

6.047/6.878/HST.507

Computational Biology: Genomes, Networks, Evolution

## Lecture 17

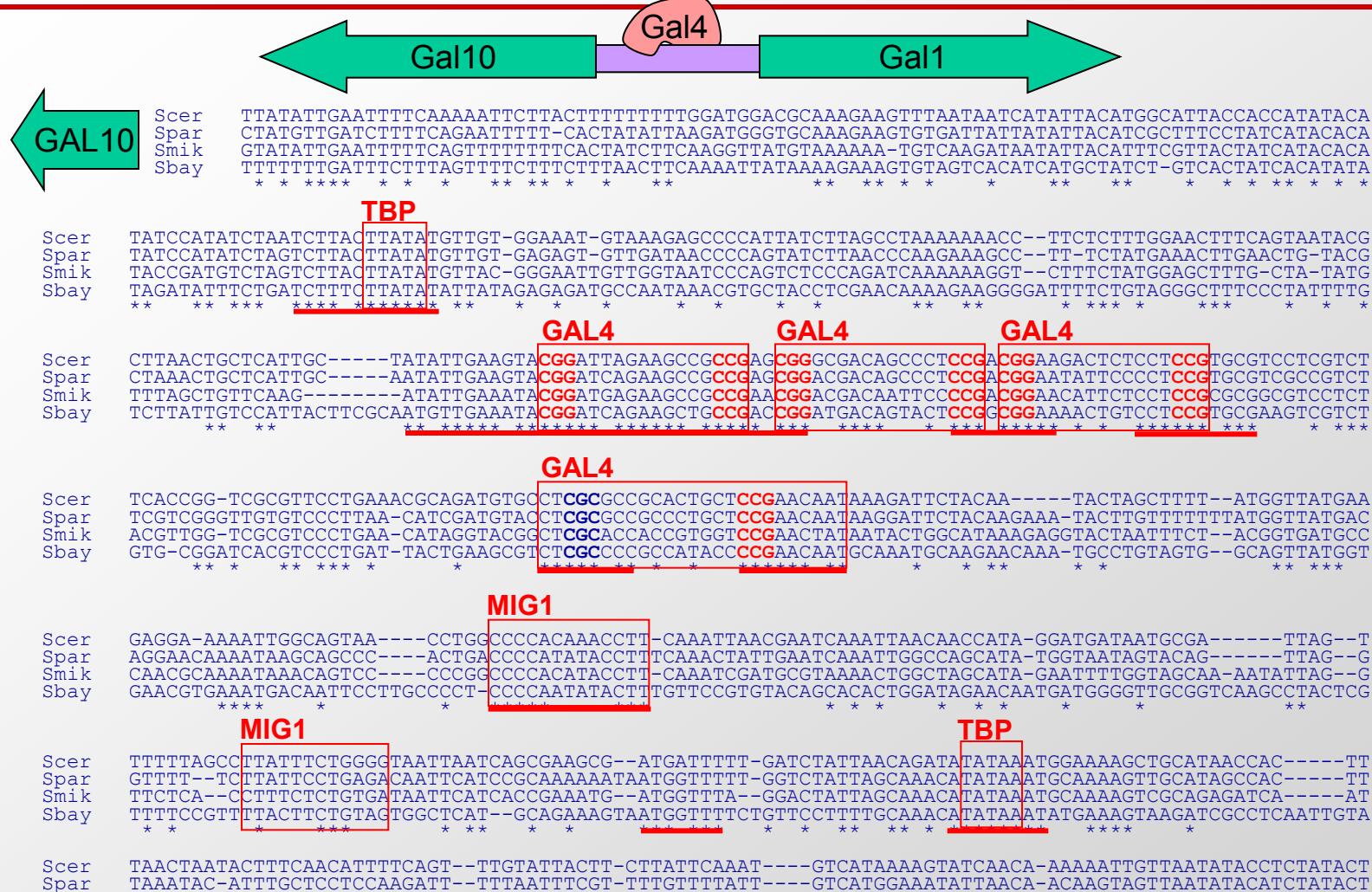
**Comparative genomics I:**

**Genome annotation using  
evolutionary signatures**

# Module V: Comparative genomics and evolution

- Today: Whole-genome comparative genomics
  - Evolutionary signatures for systematic genome annotation
- Next week: Phylogenetics and Phylogenomics
  - Distance-based and model-based phylogenetics approaches
  - Gene trees and species trees, reconciliation, coalescence
- Computational foundations:
  - Evolutionary rates and models of evolution
  - Dynamic programming on two-dimensional tree structures
  - Synteny-based alignment, genome assembly

# Key goal: Evolution preserves functional elements

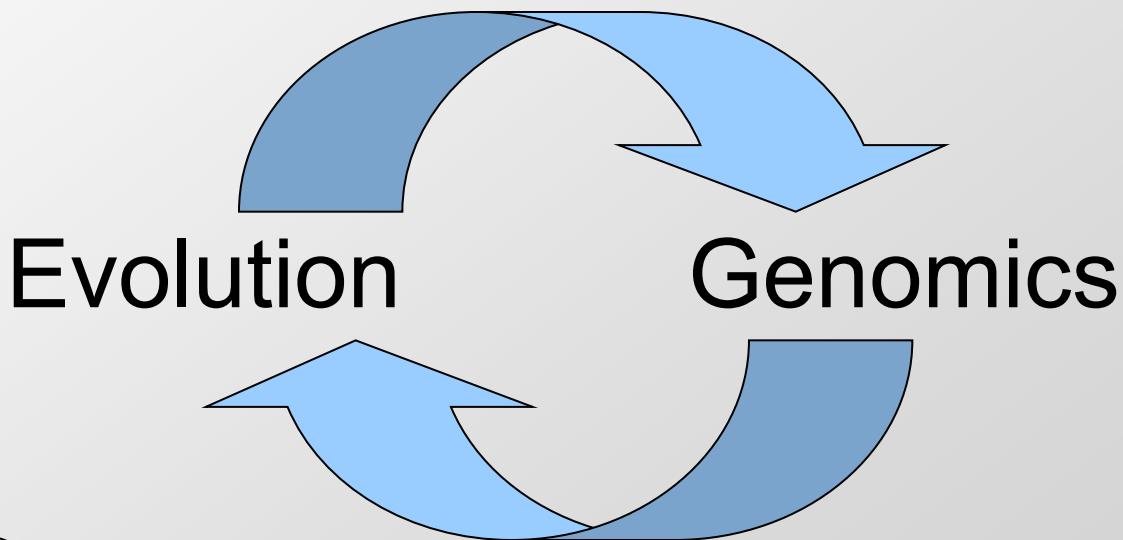


We can ‘read’ evolution to reveal functional elements

# Comparative Genomics

# Lecture 17 (Today):

# Using evolution to study genomes



# Lectures 18-19 (Thursday):

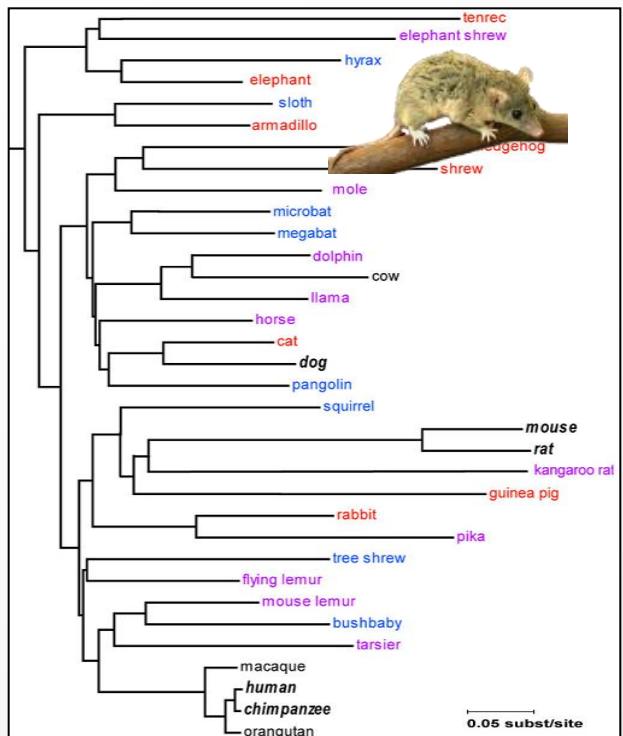
# Using genomics to study evolution

# **Comparative genomics I: Evolutionary signatures**

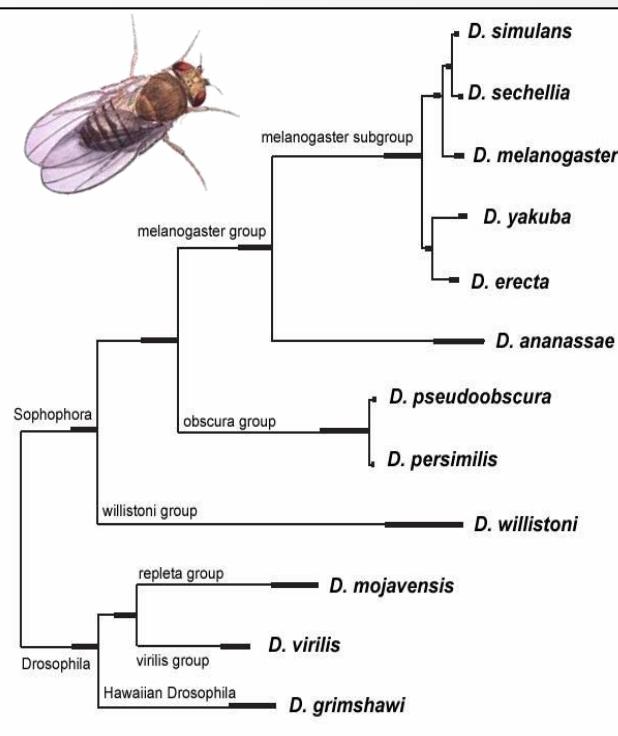
- **Nucleotide conservation: evolutionary constraint**
  - Purifying selection, neutral branch length, discovery power
  - Detect constrained elements: nucleotides, windows, HMM
  - Estimate fraction constrained: signal vs. background
- **Evolutionary signatures: focus on pattern of change**
  - Different functions  $\Leftrightarrow$  Characteristic patterns of evolution
- **Signatures of protein-coding genes**
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- **Signatures of microRNA genes**
  - Structural and evolutionary features of microRNAs
  - Combining features: decision trees, random forests
  - Sense/anti-sense miRNAs, mature/star arm cooperation
- **Measuring selection within the human lineage**

# Comparative genomics for genome annotation

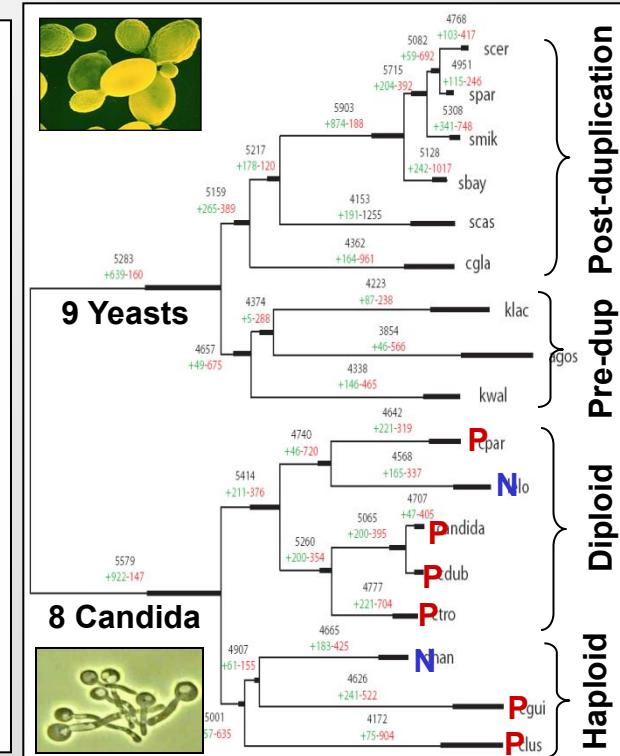
# 29 mammals



**12 flies**



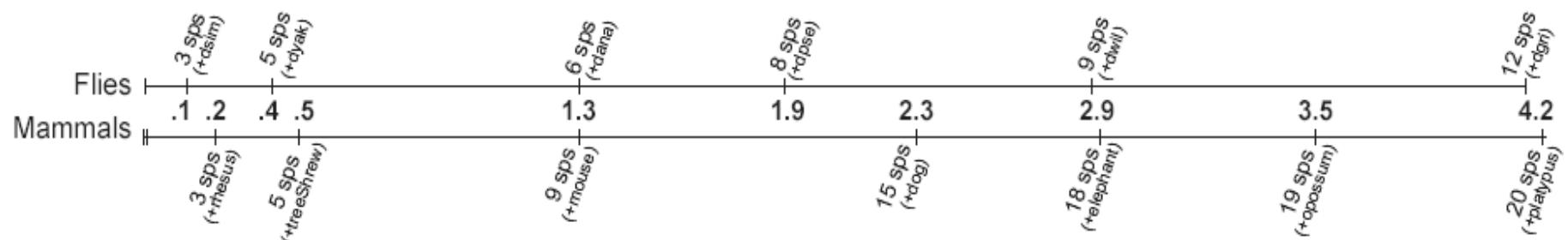
17 fungi



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- **Compare related species to discover functional elmts**
  - **Evolution process: random mutation, natural selection**
    - Non-functional regions: accumulate mutations, kept
    - Functional regions: accumulate mutations, decrease fitness
    - Evolutionary time: less fit organisms & their genes thin out

