Last name	
First name	

LARSON—MATH 601—CLASSROOM WORKSHEET 01 Review.

Concepts & Notation

- (Sec. 1.1) field F, subfield.
- (Sec. 1.2) homogenous system of linear equations, linear combination of equations, equivalent systems of linear equations.
- (Sec. 1.3) matrix of coefficients of a system of linear equations, matrix over the field F, elementary row operations on a matrix, row-equivalent matrices, row-reduced matrix, identity matrix I, Kronecker delta δ .

Problems

1. Show that the complex numbers \mathbb{C} are a field.

2. Give an example of a linear combination of the following system of equations:

- 3. Explain why any solution of the original system must be a solution to your linear combination.
- 4. What are the three elementary row operations? Why will each of them produce a system of equations that is equivalent to the original system?

5. Write this (homogeneous) system (over \mathbb{Q}) in matrix form, use the 3 row operations to find an equivalent system of equations in *row-reduced* form. Describe the solutions.

6. Write this (non-homogeneous) system in matrix form, use the 3 row operations to find an equivalent system of equations in *row-reduced* form, and find any condition on the y's that are required for any solution.

$$\begin{array}{cccccccc} x_1 & -2x_2 & +x_3 & = & y_1 \\ 2x_1 & +x_2 & +x_3 & = & y_2 \\ & +5x_2 & -x_3 & = & y_3 \end{array}$$