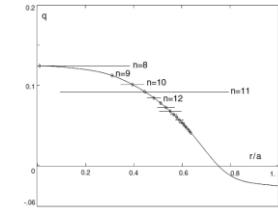
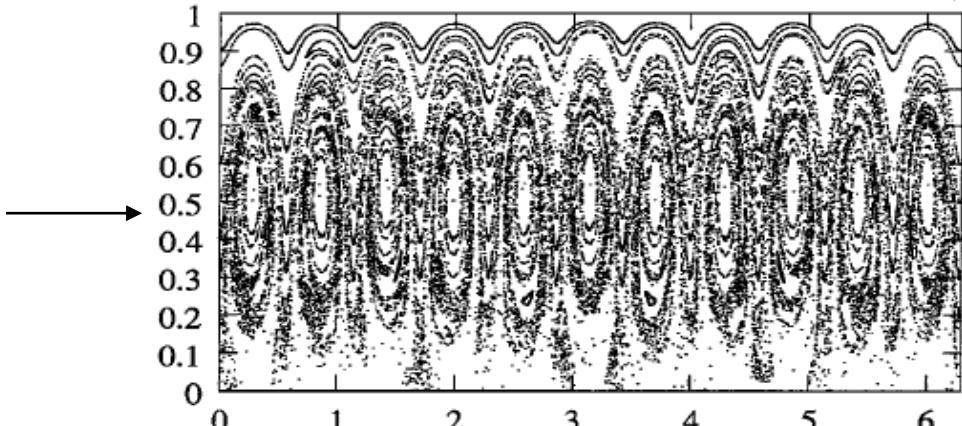
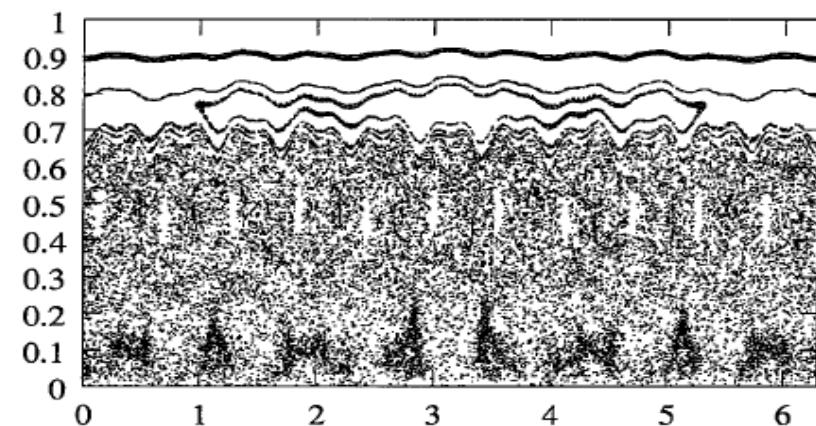
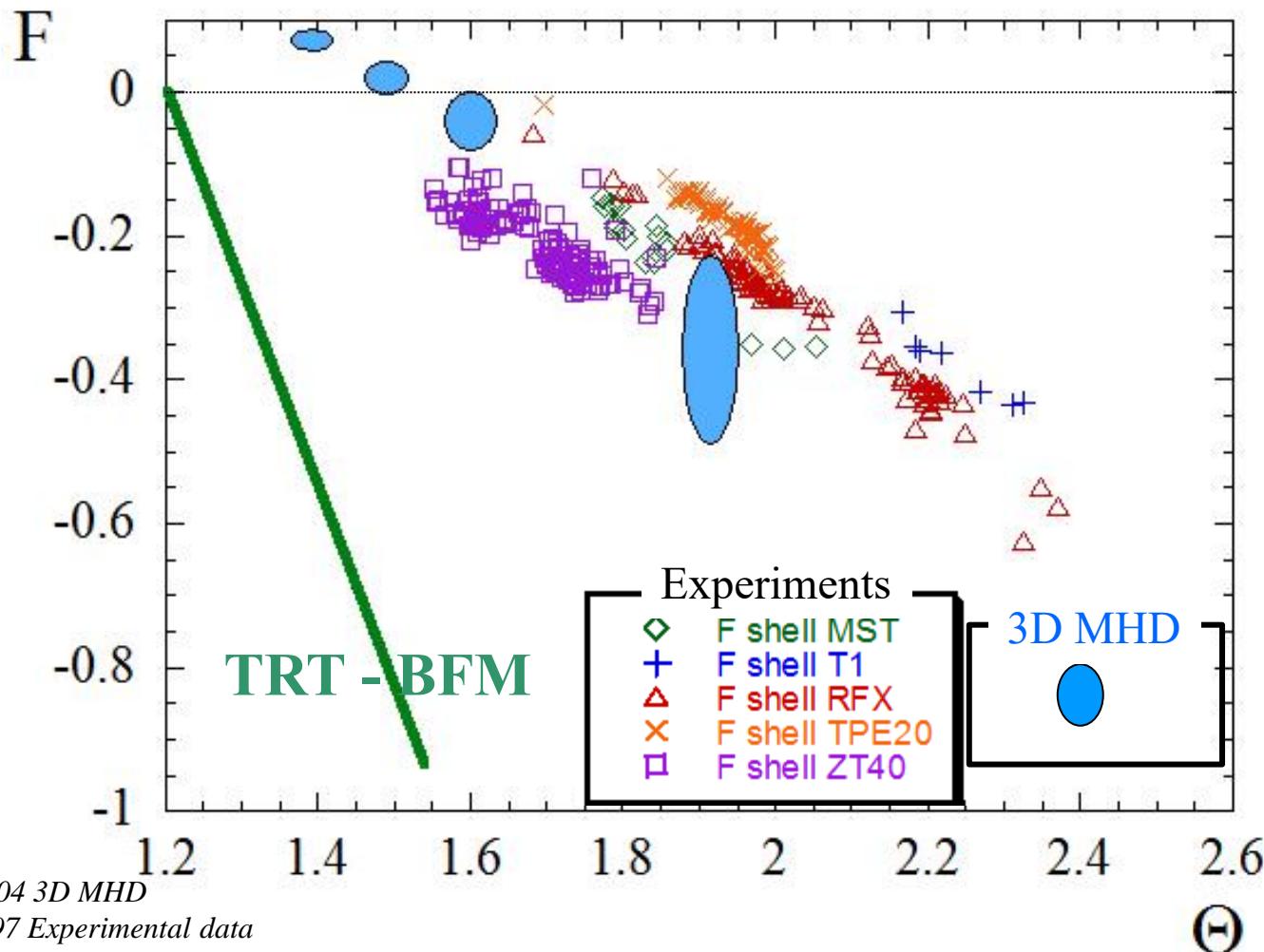