# Power of many closely related: total branch length



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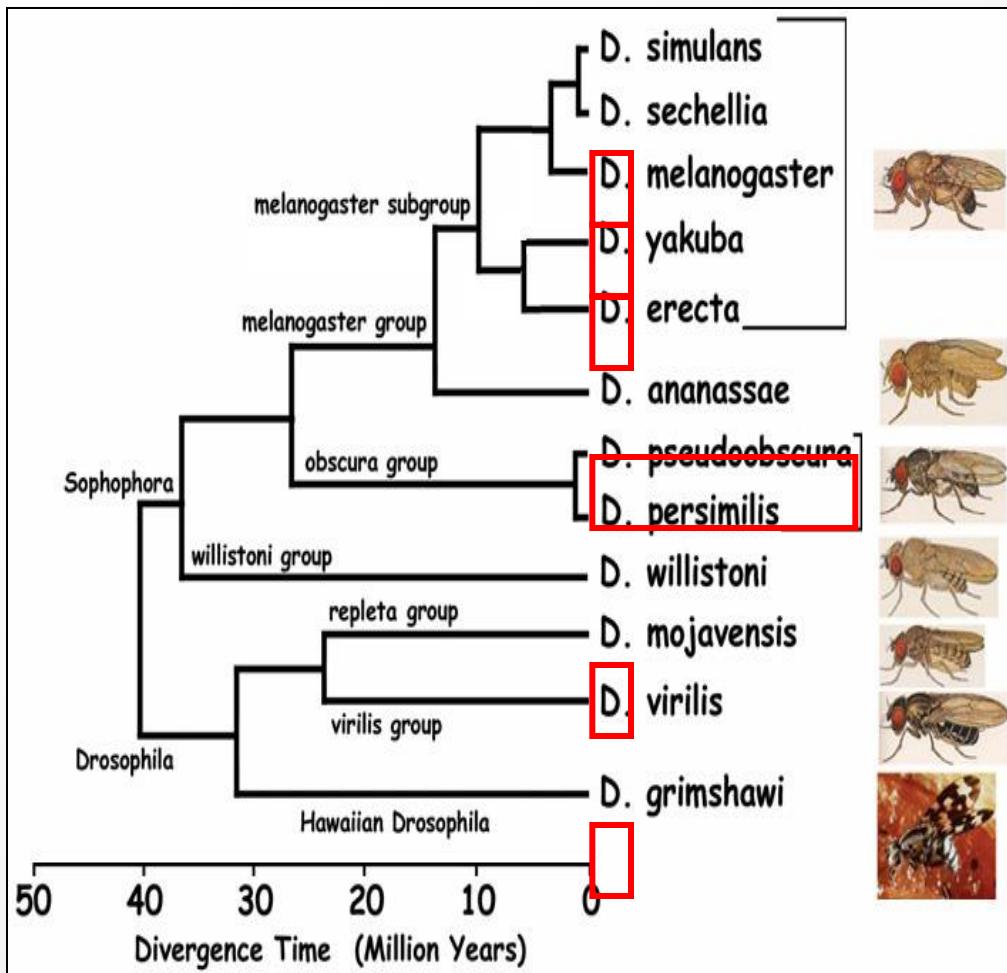
- **More branch length → more events → more power**
  - Goal: functional vs. non-functional based on # of mutations
  - Very close distances: no mutations in either region
  - Sufficient distance: ability to distinguish increases
  - Very far distances: functional regions no longer conserved
- **Many closely related species >> few distantly related**
  - For same total branch length: prefer many close species
  - Functional regions conserved for each pair of species
  - Non-functional regions accumulate noise **independently**
  - Analogy: recording a concert with multiple microphones

# **Comparative genomics I: Evolutionary signatures**

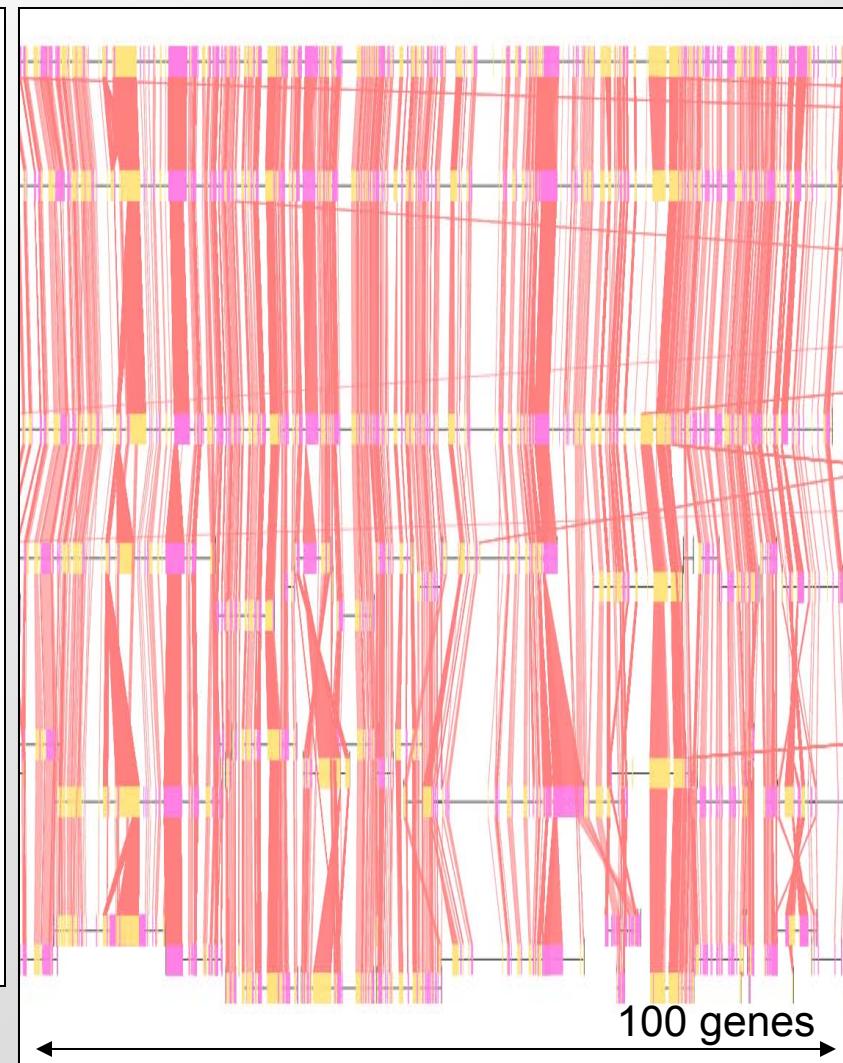
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# Genome-wide alignments reveal orthologous segments



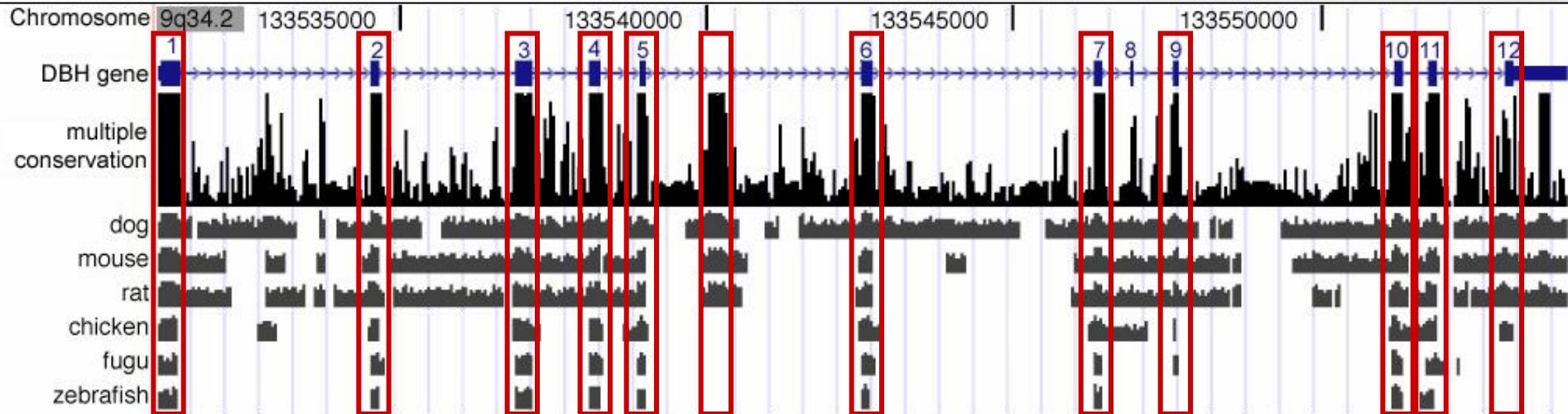
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- Genome-wide alignments span entire genome
- Comparative identification of functional elements

# Comparative genomics and evolutionary signatures



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- **Comparative genomics can reveal functional elements**
  - For example: exons are deeply conserved to mouse, chicken, fish
  - Many other elements are also strongly conserved: exons / regulatory?
- **Develop methods for estimating the level of constraint**
  - Count the number of edit operations, number of substitutions and gaps
  - Estimate the number of mutations (including estimate of back-mutations)
  - Incorporate information about neighborhood: conservation ‘windows’
  - Estimate the probability of a constrained ‘hidden state’: HMMs next week
  - Use phylogeny to estimate tree mutation rate, or ‘rejected substitutions’
  - Allow different portions of the tree to have different rates: phylogenetics

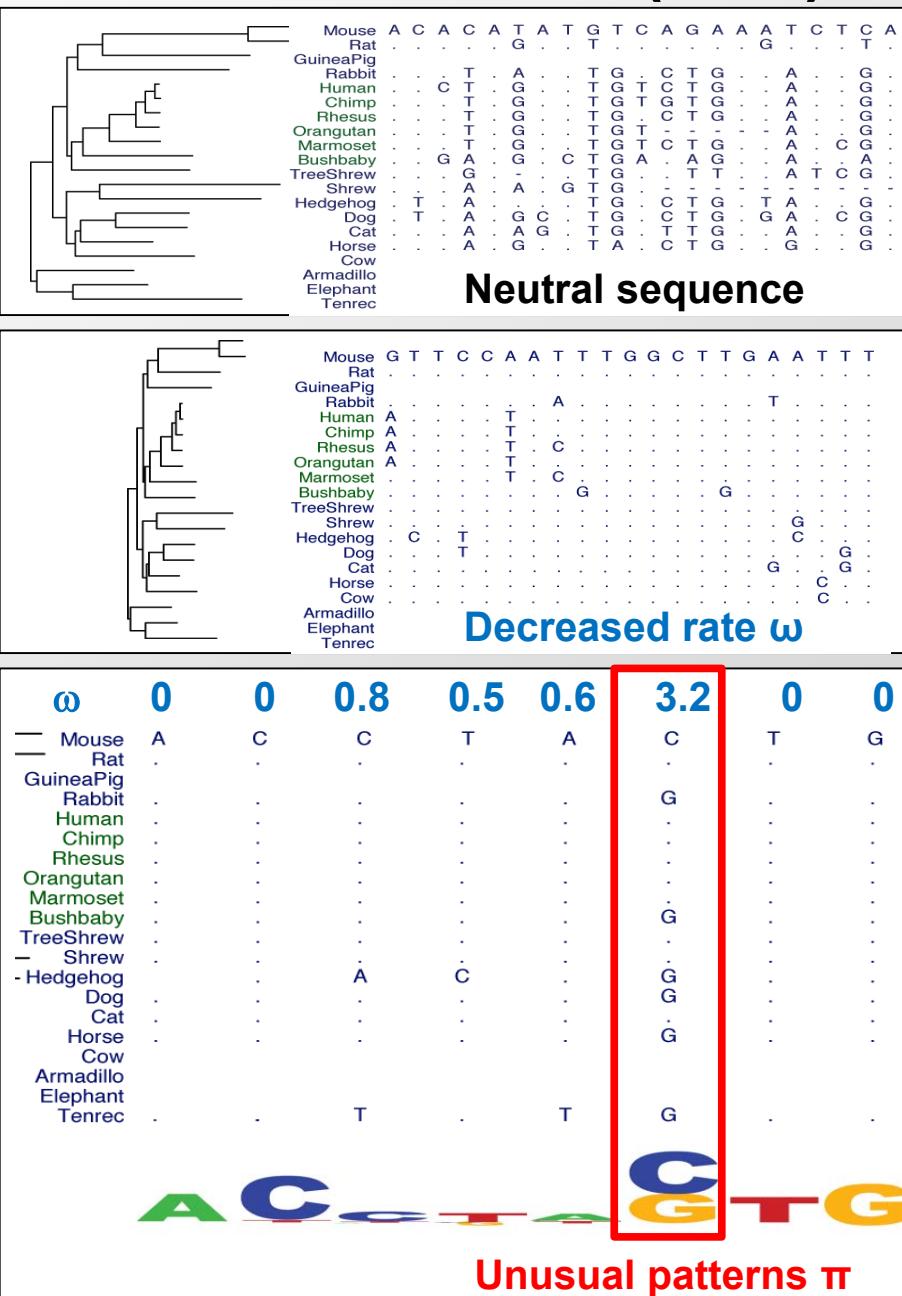
# Detecting rates and patterns of selection ( $\omega/\pi$ )

- ## Estimating intensity of constraint ( $\omega$ ):

