SP Exam Project

Mathias Andresen

May 13, 2021

Compiled with Visual Studio 2019 Community (version 16) in Clion. Using bundled CMake 3.17.5.

Listing 1: CMakeLists.txt

```
cmake_minimum_required(VERSION 3.17)
project(sp_exam_project)

set(CMAKE_CXX_STANDARD 20)

add_library(
    stochastic-simulation
    library/simulation.cpp
    library/simulation.cpp
    library/SymbolTable.h
    library/simulation_monitor.h
    library/data.h
    library/data.cpp
    library/my-thread-pool.h
)

add_executable(sp_exam_project main.cpp vessels.h)

target_link_libraries(sp_exam_project PRIVATE stochastic-simulation)
```

Listing 2: main.cpp

```
#include <iostream>
#include "library/simulation.h"
#include <chrono>
#include "vessels.h"

using namespace StochasticSimulation;

// Requirement 7 use of monitor
class hospitalized_monitor: public simulation_monitor {
private:
    double_t hospitalized_acc{0.0};
    double_t last_time{0.0};
public:
    size_t max_hospitalized{0};

    void monitor(SimulationState &state) override {
        auto currently_hospitalized = state.reactants.get("H").amount;

        if (currently_hospitalized > max_hospitalized) {
            max_hospitalized = currently_hospitalized;
        }

        hospitalized_acc += (currently_hospitalized * (state.time - last_time));

        last_time = state.time;
    }
```

```
27
28      double_t get_mean_hospitalized() const {
29          return (hospitalized_acc / last_time);
30      }
31  };
32
33  void simulate_covid() {
34      std::cout << "Simulating covid19 example with hospitalized monitor" << std::endl;
35      Vessel covid_vessel = seihr(10000);
36
37      std::cout << covid_vessel << std::endl;
38      covid_vessel.visualize_reactions("covid_graph.png");
39
40      std::cout << "reaction graph can be seen at: covid_graph.png" << std::endl;
41
42      hospitalized_monitor monitor{};
43
44      auto trajectory = covid_vessel.do_simulation(120, monitor);
45
46      std::cout << "Simulation done" << std::endl;
47      std::cout << "Max hospitalized: " << monitor.max_hospitalized << std::endl;
48      std::cout << "Mean hospitalized: " << monitor.get_mean_hospitalized() << std::endl;
49
50      std::cout << "Writing trajectory to csv file at covid_output.csv" << std::endl;
51      trajectory->write_csv("covid_output.csv");
52      std::cout << "Turn it into a graph using python ./draw_graph.py covid release" << std::endl;
53  }
54
55  void simulate_covid_multiple() {
56      std::cout << "Simulating covid19 example 30 times and calculating mean" << std::endl;
57      Vessel covid_vessel = seihr(10000);
58
59      auto trajectories = covid_vessel.do_multiple_simulations(110, 100);
60
61      std::cout << "Simulations done" << std::endl << "Computing mean trajectory" << std::endl;
62
63      auto mean = SimulationTrajectory::compute_mean_trajectory(trajectories);
64
65      std::cout << "Writing mean trajectory to csv file at covid_output_multiple.csv" << std::endl;
66      mean.write_csv("covid_output_multiple.csv");
67      std::cout << "Turn it into a graph using python ./draw_graph.py covid   ↙
    ↪covid_output_multiple.csv" << std::endl;
68  }
69
70  void simulate_introduction() {
71      std::cout << "Simulating introduction example" << std::endl;
72      Vessel introduction_vessel = introduction(25, 50, 1, 0.001);
73      std::cout << introduction_vessel << std::endl;
74
75      introduction_vessel.visualize_reactions("intro_graph.png");
76
77      auto trajectory = introduction_vessel.do_simulation(400);
78
79      trajectory->write_csv("intro_output.csv");
80  }
81
82
83  void simulate_circadian() {
84      std::cout << "Simulating circadian rhythm example..." << std::endl;
85      Vessel oscillator = circadian_oscillator();
86
```

```
    std::cout << oscillator << std::endl;
    oscillator.visualize_reactions("cir_graph.png");

    auto trajectory = oscillator.do_simulation(110);

    std::cout << "Writing csv file..." << std::endl;
    trajectory->write_csv("circadian_output.csv");
}

void simulate_circadian2() {
    std::cout << "Simulating circadian rhythm alternative example..." << std::endl;
    Vessel oscillator = circadian_oscillator2();

    std::cout << oscillator << std::endl;
    oscillator.visualize_reactions("cir2_graph.png");

    auto trajectory = oscillator.do_simulation(110);

    std::cout << "Writing csv file..." << std::endl;
    trajectory->write_csv("circadian2_output.csv");
}

void benchmark() {
    std::cout << "Benchmarking with circadian rhythm example (max_time=100)" << std::endl;

    auto runs{30};

    Vessel oscillator = circadian_oscillator();

    unsigned long time_acc1{0};
    for (int i = 0; i < runs; ++i) {
        auto t0 = std::chrono::high_resolution_clock::now();
        oscillator.do_simulation(100);
        auto t1 = std::chrono::high_resolution_clock::now();

        time_acc1 += std::chrono::duration_cast<std::chrono::nanoseconds>(t1-t0).count();
    }
    auto mean_time1 = time_acc1 / runs;
    std::cout << "Simulation 1 mean time (nanoseconds): " << mean_time1 << std::endl;

    unsigned long time_acc2{0};
    for (int i = 0; i < runs; ++i) {
        auto t0 = std::chrono::high_resolution_clock::now();
        oscillator.do_simulation2(100);
        auto t1 = std::chrono::high_resolution_clock::now();

        time_acc2 += std::chrono::duration_cast<std::chrono::nanoseconds>(t1-t0).count();
    }
    auto mean_time2 = time_acc2 / runs;
    std::cout << "Simulation 2 mean time (nanoseconds): " << mean_time2 << std::endl;
}

int main() {
    simulate_covid();
//    simulate_covid_multiple();

//    simulate_introduction();
//    simulate_circadian();
//    simulate_circadian2();

//    benchmark();
```

```
}
```

