Last name		
First name		

LARSON—OPER 731—CLASSROOM WORKSHEET 13 Dimension, Faces, Facets and Minkowski's Theorem

Dimension

1. What is the definition of the dimension of a polytope?

2. Argue that the dimension of a polytope $\mathcal{P} \subset \mathbb{R}^2$ is no more than 2.

3. Find the dimension of the polytope defined by the linear inequalities $(x \in \mathbb{R})$:

$$3x_1 + x_2 \le 3$$

$$x_1 + 3x_2 \le 3$$

$$x_i \ge 0$$
.

4. Find the dimension of the polytope which is the convex hull of $X = \{ \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \}$.

Faces & Facets

5. What is a *face* of a polytope?

6. Find any faces in the polytope defined by the linear inequalities $(x \in \mathbb{R})$

$$3x_1 + x_2 \le 3$$

$$x_1 + 3x_2 \le 3$$

$$x_i \ge 0$$
.

7. What is a *facet* of a polytope?

8. Find any facets in the polytope defined by the linear inequalities $(x \in \mathbb{R})$

$$3x_1 + x_2 \le 3$$

$$x_1 + 3x_2 \le 3$$

$$x_i \ge 0$$
.

9. What is Minkowski's Theorem?