FIG. 2. q profile and magnetic islands width (shown by horizontal bars) of different $m = 1$ modes.

...clean helical topology emerges



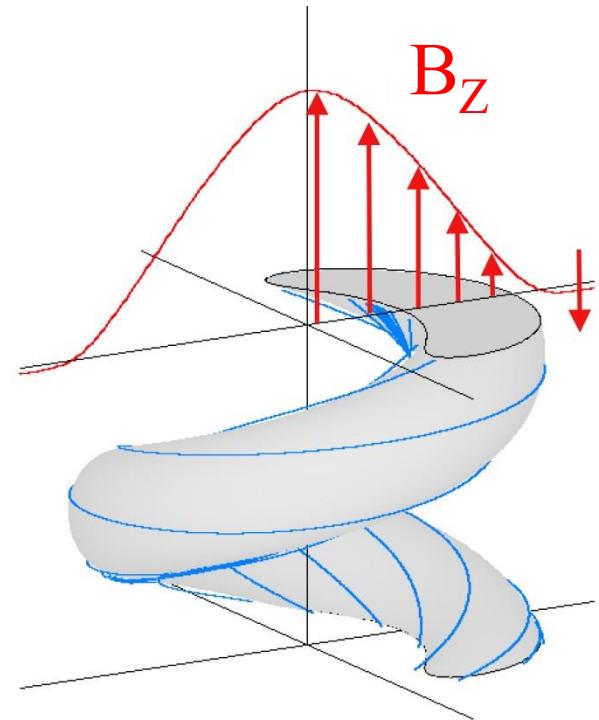
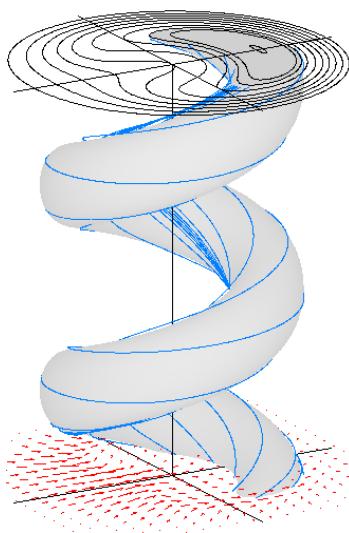
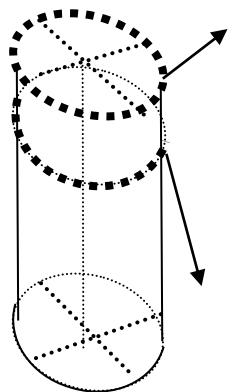
Comparison “operational points”: Numerical modelling – Experiments - Taylor’s Theory



