```
from __future__ import absolute_import
from autograd.core import primitive, Node, getval, zeros_like, cast
from six.moves import zip
import six
class TupleNode(Node):
    __slots__ = []
    def __getitem__(self, idx):
         return tuple take(self, idx)
    def __len__(self):
         return len(self.value)
    @staticmethod
    def zeros_like(value):
         return tuple([zeros_like(item) for item in getval(value)])
    @staticmethod
    def sum outgrads(outgrads):
          return primitive sum tuples(*outgrads)
Node.type_mappings[tuple] = TupleNode
@primitive
def primitive_sum_tuples(*tuples):
    return tuple([primitive_sum(elements) for elements in zip(*tuples)])
primitive_sum_tuples.gradmaker = lambda *args : lambda g : g
@primitive
def tuple_take(A, idx):
    return A[idx]
def make_grad_tuple_take(ans, A, idx):
    return lambda g: tuple_untake(g, idx, A)
tuple_take.defgrad(make_grad_tuple_take)
@primitive
def tuple_untake(x, idx, template):
    result = list(zeros_like(template))
    result[idx] = x
    return tuple(result)
tuple untake.defgrad(lambda ans, x, idx, template : lambda g : tuple take(g, idx))
```

```
tuple_untake.defgrad_is_zero(argnums=(1, 2))
class ListNode(Node):
     __slots__ = []
     def __getitem__(self, idx):
          return list_take(self, idx)
     def __len__(self):
          return len(self.value)
     @staticmethod
     def zeros_like(value):
          return [zeros_like(item) for item in getval(value)]
     @staticmethod
     def sum outgrads(outgrads):
          return primitive_sum_lists(*outgrads)
     @staticmethod
     def cast(value, example):
          return cast(value, cast_to_list)
def cast_to_list(x):
     return list(x)
Node.type_mappings[list] = ListNode
@primitive
def primitive_sum_lists(*lists):
     return [primitive_sum(elements) for elements in zip(*lists)]
primitive_sum_lists.gradmaker = lambda *args : lambda g : g
@primitive
def list_take(A, idx):
     return A[idx]
def make_grad_list_take(ans, A, idx):
     return lambda g: list_untake(g, idx, A)
list_take.defgrad(make_grad_list_take)
@primitive
def list untake(x, idx, template):
```

```
result = list(zeros_like(template))
     result[idx] = x
     return result
list_untake.defgrad(lambda ans, x, idx, template : lambda g : list_take(g, idx))
list_untake.defgrad_is_zero(argnums=(1, 2))
class DictNode(Node):
     __slots__ = []
     def getitem (self, idx):
          return dict_take(self, idx)
     def __len__(self):
          return len(self.value)
     def __iter__(self):
          return self.value.__iter__()
     @staticmethod
     def zeros_like(self):
          return {k : zeros like(v) for k, v in six.iteritems(getval(self))}
     @staticmethod
     def sum_outgrads(outgrads):
          return primitive_sum_dicts(*outgrads)
     @staticmethod
     def cast(value, example):
          return cast(value, cast_to_dict)
def cast_to_dict(x):
     return dict(x)
Node.type_mappings[dict] = DictNode
@primitive
def primitive_sum_dicts(*dicts):
     """Takes a list of dicts having identical keys.
        Returns a new dict whose values are the sum over all input dicts."""
     # assert set(dicts[0]) == set(dicts[0]).intersection(*dicts)
     keys = dicts[0]
     return {k : primitive sum([dict[k] for dict in dicts]) for k in keys}
primitive_sum_dicts.gradmaker = lambda *args : lambda g : g
```

```
@primitive
def dict_take(A, idx):
     return A[idx]
def make_grad_dict_take(ans, A, idx):
     return lambda g : dict_untake(g, idx, A)
dict_take.defgrad(make_grad_dict_take)
@primitive
def dict untake(x, idx, template):
     result = dict(zeros_like(template))
     result[idx] = x
     return result
dict_untake.defgrad(lambda ans, x, idx, template : lambda g : dict_take(g, idx))
dict_untake.defgrad_is_zero(argnums=(1, 2))
primitive_summers = {
     list: primitive_sum_lists,
     tuple: primitive_sum_tuples,
     dict: primitive_sum_dicts,
}
def primitive_sum(container):
    thetype = type(container[0])
     if thetype in primitive_summers:
          return primitive_summers[thetype](*container)
     return sum(container[1:], container[0])
```