Causal Inference in Population Trends: A Technique for finding Demographic Anomalies in Big Data

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Abstract

The proliferation of big data, wider access to advanced computing platforms, and the development of powerful statistical algorithms can uncover hidden anomalies in demographic data that have previously been dismissed as noise. Here, we demonstrate how demographers can use causal inference techniques and abductive reasoning to identify fertility and mortality anamolies in state-level data trends by investigating demographic time series data since 1999. In demonstrating our technique, we uncover real spikes and dips in fertility and mortality over time, distinguished from regular trend variations. We show that 38 states exhibited at least one mortality anomaly over time, totalling more than 318,000 additional deaths, while an additional six states exhibited periods of decline resuling in 164,000 fewer deaths. Twelve states exhibited real, marked periods of declines in fertility, totalling more than 240,000 fewer births than expected, and eleven states had periods of excess births, resulting in an addition 134,000 births. Our results show how researchers can detect demographic anomalies in trend data and use those anomalies as a beginning point for further investigation into the causes.

Keywords: mortality, fertility, causal inference, abductive reasoning, big data

^{*}Thanks y'all!

1 Introduction

The proliferation of data, advances in high performance ("super") computing, and the development of powerful statistical algorithms mark the era of "Big Data" or data science (Van Der Aalst 2016, Zikopoulos & Eaton 2011), with the potential for researchers to find hidden or understudied social phenomena (Bohon 2018). While the availability of Big Data and high performance computing allows novel exploration of data through causal inference (Bohon 2018, Brodersen et al. 2014, Shiffrin 2016), relatively few studies utilize causal inference techniques in the study of demographic phenomena. However, understanding social phenomena using these advances reveals important insights into society (Angrist et al. 1989, Mas & Moretti 2009) and allows us to better monitor population trends (Nobles & Seltzer 2019, Torche & Shwed 2015).

Causal inference, in its most common usage, is an attempt to uncover the underlying mechanism that results in changes in a phenomenon and have a long history approaches in social sciences (Grimmer 2015). Often, the identification of a casual mechanism requires either a randomized control trial (RCT) or expert knowledge applied to a natural experiment. For population-level analysis, expensive RCTs usually preclude their widespread adoption (West et al. 2008). Using natural experiments provide less certainty about causation and fewer opportunities to replicate work but they provide important and widespread insights such as the determinants of migration, however, provides important and more widespread insights on the determinants of migration after Hurricane Katrina in 2006 (Fussell et al. 2014, Hori et al. 2009), mini baby booms after electrical blackouts (Fetzer et al. 2018), and the highly publicized estimates of excess mortality after Hurricane Maria in Puerto Rico in 2016 (Kishore et al. 2018, Santos-Lozada & Howard 2018). Both RCTs and natural experiments follow traditional, hypothesis testing, inductive scientific paradigms where a question is first posed and scientists generate or find data to answer the question. Such approaches, while extensively utilized and time-tested, are likely to miss important phenomena that might go unnoticed.

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to miss important phenomena that might go unnoticed. Data scientists are rethinking these approaches and have re-envisioned causal inference as a machine learning technique that allows big data researchers to move from correlations that have been established with good accuracy to making strong conclusions about the underlying mechanisms that produce these correlations (Pearl & Mackenzie 2018).

Abductive modeling is the movement from the inductive to the deductive, and sometimes back and forth, to reach conclusions (Bryant & Raja 2014) or "inferring cause from effect" (Crowder & Carbone 2017). In situations with large data sets, an abductive approach is far superior to deductive hypothesis testing, as p-values with an extremely large number of cases are far from revealing (Head et al. 2015, Nuzzo 2014) and we do not want to make purely inductive inferences from data of questionable generalizability (Ruggles 2014). Owing to the long history of big data sets in demographic research (one of the original "big data" resources (Ruggles 2014)), the rich demographic data available in the United States make the potential revelation of interesting and important demographic phenomena not only possible, but extremely plausible – even if identification of the phenomena occurs without identifying the underlying cause. In other sciences, the identification of effects without causes has led to new theories of galactic migration of planets and other breakthroughs (Gomes et al. 2005).

