

Last name \_\_\_\_\_

First name \_\_\_\_\_

LARSON—MATH 310—CLASSROOM WORKSHEET 02  
Linear Spaces (Vector Spaces).

From Chp. 2 of Tsukada, et al., Linear Algebra with Python

**Review:**  $\mathbb{R}$ , *field*, *complex numbers*.

1. What is  $\mathbb{R}^2$ ?
2. How can we interpret the *vectors* in  $\mathbb{R}^2$  geometrically?
3. Explain addition in  $\mathbb{R}^2$  algebraically, and then geometrically.
4. Explain scalar multiplication in  $\mathbb{R}^2$  algebraically, and then geometrically.
5. What is a *linear space* (or *vector space*) over a field  $\mathbb{K}$ ?

6. Argue that  $\mathbb{R}^2$  is a vector space.
7. What is  $\mathbb{K}^n$ ?
8. Argue that  $\mathbb{K}^n$  is a vector space.
9. What is a *subspace* of a vector space?
10. What is an example?
11. What is a *linear map*  $f : V \rightarrow W$ , from linear space  $V$  to linear space  $W$ ?
12. What is an example?