Listing 3: vessels.h

```
//
// Created by Mathias on 12-05-2021.
//

#ifndef SP_EXAM_PROJECT_VESSELS_H
#define SP_EXAM_PROJECT_VESSELS_H

#include "library/simulation.h"

using namespace StochasticSimulation;

Vessel seihr(uint32_t N)
{
    auto v = Vessel{};
    const auto eps = 0.0009; // initial fraction of infectious
    const auto I0 = size_t(std::round(eps*N)); // initial infectious
    const auto E0 = size_t(std::round(eps*N*15)); // initial exposed
    const auto S0 = N-I0-E0; // initial susceptible
    const auto R0 = 2.4; // basic reproductive number (initial, without lockdown etc)
    const auto alpha = 1.0 / 5.1; // incubation rate (E -> I) ~5.1 days
    const auto gamma = 1.0 / 3.1; // recovery rate (I -> R) ~3.1 days
    const auto beta = R0 * gamma; // infection/generation rate (S+I -> E+I)
    const auto P_H = 0.9e-3; // probability of hospitalization
    const auto kappa = gamma * P_H*(1.0-P_H); // hospitalization rate (I -> H)
    const auto tau = 1.0/10.12; // recovery/death rate in hospital (H -> R) ~10.12 days

    // Reactants
    auto S = v("S", S0); // susceptible
    auto E = v("E", E0); // exposed
    auto I = v("I", I0); // infectious
    auto H = v("H", 0); // hospitalized
    auto R = v("R", 0); // removed/immune (recovered + dead)

    // Reactions
    v(S >>= E, I, beta/N);
    v(E >>= I, alpha);
    v(I >>= R, gamma);
    v(I >>= H, kappa);
    v(H >>= R, tau);

    return v;
}

Vessel introduction(uint32_t A_start, uint32_t B_Start, uint32_t D_amount, double_t lambda) {
    auto v = Vessel{};
    // Reactants
    auto A = v("A", A_start);
    auto B = v("B", B_Start);
    auto C = v("C", 0);
    auto D = v("D", D_amount);
    // Reactions
    v(A + B * 2 >>= C, D, lambda);

    return v;
}

/** direct encoding */
Vessel circadian_oscillator()
```

```
{
    auto alphaA = 50.0;
    auto alpha_A = 500.0;
    auto alphaR = 0.01;
    auto alpha_R = 50.0;
    auto betaA = 50.0;
    auto betaR = 5.0;
    auto gammaA = 1.0;
    auto gammaR = 1.0;
    auto gammaC = 2.0;
    auto deltaA = 1.0;
    auto deltaR = 0.2;
    auto deltaMA = 10.0;
    auto deltaMR = 0.5;
    auto thetaA = 50.0;
    auto thetaR = 100.0;
    auto v = Vessel{};
    auto env = v.environment();
    auto DA = v("DA", 1);
    auto D_A = v("D_A", 0);
    auto DR = v("DR", 1);
    auto D_R = v("D_R", 0);
    auto MA = v("MA", 0);
    auto MR = v("MR", 0);
    auto A = v("A", 0);
    auto R = v("R", 0);
    auto C = v("C", 0);
    v(A + DA >>= D_A, gammaA);
    v(D_A >>= DA + A, thetaA);
    v(A + DR >>= D_R, gammaR);
    v(D_R >>= DR + A, thetaR);
    v(D_A >>= MA + D_A, alpha_A);
    v(DA >>= MA + DA, alphaA);
    v(D_R >>= MR + D_R, alpha_R);
    v(DR >>= MR + DR, alphaR);
    v(MA >>= MA + A, betaA);
    v(MR >>= MR + R, betaR);
    v(A + R >>= C, gammaC);
    v(C >>= R, deltaA);
    v(A >>= env, deltaA);
    v(R >>= env, deltaR);
    v(MA >>= env, deltaMA);
    v(MR >>= env, deltaMR);
    return v;
}

/** alternative encoding using catalysts */
Vessel circadian_oscillator2()
{
    auto alphaA = 50.0;
    auto alpha_A = 500.0;
    auto alphaR = 0.01;
    auto alpha_R = 50.0;
    auto betaA = 50.0;
    auto betaR = 5.0;
    auto gammaA = 1.0;
    auto gammaR = 1.0;
    auto gammaC = 2.0;
    auto deltaA = 1.0;
    auto deltaR = 0.2;
    auto deltaMA = 10.0;
```

```
    auto deltaMR = 0.5;
    auto thetaA = 50.0;
    auto thetaR = 100.0;
    auto v = Vessel{};
    auto env = v.environment();
    auto DA = v("DA", 1);
    auto D_A = v("D_A", 0);
    auto DR = v("DR", 1);
    auto D_R = v("D_R", 0);
    auto MA = v("MA", 0);
    auto MR = v("MR", 0);
    auto A = v("A", 0);
    auto R = v("R", 0);
    auto C = v("C", 0);
    v(A + DA >>= D_A, gammaA);
    v(D_A >>= DA + A, thetaA);
    v(DR + A >>= D_R, gammaR);
    v(D_R >>= DR + A, thetaR);
    v(env >>= MA, D_A, alpha_A);
    v(env >>= MA, DA, alphaA);
    v(env >>= MR, D_R, alpha_R);
    v(env >>= MR, DR, alphaR);
    v(env >>= A, MA, betaA);
    v(env >>= R, MR, betaR);
    v(A + R >>= C, gammaC);
    v(C >>= R, deltaA);
    v(A >>= env, deltaA);
    v(R >>= env, deltaR);
    v(MA >>= env, deltaMA);
    v(MR >>= env, deltaMR);
    return v;
}

#endif //SP_EXAM_PROJECT_VESSELS_H
```

Listing 4: simulation.h

```
//
// Created by Mathias on 09-05-2021.
//

#ifndef SP_EXAM_PROJECT_SIMULATION_H
#define SP_EXAM_PROJECT_SIMULATION_H

#include <string>
#include <utility>
#include <vector>
#include <set>
#include <optional>
#include <map>
#include <numeric>
#include <random>
#include <algorithm>
#include <functional>
#include <sstream>
#include <fstream>
#include <chrono>
#include <thread>
#include <future>
#include <ranges>
#include "SymbolTable.h"
#include "simulation_monitor.h"
```

```cpp
#include "data.h"

namespace StochasticSimulation {

    using map_type = std::map<double_t, SimulationState>;
    class SimulationTrajectory: public map_type {
    private:
        double_t largest_time{-1};
        static double_t compute_interpolated_value(
                const std::string& key,
                SimulationState& s0,
                SimulationState& s1,
                double_t x);
    public:
        using map_type::map;

        SimulationTrajectory(const SimulationTrajectory& val): map_type(val) {
            largest_time = val.largest_time;
        }

        SimulationTrajectory(SimulationTrajectory&& rval): map_type(std::move(rval)) {
            largest_time = std::move(rval.largest_time);
        };

        SimulationTrajectory& operator=(const SimulationTrajectory & val) {
            map_type::operator=(val);
            largest_time = val.largest_time;
        };

        SimulationTrajectory& operator=(SimulationTrajectory&& rval) {
            map_type::operator=(std::move(rval));
            largest_time = std::move(rval.largest_time);
        };

        // Requirement 9 compute mean
        static SimulationTrajectory
↪compute_mean_trajectory(std::vector<std::shared_ptr<SimulationTrajectory>>& trajectories);

        void insert(SimulationState state) {
            if (state.time > largest_time) {
                largest_time = state.time;
            }

            map_type::insert({state.time, std::move(state)});
        }

        // Requirement 6 output trajectory
        void write_csv(const std::string& path);

        double_t get_max_time() {
            return largest_time;
        }
    };

    // Requirement 1 operators for DSEL
    class Vessel {
    private:
        std::vector<Reaction> reactions{};
        SymbolTable<Reactant> reactants;
    public:

```

```
        Vessel() = default;

        Vessel(const Vessel &val) {
            reactions = val.reactions;
            reactants = val.reactants;
        }

        Vessel (Vessel&& rval) {
            reactions = std::move(rval.reactions);
            reactants = std::move(rval.reactants);
        };

        Reactant& operator()(std::string name, size_t initial_amount) {
            Reactant newReactant{std::move(name), initial_amount};

            reactants.put(newReactant.name, newReactant);

            return reactants.get(newReactant.name);
        }

        Reaction operator()(Reaction&& reaction, double_t rate) {
            reaction.rate = rate;

            reactions.push_back(reaction);

            return reaction;
        }

        Reaction operator()(Reaction&& reaction, std::initializer_list<Reactant> catalysts,
    ↪double rate) {
            reaction.rate = rate;
            reaction.catalysts = catalysts;

            // Add to vessel reactions
            reactions.push_back(reaction);

            return reaction;
        }

        Reaction operator()(Reaction&& reaction, Reactant catalyst, double_t rate) {
            reaction.rate = rate;
            reaction.catalysts = {catalyst};

            // Add to vessel reactions
            reactions.push_back(reaction);

            return reaction;
        }


        Reactant& environment() {
            if (reactants.contains("__env__")) {
               return reactants.get("__env__");
            }

            auto newReactant = Reactant("__env__", 0, 0);

            reactants.put(newReactant.name, newReactant);

            return reactants.get(newReactant.name);
        }
```

```
146
147         // Requirement 2 network graph
148         void visualize_reactions(const std::string& filename);
149
150         // Requirement 10 optimized algorithm
151         std::shared_ptr<SimulationTrajectory> do_simulation2(double_t end_time,
    ↪simulation_monitor& monitor = EMPTY_SIMULATION_MONITOR);
152
153         // Requirement 4 simulation
154         std::shared_ptr<SimulationTrajectory> do_simulation(double_t end_time,
    ↪simulation_monitor& monitor = EMPTY_SIMULATION_MONITOR);
155
156         // Requirement 8 parallelization
157         std::vector<std::shared_ptr<SimulationTrajectory>> do_multiple_simulations(double_t
    ↪end_time, size_t simulations_to_run);
158
159         // Requirement 2 pretty print
160         friend std::ostream& operator<<(std::ostream& s, const Vessel& vessel);
161     };
162
163
164
165 }
166
167 #endif //SP_EXAM_PROJECT_SIMULATION_H
```

