## Matemática do Ensino Médio Grupo PET-Matemática UFCG

## 6ª Lista de Exercícios UFCG/CCT/UAMat

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Aluno(a):

1. Resolva as inequações:

(a) 
$$\log_3(5x-2) < \log_3 4$$

(b) 
$$\log_{\frac{1}{2}}(3x-1) \ge \log_{\frac{1}{2}}(2x+3)$$

(c) 
$$\log_2(2x^2 - 5x) \le \log_2 3$$

(d) 
$$\log_{\frac{1}{10}}(x^2+1) < \log_{\frac{1}{10}}(2x-5)$$

(e) 
$$\log_{\frac{1}{2}}(x^2 - x - \frac{3}{4}) > 2 - \log_2 5$$

(f) 
$$2 < \log_2(3x+1) < 4$$

(g) 
$$\frac{1}{2} < \log_{\frac{1}{2}}(2x) < 1$$

(h) 
$$|\log_2 x| > 1$$

(i) 
$$|2 + \log_2 x| > 3$$

(j) 
$$|\log_3(x^2 - 1)| < 1$$

2. Resolva as inequações:

(a) 
$$3\log_3^2 x + 5\log_3 x - 2 \le 0$$

(b) 
$$\log_2^2 x < 4$$

(c) 
$$1 < \log^2 x < 3$$

(d) 
$$\log_{\frac{1}{2}}^2 - 3\log_{\frac{1}{2}}x - 4 > 0$$

(e) 
$$\log_2 x - 6\log_x 2 + 1 > 0$$

(f) 
$$\log_2 x - \log_x 8 - 2 \ge 0$$

(g) 
$$\frac{1}{\log_2 x} - \frac{1}{\log_2 x - 1} < 0$$

3. Determine os valores de a para os quais as raízes são reais:

(a) 
$$x^2 - 4x + \log_2 a = 0$$

(b) 
$$x^2 - 2x - \log_2 a = 0$$

(c) 
$$3x^2 - 6x + \log a = 0$$

(d) 
$$x^2 - x \log_3 a + 4 = 0$$

(e) 
$$x^2 - x \log_2 a + \log_2 a = 0$$

4. Resolva as inequações:

(a) 
$$\log_{x^2}(x+2) < 1$$

(b) 
$$\log_{(2x+3)} x^2 < 1$$

- (c)  $\log_{x^2}(x^2 5x + 4) < 1$
- (d)  $\log_x \left( \frac{4x+5}{6-5x} \right) < -1$
- (e)  $\log_{(3x^2+1)} 2 < \frac{1}{2}$
- (f)  $\log_x \left(\frac{x+3}{x-1}\right) > 1$
- (g)  $\log_{(x+6)}(x^2 x 2) \ge 1$
- (h)  $\log_{\sqrt{2x^2-7x+6}} \left(\frac{x}{3}\right) > 0$
- (i)  $\log_{\left(\frac{2x+5}{2}\right)} \left(\frac{x-5}{2x-3}\right)^2 > 0$