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On the Design and Evaluation of Job Scheduling Algorithms [★]

Jochen Krallmann, Uwe Schwiegelshohn, and Ramin Yahyapour

Computer Engineering Institute
University Dortmund
44221 Dortmund, Germany
<http://www-ds.e-technik.uni-dortmund.de>
{uwe,yahya}@ds.e-technik.uni-dortmund.de

Abstract. In this paper we suggest a strategy to design job scheduling systems. To this end, we first split a scheduling system into three components: Scheduling policy, objective function and scheduling algorithm. After discussing the relationship between those components we explain our strategy with the help of a simple example. The main focus of this example is the selection and the evaluation of several scheduling algorithms.

1 Introduction

Job scheduling for processors is a complex task. This is especially true for massively parallel processors (MPPs) where many users with a multitude of different jobs share a large amount of system resources. While job scheduling does not affect the results of a job, it may have a significant influence on the efficiency of the system. For instance, a good job scheduling system may reduce the number of MPP nodes that are required to process a certain amount of jobs within a given time frame or it may permit more users or jobs to use the resources of a machine. Therefore, the job scheduling system is an important part in the management of computer resources which frequently represent a significant investment for a company or institution in the case of MPPs.

Hence, the availability of a good job scheduling system is in the interest of the owner or administrator of an MPP. It is therefore not surprising that in the past new job scheduling methods have been frequently introduced by institutions which were among the first owners of MPPs like, for instance, ANL [10], CTC [11] or NASA Ames [12]. On the other hand, some machine manufacturers showed only limited interest in this issue as they frequently seem to have the opinion that “machines are not sold because of superior job schedulers”. Moreover, the design of a job scheduling system must be based on the specific environment of a parallel system as we will argue in this paper. Consequently, administrators of MPPs will remain to be involved in the design of job scheduling systems in the future. Methods or at least guidelines for the selection and evaluation of such a

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system would therefore be beneficial. It is the goal of this paper to make a first step into this direction.

We start this paper by taking a close look at job scheduling systems. For us such a system is divided into 3 components: Scheduling policy, objective function and scheduling algorithm. We discuss those components and the dependences between them. In the second part of the paper we use a simple example to describe the process of scheduling algorithm selection and evaluation. We do not believe that there is a single scheduling algorithm that suits all systems. Therefore, it is not the purpose of this example to show the superiority of any particular algorithm but to illustrate a method for the design of scheduling systems.

2 Scheduling Systems

The scheduling system of a multiprocessor receives a stream of job submission data and produces a valid schedule. We use the term ‘stream’ to indicate that submission data for different jobs need not arrive at the same time. Also the arrival of any specific data is not necessarily predictable, that is, the scheduling system may not be aware of any data arriving in the future. Therefore, the scheduling system must deal with a so called ‘on-line’ behavior.

Further, we do not specify the amount and the type of job submission data. Different scheduling systems may accept or require different sets of submission data. For us submission data comprise all data which are used to determine a schedule. However, a few different categories can be distinguished:

- **User Data:** These data may be used to determine job priorities. For instance, the jobs of some user may receive faster service at a specific location while other jobs are only accepted if sufficient resources are available.
- **Resource Requests:** These data specify the resources which are requested for a job. Often they include the number and the type of processors, the amount of memory as well as some specific hardware and software requirements. Some of these data may be estimates, like the execution time of a job, or describe a range of acceptable values, like the number of processors for a malleable job.
- **Scheduling Objectives:** These data may help the scheduling system to generate ‘good’ schedules. For instance, a user may state that she needs the result by 8am the next morning while an earlier job completion will be of no benefit to her. Other users may be willing to pay more if they obtain their results within the next hour.

Of course other submission data are possible as well. Job submission data are entered by the user and typically provided to the system when a job is submitted for execution. However, some systems may also allow reservation of resources before the actual job submission. Such a feature is especially beneficial for multisite metacomputing [17]. In addition, technical data are often required to start a job, like the name and the location of the input data files of the job.

But as these data do not affect the schedule if they are correct, we ignore them here. Finally note that the submission of erroneous or incorrect data is also possible. However, in this case a job may be immediately rejected or fail to run.

Now, we take a closer look at the schedule. A schedule is an allocation of system resources to individual jobs for certain time periods. Therefore, a schedule can be described by providing all the time instances where a change of resource allocation occurs as long as either this change is initiated by the scheduling system or the scheduling system is notified of this change. To illustrate this restriction assume a job being executed on a processor that is also busy with some operating system tasks. Here, we do not consider changes of resource allocation which are due to the context switches between OS tasks and the application. Those changes are managed by the system software without any involvement of our scheduling system.

For a schedule to be valid some restrictions of the hardware and the system software must be observed. For instance, a parallel processor system may not support gang scheduling or require that at most one application is active on a specific processor at any time. Therefore, the validity constraints of a schedule are defined by the target machine. We assume that a scheduling system does not attempt to produce an invalid schedule. However, note that the validity of a schedule is not affected by the properties of a submitted job as those properties are not guaranteed to comply with submission data. For instance, if not enough memory is requested from and assigned to a job, the job will simply fail to run. But this does not mean that the resulting schedule is invalid. Also, a schedule depends upon other influences which cannot be controlled by the scheduling system, like the sudden failure of a hardware component. Therefore, the final schedule is only available after the execution of all jobs.

Next, the scheduling system is divided into 3 parts:

1. A *scheduling policy*,
2. an *objective function* and
3. a *scheduling algorithm*.

In the rest of this section we first describe these parts separately. Then the dependences between them are discussed. Finally, we compare the evaluation of scheduling systems with the evaluation of computer architectures.

2.1 Scheduling Policy

The scheduling policy forms the top level of a scheduling system. It is defined by the owner or administrator of a machine. In general, the scheduling strategy is a collection of rules to determine the resource allocation if not enough resources are available to satisfy all requests immediately. To better illustrate our approach, we give an example:

Example 1. The department of chemistry at University A has bought a parallel computer which was financed to a large part by the drug design lab. The department establishes the following rules for the use of the machine:

1. All jobs from the drug design lab have the highest priority and must be executed as soon as possible.
2. 100 GB of secondary storage is reserved for data from the drug design lab.
3. Applications from the whole university are accepted but the labs of the chemistry department have preferred access.
4. Some computation time is sold to cooperation partners from the chemical industry in order to pay for machine maintenance and software upgrades.
5. Some computation time is also made available to the theoretical chemistry lab course during their scheduled hours.

