

Last name \_\_\_\_\_

First name \_\_\_\_\_

**LARSON—MATH 255—CLASSROOM WORKSHEET 03**  
**Getting Started.**

1. Create a Cocalc/Sage Cloud account.
  - (a) Start the Chrome browser.
  - (b) Go to `http://cocalc.com`
  - (c) “Create new account” using **your VCU email address** .
  - (d) You should see an existing Project for our class. Click on that.
  - (e) Click “New”, then “Sage Worksheet”, then call it **c03**.
  - (f) For each problem number, label it in the SAGE cell where the work is. So for Problem 1, the first line of the cell should be **#Problem 1**.

**Review**

- The multiplication operator in SAGE is “\*”. The most common error in SAGE is forgetting to put in a “\*” when multiplying.
- produces *exact* answers. You often have to *force* SAGE to give you a decimal approximation of what you’ve calculated.
- log in SAGE is the *natural log* (it *is* possible to compute logs in *any* base though).
- Angles in SAGE are assumed to be in radians (angles in degrees must be converted to radian measure).

**New**

`plot` is SAGE’s powerful and flexible command for plotting functions of a single variable.

2. Sketch the graph of  $x^3$  on the interval  $(-2, 2)$ .
3. Sketch the graph of  $|x - 1|$  on a “nice” interval.
4. Sketch  $\cos x$ .
5. Sketch  $\cos t$ . What happens? What do you think the difference is?
6. Sketch  $\cos x$  on the interval  $(-2\pi, 2\pi)$ .
7. Sketch  $x^3 - x$  with  $y$ -range between  $y = -6$  and  $y = 6$ .

8. Sketch  $x^2$  and  $x^4$  on the interval  $(-2, 2)$ .
9. Define a function  $f(x) = x^3 - x$  by evaluating `f(x)=x**3-x`. Then find  $f(1)$ ,  $f(100)$ . Evaluate `plot(f,-2,2)` and `plot(f(x),-2,2)` and `plot(f)`.
10. Define a constant  $c = \frac{27}{14}$  by evaluating `c=27/14`. Find  $f(c)$ .
11. Define a new variable “ $y$ ” by evaluating `var("y")`. Now sketch  $g(x, y) = x^2 + y^2 - 2$  for  $-1 \leq x \leq 1$  and  $-1 \leq y \leq 1$  by evaluating `g(x,y)=x**2+y**2-2` and then `plot3d(g(x,y), (x,-1,1), (y,-1,1))`.
12. Solve  $x^2 - 1 = 0$  by evaluating `solve(x**2-1,x)`.
13. Solve  $x^2 + 1 = 0$ .
14. Solve  $x^2 + x = 25$ .
15. Find all solutions of  $\sin \theta = \frac{1}{2}$  by hand. Now evaluate `solve(sin(x)-.5,x)`. Explain SAGE’s result.
16. Define variables  $a$ ,  $b$  and  $c$ . One way to do this is with the command `var("a b c")`. Solve  $ax^2 + bx + c = 0$  by evaluating `solve(a*x**2+b*x+c, x)`.
17. Draw the graphs of the following equations by hand. Find the solutions by hand.

$$\begin{cases} x^2 + y^2 = 4 \\ y = x + 1 \end{cases}$$

Now use `solve()` to find the intersection points of the graphs of this system of equations. First use the Help by typing `help(solve)`.

### Getting your classwork recorded

When you are done, before you leave class...

- (a) Click the “Make pdf” (Adobe symbol) icon and make a pdf of this worksheet. (If CoCalc hangs, click the printer icon, then “Open”, then print or make a pdf using your browser).
- (b) Send me an email with an informative header like “Math 255 - c03 worksheet attached” (so that it will be properly recorded).
- (c) Remember to attach today’s classroom worksheet!