Last name		
First name		

LARSON—OPER 731—CLASSROOM WORKSHEET 10 Complementary Slackness, Basic Solutions and Vertices

1.	What does it mean	for a feasible so	lution x of the	primal LP P	and a feasible so	lution
	y of the dual LP D	to be <i>complem</i>	entary? What	's an example	e?	

2. What is the Weak Complementary Slackness Theorem?

3. What is the Strong Complementary Slackness Theorem?

The Simplex Method, Dictionaries, Basic Solutions, and Vertices

The ideas from 0.4 that I will try to illustrate with examples are:

- (a) A system of inequalities can be extended to a system of equations with (non-negative) slack variables and the feasible points in the first are in one-to-one correspondence with the solutions of the other.
- (b) Each basic feasible solution (algebra) in the simplex method corresponds to an extreme point (geometry).
- (c) The columns corresponding to the basic variables are linearly independent and the matrix formed from these columns is invertible (and a solution of the system of equations can be found by setting the non-basic variables to 0, and inverting this matrix).

4.	Use	slack	variables	and	the	Simplex	Method	to	${\rm maximize}$	the	following	LP.	Keep
track of the basic variables and resulting extreme points along the way.													

$$z = x_1 + x_2$$

Subject to:

$$x_1 + x_2 \le 1$$

$$x_i \ge 0$$
.

5. Check that one each iteration of the Simplex Method that the columns corresponding to the basic variables are linearly independent.

6. Use slack variables and the Simplex Method to maximize the following LP. Keep track of the basic variables and resulting extreme points along the way.

$$z = x_1 + x_2$$

Subject to:

$$3x_1 + x_2 \le 3$$

$$-x_1 + 3x_2 \le 3$$

$$x_i \ge 0$$
.

7. Check that one each iteration of the Simplex Method that the columns corresponding to the basic variables are linearly independent.