

# Experiment 1.5

## AIM

To minimize a given DFA

## ALGORITHM

1. Start
2. Create a DFA Data Structure that represents the input characters as numbers between 0 to  $m-1$  and the states as 0 to  $n-1$  where  $n$  and  $m$  are the number of states and input characters respectively.
3. Read the DFA as follows:
  1. The first line contains number of states  $n$ , number of final states  $f$ , and number of input characters  $m$ .
  2. The next line contains  $f$  space separated numbers representing the final states.
  3. Next line contains a single string denoting the input characters.
  4. Next  $n$  lines contain  $m$  space separated integers representing the  $n*m$  transition table of the DFA.
4. Create a 2D boolean  $n*n$  grid to mark distinguishable state pairs.
5. For each pair of states  $(i,j)$  set  $\text{grid}[i][j] = \text{true}$  if and only if exactly one of the two states is a final state.
6. Mark all distinguishable pairs by repeating the following till no changes are made:
  1. For each pair  $(i,j)$  where  $i > j$  and  $\text{grid}[i][j]$  is false (i.e they haven't been marked as distinguishable), do the following:
    1. For each input symbol  $c$ :
      1. Let  $x, y$  be the transition state for  $i$  and  $j$  respectively for the given character  $c$ .
      2. If  $\text{grid}[x][y]$  is true, set  $\text{grid}[i][j] = \text{grid}[j][i] = \text{true}$  and mark that a change has been made.
7. Initialize a Disjoint Set Union structure  $d$  for all states.
8. For each pair  $(i,j)$  where  $i > j$  and  $\text{grid}[i][j]$  is false, merge the states  $i$  and  $j$  in  $d$
9. Based on the DSU, create a DFA where each state represents a set in the DFA.

10. For each transition from  $x$  to  $y$  with character  $c$  in the original DFA, add transition from the state corresponding to the sets containing  $x$  and  $y$  in the new DFA
11. Display the new DFA
12. Stop

## RESULT

Successfully minimized given DFA.