Note that these rules are hardly detailed enough to generate a schedule. But they allow a fuzzy distinction between *good* and *bad* schedules. Also, there may be some additional general rules which are not explicitly mentioned, like ‘Complete all applications as soon as possible if this does not contradict any other rule’. Finally, some conflicts between those rules may occur and must be resolved. For instance in Example 1, some jobs from the drug design lab may compete with the theoretical chemistry lab course. Hence, in our view a good scheduling policy has the following two properties:

1. It contains rules to resolve conflicts between other rules if those conflicts may occur.
2. It can be implemented.

We believe that there is no general method to derive a scheduling policy. Also there is no need to provide a very detailed policy with clearly defined quotas. In many cases this will result in a reduction of the number of *good* schedules. For instance, it would not be helpful at this point to demand that 5% of the computation time is sold to the chemical industry in Example 1. If there are only a few jobs from the drug design lab then the department would be able to earn more money by defining a higher industry quota. Otherwise, the department must decide whether to obtain other funding for the machine maintenance or to reduce the priority of some jobs of the drug design lab. This issue will be further discussed in Section 2.4.

2.2 Objective Function

As stated in the previous section the owner of a machine will be able to determine whether any given schedule is *good* or *bad*. However, it is the goal of a scheduling system to consistently produce schedules which are as good as possible. This leads to two problems:

1. It must be demonstrated that the scheduling system will always produce *good* schedules.
2. It is necessary to provide a ranking among *good* schedules.

Problems of the first kind are addressed in theoretical computer science by the concept of competitive analysis, see [18]. Unfortunately, this approach is not applicable for our scheduling systems for the following reasons:

- Often competitive analysis cannot be successfully applied to methods which are based on very complex algorithms or which use specific input data sets.
- Competitive factors are worst case factors that frequently are not acceptable in practice. For instance, a competitive factor of 2 for the machine load of a schedule denotes that in some cases 50% of the resources are not used. On the other hand, those worst case input data typically do not occur in real installations. Frequently, this is also true if randomization is used for the analysis.

Alternatively, a scheduling system can be applied to a multitude of different streams of submission data and the resulting schedules can be evaluated. This requires a method to automatically determine the quality of a schedule. Therefore, an objective function must be defined that assigns a scalar value, the so called *schedule cost*, to each schedule. Note that this property is essential for the mechanical evaluation and ranking of a schedule. In the simplest case all *good* schedules are mapped to 0 while all *bad* schedules obtain the value 1. Most likely however, this kind of objective function will be of little help. To derive a suitable objective function an approach based on multi criteria optimization can be used, see e.g. [20]:

1. For a typical set of jobs determine the Pareto-optimal schedules based on the scheduling policy.
2. Define a partial order of these schedules.
3. Derive an objective function that generates this order.
4. Repeat this process for other sets of jobs and refine the objective function accordingly.

To illustrate Steps 1 and 2 of our approach we consider Rules 1 and 5 of Example 1. Assume that both rules are conflicting for the chosen set of job submission data. Therefore, we determine a variety of different schedules, see Fig. 1. Note that we are not biased toward any specific algorithm in this step. We are primarily interested in those schedules which are *good* with respect to at least one criterion. Therefore, at first all Pareto-optimal schedules are selected. Those schedules are indicated by bullets in Fig. 1. Next, a partial order of the Pareto-optimal schedules is obtained by applying additional conflict resolving rules or by asking the owner. In the example of Fig. 1 numbers 0, 1 and 2 have been assigned to the Pareto-optimal schedules in order to indicate the desired partial order. Here any schedule 1 is superior to any schedule 0 and inferior to any schedule 2 while the order among all schedules 1 does not matter.

The approach is based on the availability of a few typical sets of job data. Further, it is assumed that each rule of the scheduling policy are associated with single criterion functions, like Rule 4 of Example 1 with the function ‘amount of computation time allocated to jobs from the cooperation partners from industry’. If this is not the case, complex rules must be split.

Now, it is possible to compare different schedules if the same objective function and the same set of jobs is used. Further, there are a few additional aspects which are also noteworthy:

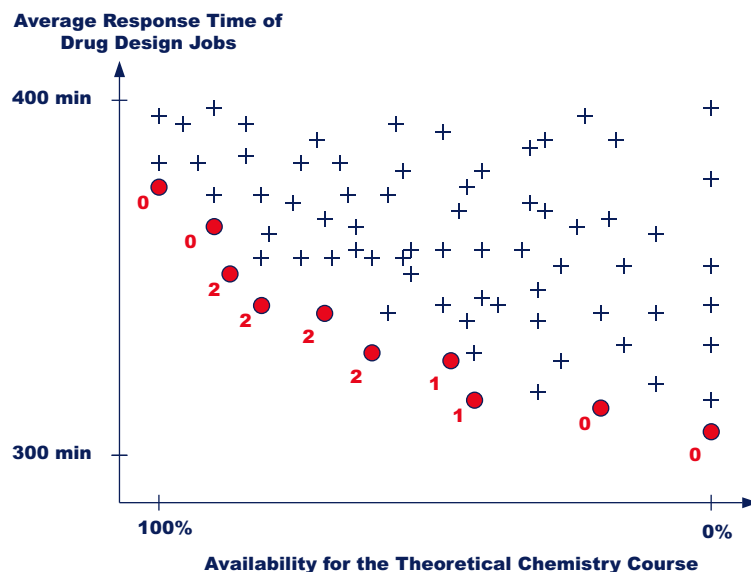


Fig. 1. Pareto Example for 2 Rules

- Schedules can be compared even if they do not have the same target architecture.
- An up front calculation of the *schedule cost* may not be possible. Most likely, it will be necessary to execute all jobs first before the correct *schedule cost* can be determined.
- No specification of job input data is given. Therefore, it is possible to compare two schedules which are based on the same set of jobs but use different job submission data.

Thus, schedules can even be used as a criterion for system selection if desired.