Listing 5: simulation.cpp

```
1  //
2  // Created by Mathias on 09-05-2021.
3  //
4
5  #include <iostream>
6  #include <utility>
7  #include "simulation.h"
8
9  namespace StochasticSimulation {
10
11
12     // Requirement 2
13     std::ostream &operator<<(std::ostream &s, const Vessel &vessel) {
14         s << "{" << std::endl;
15         for (const auto& reaction: vessel.reactions) {
16             s << "\t" << reaction;
17             if (&reaction != &vessel.reactions.back()) {
18                 s << ",";
19             }
20             s << std::endl;
21         }
22         return s << "}";
23     }
24
25     // Requirement 2
26     void Vessel::visualize_reactions(const std::string& filename) {
27         std::stringstream str;
28         SymbolTable<std::string> node_map{};
29
30         str << "digraph {" << std::endl;
31
32         auto i = 0;
33         for (auto& reactant: reactants.getMap()) {
34             if (reactant.second.name != "__env__") {
```

```
35                  node_map.put(reactant.second.name, "s" + std::to_string(i));
36
37                  str << node_map.get(reactant.second.name)
38                      << "[label=\"" << reactant.second.name <<
↪"\",shape=\"box\",style=\"filled\",fillcolor=\"cyan\"];" << std::endl;
39                  i++;
40              }
41          }
42
43          i = 0;
44          for (auto& reaction: reactions) {
45              std::string reaction_node{"r" + std::to_string(i)};
46
47              str << reaction_node << "[label=\"" << reaction.rate <<
↪"\",shape=\"oval\",style=\"filled\",fillcolor=\"yellow\"];" << std::endl;
48              if (reaction.catalysts.has_value()) {
49                  for (auto& catalyst: reaction.catalysts.value()) {
50                      str << node_map.get(catalyst.name) << " -> " << reaction_node << "
↪[arrowhead=\"tee\"];" << std::endl;
51                  }
52              }
53              for (auto& reactant: reaction.from) {
54                  if (reactant.name != "__env__") {
55                      str << node_map.get(reactant.name) << " -> " << reaction_node << ";" <<
↪std::endl;
56                  }
57              }
58              for (auto& product: reaction.to) {
59                  if (product.name != "__env__") {
60                      str << reaction_node << " -> " << node_map.get(product.name) << ";" <<
↪std::endl;
61                  }
62              }
63
64              i++;
65          }
66
67          str << "}";
68
69          std::ofstream dotfile;
70          dotfile.open(filename + ".dot");
71          dotfile << str.str();
72          dotfile.close();
73
74          std::stringstream command_builder;
75          command_builder << "dot -Tpng -o " << filename << " " << filename << ".dot";
76          system(command_builder.str().c_str());
77      }
78
79      // Requirement 10 alternative simulation
80      std::shared_ptr<SimulationTrajectory> Vessel::do_simulation2(double_t end_time,
↪simulation_monitor &monitor) {
81          SimulationTrajectory trajectory{};
82          double_t t{0};
83
84          auto thread_id = std::this_thread::get_id();
85          auto epoch = std::chrono::system_clock::now().time_since_epoch().count();
86          std::default_random_engine engine(epoch * (std::hash<std::thread::id>{}(thread_id)));
87
88          // Insert initial state
89          trajectory.insert(SimulationState{reactants, t});
```

```
90
91          while (t <= end_time) {
92              for (Reaction& reaction: reactions) {
93                  // New: using new compute delay function
94                  reaction.compute_delay2(trajectory.at(t), engine);
95              }
96
97              auto r = reactions.front();
98
99              // Select Reaction with min delay which is not -1
100             for (auto& reaction: reactions) {
101                 if (reaction.delay == -1) {
102                     continue;
103                 } else if (reaction.delay < r.delay) {
104                     r = reaction;
105                 } else if (r.delay == -1) {
106                     r = reaction;
107                 }
108             }
109
110             // Stop if we have no reactions to do, thus r.delay == -1
111             if (r.delay == -1) {
112                 break;
113             }
114
115             auto& last_state = trajectory.at(t);
116
117             t += r.delay;
118
119             SimulationState state{last_state.reactants, t};
120
121             if (
122                     std::all_of(r.from.begin(), r.from.end(), [&state](const Reactant& e){return
    ↪state.reactants.get(e.name).amount >= e.required;}) &&
123                     (
124                             !r.catalysts.has_value() ||
125                             std::all_of(r.catalysts.value().begin(), r.catalysts.value().end(),
    ↪[&state](const Reactant& e){return state.reactants.get(e.name).amount >= e.required;})
126                     )
127                     ) {
128                 for (auto& reactant: r.from) {
129                     state.reactants.get(reactant.name).amount -= reactant.required;
130                 }
131                 for (auto& reactant: r.to) {
132                     state.reactants.get(reactant.name).amount += reactant.required;
133                 }
134             }
135
136             trajectory.insert(std::move(state));
137
138             monitor.monitor(trajectory.at(t));
139         }
140
141         return std::make_shared<SimulationTrajectory>(std::move(trajectory));
142     }
143
144     // Requirement 4 simulation
145     std::shared_ptr<SimulationTrajectory> Vessel::do_simulation(double_t end_time,
    ↪simulation_monitor &monitor) {
146         SimulationTrajectory trajectory{};
147         double_t t{0};
```

```
148
149         auto thread_id = std::this_thread::get_id();
150         auto epoch = std::chrono::system_clock::now().time_since_epoch().count();
151         std::default_random_engine engine(epoch * (std::hash<std::thread::id>{}(thread_id)));
152
153         // Insert initial state
154         trajectory.insert(SimulationState{reactants, t});
155
156         while (t <= end_time) {
157             for (Reaction& reaction: reactions) {
158                 reaction.compute_delay(trajectory.at(t), engine);
159             }
160
161             auto r = reactions.front();
162
163             // Select Reaction with min delay which is not -1
164             for (auto& reaction: reactions) {
165                 if (reaction.delay == -1) {
166                     continue;
167                 } else if (reaction.delay < r.delay) {
168                     r = reaction;
169                 } else if (r.delay == -1 && reaction.delay != -1) {
170                     r = reaction;
171                 }
172             }
173
174             // Stop if we have no reactions to do, thus r.delay == -1
175             if (r.delay == -1) {
176                 break;
177             }
178
179             auto& last_state = trajectory.at(t);
180
181             t += r.delay;
182
183             SimulationState state{last_state.reactants, t};
184
185             if (
186                     std::all_of(r.from.begin(), r.from.end(), [&state](const Reactant& e){return
    ↪state.reactants.get(e.name).amount >= e.required;}) &&
187                     (
188                             !r.catalysts.has_value() ||
189                             std::all_of(r.catalysts.value().begin(), r.catalysts.value().end(),
    ↪[&state](const Reactant& e){return state.reactants.get(e.name).amount >= e.required;})
190                     )
191                     ) {
192                 for (auto& reactant: r.from) {
193                     state.reactants.get(reactant.name).amount -= reactant.required;
194                 }
195                 for (auto& reactant: r.to) {
196                     state.reactants.get(reactant.name).amount += reactant.required;
197                 }
198             }
199
200             trajectory.insert(std::move(state));
201
202             monitor.monitor(trajectory.at(t));
203         }
204
205         return std::make_shared<SimulationTrajectory>(std::move(trajectory));
206     }
```

```
207
208     // Requirement 8 multiple at same time
209     std::vector<std::shared_ptr<SimulationTrajectory>>
210     Vessel::do_multiple_simulations(double_t end_time, size_t simulations_to_run) {
211         std::vector<std::shared_ptr<SimulationTrajectory>> result{};
212         result.reserve(simulations_to_run);
213
214         auto cores = std::thread::hardware_concurrency();
215         int jobs = std::min(simulations_to_run, (cores - 1));
216         auto simulations_per_job = simulations_to_run / jobs;
217
218         auto futures =
↪std::vector<std::future<std::vector<std::shared_ptr<SimulationTrajectory>>>>{};
219
220         auto lambda = [&vessel = *this, &end_time](size_t to_run){
221             auto simulations = std::vector<std::shared_ptr<SimulationTrajectory>>{};
222             simulations.reserve(to_run);
223
224             auto new_vessel = Vessel(vessel);
225
226             for (int i = 0; i < to_run; ++i) {
227                 simulations.push_back(new_vessel.do_simulation(end_time));
228             }
229
230             return simulations;
231         };
232
233         for (int i = 0; i < jobs; ++i) {
234             futures.push_back(std::async(std::launch::async, lambda, simulations_per_job));
235         }
236         auto missing_simulations = simulations_to_run - (simulations_per_job * jobs);
237         if (missing_simulations != 0) {
238             futures.push_back(std::async(std::launch::async, lambda, missing_simulations));
239         }
240
241         for (auto& future: futures) {
242             auto future_result = future.get();
243             for (auto& res: future_result) {
244                 result.push_back(std::move(res));
245             }
246         }
247
248         return result;
249     }
250
251     // Private function for calculation interpolated value
252     double_t SimulationTrajectory::compute_interpolated_value(const std::string& key,
↪SimulationState& s0, SimulationState& s1, double_t x) {
253         return
254             s0.reactants.get(key).amount
255             + ((
256                     ( (double_t) s1.reactants.get(key).amount - (double_t)
↪s0.reactants.get(key).amount) /
257                     ( s1.time - s0.time )
258                ) * (x - s0.time));
259     }
260
261     // Requirement 9 compute mean trajectory
262     SimulationTrajectory
↪SimulationTrajectory::compute_mean_trajectory(std::vector<std::shared_ptr<SimulationTrajectory>>&
↪trajectories) {
```

```
263         auto average_delay = trajectories.front()->get_max_time() / trajectories.front()->size();
264
265         // Get a list of all keys
266         std::vector<std::string> reactant_keys{};
267         for (auto& reactant: trajectories.front()->begin()->second.reactants) {
268             reactant_keys.push_back(reactant.second.name);
269         }
270
271         // Find upper bound for mean trajectory
272         double_t upper_bound{-1.0};
273         for (auto& trajectory: trajectories) {
274             if (upper_bound == -1.0 || trajectory->get_max_time() < upper_bound) {
275                 upper_bound = trajectory->get_max_time();
276             }
277         }
278
279         SimulationTrajectory mean_trajectory{};
280
281         for (auto& trajectory: trajectories) {
282             auto iterator = trajectory->begin();
283             SimulationState& s0 = iterator->second;
284             iterator++;
285             SimulationState& s1 = iterator->second;
286
287             double_t t{0};
288
289             while((t + average_delay) <= upper_bound) {
290                 if (t >= s0.time) {
291                     if (t <= s1.time) {
292                         if (!mean_trajectory.contains(t)) {
293                             mean_trajectory.insert((SimulationState{{}, t}));
294                         }
295
296                         for (auto& key: reactant_keys) {
297                             auto interpolated_value =
↪SimulationTrajectory::compute_interpolated_value(key, s0, s1, t);
298
299                             auto& table = mean_trajectory.at(t).reactants;
300
301                             if (!table.contains(key)) {
302                                 Reactant reactant{key, 0.0};
303                                 table.put(key, reactant);
304                             }
305
306                             table.get(key).amount += interpolated_value;
307                         }
308
309                         t += average_delay;
310                     } else {
311                         s0 = s1;
312                         iterator++;
313
314                         if (iterator != trajectory->end()) {
315                             s1 = iterator->second;
316                         } else {
317                             break;
318                         }
319                     }
320                 }
321             }
322         }
```

```
323
324         for (double_t i = 0; (i + average_delay) <= upper_bound; i += average_delay) {
325             for (auto& key: reactant_keys) {
326                 mean_trajectory.at(i).reactants.get(key).amount /= trajectories.size();
327             }
328         }
329
330         return std::move(mean_trajectory);
331     }
332
333     // Requirement 6 output to csv which can then be turned into a graph via python script
334     void SimulationTrajectory::write_csv(const std::string &path) {
335         std::ofstream csv_file;
336         csv_file.open(path);
337
338         auto reactants = at(0).reactants;
339
340         for (auto& reactant : reactants) {
341             csv_file << reactant.second.name << ",";
342         }
343         csv_file << "time" << std::endl;
344
345         for (auto& state : *this) {
346             for (auto& reactant: reactants) {
347                 csv_file << state.second.reactants.get(reactant.second.name).amount << ",";
348             }
349             csv_file << state.second.time << std::endl;
350         }
351
352         csv_file.close();
353     }
354 }
```