In this paper, we use modern statistical outlier detection algorithms (Chen & Liu 1993) on nearly twenty years of mortality and fertility data at the US state-level to identify anomalous demographic behavior. In essence, we identify effects without knowledge of the cause. We ask two questions regarding demographic anomalies: What are the hidden baby booms/busts and mortality spikes/dips in the United States over the last twenty years? We do not necessarily know the causes of these anomalies but identifying them allows scientists with more detailed knowledge of local population dynamics, state-level policy making, or macro-economics to explain these phenomena post-hoc. From explanations of phenomena that may have previously gone unnoticed, demographers may be able to better forecast populations and provide policy solutions for impending problems.

2 Materials and Methods

2.1 Method

We use a statistical time series outlier detection algorithm (Chen & Liu 1993), implemented in the R programming language (R Core Team 2019) via the tsoutliers package (López-de-Lacalle 2019). This algorithm iteratively uses ARIMA models to 1) produce a counter-factual time series to initially detect an outlier or anomaly, and 2) refit the ARIMA with the outliers removed. Here we briefly summarize and describe the method.

Often, the behavior of a time series can be described and summarized in ARIMA models. If a series of values, y_t^* , is subject to m interventions or outliers at time points t_1, t_2, t_m , then y_t^* can be defined as

$$y_t^* = \sum_{j=1}^m \omega_j L_j(B) I_t(t_j) + \frac{\theta(B)}{\phi(B)\alpha(B)} \alpha_t$$

Where $I_t(t_j)$ is an indicator variable with a value of 1 at observation t_j and where the jth outlier arises, $\phi(B)$ is an autoregressive polynomial with all roots outside the unit circle, $\theta(B)$ is a moving average polynomial with all roots outside the unit circle, and $\alpha(B)$ is an autoregressive polynomial with all roots on the unit circle.

We examine three types of outliers at time point t_m : 1) additive outliers (AO), defined as $L_j(B) = 1$; 2) level shift outliers (LS), defined as $L_j(B) = 1/(1 - B)$; and 2) temporary change outliers (TC), defined as $L_j(B) = 1/(1 - \delta B)$.

Colloquially, additive outliers arise when a single event causes the time series to unexpectedly increase/decrease for a single time period; level shift outliers arise when an event causes the time series to unexpectedly increase/decrease for multiple time periods; and temporary change outliers arise when an event causes the time series to unexpectedly increase/decrease with lingering effects that decay over multiple time periods.

An outlier is detected using a regression equation

$$\pi(B)y_t^* \equiv \hat{e} = \sum_{j=1}^m \omega_j \pi(B) L_j(B) I_t(t_j) + \alpha_t$$

where $\pi(B) = \sum_{i=0}^{inf} \pi_i B^i$. The identification of outliers then involves a three step

process to (1) identify all potential outliers, t_j and $L_j(B)$, (2) joint estimates of model parameters and outlier effects are computed to identify potentially spurious outliers, and (3) the outliers and effects are re-estimated without spurious outliers. Of importance here is step 2, which relies on some critical value above which an outlier at time point m is considered spurious. Based on Chen and Liu's (1993) recommendation, we set a critical value of 3.5 which generally minimizes the possibility of Type I errors or false positive outliers.

We report outliers using a simple t-statistic and report the size of the outlier, or its impact on the time series, by subtracting \hat{y} , the adjusted time series without outliers removed, from y, the original, unadjusted time series.

2.2 Data

We search for demographic anomalies using the Center for Disease Control and Prevention's online WONDER monthly fertility (2003-2017) and mortality databases (1999-2016) for all fifty states and the District of Columbia (United States Department of Health and Human Services (US DHHS), Centers for Disease Control and Prevention (CDC) 2018, Centers for Disease Control and Prevention, National Center for Health Statistics. 2019). These data sets contain every birth and death record in the United States over the time periods of interest, representing the universe of both mortality and fertility data in the US. These data are considered the "gold standard" of data collections (Mahapatra et al. 2007) and have been considered "complete" since 1968 (Hetzel 2016). We search over each state equivalent's (n=51) mortality (n=228) and fertility (n=180) monthly time series for a total of 20,808 state-months of data.

3 Results

We detect numerous anomalous mortality and fertility events at the US state-level since 1999. A full listing of these anomalies can be found in the **Supplementary Materials**. We begin with a summary of the anomalies we detect and then we highlight highly significant mortality and fertility anomalies across all three types of outliers (Additive Outliers, Level

Table 1: Summary by Demographic Component. refers to the number of anomolies for each type and demographic component, States refers to the number of unique states exhibiting that specific Type-demographic component.