At many installations of large parallel machines simple objective functions are used, like the job throughput, the average job response time, the average slowdown of a job or the machine utilization, see [3]. We believe that it cannot be decided whether those objective functions are suitable in general. For some scheduling policy they may be the perfect choice while they should not be used for another set of rules. Also, it is not clear whether the use of those ‘simple’ objective functions allows an easier design of scheduling systems.

2.3 Scheduling Algorithm

The scheduling algorithm is the last component of a scheduling system. It has the task to generate a valid schedule for the actual stream of submission data in an on-line fashion. A good scheduling algorithm is expected to produce very

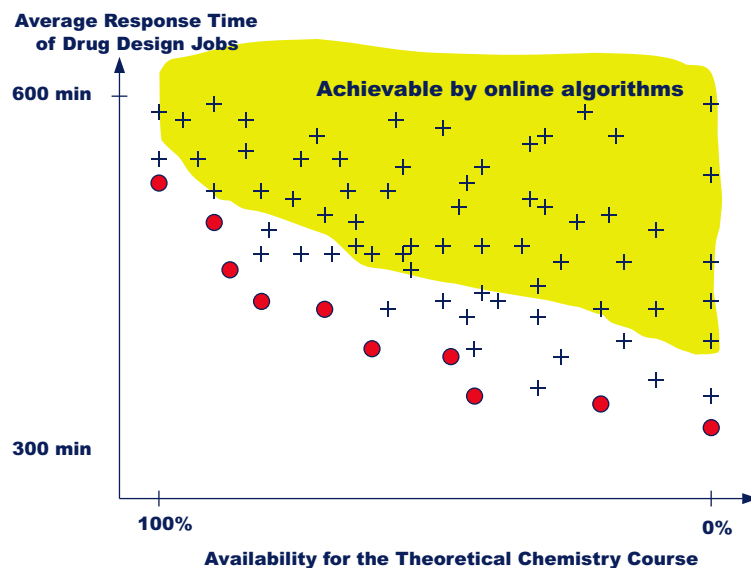


Fig. 2. On-line versus Off-line Dependence

good if not optimal schedules with respect to the objective function while not taking ‘too much’ time and ‘too many’ resources to determine the schedule.

Unfortunately, most scheduling problems are computationally very hard. This is even true for off-line problems with simple objective functions and few additional requirements, see for instance [7]. Therefore, it is not reasonable to hope in general for an algorithm that always guarantees the best possible schedule. In addition, some job data may not be immediately available or may be incorrect which makes the task for the algorithm even harder, see Section 2.

In order to obtain good schedules the administrator of a parallel machine is therefore faced with the problem to pick an appropriate algorithm among a variety of suboptimal ones. She may even decide to design an entirely new method if the available ones do not yield satisfactory results. The selection of the algorithm is highly dependent on a variety of constraints:

- Schedule restrictions given by the system, like the availability of dynamic partitioning or gang scheduling.
- System parameters, like I/O ports, node memory and processor types.
- Distribution of job parameters, like the amount of large or small jobs.
- Availability and accuracy of job information for the generation of the schedule. For instance, this may include job execution time as a function of allocated processors.
- Definition of the objective function.

Frequently, the system administrator will simply take scheduling algorithms from the literature and modify them to her needs. Then, she picks the best of her

algorithm candidates. After making sure that her algorithm of choice actually generate valid schedules, she also must decide whether it makes sense to look for a better algorithm. Therefore, it is necessary to evaluate those algorithms. We distinguish the following methods of evaluation:

1. Evaluation using algorithmic theory
2. Simulation with job data derived from
 - an actual workload
 - a workload model

In general theoretical evaluation is not well suited for our scheduling algorithms as already discussed in Section 2.2. Occasionally, this method is used to determine lower bounds for schedules. These lower bounds can provide an estimate for a potential improvement of the schedule by switching to a different algorithm. However, it is very difficult to find suitable lower bounds for complex objective functions.

Alternatively, an algorithm can be fed with a stream of job submission data. The actual schedule and its cost are determined by simulation with the help of the complete set of job data. The procedure is repeated with a large number of input data sets. The reliability of this method depends on several factors:

- Availability of correct job data
- Compliance of the used job set with the job set on the target machine

Actual workload data can be used if they are recorded on a machine with a user group such that sufficient similarity exists with the target machine and its users. This is relatively easy if traces from the target machine and the target user community are available. Otherwise some traces must be obtained from other sources, see e.g. [1]. In this case it is necessary to check whether the workload trace is suitable. This may even require some modifications of the trace.

Also note that the trace only contains job data of a specific schedule. In another schedule these job data may not be valid as is demonstrated in Examples 2 and 3:

Example 2. Assume a parallel processor that uses a single bus for communication. Here, independent jobs compete for the communication resource. Therefore, the actual performance of job i depends on the jobs executed concurrently with job i .

Example 3. Assume a machine and a scheduling system that support adaptive partitioning. In this case, the number of resources allocated to job i again depends on other jobs executed concurrently with job i .

Also, a comprehensive evaluation of an algorithm frequently requires a large amount of input data that available workload traces may not be able to provide.

If accurate workload data are not available then artificial data must be generated. To this end a workload model is used. Again conformity with future real

job data is essential and must be verified. On the other hand, this approach is able to overcome some of the problems associated with trace data simulation, if the workload model is precise enough. For a more detailed discussion of this subject, see also [3].

Unfortunately, it cannot be expected that a single scheduling algorithm will produce a better schedule than any other method for all used input data sets. In addition the resource consumption of the various algorithms may be different. Therefore, the process of picking the best suited algorithm may again require some form of multi criteria optimization.

2.4 Dependences

The main dependence stream between the components of a scheduling system is easy to see: The scheduling policy produces rules which are used to derive an objective function. The application of this objective function to a schedule yields the schedule cost which allows performance measurements for the various algorithms. However, there are also additional dependences. For instance, some policy rules may not allow efficient scheduling algorithms, see Example 4.

Example 4. Assume a machine that does not support time sharing. The scheduling policy includes the rule:

Every weekday at 10am the entire machine must be available to a theoretical chemistry class for 1 hour.

The Pareto-optimal schedules used for the determination of the objective function show an acceptable (by the owner) amount of idle resources before 10am. However, as users are not able to provide accurate execution time estimates for their jobs no scheduling algorithm can generate *good* schedules.

