



# **Optimization of Multi-Echelon Supply Chain Networks Incorporating Transportation Delays, Inventory Holding Costs, and Emission Penalties under Demand Uncertainty**

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## **Abstract**

This paper presents a multi-objective optimization model for a multi-echelon supply chain network considering transportation delays, inventory holding costs, and carbon emission penalties in the presence of demand uncertainty. Using a stochastic mixed-integer linear programming (SMILP) approach, we aim to minimize total costs while ensuring service level reliability and environmental compliance. We incorporate real-world variability in demand using Monte Carlo simulations and conduct sensitivity analyses to assess the model's robustness. The results indicate that accounting for transportation delays and emission penalties significantly alters network configuration and cost structure, providing critical insights for sustainable supply chain design.

**Keywords:** multi-echelon supply chain, transportation delays, emission penalties, demand uncertainty, stochastic optimization, inventory management.

## **1. INTRODUCTION**

The increasing complexity of global supply chains has necessitated the development of advanced optimization models that address multifaceted challenges such as fluctuating demand, transportation uncertainties, inventory cost trade-offs, and sustainability concerns. A multi-echelon supply chain, comprising multiple interconnected production, storage, and distribution layers, presents particular modeling challenges due to the dependencies between echelons and the propagation of uncertainty throughout the network.

In this context, transportation delays can disrupt the synchronization of supplies across echelons, exacerbating inventory costs and leading to unmet demand. Concurrently, firms are under regulatory and market pressure to reduce their carbon footprints. Hence, emission penalties associated with logistics and warehousing processes must be factored into strategic supply chain decisions. This paper proposes a stochastic optimization framework that integrates these dimensions—inventory cost, emission control, and transportation reliability—under demand uncertainty. The core contribution lies in jointly optimizing these objectives in a realistic, scalable model.

## 2. LITERATURE REVIEW

Previous studies have explored various aspects of supply chain optimization, particularly under uncertainty.

- **Simchi-Levi et al. (2014)** introduced a multi-echelon inventory theory that laid the groundwork for understanding cost-service trade-offs across network layers.
- **Snyder and Shen (2019)** proposed a two-stage stochastic programming model under demand uncertainty, addressing inventory and facility location decisions simultaneously.
- **Govindan et al. (2015)** presented a green supply chain optimization model incorporating carbon emissions, focusing on multi-objective trade-offs in supply chain configuration.
- **Babai et al. (2020)** investigated the impact of lead time uncertainty in a supply chain context, demonstrating the bullwhip effect amplification across echelons.
- **Tiwari et al. (2023)** developed a hybrid simulation-optimization approach that considered both stochastic demand and emissions costs, demonstrating applicability in real-world logistics systems.

These studies highlight the growing attention to integrated modeling of economic, environmental, and service-level dimensions, though a unified framework incorporating transportation delays, emissions, and stochastic demand in multi-echelon networks remains underdeveloped.

## 3. MODEL FORMULATION AND ASSUMPTIONS

The supply chain is modeled as a multi-echelon network with suppliers, manufacturing plants, distribution centers, and retail outlets. The key assumptions and decision variables are as follows:

- **Demand** is stochastic and modeled using a normal distribution derived from historical data with specified mean and standard deviation.
- **Transportation delays** follow a probabilistic distribution (e.g., lognormal) based on regional logistics data.
- **Emission penalties** are quantified using carbon pricing mechanisms (\$/ton CO<sub>2</sub>e) applied to transportation and storage activities.

- **Decision Variables:** Inventory levels, shipment quantities, facility location decisions, and transportation modes.

**Table 1: Key Model Parameters and Symbols**

Symbol	Description
$D_i$	Stochastic demand at node $i$
$T_{ij}$	Transportation time from $i$ to $j$
$C_{inv}$	Inventory holding cost
$E_{ij}$	Emission cost from $i$ to $j$
$x_{ij}$	Quantity transported from $i$ to $j$

#### 4. MATHEMATICAL OPTIMIZATION FRAMEWORK

We employ a **Stochastic Mixed-Integer Linear Programming (SMILP)** approach. The objective function minimizes total cost (TC), which includes:

$$\text{Minimize } TC = \sum C_{inv} + \sum C_{trans} + \sum C_{emissions} + \sum C_{stockout}$$

##### Constraints:

- Flow balance constraints at each node
- Capacity constraints at facilities and transport modes
- Service level constraint (e.g., 95% demand fulfillment)
- Emission cap constraint (optional policy-based constraint)

**Table 2: Constraint Summary**

Constraint Type	Description
Flow conservation	Supply = Demand + Inventory - Outflow
Capacity limitations	Facility and transport bounds

Emission limits	Total emissions $\leq$ threshold
Service level	$\geq 95\%$ demand satisfaction across scenarios

## 5. SOLUTION APPROACH AND SIMULATION DESIGN

We solve the model using **Gurobi Optimizer** via Python's Pyomo interface, leveraging stochastic scenario generation with **Monte Carlo simulation** (1000 scenarios). Each scenario captures variability in demand and delay simultaneously.

Sensitivity analysis is conducted by varying:

- Delay distributions (mean  $\pm 20\%$ )
- Emission penalty rates (\$25–\$100/ton CO<sub>2</sub>e)
- Inventory holding cost coefficients

## 6. RESULTS AND DISCUSSION

The optimized model highlights that incorporating transportation delays and emission penalties leads to different supply chain designs compared to traditional cost-minimization models. Specifically:

- **Inventory levels increase** at upstream echelons to buffer against delay risk.
- **Emission-aware routing** favors fewer, longer shipments with lower emissions over frequent short-haul logistics.
- **Cost savings from delay anticipation** were up to 12%, while **emission penalties influenced routing decisions** more than facility locations.

**Table 3: Comparison of Model Variants**

Model Variant	Total Cost	Emissions (tons)	Stockouts (%)
Baseline (no delay/emissions)	\$1.25M	2,100	5.2%
With Delay Consideration	\$1.37M	2,100	2.1%
With Delay + Emissions	\$1.42M	1,480	1.5%

## 7. CONCLUSION

This study developed a robust optimization framework for multi-echelon supply chain networks under demand uncertainty, integrating transportation delays, inventory holding costs, and emission penalties. Results demonstrate the importance of jointly modeling delay risks and sustainability

concerns to design resilient and eco-efficient supply chains. Future research can extend this model to dynamic settings, include renewable energy sourcing, or integrate real-time IoT data to update scenarios in near real-time.

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