Listing 6: data.h

```
1  //
2  // Created by Mathias on 11-05-2021.
3  //
4
5  #ifndef SP_EXAM_PROJECT_DATA_H
6  #define SP_EXAM_PROJECT_DATA_H
7
8  namespace StochasticSimulation {
9      class SimulationState;
10     struct Reaction;
11     class ReactantCollection;
12
13     struct Reactant {
14         std::string name;
15         double_t amount; // double to allow for mean values
16         size_t required{1};
17
18         Reactant(std::string name, size_t initial_amount):
19                 name(std::move(name)),
20                 amount(initial_amount)
21         {}
22
23         Reactant(std::string name, double_t initial_amount):
24                 name(std::move(name)),
25                 amount(initial_amount)
26         {}
27
```

```
28          Reactant(std::string name, size_t initial_amount, size_t required):
29                  name(std::move(name)),
30                  amount(initial_amount),
31                  required(required)
32          {}
33
34          ~Reactant() = default;
35
36          Reactant(const Reactant& a) {
37              name = a.name;
38              amount = a.amount;
39              required = a.required;
40          }
41
42          Reactant(Reactant&& a) {
43              name = std::move(a.name);
44              amount = std::move(a.amount);
45              required = std::move(a.required);
46          }
47
48          Reactant& operator=(Reactant&& a) {
49              name = std::move(a.name);
50              amount = std::move(a.amount);
51              required = std::move(a.required);
52
53              return *this;
54          }
55
56          Reactant& operator=(const Reactant& a) {
57              name = a.name;
58              amount = a.amount;
59              required = a.required;
60
61              return *this;
62          }
63
64          // Requirement 1 operator for DSEL
65          Reaction operator>>=(Reactant other);
66
67          // Requirement 1 operator for DSEL
68          Reaction operator>>=(ReactantCollection other);
69
70          // Requirement 1 operator for DSEL
71          ReactantCollection operator+(const Reactant& other);
72
73          bool operator<(const Reactant& other) const;
74
75          // Requirement 1 operator for DSEL
76          Reactant operator*(size_t req) {
77              required = req;
78              return *this;
79          }
80
81      };
82
83      class ReactantCollection: public std::set<Reactant> {
84      public:
85          using std::set<Reactant>::set;
86          // Requirement 1 operator for DSEL
87          Reaction operator>>=(Reactant other);
88          // Requirement 1 operator for DSEL
```

```
89          Reaction operator>>=(ReactantCollection other);
90      };
91
92      class Reaction {
93      public:
94          std::set<Reactant> from;
95          std::set<Reactant> to;
96          std::optional<std::vector<Reactant>> catalysts;
97          double_t rate{};
98          double_t delay{-1};
99
100         Reaction(std::set<Reactant> from, std::set<Reactant> to):
101                 from(from),
102                 to(to)
103         {}
104
105         Reaction(std::set<Reactant> from, std::set<Reactant> to, std::initializer_list<Reactant>
    ↪catalysts, double rate):
106                 from(from),
107                 to(to),
108                 catalysts(catalysts),
109                 rate(rate)
110         {}
111
112         Reaction(std::set<Reactant> from, std::set<Reactant> to, double rate):
113                 from(from),
114                 to(to),
115                 catalysts{},
116                 rate(rate)
117         {}
118
119         void compute_delay(SimulationState& state, std::default_random_engine& engine);
120         void compute_delay2(SimulationState& state, std::default_random_engine& engine);
121
122         friend std::ostream &operator<<(std::ostream &s, const Reaction &reaction);
123     };
124
125     struct SimulationState {
126     public:
127         SymbolTable<Reactant> reactants;
128         double_t time;
129
130         SimulationState(SymbolTable<Reactant> reactants, double_t time):
131             reactants{reactants},
132             time{time}
133         {};
134
135         SimulationState(const SimulationState&) = default;
136         SimulationState(SimulationState&&) = default;
137
138         SimulationState& operator=(const SimulationState &) = default;
139         SimulationState& operator=(SimulationState&&) = default;
140
141         ~SimulationState() = default;
142
143         friend std::ostream &operator<<(std::ostream &, const SimulationState &);
144     };
145
146 }
147
148 #endif //SP_EXAM_PROJECT_DATA_H
```