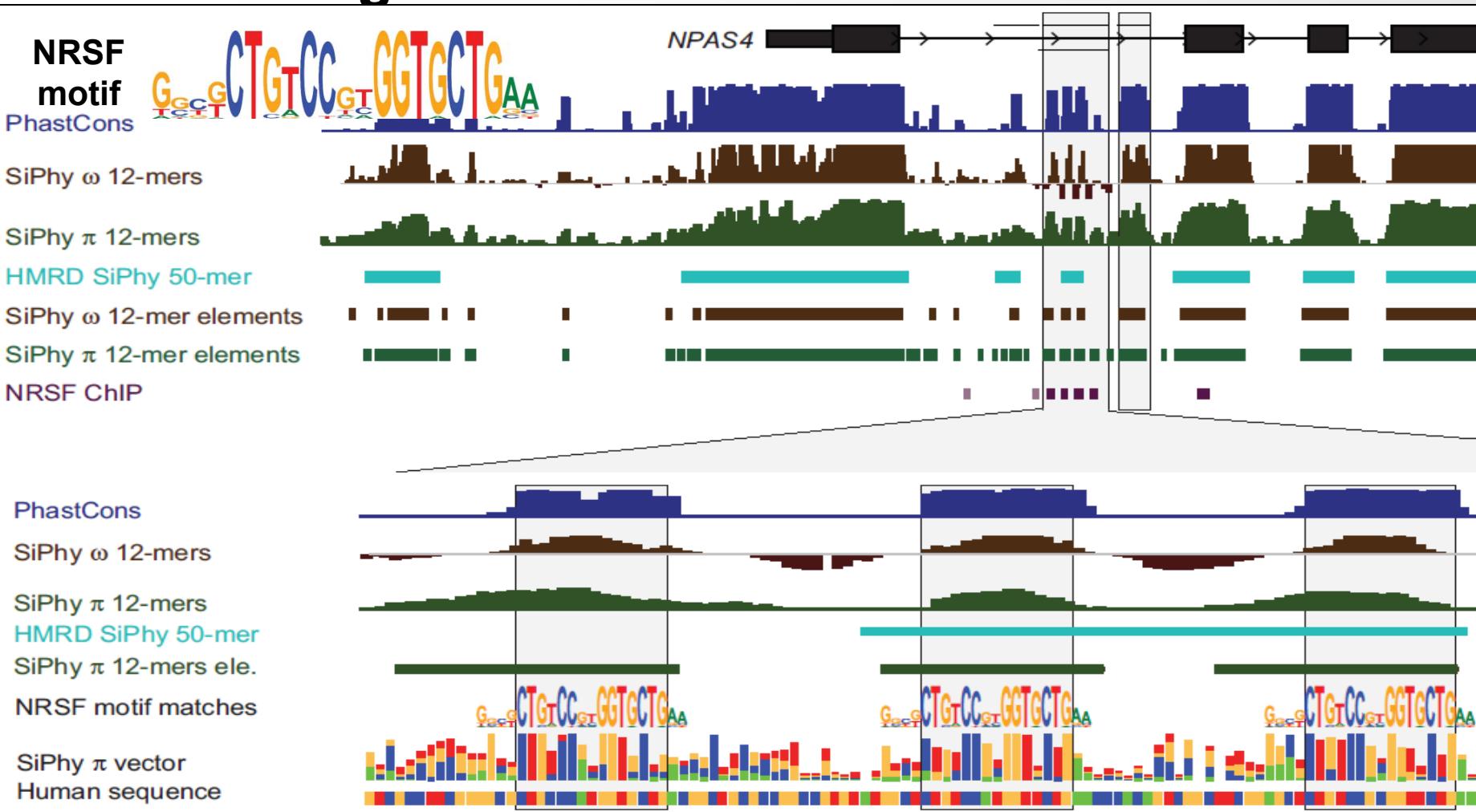
- Probabilistic model of substitution rate
  - Maximum Likelihood (ML) estimation of  $\omega$ 
    - Report rate  $\omega$
    - Report log odds score that non-neutral
  - Window-based vs. sitewise application

## Detect unusual substitution pattern ( $\pi$ ):

- Probabilistic model of stationary distribution that is different from background.
  - ML estimator ( $\pi$ ) of this vector
    - Report PWM for each k-mer in genome.
    - Report log odds score that non-neutral



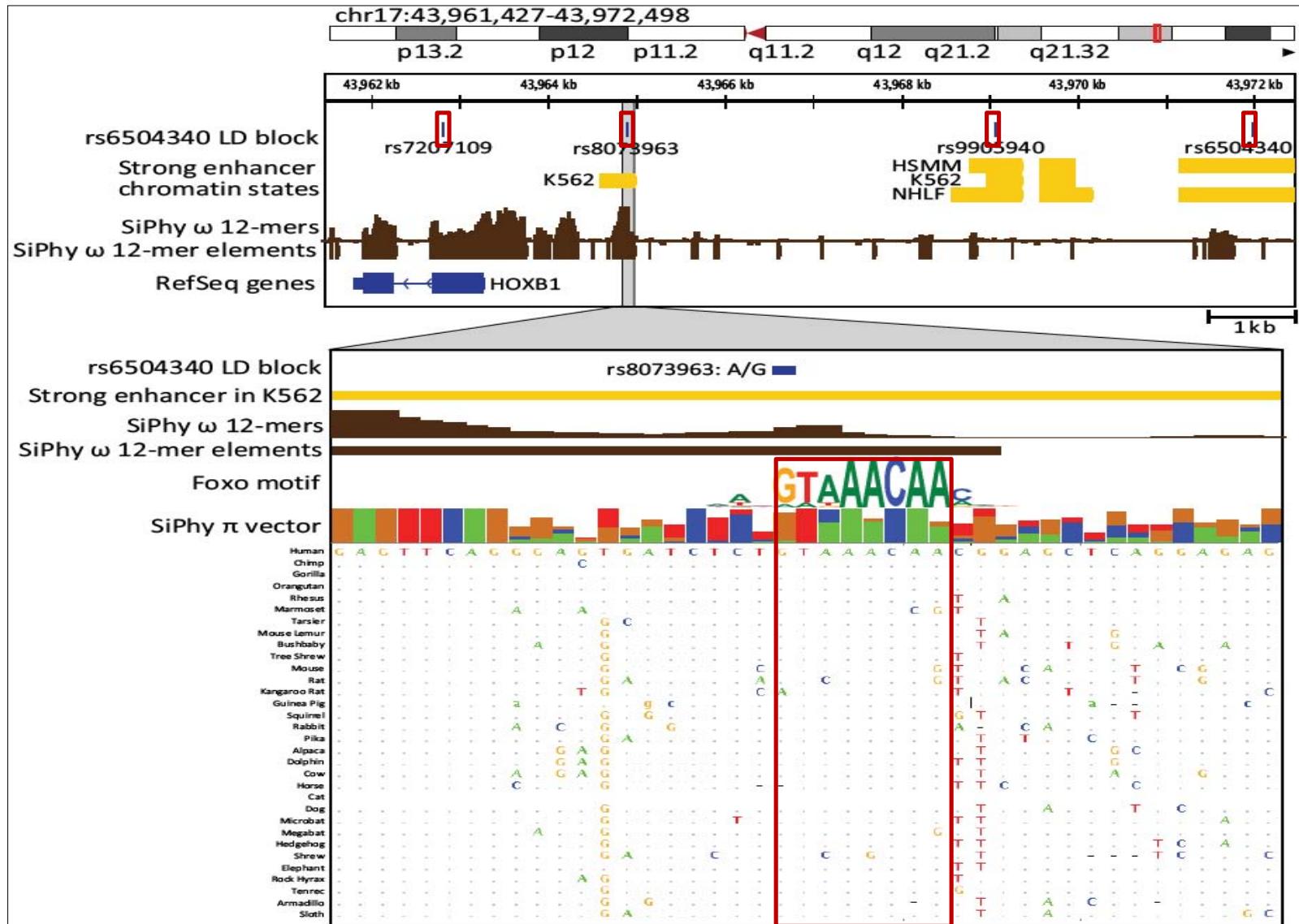
# Measuring constraint at individual nucleotides



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- Reveal individual transcription factor binding sites
- Within motif instances reveal position-specific bias
- More species: motif consensus directly revealed

# Detect SNPs that disrupt conserved regulatory motifs



- Functionally-associated SNPs enriched in states, constraint
- Prioritize candidates, increase resolution, disrupted motifs

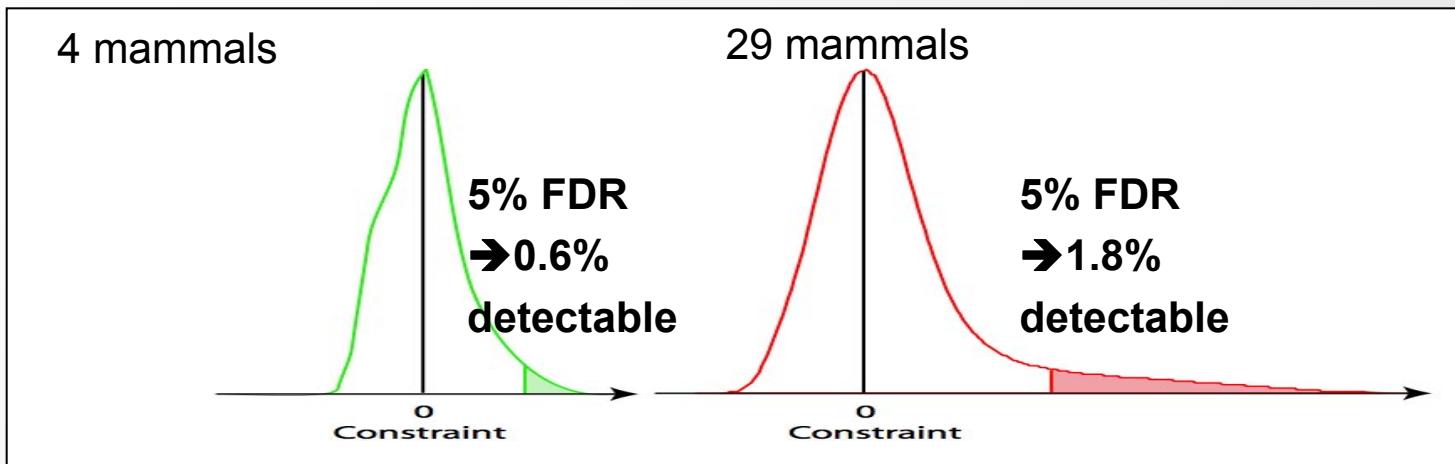
# **Comparative genomics I: Evolutionary signatures**

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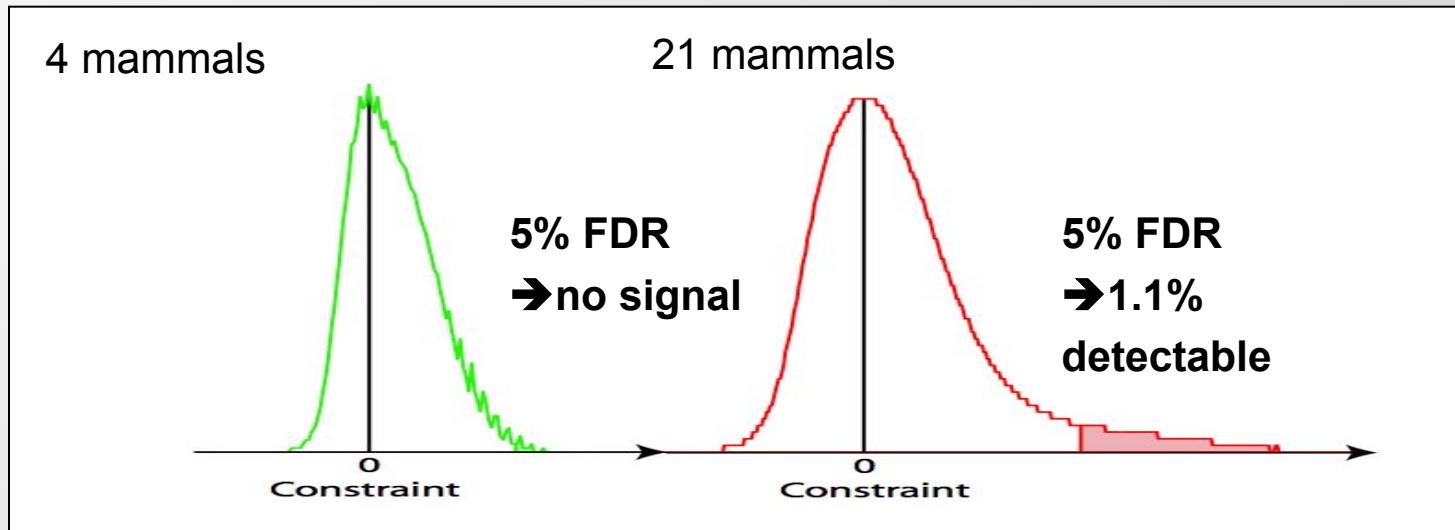
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# Estimating portion of the genome under constraint

