

Regras Indutivas Adicionadas

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If then sem else:

$$IfNoElse_1 \frac{\langle b, s \rangle \xrightarrow{b} \langle b', s' \rangle}{\langle \text{if } b \text{ then } c_1, s \rangle \xrightarrow{c} \langle \text{if } b' \text{ then } c_1, s' \rangle}$$

$$IfNoElse_2 \frac{}{\langle \text{if true then } c_1, s \rangle \xrightarrow{c} \langle c_1, s \rangle}$$

$$IfNoElse_3 \frac{}{\langle \text{if false then } c_1, s \rangle \xrightarrow{c} \langle \text{skip}, s \rangle}$$

Multiplicação:

$$Multiplicacao_1 \frac{\langle a_1, s \rangle \xrightarrow{a} \langle a_1', s' \rangle}{\langle a_1 \times a_2, s \rangle \xrightarrow{a} \langle a_1' \times a_2, s' \rangle}$$

$$Multiplicacao_2 \frac{\langle a_2, s \rangle \xrightarrow{a} \langle a_2', s' \rangle}{\langle nu \times a_2, s \rangle \xrightarrow{c} \langle nu \times a_2', s' \rangle}$$

$$Multiplicacao_3 \frac{}{\langle num_1 \times num_2, s \rangle \xrightarrow{a} \langle num, s \rangle} \text{com } num = num_1 * num_2$$

Subtração:

$$Subtracao_1 \frac{\langle a_1, s \rangle \xrightarrow{a} \langle a_1', s' \rangle}{\langle a_1 - a_2, s \rangle \xrightarrow{a} \langle a_1' - a_2, s' \rangle}$$

$$Subtracao_2 \frac{\langle a_2, s \rangle \xrightarrow{a} \langle a_2', s' \rangle}{\langle nu - a_2, s \rangle \xrightarrow{c} \langle nu - a_2', s' \rangle}$$

$$Subtracao_3 \frac{}{\langle num_1 - num_2, s \rangle \xrightarrow{a} \langle num, s \rangle} \text{com } num = num_1 - num_2$$

DoWhile:

$$DoWhile \frac{}{\langle \text{Do } c \text{ while } b, s \rangle \xrightarrow{c} \langle c; \text{if } b \text{ then } (\text{Do } c \text{ while } b), \text{else skip}, s' \rangle}$$

Incremento atômico (inc x):

$$Inc \frac{}{\langle inc\ x, s \rangle \rightarrow^c \langle skip, s[x/x+1] \rangle}$$

Comando de atribuição de valor aleatório à variável (any x):

$$Any \frac{}{\langle any\ x, s \rangle \rightarrow^c \langle skip, s[x/num] \rangle}$$

And (&&):

$$And_1 \frac{\langle bl_1, s \rangle \rightarrow False}{\langle bl_1 \&\& bl_2, s \rangle \rightarrow^c \langle False, s' \rangle}$$

$$And_2 \frac{\langle bl_1, s \rangle \rightarrow True \ \langle bl_2, s \rangle \rightarrow bl_2'}{\langle bl_1 \&\& bl_2, s \rangle \rightarrow^c \langle bl_2', s' \rangle}$$

$$And_3 \frac{\langle b_1, s \rangle \rightarrow \langle b_1', s' \rangle}{\langle b_1 \&\& b_2, s \rangle \rightarrow^c \langle b_1' \&\& b_2, s' \rangle}$$

$$And_4 \frac{\langle b_2, s \rangle \rightarrow \langle b_2', s' \rangle}{\langle bl_1 \&\& b_2, s \rangle \rightarrow^c \langle bl_1 \&\& b_2', s' \rangle}$$

Or (||):

$$Or_1 \frac{\langle bl_1, s \rangle \rightarrow False \ \langle bl_2, s \rangle \rightarrow bl}{\langle bl_1 || bl_2, s \rangle \rightarrow^c \langle bl, s \rangle}$$

$$Or_2 \frac{\langle bl_1, s \rangle \rightarrow True \ \langle bl_2, s \rangle \rightarrow b}{\langle bl_1 || b_2, s \rangle \rightarrow^c \langle True, s \rangle}$$

$$Or_3 \frac{\langle b_1, s \rangle \rightarrow \langle b_1', s' \rangle}{\langle b_1 || b_2, s \rangle \rightarrow^c \langle b_1' || b_2, s' \rangle}$$

$$Or_4 \frac{\langle b_2, s \rangle \rightarrow \langle b_2', s' \rangle}{\langle bl_1 || b_2, s' \rangle \rightarrow^c \langle bl_1 || b_2', s' \rangle}$$

Maior que (>):

$$Maior_1 \frac{\langle a_1, s \rangle \rightarrow^a \langle a_1', s' \rangle}{\langle a_1 > a_2, s \rangle \rightarrow^a \langle a_1' > a_2, s' \rangle}$$

$$Maior_2 \frac{\langle a_2, s \rangle \rightarrow^a \langle a_2', s' \rangle}{\langle nu > a_2, s \rangle \rightarrow^a \langle nu > a_2', s' \rangle}$$

$$Maior_3 \frac{}{\langle nu_1 > nu_2, s \rangle \rightarrow^a \langle if\ nu_1 > nu_2\ then\ True\ else\ False, s' \rangle}$$

Menor que (<):

$$Menor_1 \frac{\langle a_1, s \rangle \rightarrow^a \langle a_1', s' \rangle}{\langle a_1 < a_2, s \rangle \rightarrow^a \langle a_1' < a_2, s' \rangle}$$

$$Menor_2 \frac{\langle a_2, s \rangle \rightarrow^a \langle a_2', s' \rangle}{\langle nu < a_2, s \rangle \rightarrow^a \langle nu < a_2', s' \rangle}$$

$$Menor_3 \frac{}{\langle nu_1 > nu_2, s \rangle \rightarrow^a \langle if\ nu < nu\ then\ True\ else\ False, s' \rangle}$$

Igual a (=):

$$Igual_1 \frac{\langle a_1, s \rangle \rightarrow^a \langle a_1', s' \rangle}{\langle a_1 = a_2, s \rangle \rightarrow^a \langle a_1' == a_2, s \rangle}$$

$$Igual_2 \frac{\langle a_2, s \rangle \rightarrow^a \langle a_2', s' \rangle}{\langle nu = a_2, s \rangle \rightarrow^a \langle nu == a_2', s \rangle}$$

$$Igual_3 \frac{}{\langle nu_1 = nu_2, s \rangle \rightarrow^a \langle \text{if } nu_1 = nu_2 \text{ then True else False}, s \rangle}$$

Exemplo:

Exemplo 1:

```
do {
  inc x
} while (x < 1)
Resultado
y = 3
x = 1
```

Exemplo 2:

```
x = 4
y = 0
if x > 3 && y == 0 {
  y = 3 * x
  inc x
}
Resultado
y = 12
x = 5
```

Exemplo 3:

```
x = 1
y = 10
do inc x
  while x < y - 5

x = 5
```

y = 10

Exemplo 4:

x = 1

y = 0

if x == 4 || y > 10 {

 y = 5

}

any x

Resultado

x = any

y = 0

Exemplo main:

do {

 x = x + 1

} while (x < 2)

Resultado

x = 3

y = 2