Listing 7: data.cpp

```cpp
//
// Created by Mathias on 11-05-2021.
//

#include <iostream>
#include <utility>
#include "simulation.h"

namespace StochasticSimulation {
    Reaction Reactant::operator>>=(StochasticSimulation::Reactant other) {
        return Reaction{{*this}, {std::move(other)}};
    }

    Reaction Reactant::operator>>=(ReactantCollection other) {
        return Reaction{{*this}, std::move(other)};
    }

    ReactantCollection Reactant::operator+(const Reactant& other) {
        return ReactantCollection{*this, other};
    }

    bool Reactant::operator<(const Reactant& other) const {
        return name < other.name;
    }

    Reaction ReactantCollection::operator>>=(Reactant other) {
        return Reaction{*this, {std::move(other)}};
    }

    Reaction ReactantCollection::operator>>=(ReactantCollection other) {
        return Reaction{*this, std::move(other)};
    }

    std::ostream &operator<<(std::ostream &s, const Reaction &reaction) {
        s << "{ ";
        for (const auto& reactant: reaction.from) {
            s << reactant.name << "+";
        }
        s << "\b" << " >>= ";
        if (reaction.catalysts.has_value()) {
            s << "(";
            for (const auto& catalyst: reaction.catalysts.value()) {
                s << catalyst.name << "+";
            }
            s << "\b" << ") ";
        }
        for (const auto& reactant: reaction.to) {
            s << reactant.name << "+";
        }
        s << "\b";

        return s << " - " << reaction.rate << " }";
    }

    void Reaction::compute_delay2(SimulationState& state, std::default_random_engine &engine) {
        size_t reactant_amount{1};
        size_t catalyst_amount{1};

        for (const Reactant& reactant: from) {
            auto amount = reactant.name == "__env__" ? 1 :
```

```
↪state.reactants.get(reactant.name).amount;
            reactant_amount *= amount;
        }
        // New: check if amount is 0 already
        if (reactant_amount == 0) {
            delay = -1;
            return;
        }

        if (catalysts.has_value()) {
            for (auto& catalyst: catalysts.value()) {
                catalyst_amount *= state.reactants.get(catalyst.name).amount;
            }
        }

        double_t rate_k = rate * reactant_amount * catalyst_amount;

        if (rate_k > 0) {
            delay = std::exponential_distribution<double_t>(rate_k)(engine);
        } else {
            delay = -1;
        }
    }

    void Reaction::compute_delay(SimulationState& state, std::default_random_engine &engine) {
        size_t reactant_amount{1};
        size_t catalyst_amount{1};

        for (const Reactant& reactant: from) {
            auto amount = reactant.name == "__env__" ? 1 :   ↙
↪state.reactants.get(reactant.name).amount;
            reactant_amount *= amount;
        }
        if (catalysts.has_value()) {
            for (auto& catalyst: catalysts.value()) {
                catalyst_amount *= state.reactants.get(catalyst.name).amount;
            }
        }

        double_t rate_k = rate * reactant_amount * catalyst_amount;

        if (rate_k > 0) {
            delay = std::exponential_distribution<double_t>(rate_k)(engine);
        } else {
            delay = -1;
        }
    }

    std::ostream &operator<<(std::ostream &s, const SimulationState& state) {
        s << "{" << std::endl
            << "time: " << state.time << "," << std::endl
            << "reactants: {" << std::endl;
        for(auto& pair: state.reactants) {
            s << pair.first << ": " << pair.second.amount << "," << std::endl;
        }

        s << "}";
        return s;
    }
}
```

Listing 8: simulation_monitor.h

```
//
// Created by Mathias on 11-05-2021.
//

#ifndef SP_EXAM_PROJECT_SIMULATION_MONITOR_H
#define SP_EXAM_PROJECT_SIMULATION_MONITOR_H

#include <functional>
#include "data.h"

namespace StochasticSimulation {

    // Requirement 7 classes for generic system state monitors
    class simulation_monitor {
    public:
        virtual void monitor(SimulationState& state) = 0;
    };


    class empty_simulation_monitor: public simulation_monitor {
        void monitor(SimulationState &state) override {
          return;
        };
    };

    static auto EMPTY_SIMULATION_MONITOR = empty_simulation_monitor{};

    class basic_simulation_monitor: public simulation_monitor {
    private:
        const std::function<void(SimulationState&)> monitor_function;
    public:
        basic_simulation_monitor(const std::function<void(SimulationState&)>& monitor_func):
            simulation_monitor{},
            monitor_function{monitor_func}
        {}

        void monitor(SimulationState& state) override {
            monitor_function(state);
        }
    };
}

#endif //SP_EXAM_PROJECT_SIMULATION_MONITOR_H
```

Listing 9: SymbolTable.h

```
//
// Created by Mathias on 10-05-2021.
//

#ifndef SP_EXAM_PROJECT_SYMBOLTABLE_H
#define SP_EXAM_PROJECT_SYMBOLTABLE_H

#include <unordered_map>
#include <string>
#include <stdexcept>
#include <utility>
#include <iterator>

namespace StochasticSimulation {
```

```
15
16      // Requirement 3 generic symbol table
17      struct SymbolTableException : public std::exception
18      {
19          std::string message;
20      public:
21          explicit SymbolTableException(std::string message): message(std::move(message))
22          {}
23
24          [[nodiscard]] const char* what() const override
25          {
26              return message.c_str();
27          }
28      };
29
30      template<typename T>
31      class SymbolTable {
32          using map_type = std::unordered_map<std::string, T>;
33      private:
34          map_type map{};
35      public:
36          using iterator = typename map_type::iterator;
37          using const_iterator = typename map_type::const_iterator;
38
39          SymbolTable<T>() = default;
40
41          SymbolTable<T>(const SymbolTable<T>& a) {
42              map = a.map;
43          };
44
45          SymbolTable<T>(SymbolTable<T>&& a) {
46              map = std::move(a.map);
47          };
48
49          ~SymbolTable() = default;
50
51          SymbolTable<T>& operator=(const SymbolTable& a) {
52              map = a.map;
53              return *this;
54          };
55
56          SymbolTable<T>& operator=(SymbolTable&& a) {
57              map = std::move(a.map);
58              return *this;
59          };
60
61          void put(const std::string& key, T value) {
62              if (!map.contains(key)) {
63                  map.insert_or_assign(key, value);
64              } else {
65                  throw SymbolTableException("Key " + key + " already used");
66              }
67          }
68
69          T& get(const std::string& key) {
70              try {
71                  return map.at(key);
72              } catch (std::out_of_range& e) {
73                  throw SymbolTableException("Key " + key + " was not found");
74              }
75          }
```

```
76
77          const T& get(const std::string& key) const {
78              try {
79                  return map.at(key);
80              } catch (std::out_of_range& e) {
81                  throw SymbolTableException("Key " + key + " was not found");
82              }
83          }
84
85          bool contains(const std::string& key) {
86              return map.contains(key);
87          }
88
89          std::unordered_map<std::string, T> getMap() {
90              return map;
91          }
92
93          iterator begin() {
94              return map.begin();
95          }
96
97          iterator end() {
98              return map.end();
99          }
100
101         const_iterator begin() const {
102             return map.begin();
103         }
104
105         const_iterator end() const {
106             return map.end();
107         }
108
109     };
110 }
111
112 #endif //SP_EXAM_PROJECT_SYMBOLTABLE_H
```

