

Last name \_\_\_\_\_

First name \_\_\_\_\_

**LARSON—MATH 310—HOMEWORK WORKSHEET 05**  
**Vector Spaces.**

**General Instructions**

1. Write up a **neat** assignment on a **new sheet** of paper. (Do not cram your answers between the lines).
2. **Number** your problems so that it is easy to see what work matches the assigned problems.
3. Remember to **give examples** (you do not understand a concept unless you can provide an example of it).

**Definitions and Examples**

1. What is a *linear combination*? Give a definition and an example.
2. What is the *span* of vectors? Give a definition and an example.
3. What are *standard generators*? Give a definition and an example.
4. What is a *homogeneous linear equation*? Give a definition and an example.
5. What is a *homogeneous linear system*? Give a definition and an example.
6. What is a *vector space*? Give a definition and an example.
7. What is a *subspace*? Give a definition and an example.

**Problems**

8. Let  $a, b$  be real numbers. Consider the equation  $z = ax + by$ . Show that there are two 3-vectors  $\hat{v}_1, \hat{v}_2$  such that the set of points  $[x, y, z]$  satisfying the equation is exactly the set of linear combinations of  $\hat{v}_1$  and  $\hat{v}_2$ .  
(Hint: Specify the vectors using formulas involving  $a, b$ .)
9. Let  $a, b, c$  be real numbers. Consider the equation  $z = ax + by + c$ . Show that there are three 3-vectors  $\hat{v}_0, \hat{v}_1, \hat{v}_2$  such that the set of points  $[x, y, z]$  satisfying the equation is exactly  $\{\hat{v}_0 + \alpha_1\hat{v}_1 + \alpha_2\hat{v}_2 : \alpha_1, \alpha_2 \in \mathbb{R}\}$ .  
(Hint: Specify the vectors using formulas involving  $a, b, c$ .)