A finite radial magnetic field component at the boundary was suggested to favour attainment of helical ohmic equilibrium (Helical Grad-Shafranov problem)

Magnetic flux surfaces & field lines

... and corresponding reversed mean profile of B_Z

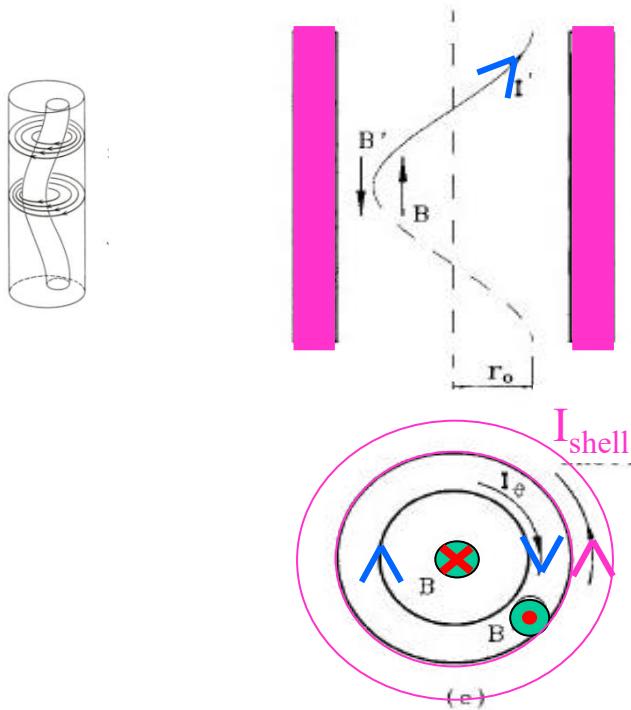


note the **velocity field** (red arrows), it is a helical pinch
it provides the Edynamo = coherent modulation $\langle \delta v \wedge \delta B \rangle$)

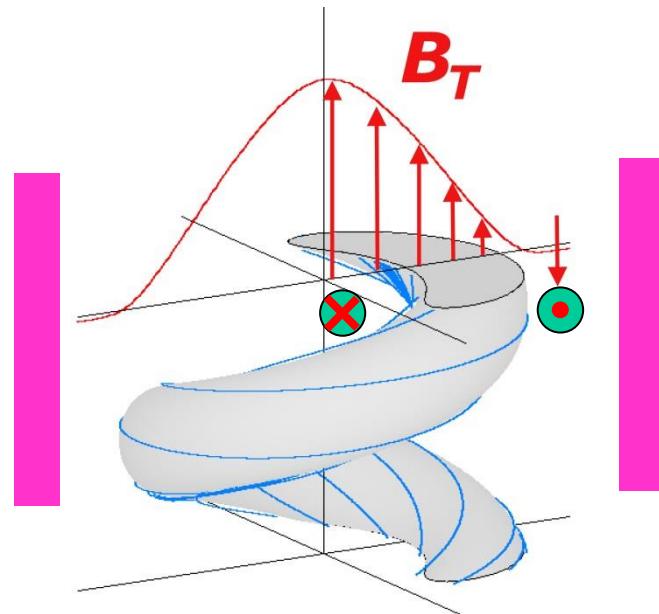
→ drift velocity induced by the electrostatic potential ...