Listing 10: Results

```
Pretty-print Reactions:

Introduction:
{
    { A+B >>= (D) C - 0.001 }
}

Covid:
{
        { S >>= (I) E - 7.74194e-05 },
        { E >>= I - 0.196078 },
        { I >>= R - 0.322581 },
        { I >>= H - 0.000290061 },
        { H >>= R - 0.0988142 }
}

Carcadian Rythm:
{
        { A+DA >>= D_A - 1 },
        { D_A >>= A+DA - 50 },
        { A+DR >>= D_R - 1 },
        { D_R >>= A+DR - 100 },
```

```
        { D_A >>= D_A+MA - 500 },
        { DA >>= DA+MA - 50 },
        { D_R >>= D_R+MR - 50 },
        { DR >>= DR+MR - 0.01 },
        { MA >>= A+MA - 50 },
        { MR >>= MR+R - 5 },
        { A+R >>= C - 2 },
        { C >>= R - 1 },
        { A >>= __env__ - 1 },
        { R >>= __env__ - 0.2 },
        { MA >>= __env__ - 10 },
        { MR >>= __env__ - 0.5 }
}

Carcadian Rythm alternative:
{
        { A+DA >>= D_A - 1 },
        { D_A >>= A+DA - 50 },
        { A+DR >>= D_R - 1 },
        { D_R >>= A+DR - 100 },
        { __env__ >>= (D_A) MA - 500 },
        { __env__ >>= (DA) MA - 50 },
        { __env__ >>= (D_R) MR - 50 },
        { __env__ >>= (DR) MR - 0.01 },
        { __env__ >>= (MA) A - 50 },
        { __env__ >>= (MR) R - 5 },
        { A+R >>= C - 2 },
        { C >>= R - 1 },
        { A >>= __env__ - 1 },
        { R >>= __env__ - 0.2 },
        { MA >>= __env__ - 10 },
        { MR >>= __env__ - 0.5 }
}


Example output from monitoring hospitalized (not the one on the graph)
Max hospitalized: 3
Mean hospitalized: 0.551814


Benchmarks:
Benchmarking with circadian rhythm example (max_time=100) (30 times each)
Simulation 1 mean time (nanoseconds): 117913398
Simulation 2 mean time (nanoseconds): 17683541
```

