

**Math 251 Fall 2017**

**Quiz #6, October 18th**

**Name:** \_\_\_\_\_

There are 25 points possible on this quiz. This is a closed book quiz. Calculators and notes are not allowed. **Please show all of your work!** If you have any questions, please raise your hand.

*Exercise 1.* (4 pts.) Find  $\frac{dy}{dx}$  by implicit differentiation for  $\sin y = x^3 - y$ .

*Exercise 2.* (6 pts.) Find the derivatives of the following functions.

(a)  $f(x) = x \arcsin(3x)$

(b)  $g(x) = \arctan(\sqrt{x})$

*Exercise 3.* (3 pts.) Find the derivative of the function  $g(x) = \sqrt{\ln x}$ .

*Exercise 4.* (4 pts.) Use logarithmic differentiation to find the derivative of the function

$$y = (\cos x)^{3x}.$$

*Exercise 5.* (8 pts.) The position function of a particle is given by  $s = \frac{1}{3}t^3 - 4t^2 + 7t$  where  $t$  is measured in seconds and  $s$  in meters. Further, assume the first and second derivatives are  $s'(t) = t^2 - 8t + 7$  and  $s''(t) = 2t - 8$ .

- a.) What is the velocity function of the particle?
  
  
  
  
  
- b.) What is the acceleration function of the particle?
  
  
  
  
  
- c.) When is the particle at rest?
  
  
  
  
  
- d.) When is the particle moving to the right?
  
  
  
  
  
- e.) At time  $t = 5$ , is the particle speeding up or slowing down? Explain your answer.