Such a situation is shown in Fig. 2 for Example 1. There, it is assumed that on-line algorithms cover a significantly smaller area of schedules than off-line methods with complete job knowledge. This may require a review of the conflict resolving strategy and thus affect the schedule cost. Unfortunately, this on-line area of schedules will typically be the result of a combination of several on-line algorithms. Therefore, the off-line methods in the approach of Section 2.2 cannot be simply replaced by a single or a few on-line algorithms. In addition, a suitable on-line algorithm may not be available at this time.

More of these additional dependences are listed below:

- Too many or too restrictive policy rules may prevent acceptable schedules at all.
- There may not be sufficient rules to discriminate between *good* and *bad* schedules as some implicitly assumed rules are not explicitly stated.
- While there may be a variety of different objective functions which all support the policy rules, a specific objective function may not be suitable as a criterion for an on-line scheduling algorithm.
- The workload model may not be correct if users adapt their submission pattern due to their knowledge of the policy rules.

- The workload model must be modified as the number of users and/or the types and sizes of submitted jobs change over time.

Due to these dependences a few design iterations may be required to determine the best suitable scheduling algorithms and/or it may be appropriate to repeat the design process occasionally.

2.5 Comparison

In this section we briefly compare the evaluation of scheduling systems with the well known procedure used for computer architectures. Today, computer architectures are typically evaluated with the help of standard benchmarks, like SPEC95 or Linpack, see [8]. For instance, the SPEC95 benchmark suite contains a variety of programs and frequently, no architecture is the best for all those programs. Depending on his own applications the user must select the machine best suited for him. This leads to the question whether a similar approach is also applicable for scheduling systems. With other words, can we provide a few benchmark workloads which are used to test various scheduling systems?

We claim that this cannot be done in the moment and doubt whether this will ever become possible. For computer architectures there is a standard objective function: the execution time of a certain job. As we discussed in the previous sections each scheduling system has its own objective function. Therefore, we cannot really compare two different scheduling systems. On the other hand, the comparison of different scheduling algorithms only makes sense if the same objective function is used. Hence, the evaluation of scheduling algorithms must be based on benchmarks consisting of workloads and objective functions. However, it is not clear to us that there will ever be a small set of objective functions that will more or less cover all scheduling systems.

3 Evaluation Example

In this section we give an example for the design and evaluation of scheduling algorithms. As the focus is on scheduling algorithms we will assume simple scheduling policy rules and only briefly cover the determination of the objective function. Also we use a simple machine model. Although the used constraints have been taken from real installations it is not the purpose of this paper to discuss whether they are appropriate for an installation of a parallel machine.

Example 5. Assume an Institution B that has just bought a large parallel computer with 288 identical nodes. The institution has established the following policy rules:

1. The batch partition of the computer must be as large as possible, leaving a few nodes for interactive jobs and for some services.
2. The user must provide the exact number nodes for each job (rigid job model) and an upper limit for the execution time. If the execution of a job exceeds this upper limit, the job may be cancelled.

3. The user is charged for each job. This cost is based on a combination of projected and actual resource consumption.
4. Every user is allowed at most two batch jobs on the machine at any time.
5. Between 7am and 8pm on weekdays the response time for all jobs should be as small as possible.
6. Between 8pm and 7am on weekdays and all weekend or on holidays it is the goal to achieve a high system load.

The machine supports variable partitioning [2] but does not allow time sharing. Further, it is required that all batch jobs have exclusive access to their partition.

The administrator decides that 256 nodes can be used for the batch partition. She further believes that the user community at the Cornell Theory Center (CTC) and at Institution B will be very similar. As the parallel machines at the CTC and at Institution B are of the same type she decides to use a CTC workload as a basis for the selection of the objective function and the determination of a suitable scheduling algorithm. Due to the interdependence between user community and scheduling policy this decision also requires knowledge of the scheduling policy used at the CTC, see [9]. Only if there is no major disagreement between the scheduling policies at the CTC and at Institution B the profiles of both user communities can be assumed to remain similar.

4 Determination of the Objective Function

Next, the administrator must determine an objective function. To this end she ignores Rules 1 to 4 because they do not affect the schedule for a specific workload or are only relevant to the on-line situation (Rule 2). As Rules 5 and 6 do not apply at the same time she decides to consider each rule separately.

Rule 4 indicates that all jobs should be treated equally independent of their resource consumption. Therefore, the administrator uses the **average response time** as objective function for the daytime on weekdays (Rule 5). The average response time is the sum of the differences between the completion time and submission time for each job divided by the number of jobs.

For the remaining time (Rule 6) the **sum of the idle times** for all resources in a given time frame seems to be the best choice.

The administrator intends to independently determine an appropriate scheduling algorithm for each objective function and then to address the combination of both algorithms. Note that multi criteria optimization is therefore not necessary in our simple example.

When starting to look for scheduling algorithms the administrator realizes that the sum of idle times is based on a time frame. Therefore, it does not support on-line scheduling. Using the **makespan** instead has the advantage that several theoretical results are available, see e.g. [5], but again the makespan is mainly an off-line criterion [3]. Hence, she decides to use instead the **average weighted response time** where the weight is identical to the resource consumption of a

job, that is, the product of the execution time and the number of required nodes, see [15]. It is calculated in the same fashion as the average response time with the exception that the difference between the completion and the submission time for each job is multiplied with the weight of this job. In comparison the job weight is always 1 for the average response time criterion. Note that for the average weighted response time the order of jobs does not matter if no resources are left idle [16].

5 Description of the Algorithms

After the objective function has been determined it is necessary to find a suitable scheduling algorithm. Instead of producing an algorithm from scratch it is often more efficient to use algorithms from the literature and to modify them if necessary. In this first step it is frequently beneficial to consider a wide range of algorithms unless previous experiences strongly suggest the use of a specific type of algorithm. Further, there may be algorithms which have been designed for another objective function but can be adapted to the target function.

In Example 5 the administrator picks several algorithms from the literature. These algorithms are discussed in the following subsections.

5.1 FCFS

First-Come-First-Serve (FCFS) is a well known scheduling scheme that is used in some production environments. All jobs are ordered by their submission time. Then a greedy list scheduling method is used, that is the next job in the list is started as soon as the necessary resources are available. This method has several advantages:

1. It is fair as the completion time of each job is independent of any job submitted later.
2. No knowledge about the execution time is required.
3. It is easy to implement and requires very little computational effort.