Component	Anomalies	y	\hat{y}	$y - \hat{y}$	$ y - \hat{y} $	% of Total
Fertility	22	25.48M	25.68M	-202,217	226,476	0.889
Mortality	156	$43.57\mathrm{M}$	$43.52\mathrm{M}$	48,535	627,364	1.440

Shift Outliers, and Temporary Change Outliers) with plausible explanations. Finally, we highlight two strong anomalies that bely explanation.

3.1 Overall Anomalies

Table 1 report the overall number of anomalies we detect of each type for births and deaths and some summary statistics across all anomaly types. We find considerably more mortality anomalies (n = 156) than fertility anomalies (n = 22). Given that anomalies are always the produce of events (Ass 2018), the finding of more mortality than fertility anomalies is not surprising. Mortality is likely to spike in response to a catastrophic event (like an earthquake or terrorist attack) while the effects of a catastrophic event on fertility is less predictable. One reason for this is that fertility is linked to human decision-making more directly than mortality (Stein et al. 2014) which results in more varied outcomes, so, for example, researchers find that catastrophic weather events can increase childbearing among those who already have a child, but not among the childless (Evans et al. 2010). Some events, like the 1995 Oklahoma City bombings, resulted in both fertility and mortality changes. However, changes in fertility manifest over a longer time horizon after an event, and the relationship between a fertility-inducing event and behavior change is less strong than the relationship between a mortality-inducing event (such as a terrorist incident) and death (Rodgers et al. 2005). Of course, not all events that impact fertility and mortality are catastrophic. Researchers have documented that more commonplace events such as massive layoff (Venkataramani et al. 2019) or policy changes (Livingston et al. 2018) can also create anomalies in mortality patterns, but we have not found such evidence for fertility.

Consistent with more anomalies across the time lines, we find more anomalous deaths (627,364) than anomalous births (226,476). Fertility anomalies overwhelmingly tend toward lower fertility, with only a few fertility anomalies yielding more births. This is consistent with research findings that link high severity weather events to significantly lower fertility (Evans et al. 2010). Conversely, mortality anomalies tend to be more evenly split between positive and negative anomalies, but tend toward more deaths rather than less deaths. Again, this is not surprising, as the kinds of events that increase death (e.g., plant closings are associated with increased opioid death (Venkataramani et al. 2019)) are more common than the events that decrease death (e.g., cannabis legalization is associated with decreased opioid deaths (Livingston et al. 2018)) These anomalous deaths and births account for 1.44% and 0.889% over the entire time series, respectively.

Figure 1 maps these results. Three states exhibited neither mortality nor fertility anomalies: Alaska, North Dakota, and South Dakota. Another nine states exhibited just a single anomaly (DE, DC, ID, IL, KS, NV, NM, UT, and WY). Both New York and Massachusetts exhibited the most anomalies with nine.

3.2 Mortality

Since the purpose of our paper is to demonstrate how demographers can make use of causal inference technique, we will not discuss all of our findings in this paper. Instead, we will use a few cases for illustration. For mortality, we will use New York State as an example (**Figure 2a**). We identify seven anomalies in the mortality time series for New York, all with t-statistics in excess of 3.91, making these anomalies unlikely to be due to chance. The algorithm correctly identifies September 2001 as an additive outlier (2001:09 t=6.40) where mortality in that month was 1,628 higher than anticipated. This mortality event is likely caused by the September 11 tragedy and the detection of this mortality event provides confidence in our detection of other anomalies.

In Figure 2a, notice the strong level shift (LS) that occurs in February 2004 (2004:02 t=5.59) which prevented almost 870 deaths per month. This shift totals more than 144,000 averted deaths compared to the counter-factual time series and is the single largest mortality protective anomaly among all states. This translates to 4.5% fewer deaths than expected