Constraint calculated over a **50mer**

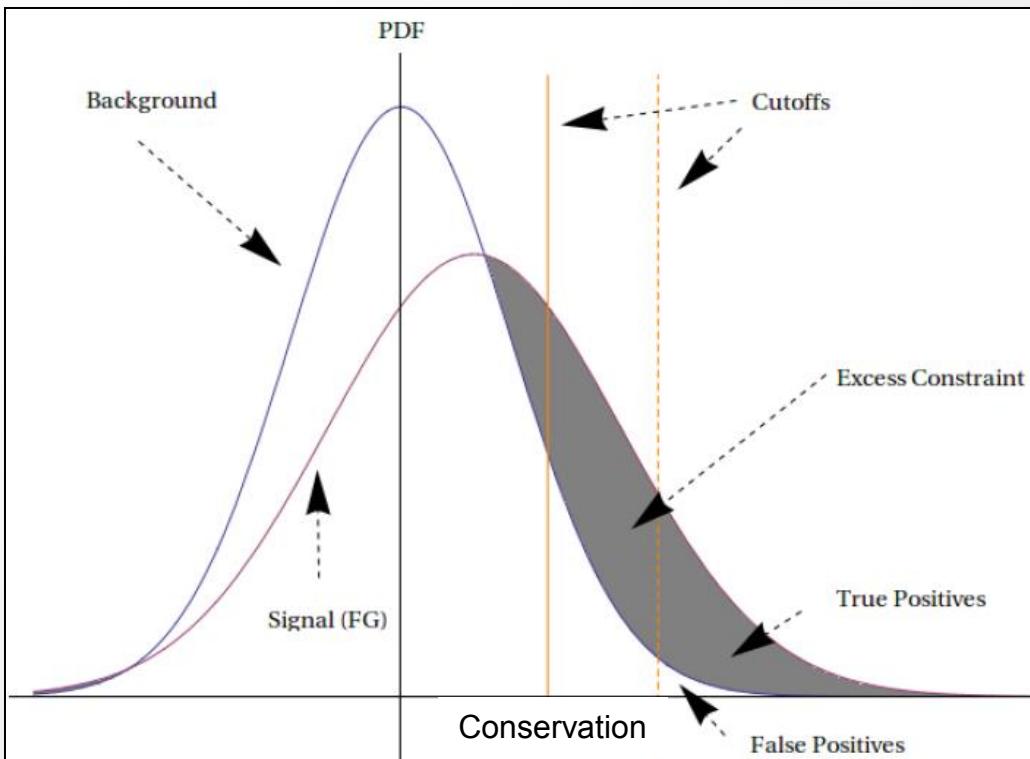


Constraint calculated over a **12mer**



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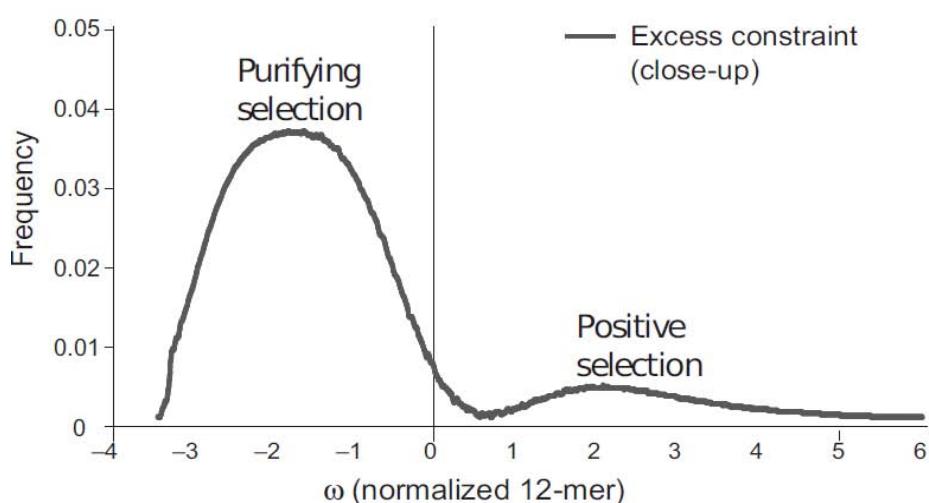
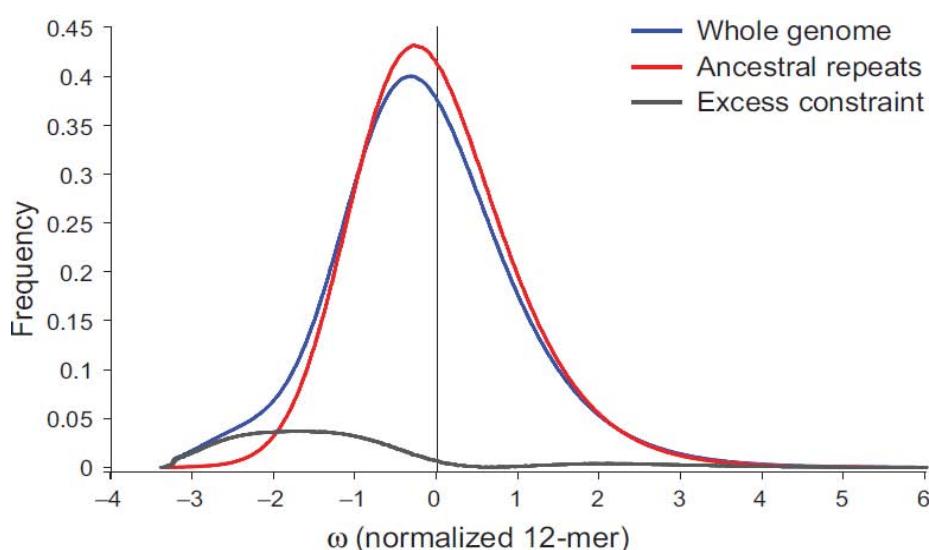
# Estimating total fraction under constraint



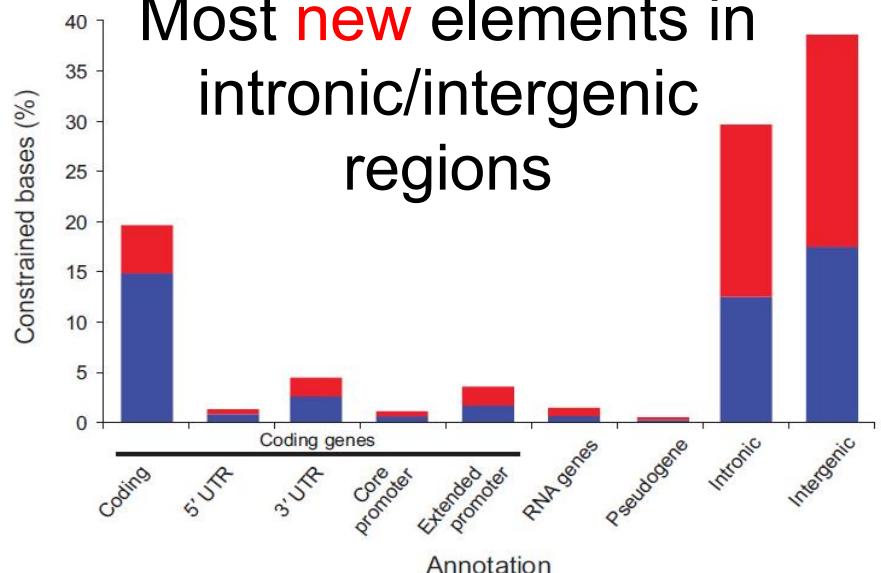
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- Actual distribution of conservation scores (Signal) vs. expected distribution if no constraint (Background).
- At any cutoff: true positives (TP) and false predictions (FP)
- Can't **detect** all constrained elements since curves overlap
- But we can **estimate** the total amount of excess constraint by integrating over entire area between the two curves

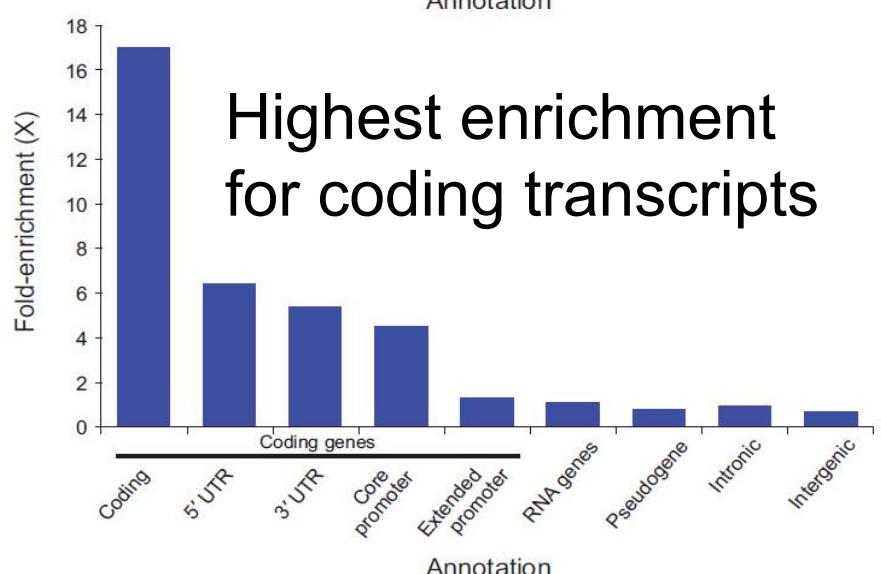
# Detection of evolutionarily constrained elements



Most **new** elements in  
intronic/intergenic  
regions

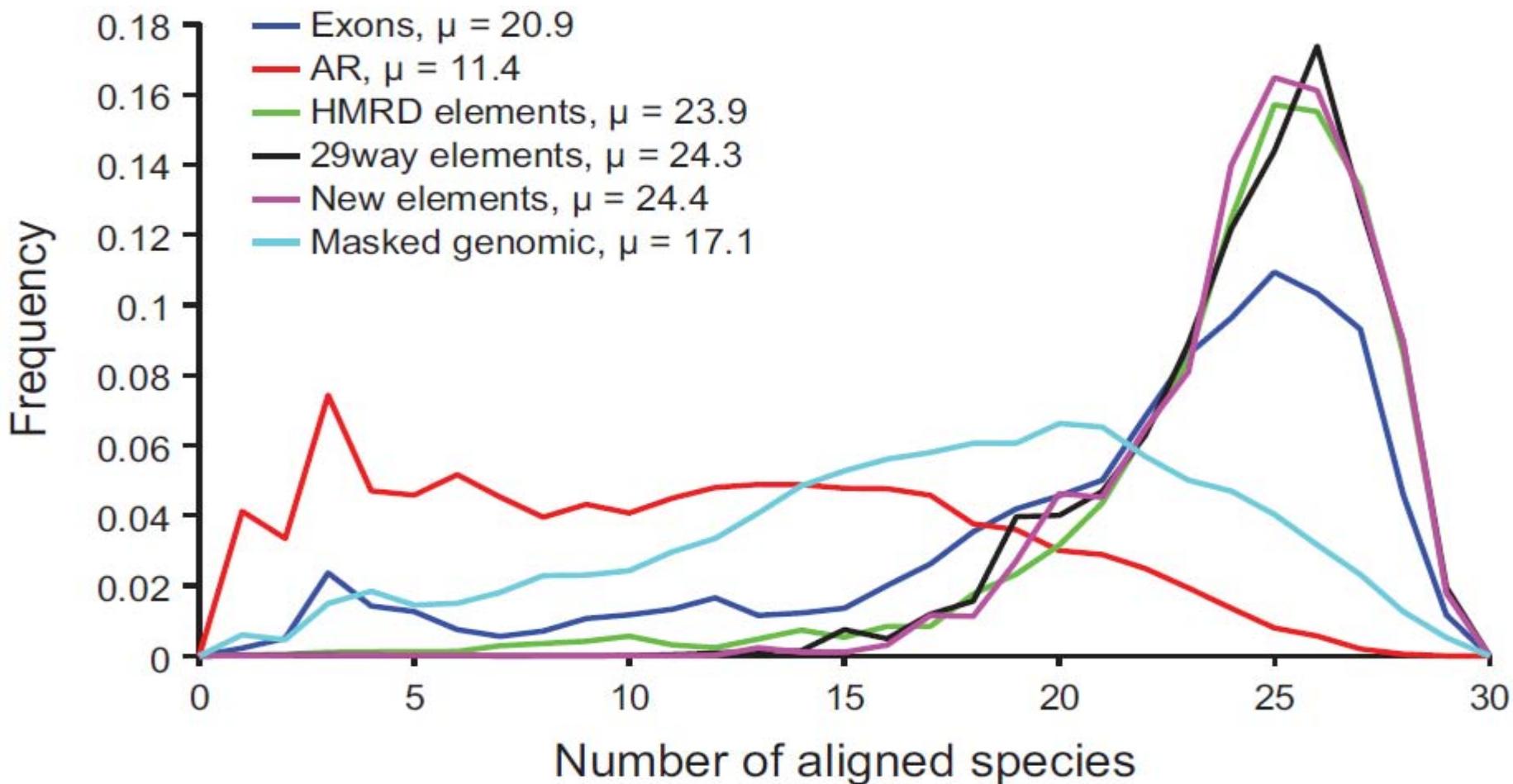


Highest enrichment  
for coding transcripts



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# Coverage depth higher in functional regions



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Challenges of low-coverage genomes: varying alignment depth  
Evidence of selection against deletions in functional regions

# Increase in power from HMRD to 29 mammals

	$\pi$ log-odds (12mers)	$\pi$ log-odds (50mers)	$\omega$ (12mers)	$\omega$ (50mers)
29 mammals	7.1/1.5/4.6	6.8/1.8/4.1	5.7/ 1.1/3.8	5.7/1.8/3.0
(HMRD) Human Mouse Rat Dog	4.2/0.0/0.0	5.3/0.1/0.3	4.5/0.0/0.0	5.1/0.6/1.7

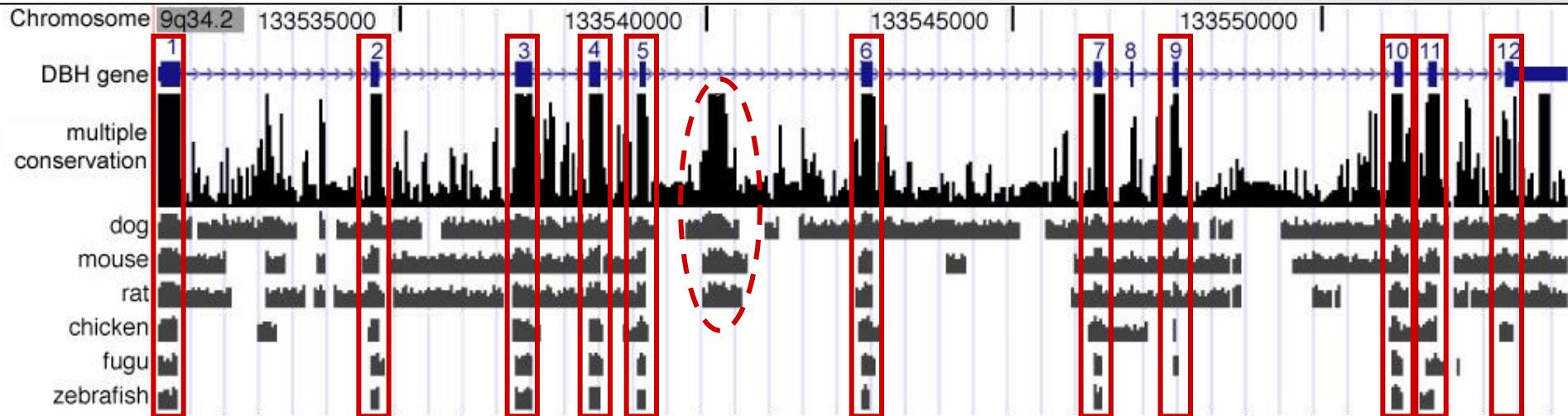
Estimated / kmers detectable at 5% FDR / base pairs detectable at 5% FDR