However, FCFS may produce schedules with a relatively large percentage of idle nodes especially if many highly parallel jobs are submitted. Therefore, FCFS has been replaced by FCFS with some form of **backfilling** at many locations including the CTC. Nevertheless, the administrator does not want to ignore FCFS at this time as a theoretical study has recently shown that FCFS may produce acceptable results for certain workloads [16].

5.2 Backfilling

The backfilling algorithm has been introduced by Lifka [10]. It requires knowledge of the job execution times and can be applied to any greedy list schedule. If the next job in the list cannot be started due to a lack of available resources,

then backfilling tries to find another job in the list which can use the idle resources but will not postpone the execution of the next job in the list. In other words, backfilling allows some jobs down the list to be started ahead of time.

There are 2 variants of backfilling as described by Feitelson and Weil [4]:

EASY backfill is the original method of Lifka. It has been implemented in several IBM SP2 installations. While EASY backfill will not postpone the *projected* execution of the next job in the list, it may increase the completion time of jobs further down the list, see [4].

Conservative backfill will not increase the *projected* completion time of a job submitted before the job used for backfilling. On the other hand conservative backfill requires more computational effort than EASY.

However, note that the statements regarding the completion time of skipped jobs in the list are all based on the provided execution time for each job. Backfilling may still increase the completion time of some jobs compared to FCFS as in an on-line scenario another job may release some resources earlier than assumed. In this case it is possible that a backfilled job may prevent the start of the next job in the list. For instance, while some active job is expected to run for another 2 hours it may be terminated within the next 5 minutes. Therefore, backfilling with a job having an expected execution time of 2 hours may delay the start of the next job in the list by up to 1 hour and 55 minutes.

The administrator decides to use both types of backfilling as it is not obvious that one method is better than the other.

5.3 List Scheduling (Garey and Graham)

The classical list scheduling algorithm by Garey and Graham [6] always starts the next job for which enough resources are available. Ties can be broken in an arbitrary fashion. The algorithm guarantees good theoretical bounds in some on-line scenarios (unknown job execution time) [5], it is easy to implement and requires little computational effort. As in the case of FCFS no knowledge of the job execution time is required. Application of backfilling will be of no benefit for this method.

5.4 SMART

The SMART algorithm has been introduced by Turek et al. [21]. The algorithm consists of 3 steps:

1. All jobs are assigned to bins based on their execution time. The upper bounds of those bins form a geometric sequence based on a parameter γ . In other words, the bins can be described by intervals of the possible execution time: $[0, 1], [1, \gamma^1], [\gamma^1, \gamma^2], \dots$. The parameter γ can be chosen to optimize the schedule.
2. All jobs in a bin are assigned to shelves (subschedules) such that all jobs in a shelf are started concurrently. To this end the jobs in a bin are ordered and then arranged in a shelf as long as sufficient resources are available.

3. The shelves are ordered using Smith's rule [19], that is for each shelf the sum of the weights of all jobs in the shelf is divided by the maximal execution time of any job in the shelf. Finally, those shelves with the largest ratio are scheduled first.

Schwiegelshohn et al. [14] have presented two variants of ordering the jobs in a bin and assigning them to shelves (Step 2):

SMART-*FFIA*

1. The jobs of a bin are sorted according to the product of execution time and the number of required nodes, also called *area*, such that the smallest area goes first.
2. The next job in this list is assigned to the first shelf with sufficient idle resources, that is, all shelves of this bin are considered.
3. If there is no such shelf, a new one is created and placed on top of the other shelves of this bin.

This approach is called the *First Fit Increasing Area* variant.

SMART-*NFIW*

1. All jobs of a bin are ordered by an increasing ratio of the number of required nodes to the weight of the job.
2. The next job in this list is added to the current shelf if sufficient resources are available on this shelf.
3. Otherwise a new shelf is created, placed on top of the current shelf and then becomes the current shelf itself.

This is the *Next Fit Increasing Width to Weight* variant.

The SMART algorithm has a constant worst case factor for weighted and unweighted response time scheduling. However, it is an off-line algorithm and cannot be directly applied to the scheduling problem of Example 5. It requires a priori knowledge of the execution time for all jobs and assumes that all jobs are available for scheduling at time 0. Therefore, the administrator modifies the SMART algorithm as follows:

1. She does not use the SMART algorithm to determine an actual schedule but to provide a job order for all jobs already submitted but not yet started. Whenever new jobs are submitted the SMART algorithm is started again. Based on this order a greedy list schedule is generated, see FCFS.
2. Instead of the actual execution time of a job the value provided by the user at job submission is used.

In order to reduce the number of recomputations for the SMART algorithm the schedule is recalculated when the ratio between the already scheduled jobs in the wait queue to all the jobs in this queue exceeds a certain value. In the example a ratio of $\frac{2}{3}$ is used. The parameter γ is chosen to be 2.

As the final schedule is a list schedule the administrator decides to apply backfilling here as well.

5.5 PSRS

The PSRS algorithm [13] generates preemptive schedules. It is based on the modified Smith ratio of a parallel job, that is the ratio of job weight to the product of required resources and the execution time of the job. The basic steps of PSRS are described subsequently:

1. All jobs are ordered by their modified Smith ratio (largest ratio goes first).
2. A greedy list schedule is applied for all jobs requiring at most 50% of the machine nodes. If a job needs more than half of all nodes and has been waiting for some time, then all running jobs are preempted and the parallel job is executed. After the completion of the parallel job, the execution of the preempted jobs is resumed.

Similar to SMART, PSRS is also an off-line algorithm and requires knowledge of the execution time of the jobs. In addition it needs support for time sharing. Therefore, it cannot be applied to our target machine without modification.

The off-line problems can be addressed in the same fashion as for the SMART algorithm. Further, it is necessary to transfer the preemptive schedule into a non-preemptive one. To this end, it is beneficial that a job is not executed concurrently with any other job if it causes the preemption of other jobs.