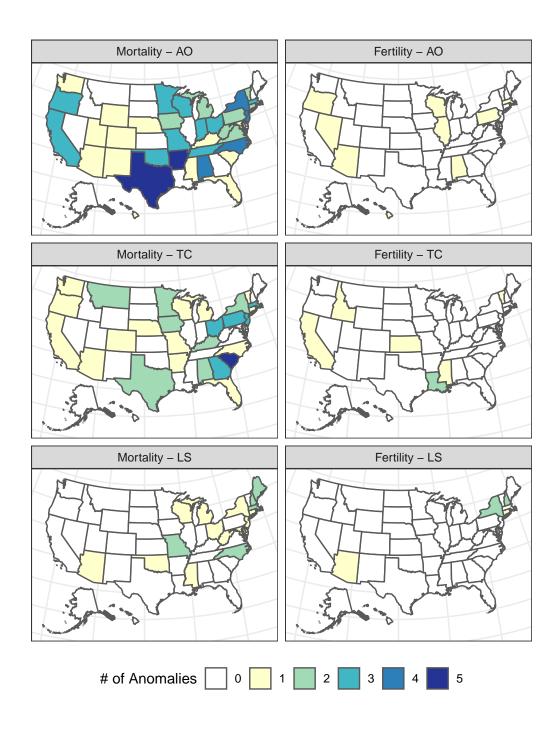


Figure 1: Summary of Anomalies by type, demographic component, and State. We observe much fewer fertility anomalies than mortality anomalies.

over the time period. What is driving this mortality protection? What policies did NY put into place that might have contributed to this considerable mortality reduction? What environmental conditions may have changed? These are the kinds of questions that arise from our analyses. The purpose of our paper is not to answer these questions, but our findings underscore the need for more research that takes an abductive approach. By identifying anomalies through an inductive process, researchers can then look for underlying causes. Once those causes are identified, researchers can then use a deductive process to see if such events predict other (or future) anomalies.

To see the potential for combinging abductive reasoning with causal inference, contrast the mortality protection in New York with the enhanced mortality in New Hampshire (**Figure 2b**). In New Hampshire we detect two significant level shifts (LS) in the monthly mortality data, first in April 2010 and again in November 2014 (2010:04 t=3.51; 2014:11 t=6.68). These anomalies suggest New Hampshire experienced 9,700 more deaths (+14% more than expected) in a seven-year period beginning in early 2010. These are events not experienced by neighborhing states during the same time period, and this is the single largest percentage mortality increase/decrease we detected among all states. Not coincidentally, NH has the second highest opioid-related mortality in the US (Beetham et al. 2019) and it is likely that we detect this epidemic in our results. Isolating these anomalies and testing them against opioid sales data might yeild intriguing results.

3.3 Fertility

To illustrate how researchers can examine fertility anomalies, we begin with a clear temporary change (TC) outlier for fertility in Louisiana (**Figure 3a**). Here we detect two TC outliers, nearly back-to-back in 2005 (2005:08 t = -6; and 2005:10 t = -5), coinciding with the destruction of Hurricane Katrina from the same year. The migration associated with Hurricane Katrina has garnered most of the attention of demographers (Fussell et al. 2014, Hori et al. 2009), but the hurricane had a very clear impact on fertility behaviors too, creating a mini "baby bust" in Louisiana with the departure of many people in their child-bearing years. We estimate 4,411 fewer births in Louisiana compared to the counterfactual, likely attributable to the Hurricane.

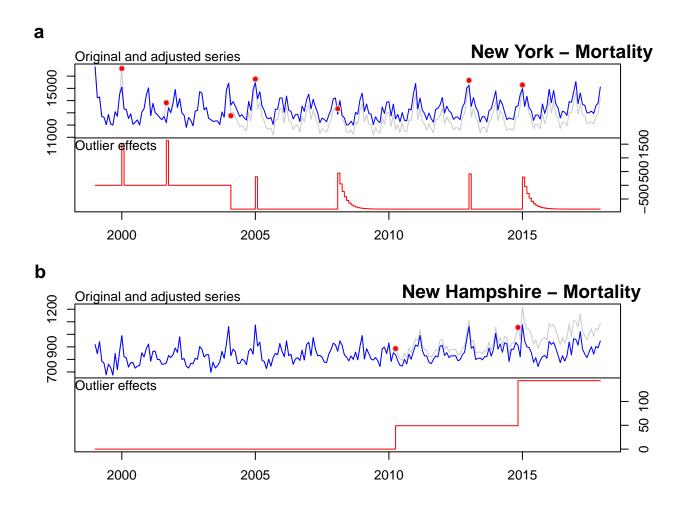


Figure 2: Anomaly Detection for New York (a) and New Hampshire (b) state mortality, 1999-2016. The top part of each panel contains the original time series (light gray), the corrected, counter-factual time series in the absence of anomalies (blue), and the red dots correspond to the onset of detected anomalies. The bottom part of each panel contains the magnitude and type of the outlier in red. In New York (a), we detect additive outliers (AO) in January 2000, September 2001, January 2005, and January 2013; temporary change (TC) outliers in February 2007 and January 2015; and a level shift (LS) starting in February 2004. In New Hampshire (b), we detect two outliers, both level shift outliers (LS) in April 2010 and again in November 2014. These anomalies suggest New York experienced a significant mortality event in September 2001 and New Hampshire experienced approximately 9,700 more deaths than expected since 2010 or 14% more deaths in the state over just seven years.