SH solutions resemble the toy model

(c) Stabilization of long-wavelength kinks with outer conductor



kinked wire



SH in viscoresistive modelling

Nearly-periodic relaxations QSH akin to experimental ones

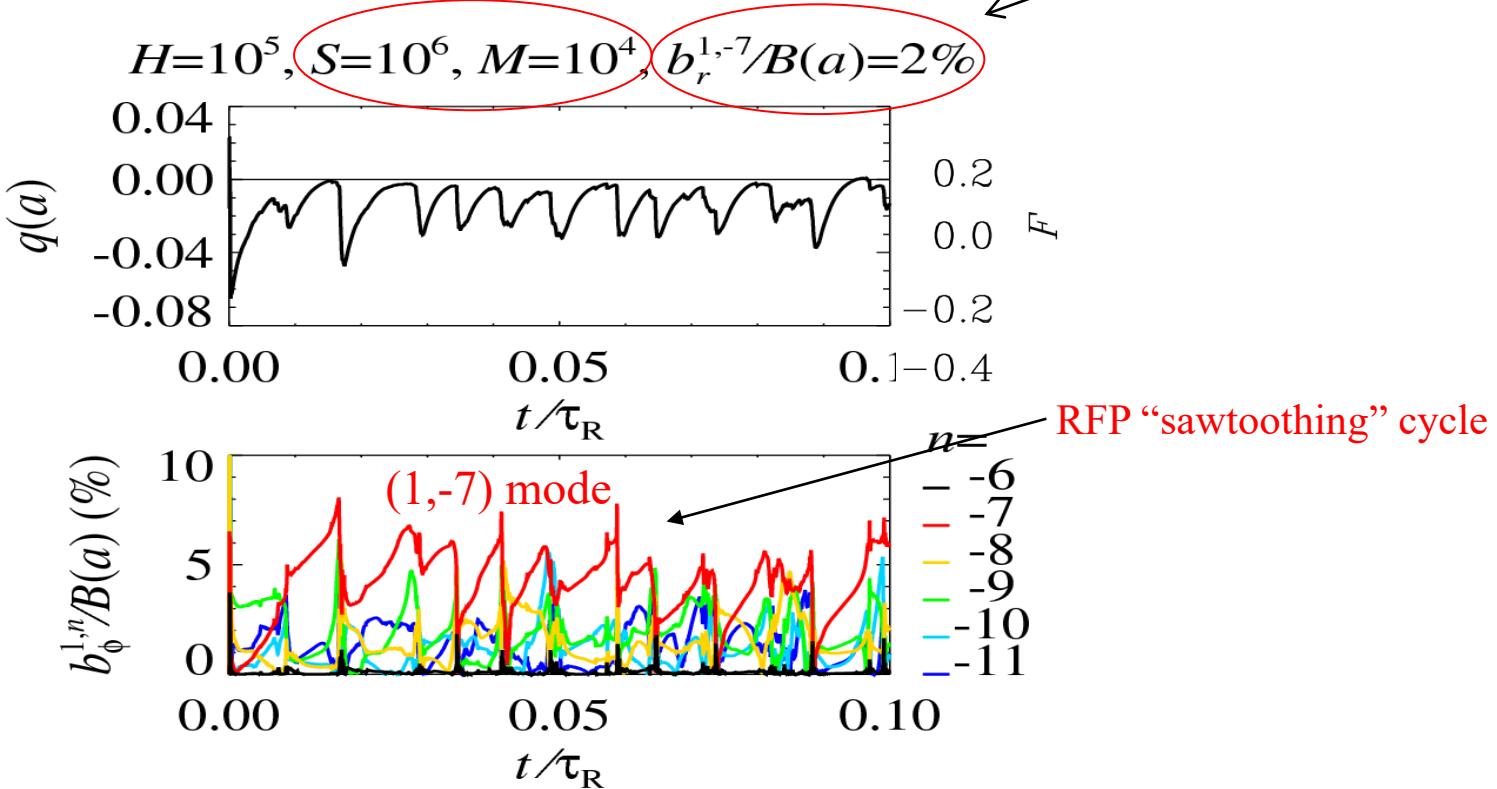
with MP (1,7)

(Ideal wall + MP)

Typical RFP sawtoothing

Mode amplitude

Bonfiglio NF 2011
Veranda PPCF 2013
Bonfiglio PRL 2013

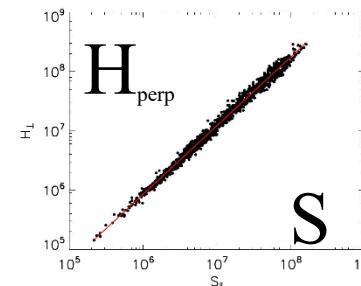
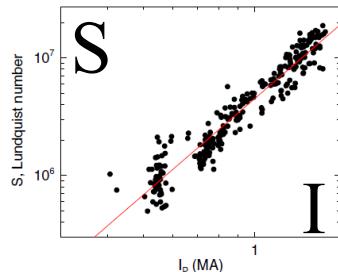


The amplitude of secondary modes decreases with Lundquist, S, and Hartmann H

**The threshold MP% to excite a dominant mode decreases with S (H) too,
... explains the experimental trend of the helical regime emerging clearly at high currents.**

RFX-mod:
 $I \geq 1\text{MA}$
 $S \geq 5 \cdot 10^6$

Piovesan,
Zuin et al
NF 2009



Vivenzi, Spizzo, Veranda,
Bonfiglio, Cappello et al
Theory Fusion Plasmas
Varenna 2022