



# Variations on Stochastic Gradient Descent

## Computational Statistics

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October 23, 2024



## Distributing and Organizing Code

- Reproducibility
- R packages

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## Course Summary

What did we actually do?

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## **Oral Examination Prep**

What to think of during examination

## Organizing Code as an R Package

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## Components

- Code for experiments
- Source code for functions (which we should be able to reuse)
- Tests
- Rcpp code
- Data

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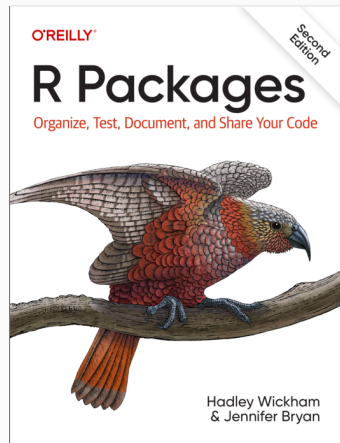
## R Package

One way is to make an R package, which helps in many ways:

- Easy to connect to C++ code through Rcpp.
- Built-in support for automatic testing
- Documentation
- Declare dependencies (other packages, R version)



Different approaches, but we will follow **R Packages** (Wickham and Bryan 2023), which is based around the **devtools** package.

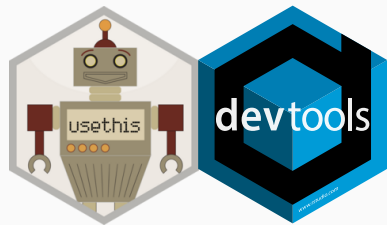


**Figure 1:** R Packages

Meta-package for various helpers that aid in developing R packages (and projects).  
First off, install and load **devtools**:

```
install.packages("devtools")  
library(devtools)
```

This loads other packages that will be useful for setting up your package, most importantly the **usethis** package.



## A Toy Example

### Rosenbrock Package

Let's build a simple package that solves the Rosenbrock optimization problem, i.e. find

$$x^* = \arg \min \left( (a - x_1)^2 + b(x_2 - x_1^2)^2 \right).$$

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- Adding R functions to our package
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- Testing our code
- Adding dependencies to other packages
- Licensing our package



# A First Package

## Create It

Call

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├── R/  
├── DESCRIPTION  
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## Install It

Open up the package in your editor (R Studio<sup>a</sup>).

```
devtools::install()
```

Voila, you have made an R package!

---

<sup>a</sup>In which case it should already be opened.

**Thank you!**

## `.R/`

- All R code should live in `.R`-files in `R/`.
- These files should (almost) always contain **only** functions.
- Many ways to organize your files: one function per file, all functions of a certain S3 class in one file etc.

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- These files should (almost) always contain **only** functions.
- Many ways to organize your files: one function per file, all functions of a certain S3 class in one file etc.

Let's create a first file: R/objective.R. Use `usethis::use_r("objective")` and insert this:

```
objective <- function(x, a = 1, b = 100) {  
  (a - x[1])^2 + b * (x[2] - x[1]^2)^2  
}
```

We have created a first R file, but how do we use it? Two major options:

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devtools::install()
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Installs the package, like calling

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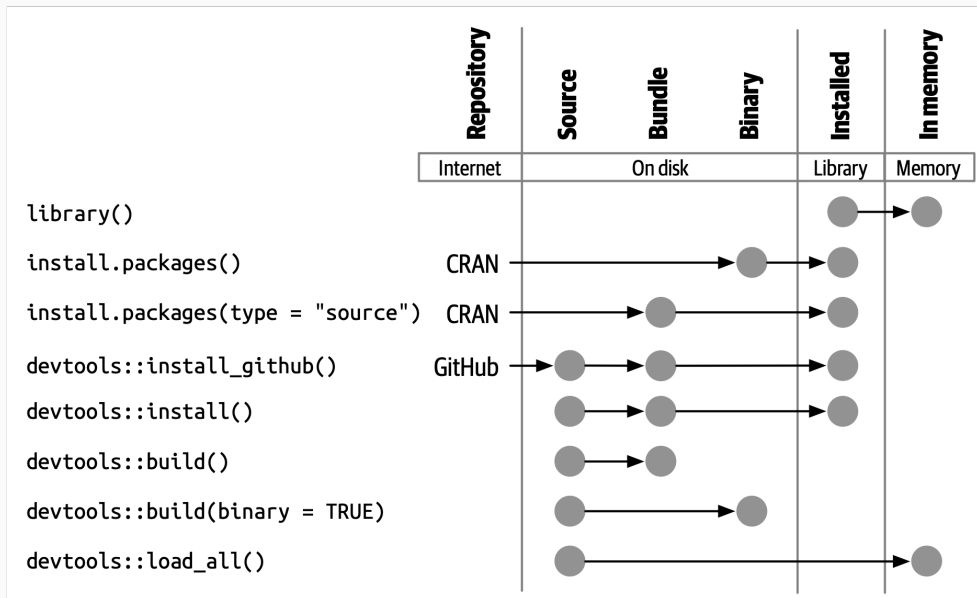
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## Try It

Try both options and see if you can call your newly defined function, `objective()`.