We also highlight a level shift (LS) outlier for fertility in Connecticut. Here we detect a strong (t= -3.71; -285 births/month) level shift toward lower fertility beginning in August 2009 (2009:08) that continues through the end of the period (**Figure 3b**). This LS toward lower fertility reduced the # of births by -28,752 or -8.57% lower than the counterfactual time series. The stock market crash of 2008, where the Dow Jones Industrial Average had the largest single-day loss up to that point, occurred just 11 months before we detect a shift toward lower fertility. It is possible that the trend toward lower fertility in August 2009 and the stock market crash in September 2008 are linked, although, as stated previously, we are speculating only to illustrate how causal inference could work in an abductive research agenda.

3.4 Interesting Anomalous Fertility/Mortality events

In the examples above, we highlighted four fertility/mortality anomalies with plausible explanations. In the case of New York and New Hampshire, the mortality anomalies have plausible explanations. It seems likely that New York's AO anomaly in September 2001 is caused by the 9/11 tragedy and the rise in New Hampshire's mortality starting in 2010 could be linked to the opioid epidemic. Similarly, Louisiana's TC anomalies seem linked to Hurricanes Katrina and Rita while the LS anomaly in Connecticut's fertility appears linked to the Great Recession. However, we detect numerous seemingly unexplainable demographic anomalies in other states. **Figure 4** shows two such unexplained anomalies.

In **Figure 4a** we identify a single additive anomaly in Hawaiian fertility in May 2014. This is a strong anomaly with a t-statistic of 4.96, 14% above the counter-factual time series. This single, anomalous month is also the second highest monthly births in the time series. We have no plausible explanation for this anomaly. We do not believe this is simply a data error as the other extreme values, September 2008 and February 2005 with the highest and lowest recorded fertility respectively, were not identified as anomalous events. Even if we were to assume this anomaly resulted from data entry error, it remains an unaltered data error in the Hawaiian monthly fertility data.

This is contrast to **Figure 4b**, where we identify a strange mortality reduction in Ohio (t-stat: -4.27). This LS is more than 1,100 deaths per month less than the counterfactual

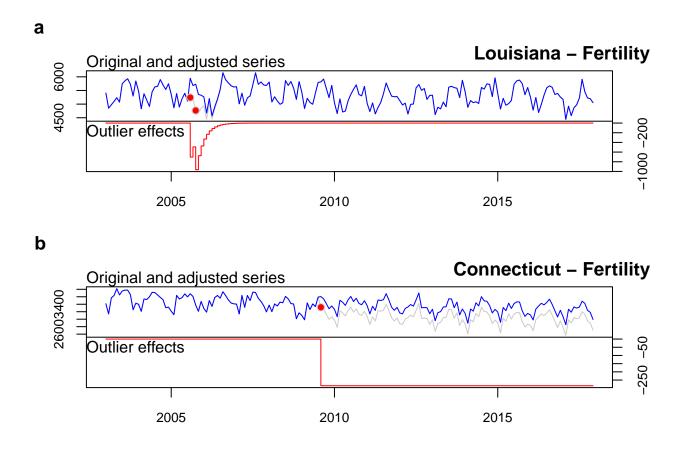


Figure 3: Anomaly detection in Louisiana (a) and Connecticut (b) state fertility, 2003-2018. In (a), we detect two outliers, back-to-back, likely resulting from Hurricane Katrina in August and October 2005, representing a decrease of more than 4,400 births due to the hurricane. In (b), we detect one outlier, a level shift outlier (LS) in August 2009. We believe this reduction is attributable to the stock market crash 11 months earlier.

time series, suggesting had nearly 40,000 fewer deaths since February 2015 than expected. This is the single-largest LS among all states. We could not identify the potential policies Ohio might have put into place to provide such a strong mortality protection.

