

Last name \_\_\_\_\_

First name \_\_\_\_\_

**LARSON—MATH 601—CLASSROOM WORKSHEET 01**  
**Review.**

**Concepts & Notation**

- (Chp. 1) *field*  $\mathbb{F}$ , *list*, *vector space*,  $\mathbb{F}^n$ ,  $\mathbb{F}^S$ ,  $\mathbb{F}^\infty$ , *subspace*, sums of subspaces, *direct sum*.
- (Chp. 2) *linear combination*, *span*, *finite-dimensional* vector space, *linear independence*.

1. What is a field  $\mathbb{F}$ ?
2. What is a *vector space*?
3. What is  $\mathbb{F}^S$ , for a set  $S$ ?
4. What is  $\mathbb{F}^\infty$ ?
5. What is a *subspace* of a vector space  $V$ ?
6. What is  $U_1 + \dots + U_m$  for subspaces  $U_1, \dots, U_m$  of  $V$ ?
7. When is  $U_1 + \dots + U_m$  a *direct sum*? What is the notation?

8. What is a *linear combination* of vectors  $v_1, \dots, v_m$  (over a field  $\mathbb{F}$ )?
9. What is the *span* of vectors  $v_1, \dots, v_m$  (over a field  $\mathbb{F}$ )?
10. (**Claim**). The span of vectors  $v_1, \dots, v_m$  in  $V$  is a subspace of  $V$ ?
11. When is a vector space  $V$  *finite-dimensional*?
12. What is a *polynomial* function  $p : \mathbb{F} \rightarrow \mathbb{F}$ ?
13. What is  $\mathcal{P}(\mathbb{F})$ ?
14. What is a *linearly independent* list of vectors?
15. What is a *linearly dependent* list of vectors?
16. (**Linear Dependence Lemma**) If  $v_1, \dots, v_m$  in  $V$  are linearly dependent, then:
- (a)  $\exists j \in \{1, \dots, m\} \ v_j \in \text{span}(v_1, \dots, v_{j-1})$ .
  - (b)  $\text{span}(v_1, \dots, v_m) = \text{span}(v_1, \dots, \hat{v}_j, \dots, v_m)$ .