Unit 4: Inference for numerical data

1. Decision errors, significance levels, sample size & power

Sta 104 - Summer 2015

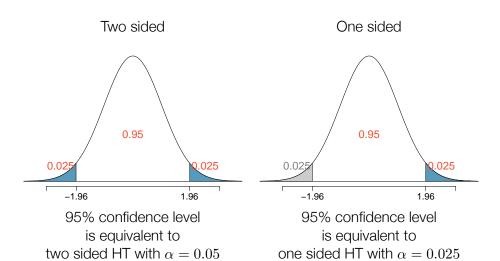
Duke University, Department of Statistical Science

June 1, 2015

Dr. Çetinkaya-Rundel

Slides posted at http://bit.ly/sta104su15

1. Hypothesis tests and confidence intervals at equivalent significance/confidence levels should agree



- ▶ PS3 due tonight
- ▶ Project proposals due Thursday night
- ► MT corrections extra credit: Work **as a team** to write up a collective exam corrections document that discusses all questions missed by any member of the team. Your corrections should show full work and explain reasoning, even for the multiple choice questions. Due by the end of the day on Wednesday, June 3. **Extra credit:** +2 points on the exam.

3

Clicker question

What is the significance level of a two-sided hypothesis test that is equivalent to a 90% confidence interval? *Hint: Draw a picture and mark the confidence level in the center.*

- (a) 0.001
- (b) 0.01
- (c) 0.025
- (d) 0.05
- (e) 0.10

2

Clicker question

What is the significance level of a one-sided hypothesis test that is equivalent to a 90% confidence interval? *Hint: Draw a picture and mark the confidence level in the center.*

- (a) 0.001
- (b) 0.01
- (c) 0.025
- (d) 0.05
- (e) 0.10

Clicker question

What is the confidence level of a confidence interval that is equivalent to a two-sided hypothesis test with $\alpha=0.01$. Hint: Draw a picture and mark the confidence level in the center.

- (a) 0.80
- (b) 0.90
- (c) 0.95
- (d) 0.98
- (e) 0.99

4

5

Clicker question

What is the confidence level of a confidence interval that is equivalent to a one-sided hypothesis test with $\alpha=0.01$. Hint: Draw a picture and mark the confidence level in the center.

- (a) 0.80
- (b) 0.90
- (c) 0.95
- (d) 0.98
- **(e)** 0.99

Clicker question

A 95% confidence interval for the average normal body temperature of humans is found to be (98.1 F, 98.4 F). Which of the following is true?

- (a) The hypothesis $H_0: \mu=98.2$ would be rejected at $\alpha=0.05$ in favor of $H_A: \mu\neq 98.2$.
- (b) The hypothesis $H_0: \mu=98.2$ would be rejected at $\alpha=0.025$ in favor of $H_A: \mu>98.2$.
- (c) The hypothesis H_0 : $\mu=98$ would be rejected using a 90% confidence interval.
- (d) The hypothesis H_0 : $\mu=98.2$ would be rejected using a 99% confidence interval.

6

2. Results that are statistically significant are not necessarily practically significant

3. Calculate the sample size a priori to achieve desired margin of error

Clicker question

All else held equal, will p-value be lower if n = 100 or n = 10,000?

- (a) n = 100
- (b) n = 10,000

Application exercise: 4.1 Sample siz

See course website for details.

8

4. Hypothesis tests are prone to decision errors

Decision

- ▶ A *Type 1 Error* is rejecting the null hypothesis when H_0 is true: α
 - For those cases where H_0 is actually true, we do not want to incorrectly reject it more than 5% of those times
 - Increasing α increases the Type 1 error rate, hence we prefer to small values of α
- ▶ A *Type 2 Error* is failing to reject the null hypothesis when H_A is true: β
- ▶ *Power* is the probability of correctly rejecting H_0 , and hence the complement of the probability of a Type 2 Error: 1β

5. Power depends on the n, a, α , effect size

Power can be increased (and hence Type 2 error rate can be decreased) by

- ▶ increasing the sample size
- ▶ decreasing the standard deviation of the sample (difficult to ensure but cautious measurement process and limiting the population so that it is more homogenous may help)
- ightharpoonup increasing α
- ► increasing the *effect size*

9

10

- 1. Hypothesis tests and confidence intervals at equivalent significance/confidence levels should agree
- 2. Results that are statistically significant are not necessarily practically significant
- 3. Calculate the sample size a priori to achieve desired margin of error
- 4. Hypothesis tests are prone to decision errors
- 5. Power depends on the effect size, α , n, and s