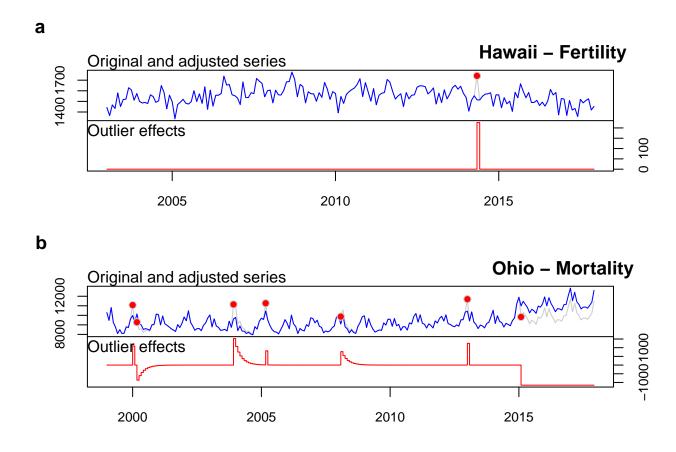


Figure 4: Anomaly detection in Hawaii state fertility (a) and Ohio state mortality (b). Here we detect one outlier, an additive outlier (AO) in May 2014 in Hawaii (a), representing a large, unexplainable 14% increase in expected births in that month. We also detect a strong level shift (LS) reduction (b), representing a large, unexplainable reduction of nearly 40,000 deaths in Ohio.

References

- Angrist, J. D. et al. (1989), Lifetime Earnings and the Vietnam Era Draft Lottery: Evidence from Social Security Administrative Records, number 251, Industrial Relations Section, Princeton University.
- Ass (2018), Anomaly Detection and Explanation Discovery on Event Streams, Proceedings of the International Workshop on Real-Time Business Intelligence and Analytics.
- Beetham, T., Saloner, B., Wakeman, S. E., Gaye, M. & Barnett, M. L. (2019), 'Access to office-based buprenorphine treatment in areas with high rates of opioid-related mortality: An audit study', *Annals of internal medicine* **171**(1), 1–9.
- Bohon, S. A. (2018), 'Demography in the big data revolution: Changing the culture to forge new frontiers', *Population Research and Policy Review* **37**(3), 323–341.
- Brodersen, K. H., Gallusser, F., Koehler, J., Remy, N. & Scott, S. L. (2014), 'Inferring causal impact using Bayesian structural time-series models', *Annals of Applied Statistics* **9**, 247–274.
- Bryant, A. & Raja, U. (2014), 'In the realm of big data', First Monday 19(2).
- Centers for Disease Control and Prevention, National Center for Health Statistics. (2019), 'Underlying Cause of Death 1999-2017 on CDC WONDER Online Database, released December, 2018. Data are from the Multiple Cause of Death Files, 1999-2017, as compiled from data provided by the 57 vital statistics jurisdictions through the Vital Statistics Cooperative Program', pp. Accessed at http://wonder.cdc.gov/ucd-icd10.html (data downloaded on 17 August 2019).
- Chen, C. & Liu, L.-M. (1993), 'Joint estimation of model parameters and outlier effects in time series', *Journal of the American Statistical Association* 88(421), 284–297.
- Crowder, J. A. & Carbone, J. N. (2017), Cognitive architectures for prognostic health management, in S. Ekwaro-Osire, A. C. Gonçalves & F. M. Alemayehu, eds, 'Probabilistic Prognostics and Health Management of Energy Systems', Springer International Publishing, Cham, pp. 91–107.

- Evans, R. W., Hu, Y. & Zhao, Z. (2010), 'The fertility effect of catastrophe: U.s. hurricane births', *Journal of Population Economics* **23**(1), 1–36.
- Fetzer, T., Pardo, O. & Shanghavi, A. (2018), 'More than an urban legend: The short-and long-run effects of unplanned fertility shocks', *Journal of Population Economics* **31**(4), 1125–1176.
- Fussell, E., Curtis, K. J. & DeWaard, J. (2014), 'Recovery migration to the City of New Orleans after Hurricane Katrina: A migration systems approach', *Population and Environment* **35**(3), 305–322.
- Gomes, R., Levison, H. F., Tsiganis, K. & Morbidelli, A. (2005), 'Origin of the cataclysmic Late Heavy Bombardment period of the terrestrial planets', *Nature* **435**(7041), 466–469.
- Grimmer, J. (2015), 'We Are All Social Scientists Now: How Big Data, Machine Learning, and Causal Inference Work Together', *PS: Political Science & Politics* **48**(1), 80–83.
- Head, M. L., Holman, L., Lanfear, R., Kahn, A. T. & Jennions, M. D. (2015), 'The extent and consequences of p-hacking in science', *PLoS biology* **13**(3), e1002106.
- Hetzel, A. (2016), 'US vital statistics system: Major activities and developments, 1950–95.(DHHS publication no.(PHS) 97-1003). hyattsville, MD: National center for health statistics; 1997'.
- Hori, M., Schafer, M. J. & Bowman, D. J. (2009), 'Displacement Dynamics in Southern Louisiana After Hurricanes Katrina and Rita', *Population Research and Policy Review* **28**(1), 45–65.
- Kishore, N., Marqués, D., Mahmud, A., Kiang, M. V., Rodriguez, I., Fuller, A., Ebner, P., Sorensen, C., Racy, F., Lemery, J. et al. (2018), 'Mortality in puerto rico after hurricane maria', New England journal of medicine 379(2), 162–170.
- Livingston, M. D., Barnett, T. E., Delcher, C. & Wagenaar, A. C. (2018), 'Recreational cannabis legalization and opioid-related deaths in colorado, 2000-2015', *American Journal of Public Health* **107**(11), 1827–1829.