1. First, 2 geometric sequences of time instances in the preemptive schedule are defined, one for those jobs causing preemption (wide jobs) and one for all other jobs (small jobs). In both cases the factor 2 is used with different offsets. These sequences define bins.
2. All jobs are assigned to those bins according to their completion time in the preemptive schedule. Within a bin the original Smith ratio order is maintained.
3. A complete order of jobs is generated by alternatively picking bins from each sequence and starting with the small job sequence.

As with SMART the modified PSRS algorithm guarantees a constant approximation factor for the off-line case (with and without preemption).

The administrator decides to apply backfilling to PSRS schedules as well.

6 Workload

As already mentioned in Section 3 the administrator wants to base her algorithmic evaluation on workload data from the CTC. In addition she decides to use two artificial workloads:

1. Artificial workload based on probability distributions
2. Artificial workload based on randomization

The number of jobs in each workload is given in Table 1. The reasons for this selection are discussed in the following subsections.

6.1 Workload Trace

In Section 3 the administrator has already verified that a CTC workload trace would be suitable in general. She obtains a workload trace from the CTC batch partition for the months July 1996 to May 1997. The trace contains the following data for each job:

- Number of nodes allocated to the job
- Upper limit for the execution time
- Time of job submission
- Time of job start
- Time of job completion
- Additional hardware requests of the job: amount of memory, type of node, access to mass storage, type of adapter.
- Additional job data like job name, LoadLeveler class, job type, and completion status.

Those additional job data are ignored as they are of no relevance to the simulation at this point. But the administrator must address two differences between the CTC machine and the parallel computer at her institution:

1. The CTC computer has a batch partition of 430 nodes while the batch partition at Institution B contains only 256 nodes.
2. The nodes of the CTC computer are not all identical. They differ in type and memory. This is not true for the machine at Institution B.

A closer look at the CTC workload trace reveals that less than 0.2% of all jobs require more than 256 nodes. Therefore, the administrator modifies the trace by simply deleting all those highly parallel jobs. Further, she determines that most nodes of the CTC batch partition are identical (382). Therefore, she decides to ignore all additional hardware requests.

Unfortunately, these modifications will affect the accuracy of the simulation. For instance, the simulation time frame of the whole modified CTC workload will most likely exceed the time span of the original trace as less resources are available. This will result in a larger job backlog during the simulation. Therefore, it is not possible to compare the original CTC schedule with the schedules generated by simulation. On the other hand, the administrator wants to separately test for two different objective functions, each of which will typically be valid for half a day. Hence, the present approach is only suited for a first evaluation of different algorithms. Any parametric fine tuning must be done with a better workload.

Besides using the CTC workload with the job submission data described above the administrator also wants to test her algorithms under the assumption that precise job execution times are available at job submission. This simulation allows her to determine the dependence of the various algorithms on the accuracy of the provided job execution times and the potential for improvement of the schedule. For this study the estimated execution times of the trace were simply replaced by the actual execution times.

6.2 Workload with Probability Distribution

In order to overcome some of the difficulties mentioned in Section 6.1 the administrator decides to extract statistical data from the CTC workload trace. These data are then used to generate an artificial workload with the same distribution as the workload trace.

An analysis of the CTC workload trace yields that a Weibull distribution matches best the submission times of the jobs in the trace. It is difficult to find a suitable distribution for the other parameters. Therefore, bins are created for every possible requested resource number (between 1 and 256), various ranges of requested time and of actual execution length. Then probability values are calculated for each bin from the CTC trace. Randomized values are used and associated to the bins according to their probability. This generates a workload that is very similar to the CTC data set. In the first simulation mainly consistence between the results for the CTC and the artificial workload is checked. Once this consistence has been demonstrated the artificial workload can be adapted to consider the various differences between the CTC and Institution B.

6.3 Randomized Workload

Finally, totally randomized data are used as a third input data set. The administrator is aware of the fact that this workload will not represent any real workload on her machine. But she wants to determine the performance of scheduling algorithms even in case of unusual job combinations. For the workload, jobs are generated with the parameters in Table 2 being equally distributed.

Workload	Number of jobs
CTC	79,164
Probability distribution	50,000
Randomized	50,000

Table 1. Number of jobs in various workloads

Submission of jobs	≥ 1 job per hour
Requested number of nodes	1 – 256
Upper limit for the execution time	5 min – 24 h
Actual execution time	1 s – upper limit

Table 2. Parameters for randomized job generation

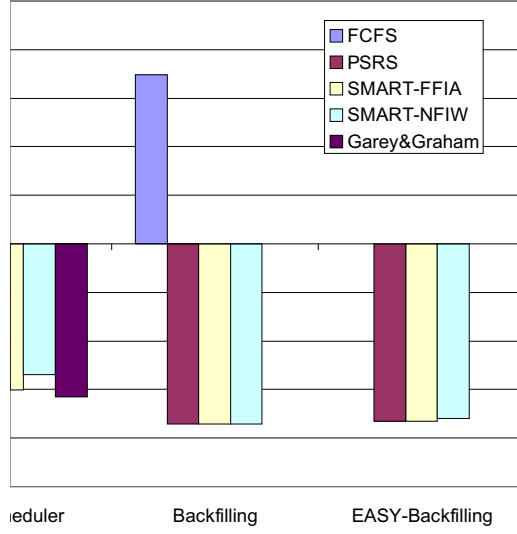


Fig. 3. Average Response Time for the Unweighted CTC-Workload

7 Evaluation Results

The administrator selects the simulation of FCFS with EASY backfilling to be a reference value as this algorithm is used by the CTC. First she compares the results for the CTC workload trace, see Fig. 3 and Table 3. For the unweighted case she comes to the following conclusions:

- All algorithms are clearly better than FCFS even if some form of backfilling is used together with FCFS.
- PSRS and SMART can be improved significantly with backfilling.
- The classical list scheduling produces good results but is inferior to the PSRS and SMART with backfilling.
- Conservative backfilling outperforms EASY backfilling when applied to PSRS and SMART schedules.
- There are little differences between PSRS and SMART schedules when backfilling is used.

The administrator does not give much weight to the absolute numbers as the workload trace has been recorded on a machine with 430 nodes while the simulations are done for a machine with 256 nodes. Although some highly parallel jobs have been removed from the trace a machine with 256 nodes will experience a larger backlog which results in a longer average response time.