Small increase in estimate of genome percentage under constraint  
Dramatic increase in power to detect small constrained elements

# **Comparative genomics I: Evolutionary signatures**

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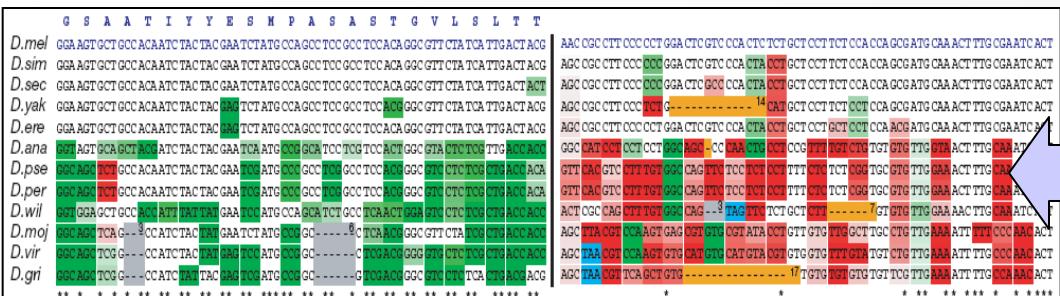
# Comparative genomics and evolutionary signatures



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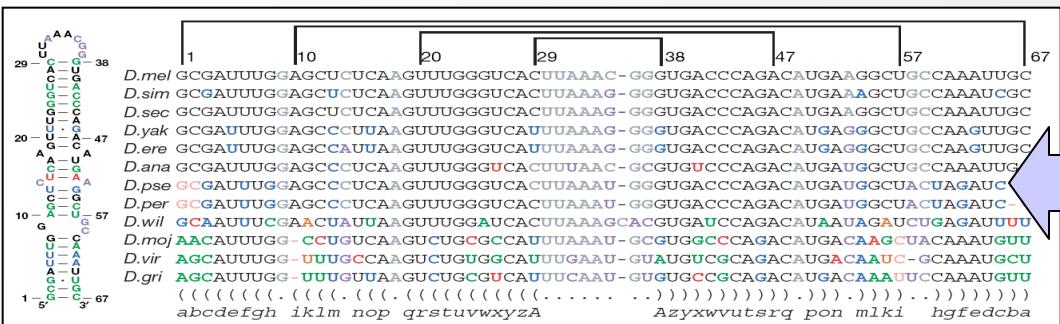
- **Comparative genomics can reveal functional elements**
  - For example: exons are deeply conserved to mouse, chicken, fish
  - Many other elements are also strongly conserved: exons / regulatory?
- **Can we also pinpoint specific functions of each region? Yes!**
  - Patterns of change distinguish different types of functional elements
  - Specific function  $\Leftrightarrow$  Selective pressures  $\Leftrightarrow$  Patterns of mutation/inse/del
- **Develop evolutionary signatures characteristic of each function**

# Evolutionary signatures for diverse functions



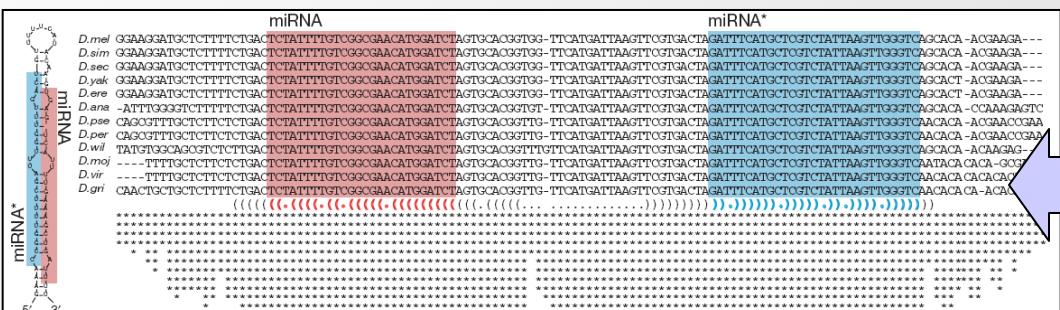
## Protein-coding genes

- Codon Substitution Frequencies
  - Reading Frame Conservation



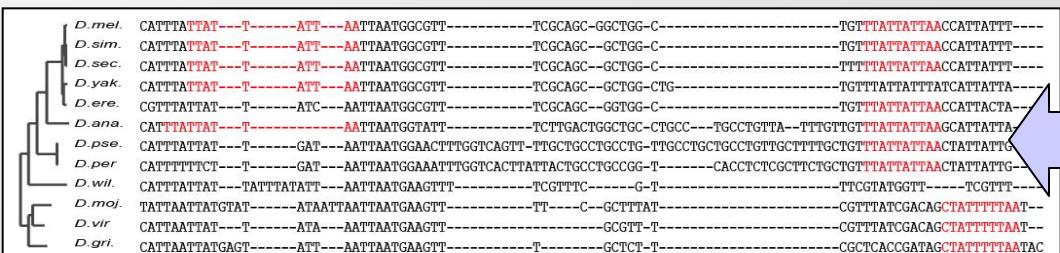
# RNA structures

- Compensatory changes
  - Silent G-U substitutions



# microRNAs

- Shape of conservation profile
  - Structural features: loops, pairs
  - Relationship with 3'UTR motifs



## Regulatory motifs

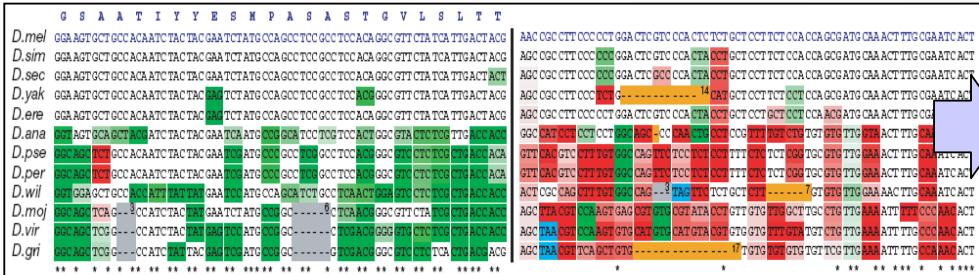
- Mutations preserve consensus
  - Increased Branch Length Score
  - Genome-wide conservation

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Source: Stark, Alexander et al. "Discovery of functional elements in 12 Drosophila genomes using evolutionary signatures." *Nature* 450, no. 7167 (2007): 219-232.

Stark et al., Nature 2007

# Implications for genome annotation / regulation



Novel protein-coding genes  
Revised gene annotations  
Unusual gene structures



Novel structural families  
Targeting, editing, stability  
Riboswitches in mammals



Novel/expanded miR families  
miR/miR\* arm cooperation  
Sense/anti-sense miR switches



Novel regulatory motifs  
Regulatory motif instances  
TF/miRNA regulatory networks  
Single binding site resolution

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Source: Stark, Alexander et al. "Discovery of functional elements in 12 Drosophila genomes using evolutionary signatures." Nature 450, no. 7167 (2007): 219-232.

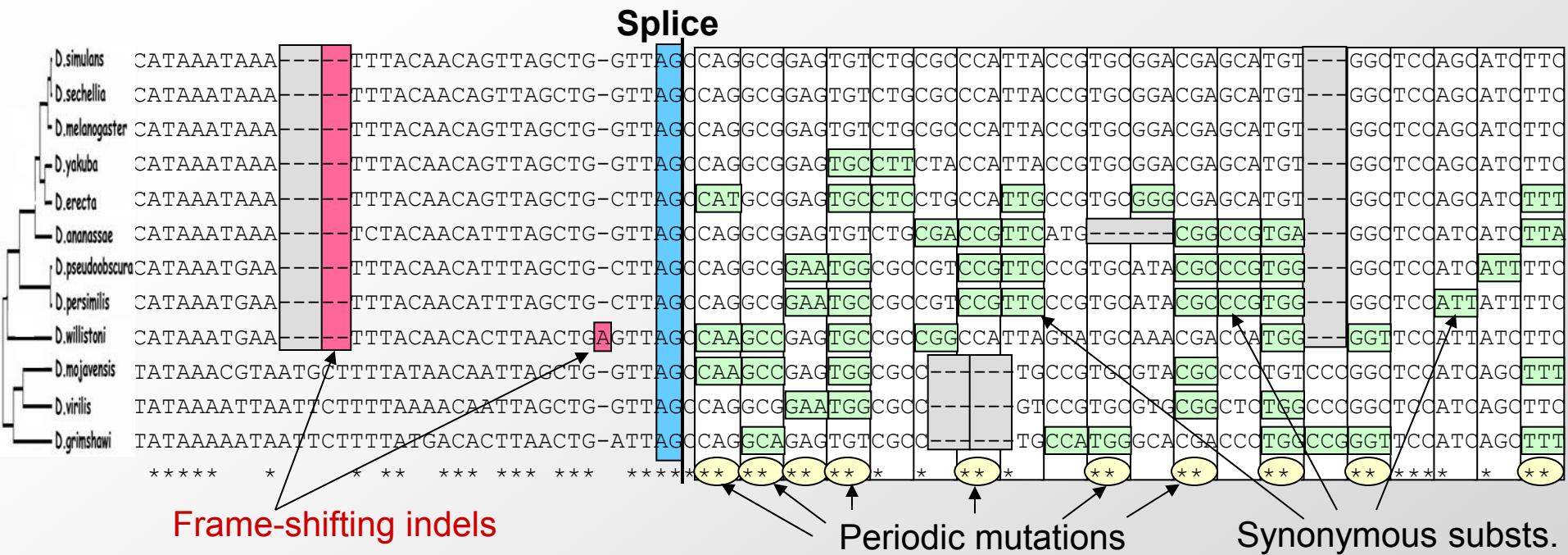
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# Evolutionary signatures for protein-coding genes



- **Same conservation levels, distinct patterns of divergence**
  - Gaps are multiples of three (preserve amino acid translation)
  - Mutations are largely 3-periodic (silent codon substitutions)
  - Specific triplets exchanged more frequently (conservative substs.)
  - Conservation boundaries are sharp (pinpoint individual splicing signals)

→ **Evolutionary signatures of protein-coding selection**

# Evolutionary signatures of protein-coding genes

	the	<b>fat</b>	cat	sat
<b>Δ1</b>	the	atc	ats	at
<b>Δ2</b>	the	tca	tsa	t
<b>Δ3</b>	the	cat	sat	

DNA insertions and deletions can either insert/remove AAs, or totally mangle the remainder of the protein (frameshift).

		Second Letter						
		T	C	A	G			
		T	TTT } Phe TTC TTA } Leu TTG	TCT } Ser TCC TCA TCG	TAT } Tyr TAC TAA } Stop TAG	TGT } Cys TGC TGA } Stop TGG Trp	TCAG	
		C	CTT } Leu CTC CTA CTG	CCT } Pro CCC CCA CCG	CAT } His CAC CAA } Gin CAG	CGT } Arg CGC CGA CGG	TCAG	
		A	ATT } Ile ATC ATA ATG Met	ACT } Thr ACC ACA ACG	AAT } Asn AAC AAA } Lys AAG	AGT } Ser AGC AGA } Arg AGG	TCAG	
		G	GTT } Val GTC GTA GTG	GCT } Ala GCC GCA GCG	GAT } Asp GAC GAA } Glu GAG	GGT } Gly GGC GGA GGG	TCAG	
							Third Letter	

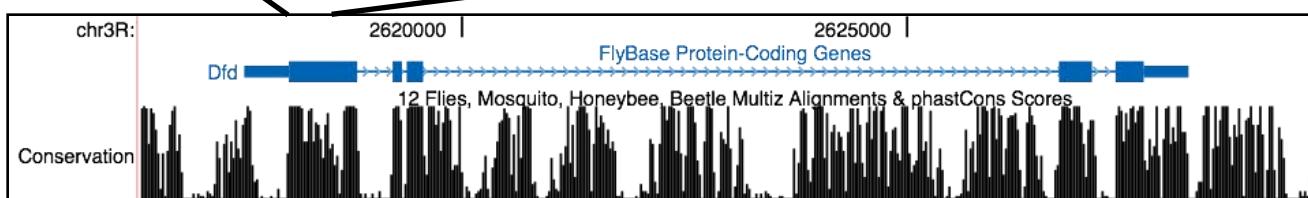
Some point mutations to the DNA sequence do not change its protein translation at all.

Natural selection tends to tolerate mutations with little/no effect on the protein.

