

## LECTURE: 3-2 THE PRODUCT AND QUOTIENT RULES [PART 1]

**Example 1:** How do we find the derivative of a product? Is it true that  $(fg)' = f'g'$ ? Why or why not?

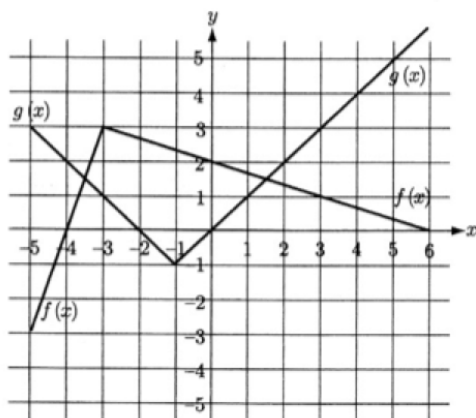
**The Product Rule:** If  $f$  and  $g$  are differentiable then,

$$\frac{d}{dx}[f(x)g(x)] = f(x)\frac{d}{dx}[g(x)] + g(x)\frac{d}{dx}[f(x)]$$

**Proof of why this is true:**

**Example 2:** If  $f(x) = xe^x$  find  $f'(x)$ . Then find the second and third derivatives to find a formula for the  $n$ th derivative  $f^{(n)}(x)$ .

**Example 3:** If  $h(x) = f(x)g(x)$  as shown below, find  $h'(3)$ .



**The Quotient Rule** If  $f$  and  $g$  are differentiable, then

$$\frac{d}{dx} \left[ \frac{f(x)}{g(x)} \right] = \frac{g(x) \frac{d}{dx} [f(x)] - f(x) \frac{d}{dx} [g(x)]}{[g(x)]^2}$$

**Example 4:** Find  $y'$  when  $y = \frac{x^2 + x - 2}{x^3 + 6}$

**Example 5:** Suppose that  $f(5) = 1$ ,  $f'(5) = 6$ ,  $g(5) = -3$  and  $g'(5) = 2$ . Find the following values.

(a)  $(f - g)'(5)$

(b)  $(fg)'(5)$

(c)  $(g/f)'(5)$

**Note:** Don't use the product or quotient rule unless you have to. Here are a few examples where you can use the product or quotient rules, but it's easier not to!

**Example 6:** Find the derivative of the following functions.

(a)  $f(t) = \sqrt{t}(2t + 5)$

(b)  $y = \frac{t^3 + t + 5}{t^4}$

**Example 7:** Find the derivatives of the following functions

(a)  $f(z) = (z^2 - \sqrt{z})(z^2 + \sqrt{z})$

(b)  $y = \frac{\sqrt{x} - 1}{\sqrt{x} + 1}$