In the weighted case as shown in Fig. 4, the results are different:

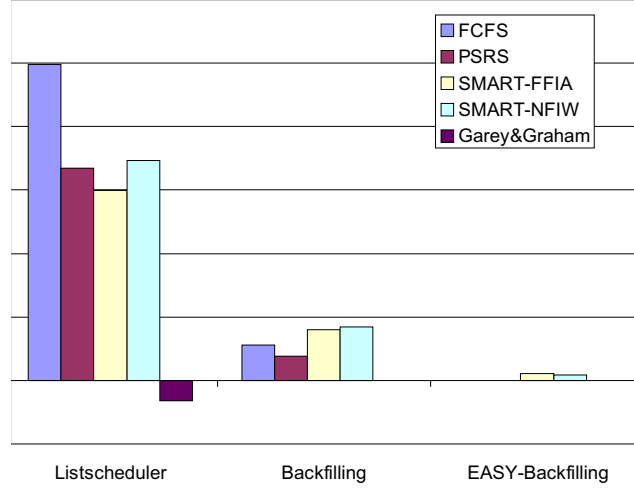


Fig. 4. Average Response Time for the Weighted CTC-Workload

- The classical list scheduling algorithms clearly outperforms all other algorithms.
- PSRS and SMART can be improved with either form of backfilling but are never better than FCFS with EASY.
- EASY is superior to conservative backfilling.
- PSRS is slightly better than either form of SMART.

The artificial workload based on probability distributions basically supports the results derived with the CTC workload, see Fig. 5 and Table 4. This seems to indicate that the larger backlog in the CTC workload does not significantly affect the simulation results. However, it is strange that the absolute values for the average response time are even larger than in the CTC workload case although the number of jobs in the same time frame is significantly less. The only difference to the CTC workload is the fact that EASY is better than conservative backfilling if combined with PSRS or SMART in the unweighted case.

The derived qualitative relationship between the various algorithms is also supported by the randomized workload, see Table 5. Therefore, the administrator need not worry if a workload will occasionally deviate from her model.

Next the administrator addresses the simulation using the CTC workload with exact job execution times, see Fig. 6 and Table 6. By comparing those results with the CTC workload simulations (Table 3) she wants to determine how much the accuracy of the job execution time estimation affects the schedules. This comparisons yields the following results:

- In the unweighted case the average response time of PSRS and SMART schedules can be improved by almost a factor of 2.

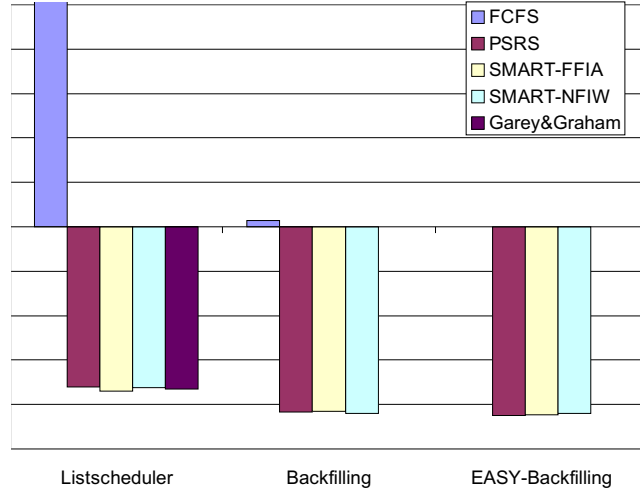


Fig. 5. Average Response Time for the Unweighted Probabilistic Workload

- In the weighted case both forms of backfilling achieve better results than the classical list scheduling if applied to FCFS or PSRS schedules.
- Surprisingly, SMART schedules with backfilling give worse results in the weighted case for the CTC workload using the estimated job execution time than for the original submission data.

Finally, the administrator considers the computation time to execute the various algorithms for the CTC workload (Table 7) and the artificial workload based on probability distributions (Table 8). In both cases similar results are obtained with a few observations being noteworthy:

- It is surprising that the classical list scheduling algorithm requires a similar computation time for both workloads while the larger number of jobs in the CTC workload results in more computational effort in almost all other cases.
- In the unweighted case SMART and PSRS together with EASY require approximately the same computation time which is significantly less than needed by FCFS and EASY.
- In the weighted case PSRS and SMART need a significant amount of computation time.

Concluding the administrator decides to use the classical list scheduling algorithm for the weighted case. In the unweighted case the results are not that clear. She intends to use either SMART or PSRS together with some form of backfilling. However, she wants to execute more simulations to fine tune the parameters of those algorithms before making the final decision. In addition she

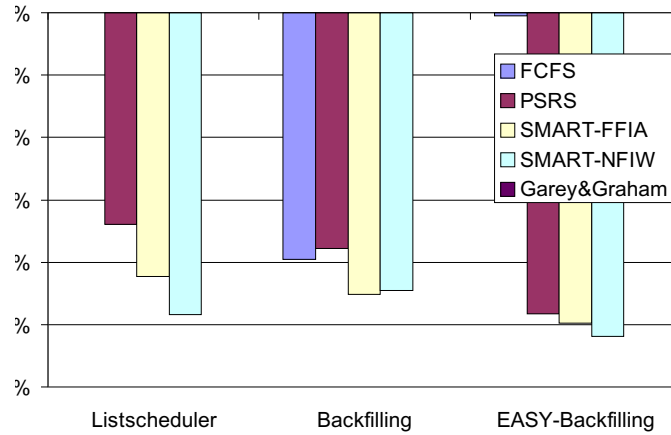


Fig. 6. Comparison of the Average Response Time for Exact vs. Estimated Job Execution Length

must evaluate the effect of combining the selected algorithms. This concludes the evaluation example.

Note that there may be plenty of reasons to consider other algorithms or to modify the simulation model. It is only the purpose of this paper to describe a method for the systematic design and evaluation of scheduling systems.

8 Conclusions

In this paper we have presented a strategy to design scheduling systems for parallel processors. This strategy was illustrated in part with the help of an example that addressed the following items in particular:

1. Determination of an objective function from a given simple set of policy rules
2. Selection of a several scheduling algorithms from the literature
3. Modification of the selected algorithms where necessary
4. Evaluation of the algorithms with the help of real and artificial workloads

We want to point out that it is not the goal of this paper to show the superiority of any single scheduling algorithm. On the contrary, we believe that there is no algorithm that is suited for all scheduling systems. In our view the design of a good scheduling system will remain an important task for the administrators or owners of large parallel systems. This paper only tries to provide some guidelines.