# Protein-coding sequences tolerate distinctive types of change

ancestor ATG AGC TCA TTC CTC ATG GGT TAT CGG CAT GCC CCA CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dmel ATG AGC **TCT** **TTT** CTC ATG GGT TAT CGG CAT **GCA** CCA CAT **CAT** GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC **TTG** **GAC**  
dsim ATG AGC **TCT** **TTT** CTC ATG GGT TAT CGG CAT **GCA** CCA CAT **CAT** GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC **TTG** **GAC**  
dsec ATG AGC **TCT** **TTT** CTC ATG GGT TAT CGG CAT **GCA** CCA CAT **CAT** GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC **TTG** **GAC**  
dyak ATG AGC **TCT** **TTT** CTC ATG **GCG** TAT CGG CAT **GCT** CCA CAT **CAT** **GTT** **CAA** AGT CCC ATG TCC ATG GGC AAT GGC **TTG** **GAC**  
dere ATG AGC **TCT** **TTT** CTC ATG GGT TAT CGG CAT **GCT** CCA CAT **CAT** **GTT** CAG AGT CCC ATG TCC ATG GGC AAT **GCT** **TTG** **GAC**  
dana ATG AGC **TCC** **TTC** CTC ATG **GCG** **TAC** **CCC** **CAC** **GCC** CCA CAT CAC GTC CAG **AGC** CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dpse ATG AGC TCA TTC CTC ATG GGT TAT **CCA** CCA CAT **GCC** **CCC** CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dper ATG AGC TCA TTC CTC ATG GGT TAT **CCA** CCA CAT **GCC** **CCC** CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dwil ATG AGC TCA TTC CTC ATG GGT TAT CGG CCA CAT **CAT** GTC CAG AGT CCC ATG TCC ATG GGC AAT **GGA** **CTC** GAT  
dvir ATG AGC TCA TTC CTC ATG GGT TAT **CCA** CCA CAT **GCG** CCA CAT **CAT** GTC CAG **AGC** CCC ATG TCC ATG **GCT** AAT GGC **CTA** GAT  
dmoj ATG AGC TCA TTC **CTA** ATG **GCG** TAT **CCA** CCA CAT **GCG** CCA CAT **CAT** GTC CAG **AGC** CCC ATG TCC ATG GGC AAT **GGA** CTG **GAA**  
dgri ATG AGC TCA TTC CTC ATG GGT **TAC** **CCA** CCA CAT **GCG** CCA CAT CAC GTC CAG **AGC** CCC ATG TCC ATG GGC AAT GGC CTG GAT

protein-coding exon



synonymous

conservative

non-conservative

frame-shifted

three stop codons

ancestor GTG GCG AGT GCA TTT CCC AGA GGG GTT GAT AGG AGT CTG AAA CTA CTG ATA AAT TGC TTT TTA ATT AGC ACA GAG CAG  
dmel GTG **ACG** **AAT** **GCG** TTT CCC AGA GGG **TCC** GAT **CGA** **GGT** CTG **AAG** CTA CTG ATA **GAT** TGC TTT TTA ATT AGC ACA **GCA** CAG  
dsim GTG **ACG** **AAT** **GCG** TTT CCC AGA GGG **TCC** GAT **CGA** **GGT** CTG AAA CTA CTG ATA **GAT** TGC TTT TTA ATT ACC ACA **GCA** CAG  
dsec GTG **ACA** **AAT** **ACG** TTT CCC AGA GGG **TCC** GAT **CGA** **GGT** CTG AAA **CTT** CTG ATA **GAT** TGC TTT TTA ATT AGC ACA **GCA** CAG  
dyak GTG **ACG** **AAT** GCA TTT **CCT** **AGT** GGA **TCC** **GAA** **GAA** **GGG** CTG AAA **GTA** CTG ATA **GAT** **GTC** TTT TTA **ACT** AGC ACA **GCA** CAG  
dere GTG **ACG** **AAT** GCA TTT **CCT** AGA GGA **TCC** GAT **GCT** **GGT** **TTG** AAA **GCG** CTG ATA **GAT** TGC TTT TTA ATT AGC ACA **GCA** CAG  
dana GTG **ACG** **AAT** GCA TTT **ACT** AGA **CGA** **TCT** **AGC** AGG **TCC** **GGG** AAA **RAC** CTG **ATG** **GAT** TGC TTT TTA ATT AGC ACA GAG **TCG**  
dpse GTG **TCG** **ACT** GCA TTT **ACG** **CGG** AGG **CCC** **ACG** AGG AGT **CTC** **CAC** **GCA** CTG ATA **GAT** TGC TTT TTA ATT AGC ACA GAG **AGA**  
dper GTG **TCG** **ACT** GCA TTT **ACG** **CGG** AGG **CCC** **ACG** AGG AGT **CTC** **CAC** **GCA** CTG ATA **GAT** TGC TTT TTA ATT AGC ACA GAG **AGA**  
dwil GTG GCG AGT GCA **TTA** **AAA** AGA **ACA** GTT **GAG** TTT AGT **CGA** **GAG** **GGT** CTG ATT AAT TGC TTT TTA ATT AGC **ACT** **AGT** **TAA**  
dvir GTG GCG AGT GCA **TGT** **GGG** GGA **TGG** **CTT** **GGT** **CGG** CAA CTG **GGT** **TAG** CTG ATA AAT TGC TTT TTA ATT AGC **ATA** **GCG** CAG  
dmoj GTG GCG ACT GCA TAT GCA GGT CGT GTT **GGC** **CGG** **GCT** **CTC** **GGT** CAG CTG ATG GAT GAC TTT TTA ATT AGT ATA GCG CAG  
dgri **GTG** **GCG** AGT GCA TCT **CGG** **CCA** TGT **GGT** **CAG** CCA CTG **GGT** **TCC** CTG ATA AAT **GGT** TTT TTA ATT AGC CTA GCG CAG

# Known genes stand out

Substitution typical of protein-coding regions  
 Substitution typical of intergenic regions

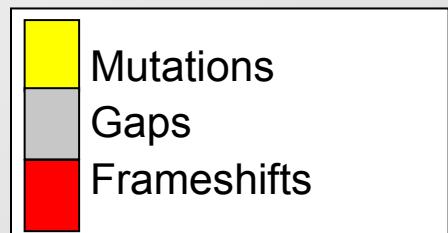
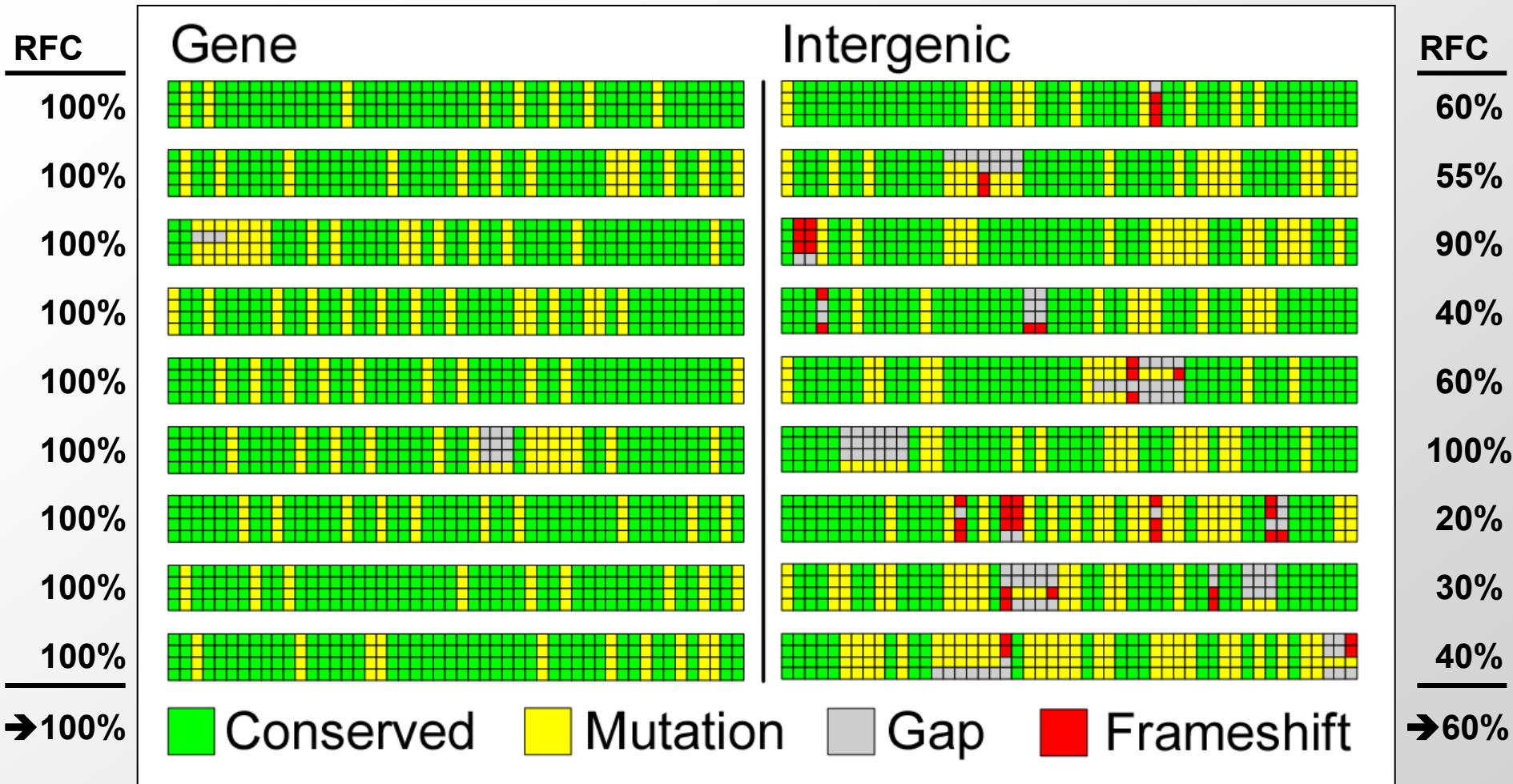


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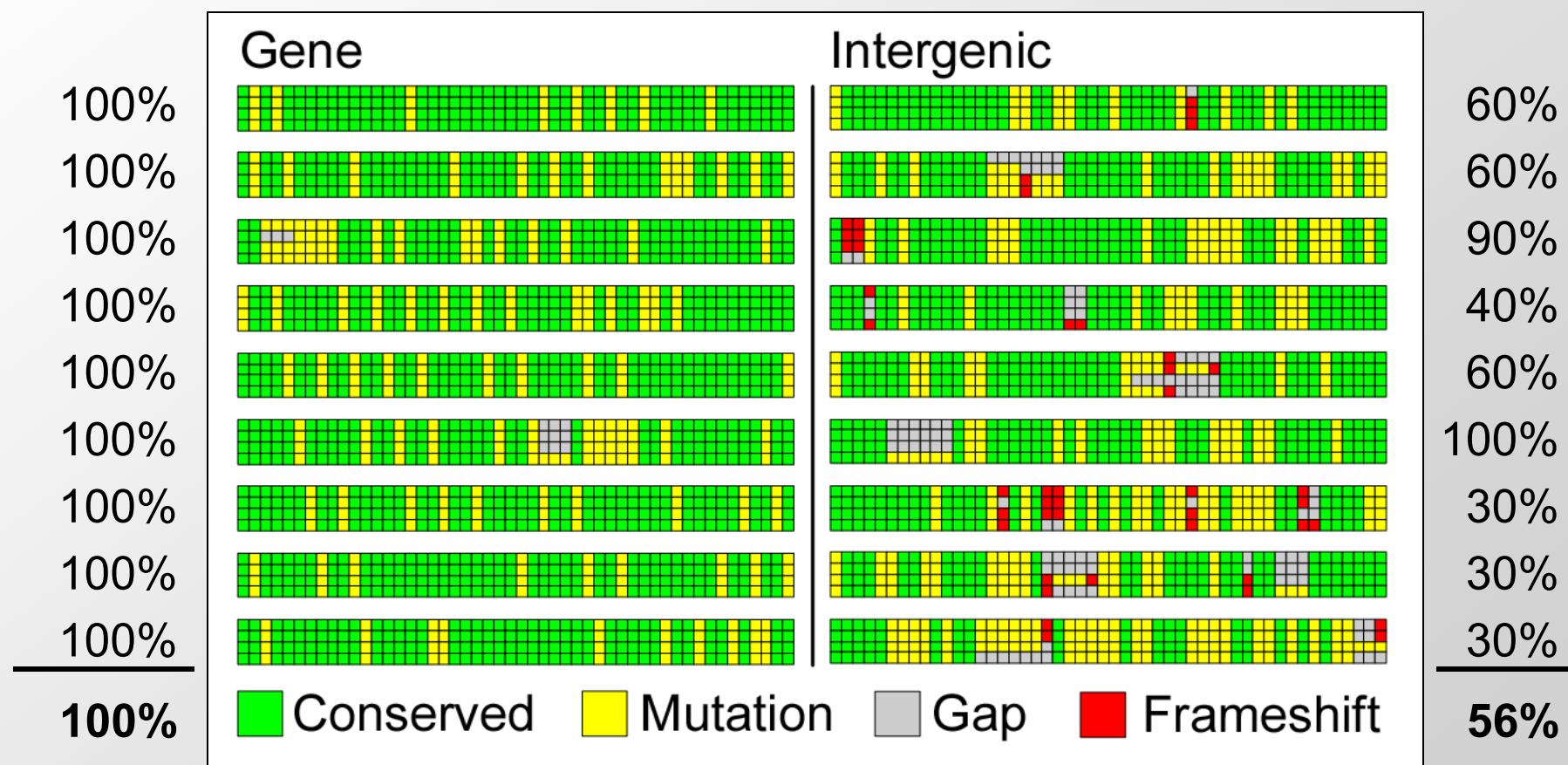
- **Nucleotide conservation: evolutionary constraint**
  - Purifying selection, neutral branch length, discovery power
  - Detect constrained elements: nucleotides, windows, HMM
  - Estimate fraction constrained: signal vs. background
- **Evolutionary signatures: focus on pattern of change**
  - Different functions  $\Leftrightarrow$  Characteristic patterns of evolution
- **Signatures of protein-coding genes**
  - Reading-frame conservation, codon-substitution frequency
  - Likelihood ratio framework: Estimating  $Q_C Q_N$ , scoring
  - Revise genes, read-through, excess constraint regions
- **Signatures of microRNA genes**
  - Structural and evolutionary features of microRNAs
  - Combining features: decision trees, random forests
  - Sense/anti-sense miRNAs, mature/star arm cooperation

# Signature 1: Reading frame conservation



	Genes	Intergenic	Separation
Mutations	30%	58%	→ 2-fold
Gaps	1.3%	14%	→ 10-fold
Frameshifts	0.14%	10.2%	→ 75-fold