**Figure 2:** The various states of a package and how to move between them.

## Exporting Functions

If you called `devtools::load_all()` then everything is sourced and you can just call `objective()` directly.

But if you use `devtools::install()` and `library(rosenbrock)`, then you would need to use `rosenbrock::objective()`. The reason is that the function is not yet exported.

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```
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If you want to just export everything, you can remove this file and recreate it with this content:

```
exportPattern("^[:alpha:]]+")
```

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Go ahead and place this before your `objective()` definition. Then run `devtools::document()` to roxygenize your package.

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export(objective)
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Reinstall the package and see if you can call `objective()` after loading it.

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```
usethis::use_testthat()
```

This creates some new files and directories:

```
rosenbrock/
├── tests/
│   ├── testthat/
│   │   ├── test-<some_fun>.R ..... Your test file for some_fun()
│   └── testthat.R
```

## A First Simple Test

For the Rosenbrock function,  $f^* = f(a, a^2) = f(1, 1) = 0$ . Let's make sure this is the case for us too!



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To create a test, we can use `usethis::use_test()`.

Call `use_test("objective")`<sup>2</sup> and insert this:

```
test_that("multiplication works", {  
  # add a test using expect_equal()  
})
```

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## Check That Everything Works

Run `devtools::test()`, and hopefully see:

```
[ FAIL 0 | WARN 0 | SKIP 0 | PASS 1 ]
```

---

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**NOTE** Typically small issues with your package

Now run `devtools::check()`. Is there a problem? Yes, let's fix it!

# Metadata

The metadata for your package lives in DESCRIPTION. Right now it looks like this:

```
Package: rosenbrock
Title: What the Package Does (One Line, Title Case)
Version: 0.0.0.9000
Authors@R:
  person("First", "Last", , "first.last@example.com", role =
    c("aut", "cre"),
    comment = c(ORCID = "YOUR-ORCID-ID"))
Description: What the package does (one paragraph).
License: `use_mit_license()`, `use_gpl3_license()` or friends
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Roxygen: list(markdown = TRUE)
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For now we'll leave most of these files alone, but let's fix one thing: the license

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```
usethis::use_mit_license()
```

This will add new files to your package: LICENSE, LICENSE.md, and modify DESCRIPTION, in which you should see:

```
License: MIT + file LICENSE
```

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One way to do so is to use numerical differentiation through the **numDeriv** package:

```
gradient <- function(x, a = 1, b = 100) {  
  numDeriv::grad(objective, x, a = a, b = b)  
}
```

Now our package depends on **numDeriv**, so we need to add it to DESCRIPTION:

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In DESCRIPTION, you should now see this:

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Imports:  
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To export, easiest is to write an R wrapper.

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Many aspects of documentation

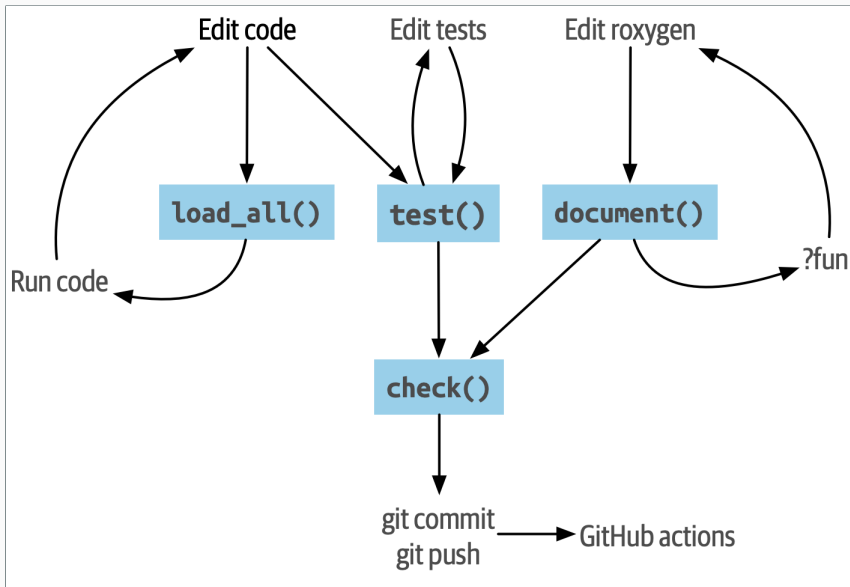
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- Manual (help files)
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Many aspects of documentation

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For the manual part, you can use **roxygen2** (it's main purpose).



**Figure 3:** The whole game

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Write a gradient descent (or stochastic gradient descent) that minimizes the rosenbrock function.



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Export everything and document the package.

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## Oral Examination Prep

---

Remember the five points:

- How can you test that your implementation is correct?
- Can you implement alternative solutions?
- Can the code be restructured e.g. by modularization, abstraction or object oriented programming to improve generality, extendability and readability?
- How does the implementation perform (benchmarking)?
- Where are the bottlenecks (profiling), and what can you do about them?



## Course Summary

---

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## Computational Topics

- Debugging
- Profiling
- Benchmarking
- Debugging
- Writing performant code