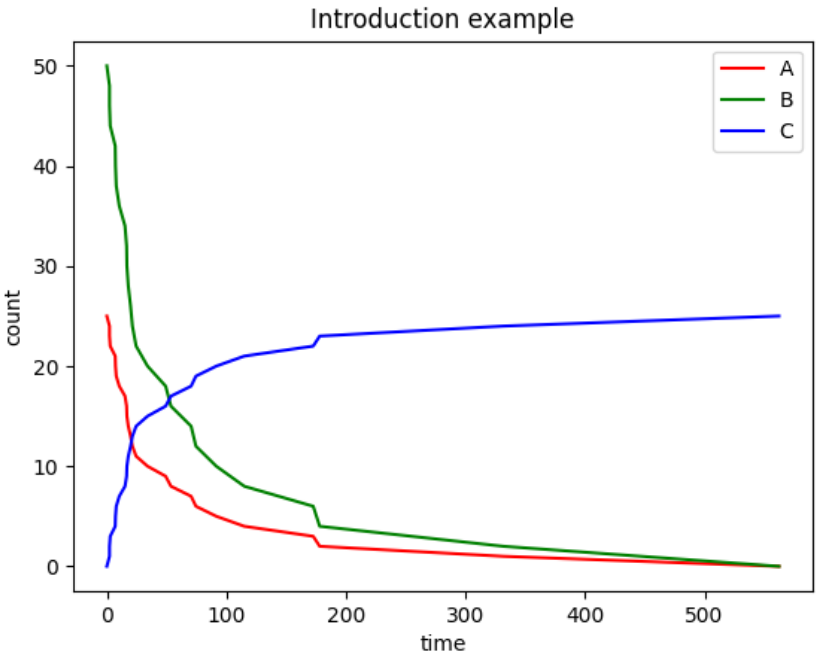

Figure 1: A(0)=25, B(0)=50, D=1

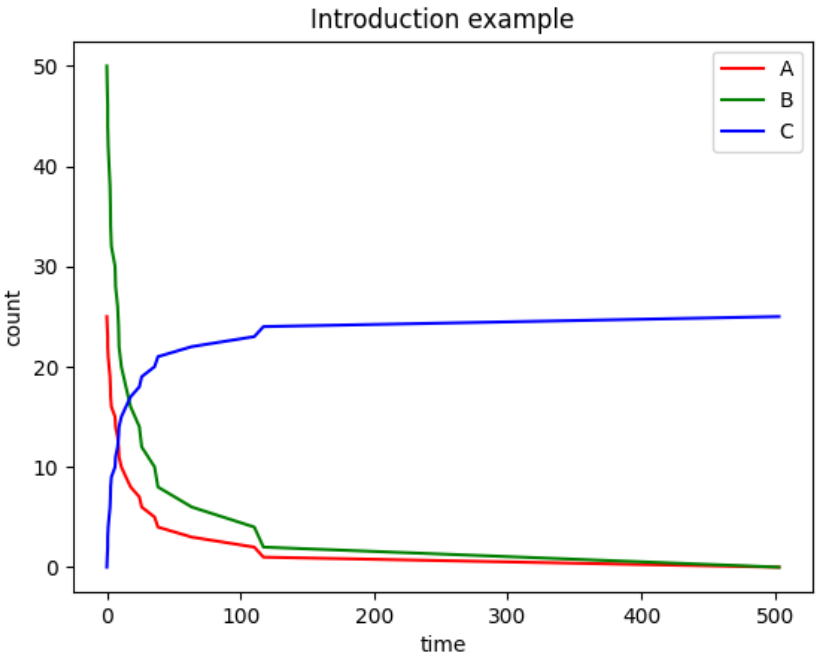

Figure 2: A(0)=25, B(0)=50, D=2

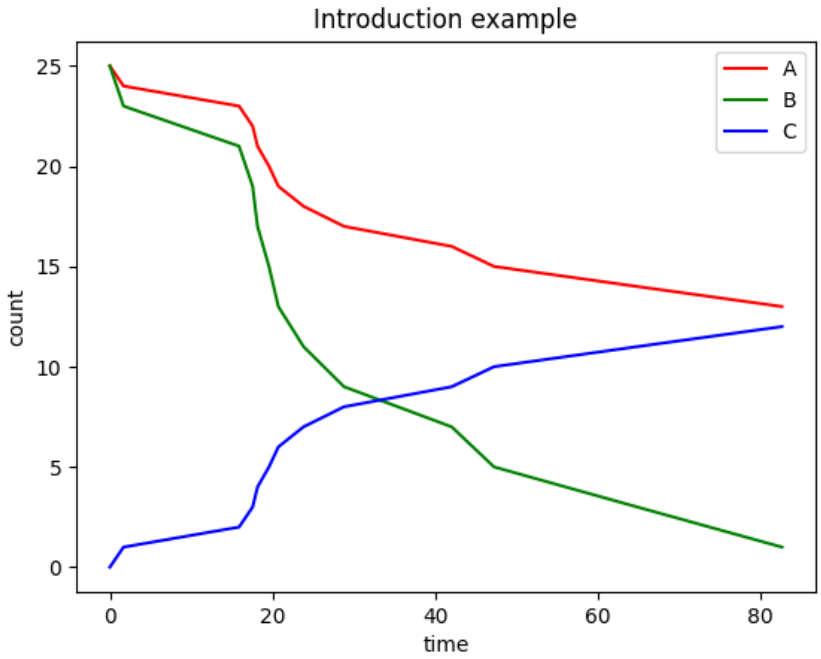

Figure 3: A(0)=25, B(0)=25, D=1

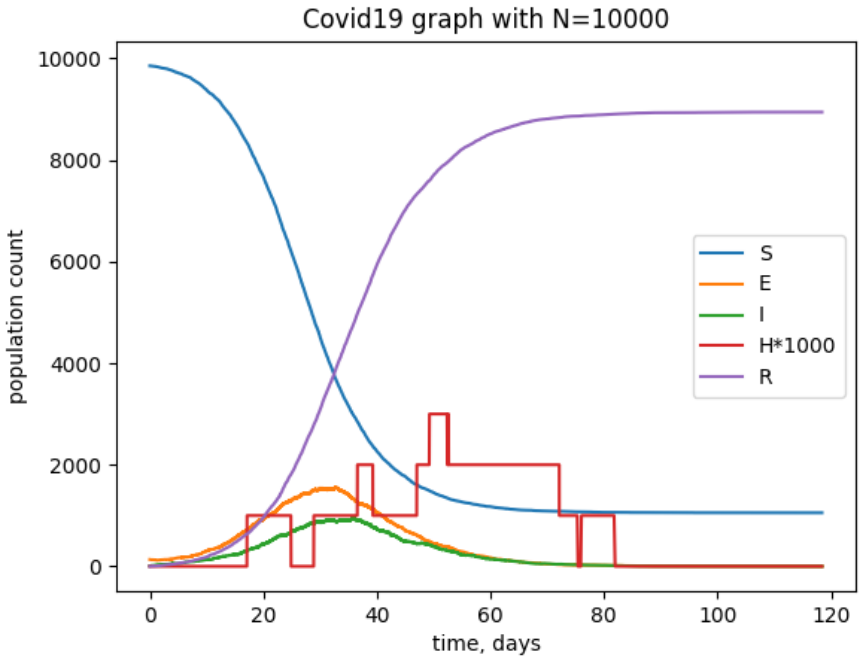

Figure 4: Sample covid trajectory

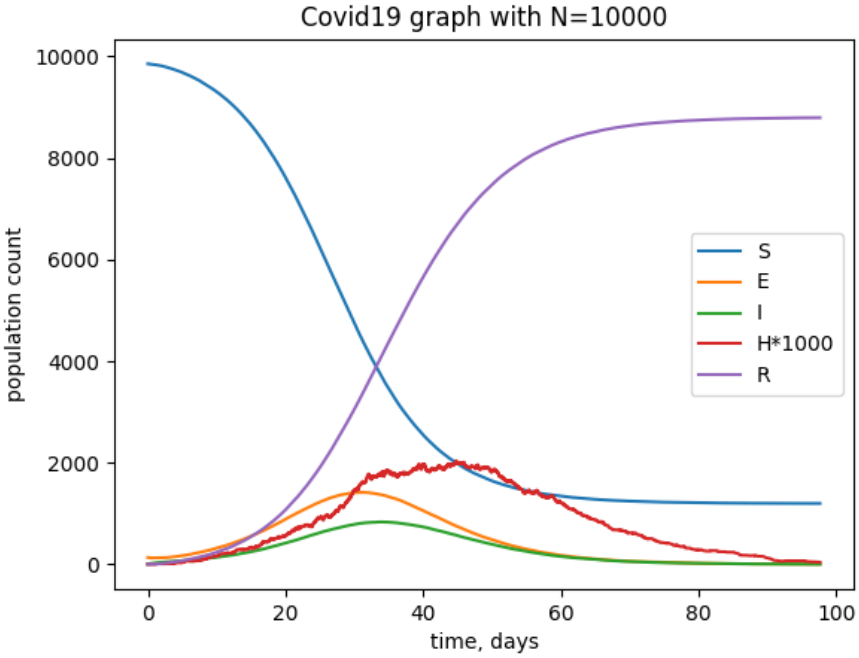

Figure 5: Mean covid trajectory of 30 simulations