# Reading Frame Conservation Test

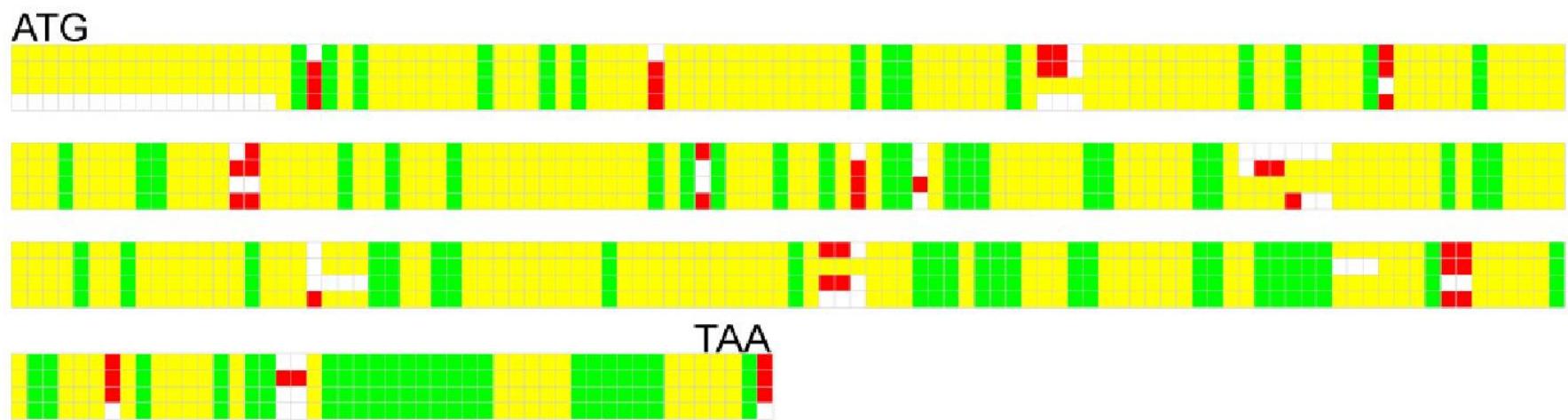


# Revisiting gene content with RFC test

	Accept	Reject
~4000 named genes	99.9%	0.1%
~300 intergenic regions	1%	99%
2000 Hypothetical ORFs	1500	500

High sensitivity and specificity

Example of a rejected ORF



# **Comparative genomics I: Evolutionary signatures**

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- **Nucleotide conservation: evolutionary constraint**
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ancestor ATG AGC TCA TTC CTC ATG GGT TAT CCG CAT GCC CCC CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dmel ATG AGC TCT TTG CTC ATG GGT TAT CCG CAT CGA CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTG GAC  
dsim ATG AGC TCT TTG CTC ATG GGT TAT CCG CAT CGA CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTG GAC  
dsec ATG AGC TCT TTG CTC ATG GGT TAT CCG CAT CGA CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTG GAC  
dyak ATG AGC TCT TTG CTC ATG GGT TAT CCG CAT CGA CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTG GAC  
dere ATG AGC TCT TTG CTC ATG GGT TAT CCG CAT CGT CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTG GAC  
dana ATG AGC TCC TTC CTC ATG GGT TAT CCG CAT CGC CAC CGC CCC CAT CAC GTC CAG ACC CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dpse ATG AGC TCA TTC CTC ATG GGT TAT CCA CAT CGC CCC CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dper ATG AGC TCA TTC CTC ATG GGT TAT CCA CAT CGC CCC CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dwil ATG AGC TCA TTC CTC ATG GGT TAT CCG CAT GCC CCC CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dvir ATG AGC TCA TTC CTC ATG GGT TAT CGA CAT CGG CCA CAT CAT GTC CAG ACC CCC ATG TCC ATG GGC AAT CGA CTG GAT  
dmoj ATG AGC TCA TTC CGA ATG CGC TAT CGA CAT CGG CCA CAT CAT GTC CAG ACC CCC ATG TCC ATG GGC AAT CGA CTG GAT  
dgri ATG AGC TCA TTC CTC ATG GGT CGC CGC CAT CAC GTC CAG ACC CCC ATG TCC ATG GGC AAT GGC CTG GAT

protein-coding exon

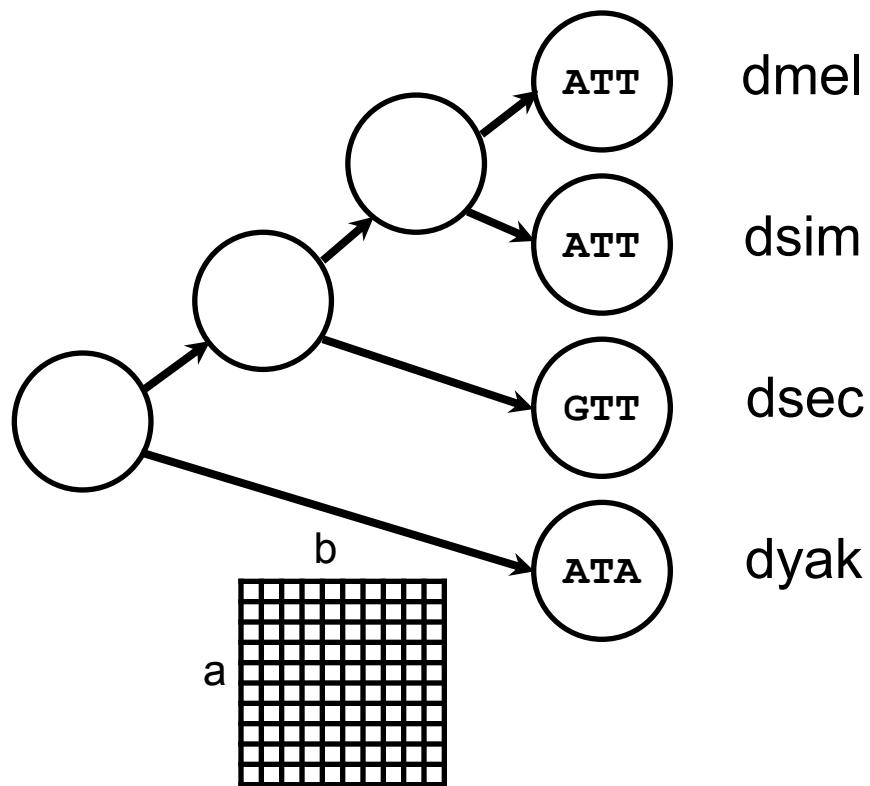
ancestor GTG GCG AGT GCA TTT CCC AGA GGA GTT GAT AGG AGT CTG AAA CTA CTG ATA AAT TGC TTT TTA ATT ACC ACA GAG CAG  
dmel GTG ACG AAT CGC TTT CCC AGA GGA TCG GAT CGA GGT CTG AAG CTA CTG ATA GAT TGC TTT TTA ATT ACC ACA CGA CAG  
dsim GTG ACG AAT CGC TTT CCC AGA GGA TCG GAT CGA GGT CTG AAA CTA CTG ATA GAT TGC TTT TTA ATT ACC ACA CGA CAG  
dsec GTG ACG AAT ACC TTT CCC AGA GGA TCG GAT CGA GGT CTG AAA CTT CTC ATA GAT TGC TTT TTA ATT ACC ACA CGA CAG  
dyak GTG ACG AAT GCA TTT CCT ACT CGA TCC GAA GAA CGG CTC AAA GTC CTG ATA GAT TCA ACT TTT TTA ACT ACC ACA CGA CAG  
dere GTG ACG AAT GCA TTT CCT AGA GGA TCG GAT GCT GGT TTG AAA CGG CTG ATA GAT TGC TTT TTA ATT ACC ACA CGA CAG  
dana GTG ACG AAT GCA TTT ACT AGA CGA TCT CGC AGG TGG CGG AAA AAC CTG ATG GAT TGC TTT TTA ATT ACC ACA GAG TCG  
dpse GTG TCG ACT GCA TTT ACC CGG AGG CCC ACC AGG ACT CTC CGC CTG ATA GAT TGC TTT TTA ATT ACC ACA GAG ATG  
dper GTG TCG ACT GCA TTT ACC CGG AGG CCC ACC AGG ACT CTC CGC CTG ATA GAT TGC TTT TTA ATT ACC ACA GAG ATG  
dwil GTG CGC ACT GCA TTA AAA AGA AGA GTT GAC TTG AGT CGA CGG GGT CTG ATT AAT TGC TTT TTA ATT ACC ACT ATG TAA  
dvir GTG GCG AGT GCA TCT CGC CGA TCG CCT GGT CGG CGA CTG GGT TAG CTG ATA AAT TGC TTT TTA ATT ACC ATA CGC CAG  
dmoj GTG GCG ACT GCA TAT GCA GGT CGT GTT CGG CGG GCT CGC GGT CGA CTG ATG GAT GAC TTT TTA ATT ACT ATA CGG CAG  
dgri GTG GCG AGT GCA TCT CGC CGA TCT GTT GGT CGC CGA CTG CCT TGG CTG ATA AAT CGT TTT TTA ATT ACC CTA CGC CAG

conserved non-coding sequence

## A method to distinguish these evolutionary signatures should:

- Quantify the distinctiveness of all  $64^2$  possible codon substitutions
  - Synonymous: very frequent in protein-coding sequences
  - Nonsense: much more frequent in non-coding than coding regions
- Model the phylogenetic relationship among the species
  - Multiple apparent substitutions may be explained by one evolutionary event
- Tolerate uncertainty in the input
  - Unknown ancestral sequences
  - Alignment gaps, missing data
- Report the [un]certainty of the result
  - Quantify confidence that given alignment is protein-coding
  - Units: p-value, bits, decibans, etc.

# Codon evolution can be modeled as a Bayesian network



Conditional probability distribution (CPD) giving,  
for all codons  $a$  &  $b$ ,  $\Pr(\text{dyak} = b | \text{Ancestor} = a)$

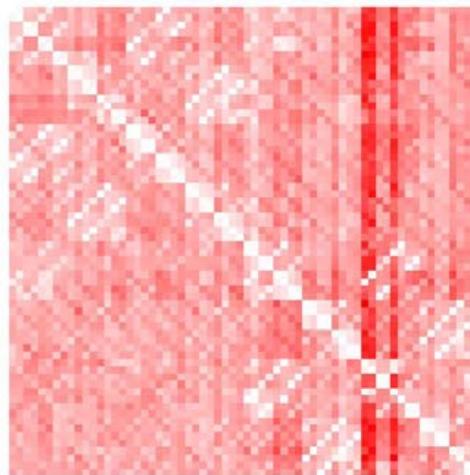
Each site (codon alignment column) is treated independently.

Given the topology and CPDs, we can simulate evolution of an ancestral sequence.

Additionally given extant (leaf) sequences, the ancestral sequences can be inferred.

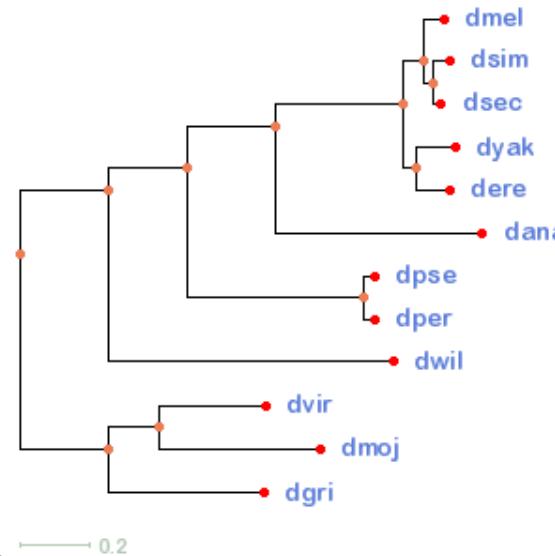
For  $L$  leaves, CPDs total about  $(2L - 2) \cdot 64^2$  parameters.

# The Bayes net is parameterized as a continuous-time Markov process



Rate matrix ( $\mathbf{Q}$ )

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Branch lengths  $t$

Each CPD is determined by a rate matrix shared throughout the tree and a branch-specific ‘time’ (branch length):

$$\Pr(\text{child} = b | \text{parent} = a; t) = [e^{\mathbf{Q}t}]_{a,b}$$

Intuition: The branch lengths specify how much ‘time’ passed between any two nodes. The rate matrix describes the relative frequencies of codon substitutions *per unit branch length*. Synonymous substitutions have high rates and nonsense substitutions have low rates.

We can obtain maximum likelihood estimates of  $(2L - 2) + 64^2$  parameters using EM in training data.

# Example nucleotide (4x4) rate & substitution matrices

$$\mathbf{Q} = \begin{pmatrix} -4 & 2 & 1 & 1 \\ 2 & -4 & 1 & 1 \\ 1 & 1 & -4 & 2 \\ 1 & 1 & 2 & -4 \end{pmatrix} \begin{matrix} \text{A} \\ \text{G} \\ \text{C} \\ \text{T} \end{matrix}$$

$$\Pr(\text{child} = b | \text{parent} = a; t) = [e^{\mathbf{Q}t}]_{a,b}$$

$e^{\mathbf{Q}t} = \sum_{n=0}^{\infty} \frac{t^n}{n!} \mathbf{Q}^n$  is the solution to the system of differential equations describing the Markov process model of evolution.

```
MatrixExp[Q * 0] // MatrixForm
```

$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

```
MatrixExp[Q * 0.001] // MatrixForm // NumberForm[#, 4] &
```

$$\begin{pmatrix} 0.996 & 0.001993 & 0.000998 & 0.000998 \\ 0.001993 & 0.996 & 0.000998 & 0.000998 \\ 0.000998 & 0.000998 & 0.996 & 0.001993 \\ 0.000998 & 0.000998 & 0.001993 & 0.996 \end{pmatrix}$$

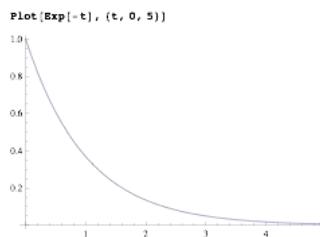
```
MatrixExp[Q * 0.01] // MatrixForm // NumberForm[#, 4] &
```

$$\begin{pmatrix} 0.9611 & 0.01932 & 0.009803 & 0.009803 \\ 0.01932 & 0.9611 & 0.009803 & 0.009803 \\ 0.009803 & 0.009803 & 0.9611 & 0.01932 \\ 0.009803 & 0.009803 & 0.01932 & 0.9611 \end{pmatrix}$$

Analogy:  $y(t) = e^{qt}$

solves the differential equation

$$\frac{dy}{dt} = qy$$



```
MatrixExp[Q * 0.1] // MatrixForm // NumberForm[#, 4] &
```

$$\begin{pmatrix} 0.692 & 0.1432 & 0.08242 & 0.08242 \\ 0.1432 & 0.692 & 0.08242 & 0.08242 \\ 0.08242 & 0.08242 & 0.692 & 0.1432 \\ 0.08242 & 0.08242 & 0.1432 & 0.692 \end{pmatrix}$$

```
MatrixExp[Q * 1.0] // MatrixForm // NumberForm[#, 4] &
```

$$\begin{pmatrix} 0.2558 & 0.2533 & 0.2454 & 0.2454 \\ 0.2533 & 0.2558 & 0.2454 & 0.2454 \\ 0.2454 & 0.2454 & 0.2558 & 0.2533 \\ 0.2454 & 0.2454 & 0.2533 & 0.2558 \end{pmatrix}$$

```
MatrixExp[Q * 10.0] // MatrixForm // NumberForm[#, 4] &
```

$$\begin{pmatrix} 0.25 & 0.25 & 0.25 & 0.25 \\ 0.25 & 0.25 & 0.25 & 0.25 \\ 0.25 & 0.25 & 0.25 & 0.25 \\ 0.25 & 0.25 & 0.25 & 0.25 \end{pmatrix}$$

Side note: Jukes-Cantor and Kimura models are set up so that the entries of  $e^{\mathbf{Q}t}$  have closed-form solutions.