- López-de-Lacalle, J. (2019), Tsoutliers: Detection of Outliers in Time Series. R package version 0.6-8.
- Mahapatra, P., Shibuya, K., Lopez, A. D., Coullare, F., Notzon, F. C., Rao, C., Szreter, S. et al. (2007), 'Civil registration systems and vital statistics: Successes and missed opportunities', *The Lancet* **370**(9599), 1653–1663.
- Mas, A. & Moretti, E. (2009), 'Peers at work', American Economic Review 99(1), 112–45.
- Nobles, J. & Seltzer, N. (2019), Finding and Characterizing the Displaced: A method using administrative data, in 'Population Association of America Conference, Austin, Texas'.
- Nuzzo, R. (2014), 'Scientific method: Statistical errors', Nature News 506(7487), 150.
- Pearl, J. & Mackenzie, D. (2018), The book of why: the new science of cause and effect, Basic Books.
- R Core Team (2019), R: A Language and Environment for Statistical Computing, R Foundation for Statistical Computing, Vienna, Austria.
 - **URL:** https://www.R-project.org/
- Rodgers, J. L., St. John, C. A. & Coleman, R. (2005), 'Did fertility go up after the oklahoma city bombing? an analysis of births in metropolitan counties in oklahoma, 19901999', *Demography* 42, 675–692.
- Ruggles, S. (2014), 'Big microdata for population research', *Demography* **51**(1), 287–297.
- Santos-Lozada, A. R. & Howard, J. T. (2018), 'Use of death counts from vital statistics to calculate excess deaths in Puerto Rico following Hurricane Maria', *Jama* **320**(14), 1491–1493.
- Shiffrin, R. M. (2016), 'Drawing causal inference from big data', *Proceedings of the National Academy of Sciences* **113**(27), 7308–7309.
- Stein, P., Willen, S. & Pavetic, M. (2014), 'Couples fertility decision-making', *Demographic Research* **30**, 1697–1732.

- Torche, F. & Shwed, U. (2015), 'The hidden costs of war: Exposure to armed conflict and birth outcomes', *Sociological Science* 2, 558–581.
- United States Department of Health and Human Services (US DHHS), Centers for Disease Control and Prevention (CDC) (2018), 'National center for health statistics (NCHS), division of vital statistics, natality public-use data 2007-2017, on CDC WONDER online database, march 2009', pp. Accessed at http://wonder.cdc.gov/natality-current.html (data downloaded on 19 September 2019).
- Van Der Aalst, W. (2016), Data science in action, in 'Process Mining', Springer, pp. 3–23.
- Venkataramani, A. S., Bair, E., O'Brien, R. L. & Tsai, A. C. (2019), 'Association between automotive assembly plant closures and opioid overdose mortality in the united states: A difference-in-differences analysis', *JAMA Internal Medicine*.
- West, S. G., Duan, N., Pequegnat, W., Gaist, P., Des Jarlais, D. C., Holtgrave, D., Szapocznik, J., Fishbein, M., Rapkin, B., Clatts, M. & Mullen, P. D. (2008), 'Alternatives to the Randomized Controlled Trial', *American Journal of Public Health* **98**(8), 1359–1366.
- Zikopoulos, P. & Eaton, C. (2011), Understanding Big Data: Analytics for Enterprise Class Hadoop and Streaming Data, McGraw-Hill Osborne Media.