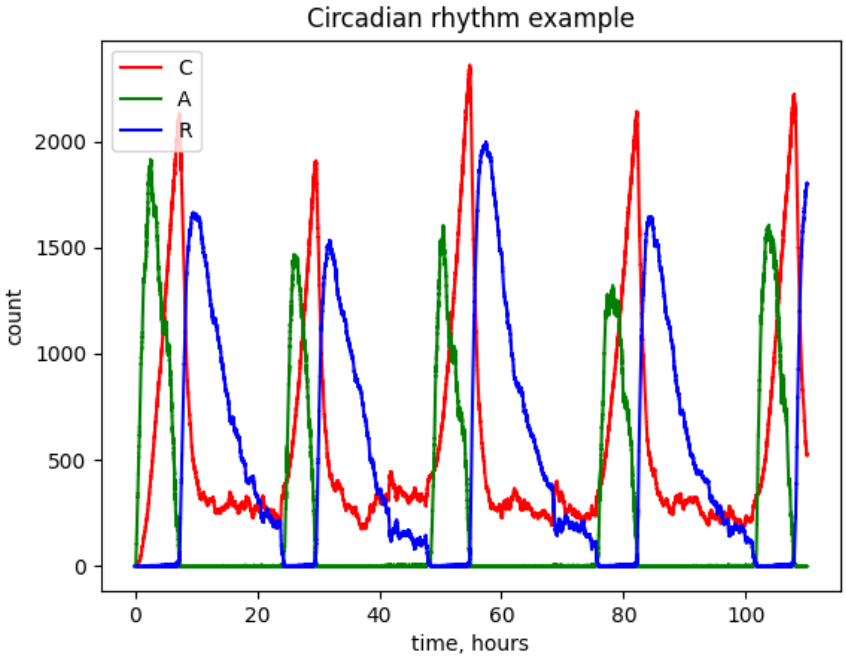

Figure 6: Sample circadian rythm trajectory

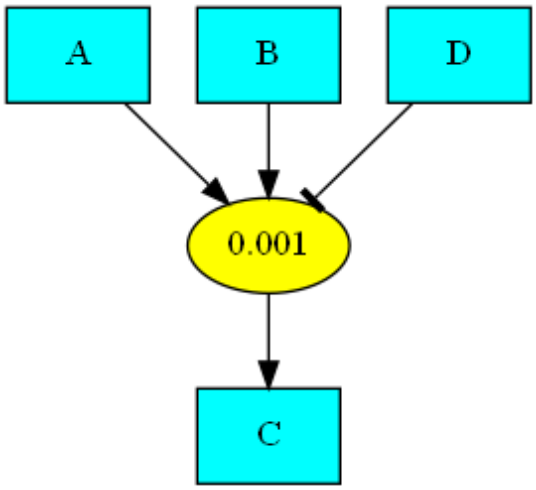

Figure 7: Intro reaction graph

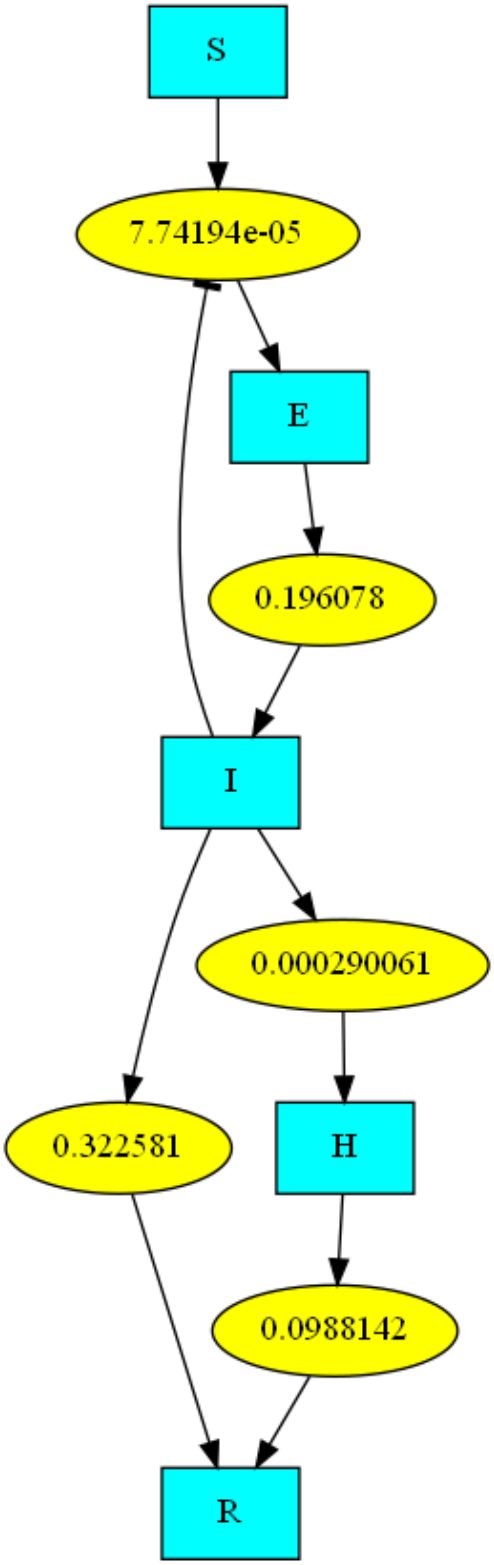

Figure 8: Covid reaction graph

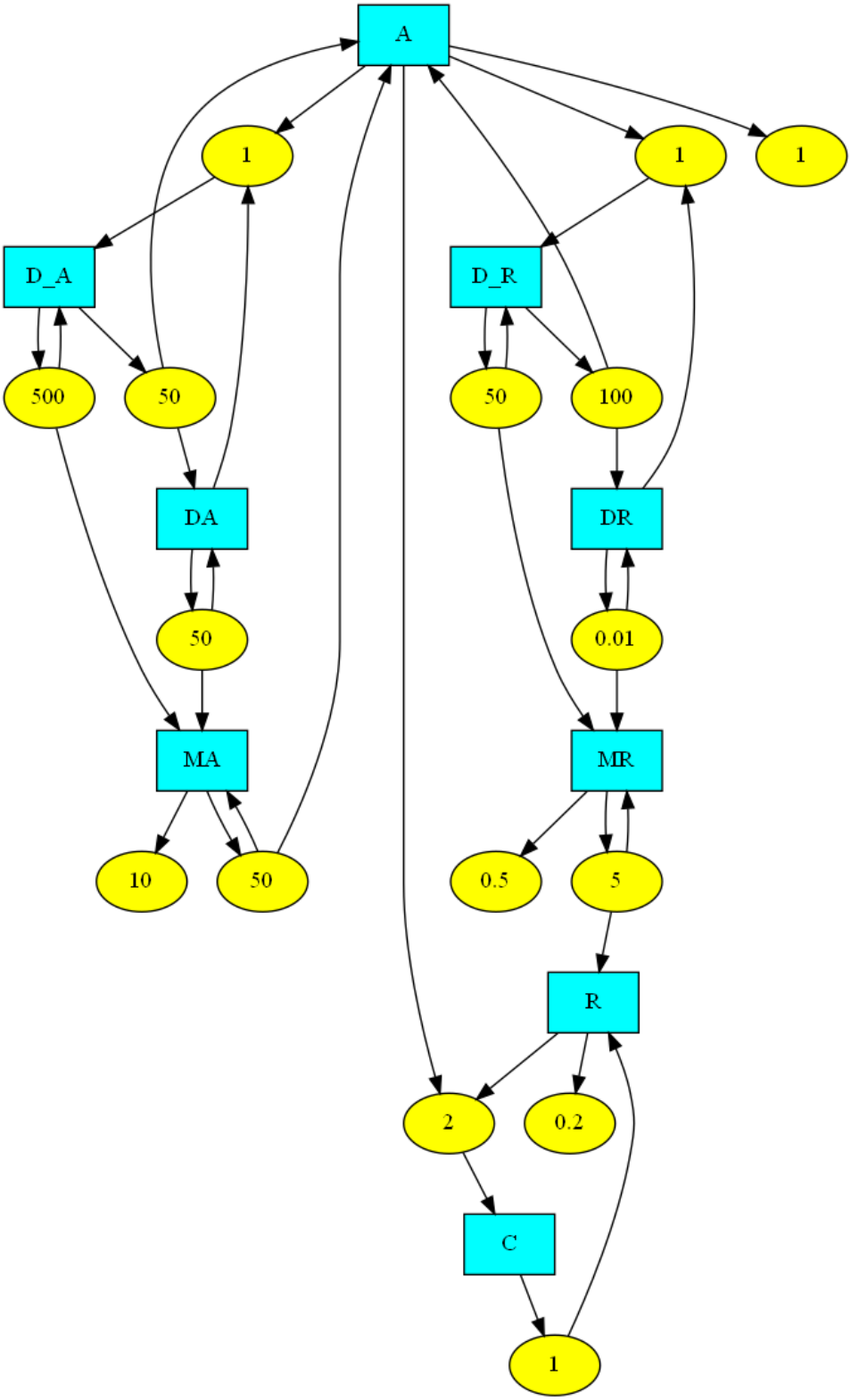

Figure 9: Circadian reaction graph

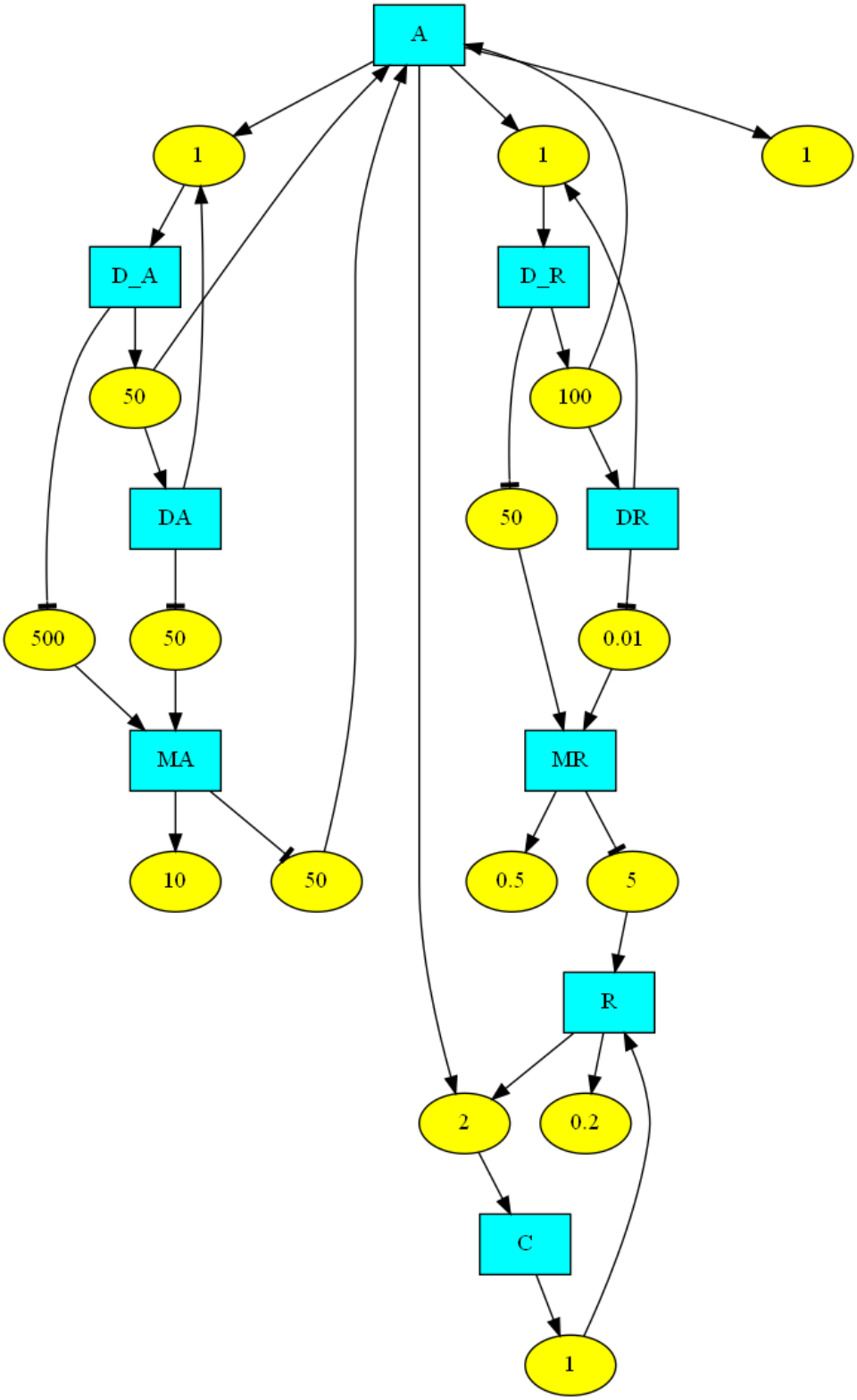

Figure 10: Circadian alternative reaction graph