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		Listscheduler		Backfilling		EASY-Backfilling	
		sec	pct	sec	pct	sec	pct
Unweighted Case	FCFS	4.91E+06	+1143.0%	6.70E+05	-69.6%	<i>3.95E+05</i>	<i>0%</i>
	PSRS	1.59E+05	-59.7%	1.02E+05	-74.2%	1.06E+05	-73.2%
	SMART-FFIA	1.57E+05	-60.2%	1.00E+05	-74.7%	1.17E+05	-70.4%
	SMART-NFIW	1.82E+05	-53.9%	1.02E+05	-74.2%	1.11E+05	-71.9%
	Garey&Graham	1.46E+05	-63.0%				
Weighted Case	FCFS	4.99E+11	+249.0%	1.83E+11	+28.0%	<i>1.43E+11</i>	<i>0%</i>
	PSRS	3.82E+11	+167.1%	1.70E+11	+18.9%	1.43E+11	0%
	SMART-FFIA	3.57E+11	+149.6%	2.00E+11	+39.9%	1.51E+11	+5.6%
	SMART-NFIW	3.91E+11	+173.4%	2.03E+11	+42.0%	1.49E+11	+4.2%
	Garey&Graham	1.20E+11	-16.1%				

Table 3. Average Response Time for the CTC-Workload

		Listscheduler		Backfilling		EASY-Backfilling	
		sec	pct	sec	pct	sec	pct
Unweighted Case	FCFS	6.17E+06	+499.0%	1.06E+06	+2.9%	<i>1.03E+06</i>	<i>0%</i>
	PSRS	2.86E+05	-72.2%	1.71E+05	-83.4%	1.55E+05	-85.0%
	SMART-FFIA	2.67E+05	-74.1%	1.74E+05	-83.1%	1.57E+05	-84.8%
	SMART-NFIW	2.85E+05	-72.3%	1.65E+05	-84.0%	1.64E+05	-84.1%
	Garey&Graham	2.78E+05	-73.0%				
Weighted Case	FCFS	6.17E+11	+108.4%	3.03E+11	+2.4%	<i>2.96E+11</i>	<i>0%</i>
	PSRS	5.10E+11	+72.3%	3.05E+11	+3.0%	2.91E+11	-1.7%
	SMART-FFIA	4.84E+11	+63.5%	3.33E+11	+12.5%	2.97E+11	+0.3%
	SMART-NFIW	4.86E+11	+64.2%	3.31E+11	+11.8%	3.03E+11	+2.4%
	Garey&Graham	2.72E+11	-8.1%				

Table 4. Average Response Time for the Probability Distributed Workload

		Listscheduler		Backfilling		EASY-Backfilling	
		sec	pct	sec	pct	sec	pct
Unweighted Case	FCFS	3.40E+08	+96.5%	1.72E+08	-0.6%	<i>1.73E+08</i>	<i>0%</i>
	PSRS	1.66E+08	-4.0%	1.44E+08	-16.8%	1.32E+08	-23.7%
	SMART-FFIA	1.57E+08	-9.2%	1.41E+08	-18.5%	1.37E+08	-20.8%
	SMART-NFIW	1.61E+08	-6.9%	1.42E+08	-17.9%	1.39E+08	-19.7%
	Garey&Graham	1.73E+08	0%				
Weighted Case	FCFS	9.40E+14	+41.6%	6.66E+14	+0.3%	<i>6.64E+14</i>	<i>0%</i>
	PSRS	8.66E+14	+30.4%	6.61E+14	-0.5%	6.60E+14	-0.6%
	SMART-FFIA	8.15E+14	+22.7%	7.54E+14	+13.6%	6.96E+14	+4.8%
	SMART-NFIW	9.05E+14	+36.3%	7.96E+14	+19.9%	7.09E+14	+6.8%
	Garey&Graham	6.68E+14	+0.6%				

Table 5. Average Response Time for the Randomized Workload

		Listscheduler		Backfilling		EASY-Backfilling	
		sec	pct	sec	pct	sec	pct
Unweighted Case	FCFS	4.91E+06	0%	4.05E+05	-39.6%	3.93E+05	-0.5%
	PSRS	1.05E+05	-34.0%	6.35E+04	-37.7%	5.48E+04	-48.3%
	SMART-FFIA	9.07E+04	-42.2%	5.60E+04	-45.1%	5.33E+04	-49.7%
	SMART-NFIW	9.39E+04	-48.4%	5.66E+04	-44.5%	5.34E+04	-51.9%
	Garey&Graham	1.46E+05	0.0%				
Weighted Case	FCFS	4.99E+11	0%	1.14E+11	-37.7%	9.82E+10	-31.3%
	PSRS	3.91E+11	+2.4%	1.15E+11	-32.4%	9.91E+10	-30.7%
	SMART-FFIA	3.03E+11	-15.1%	2.73E+11	+36.5%	2.58E+11	+70.9%
	SMART-NFIW	3.33E+11	-14.8%	2.92E+11	+43.8%	2.68E+11	+79.9%
	Garey&Graham	1.20E+11	0.0%				

Table 6. Average Response Time for the CTC-Workload with Knowledge of the Exact Job Execution Time

		Listscheduler	EASY-Backfilling
		pct	pct
Unweighted Case	FCFS	-81.6%	0%
	PSRS	-76.7%	-33.7%
	SMART	-75.6%	-32.7%
	Garey&Graham	-58.4%	
Weighted Case	FCFS	-80.6%	0%
	PSRS	+30.6%	-39.4%
	SMART	-13.7%	-34.3%
	Garey&Graham	-57.2%	

Table 7. Computation Time for the CTC Workload

		Listscheduler	EASY-Backfilling
		pct	pct
Unweighted Case	FCFS	-92.1%	0%
	PSRS	-88.5%	-79.6%
	SMART	-87.1%	-80.1%
	Garey&Graham	-72.3%	
Weighted Case	FCFS	-91.6%	0%
	PSRS	-27.2%	-57.4%
	SMART	-50.5%	-72.7%
	Garey&Graham	-69.2%	

Table 8. Computation Time for the Probability Distributed Workload