# The hairy math: how do we estimate $\mathbf{Q}$ ?

- Collect many alignments of known protein-coding sequences (training data)
- Consider the probability of the training data as a function of  $\mathbf{Q}$

$$\text{Likelihood}(\mathbf{Q}) = \Pr(\text{Training Data}; \mathbf{Q}, \underline{t})$$

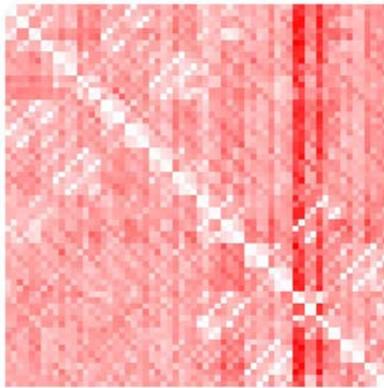
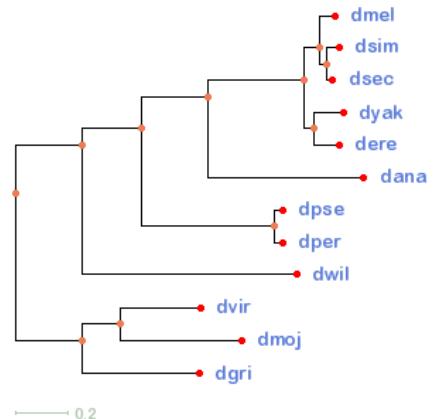
Still computed using Felsenstein algorithm

- Choose the  $\mathbf{Q}$  that maximizes that probability:

$$\hat{\mathbf{Q}} = \underset{\mathbf{Q}}{\operatorname{argmax}} (\text{Likelihood}(\mathbf{Q}))$$

Note:  $\mathbf{Q}$  represents thousands of parameters

- Maximization strategies: expectation-maximization; gradient ascent; simulated annealing; spectral decomposition; others
- Branch lengths can also be optimized in the same way (simultaneously)
- Non-coding model estimated similarly, with random non-coding regions as training data.



Rate matrix ( $\mathbf{Q}$ )

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Branch lengths  $t$

We can compute the probability of any given alignment, marginalizing over all possible ancestral sequences, using Felsenstein's pruning algorithm.

ancestor ATG AGC TCA TTC CTC ATG GGT TAT CCG CAT GCC CCA CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dmel ATG AGC **TCT** **TTC** CTC ATG GGT TAT CCG CAT **GCA** CCA CAT **CAT** GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC **TTC** **GAC**  
dsim ATG AGC **TCT** **TTC** CTC ATG GGT TAT CCG CAT **GCA** CCA CAT **CAT** GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC **TTC** **GAC**  
dsec ATG AGC **TCT** **TTC** CTC ATG GGT TAT CCG CAT **GCA** CCA CAT **CAT** GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC **TTC** **GAC**  
dyak ATG AGC **TCT** **TTC** CTC ATG **GCA** TAT CCG CAT **GCT** **CAT** GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC **TTC** **GAC**  
dere ATG AGC **TCT** **TTC** CTC ATG GGT TAT CCG CAT **GCT** CCA CAT **CAT** GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC **TGT** **TTC** **GAC**  
dana ATG AGC **TCC** **TTC** CTC ATG **GCG** TAT CCG CAT **GCA** CAC GTC CAG **AGC** CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dpse ATG AGC TCA TTC CTC ATG GGT TAT **GCA** CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dper ATG AGC TCA TTC CTC ATG GGT TAT **GCA** CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT  
dwil ATG AGC TCA TTC CTC ATG GGT TAT CCG CAT **GCC** CCA CAT **CAT** GTC CAG AGT CCC ATG TCC ATG GGC AAT **GGA** **TTC** GAT  
dvir ATG AGC TCA TTC CTC ATG GGT TAT **GCA** CAC GTC CAG **AGC** CCC ATG TCC ATG **GCT** AAAT GGC **TTA** GAT  
dmoj ATG AGC TCA TTC CTC ATG GGT **FAC** CCA TAT CCG CAT **GTC** CAC GTC CAG **AGC** CCC ATG TCC ATG GGC AAT **GGA** **CTG** **GAA**  
dgri ATG AGC TCA TTC CTC ATG GGT **FAC** CCA CAT **GCG** CAC GTC CAG **AGC** CCC ATG TCC ATG GGC AAT GGC CTG GAT

ancestor GTG GCG ACT GCA TTT CCC AGA GGA GTT GAT AGG AGT CTG AAA CTA CTG ATA AAAT TGC TTT TTA ATT ACC ACA GAG CAG  
dmel GTG **AGC** **AAT** **GCG** TTT CCC AGA GGA **TGG** GAT **GCA** **GCT** CTG **AAG** CTA CTG ATA **GAT** TGC TTT TTA ATT ACC ACA **GCA** CAG  
dsim GTG **AGC** **AAT** **GCG** TTT CCC AGA GGA **TGG** GAT **GCA** **GCT** CTG AAA CTA CTG ATA **GAT** TGC TTT TTA ATT ACC ACA **GCA** CAG  
dsec GTG **AGC** **AAT** **GCA** TTT CCC AGA GGA **TGG** GAT **GCA** **GCT** CTG AAA **GAT** CTA CTG ATA **GAT** TGC TTT TTA ATT ACC ACA **GCA** CAG  
dyak GTG **AGC** **AAT** **GCA** TTT CCT **ACT** **GCA** **TCC** **GAA** **GCG** CTG AAA **GTA** CTG ATA **GAT** **GTC** TTT TTA ATT ACC ACA **GCA** CAG  
dere GTG **AGC** **AAT** **GCA** TTT CCT **AGA** GGA **TGG** GAT **GCT** **GCT** **TTC** AAA **GGG** CTG ATA **GAT** TGC TTT TTA ATT ACC ACA **GCA** CAG  
dana GTG **AGC** **AAT** **GCA** TTT ACT **AGA** **GCA** **TCT** **ACC** **AGG** **TGG** **CCC** **AAA** **AAC** **GTA** CTG **ATG** **GAT** TGC TTT TTA ATT ACC ACA GAG **TGG**  
dpse GTG **AGC** **AAT** **GCA** TTT **AGC** **GCG** **AGG** **CCC** **AGC** **AGG** AGT **CTT** **CAC** **GCA** CTG ATA **GAT** TGC TTT TTA ATT ACC ACA GAG **AGA**  
dper GTG **TGC** **AGC** **AAT** **GCA** TTT **AGC** **GCG** **AGG** **CCC** **AGC** **AGG** AGT **CTC** **CAC** **GCA** CTG ATA **GAT** TGC TTT TTA ATT ACC ACA GAG **AGA**  
dwil GTG GCG ACT GCA **TTA** **AAA** AGA AGA GTT **GAT** **TTT** AGT **GCA** **GAG** **GCT** CTG **ATT** AAAT TGC TTT TTA ATT ACC **ACT** **AGT** **TAA**  
dvir GTG GCG ACT GCA **FCT** **GCG** **GCA** **FCT** **TTT** **GCT** **CGG** **CAC** **CTG** **GCT** **TAG** CTG ATA AAAT TGC TTT TTA ATT ACC **ATA** **GCG** CAG  
dmoj GTG GCG ACT GCA **TAT** **GCA** **GCT** **GTC** **GCT** **GTT** **GCG** **GCT** **CTG** **GAT** **GAC** **TTT** **TTA** **ATT** **ACT** **ATA** **GCG** CAG  
dgri **GTC** **GCG** **AGT** **GCA** **TCT** **GCG** **GCA** **FCT** **GTT** **GCT** **GCG** **GCA** **CTG** **TGG** CTG ATA AAAT **GCT** **TTT** TTA ATT ACC **CTA** **GCG** CAG

protein-coding exon

$$\Pr(\text{Leaves}; \mathbf{Q}, \underline{t}) = \frac{1}{10^{117}}$$

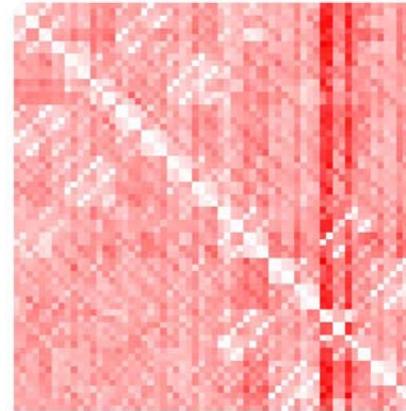


If I simulate alignments randomly according to the model, I'll get this exact alignment once every  $10^{117}$  samples

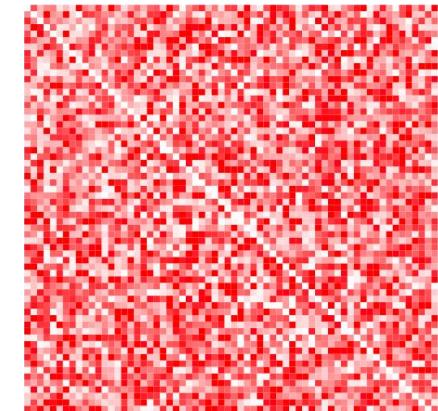
conserved non-coding sequence

$$\Pr(\text{Leaves}; \mathbf{Q}, \underline{t}) = \frac{1}{10^{275}}$$

Now suppose we've estimated  
two rate matrices:



$\mathbf{Q}_C$  estimated from known  
coding regions



$\mathbf{Q}_N$  estimated from non-  
coding regions

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These specify different rates of codon substitution, which in turn lead to different probabilities of any given alignment:

```
ancestor ATG AGC TCA TTC CTC ATG GGT TAT CCG CAT GCC CCA CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT
dmel ATG AGC TCT TTT CTC ATG GGT TAT CCG CAT GCA CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTC GAC
dsim ATG AGC TCT TTT CTC ATG GGT TAT CCG CAT GCA CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTC GAC
dsec ATG AGC TCT TTT CTC ATG GGT TAT CCG CAT GCA CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTC GAC
dyak ATG AGC TCT TTT CTC ATG GGC TAT CCG CAT GCT CCA CAT CAT GTC TAA AGT CCC ATG TCC ATG GGC AAT GGC TTC GAC
dere ATG AGC TCT TTT CTC ATG GGT TAT CCG CAT GCT CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGT TTC GAC
dana ATG AGC TCC TTC CTC ATG GGC TAT CCA CAT GCA CCA CCC CAT CAC GTC CAG AGC CCC ATG TCC ATG GGC AAT GGC CTG GAT
dpse ATG AGC TCA TTC CTC ATG GGT TAT CCA CAT GCA CCA CCC CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT
dper ATG AGC TCA TTC CTC ATG GGT TAT CCA CAT GCC CCC CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT
dwil ATG AGC TCA TTC CTC ATG GGT TAT CCG CAT GCC CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGA TTC GAT
dvir ATG AGC TCA TTC CTC ATG GGT TAT CCA CAT CGG CCA CAT CAT GTC CAG AGC CCC ATG TCC ATG GGT AAT GGC TTA GAT
dmoj ATG AGC TCA TTC CTA ATG GGC TAT CCA CAT CGG CCA CAT CAT GTC CAG AGC CCC ATG TCC ATG GGC AAT GGA CTG GAA
dgri ATG AGC TCA TTC CTC ATG GGT TAC CCA CAT CGG CCC CAT CAC GTC CAG AGC CCC ATG TCC ATG GGC AAT GGC CTG GAT
```

```
ancestor GTG GCG ACT GCA TTT CCC AGA GGA GTT GAT AGG AGT CTG AAA CTA CTG ATA AAT TGC TTT TTA ATT ACC ACA GAG CAG
dmel GTG AGC ATT GGC TTT CCC AGA GGA TCC GAT GCA GGT CTG TAA GAG TGC TTT TTA ATT ACC ACA GCA CAG
dsim GTG AGC ATT GGC TTT CCC AGA GGA TCC GAT GCA GGT CTG AAA CTA CTG ATA GAT TGC TTT TTA ATT ACC ACA GCA CAG
dsec GTG AGC ATT AGC TTT CCC AGA GGA TCC GAT GCA GGT CTG AAA CTT CTG ATA GAT TGC TTT TTA ATT ACC ACA GCA CAG
dyak GTG AGC ATT GCA TTT CCT ACT GGA TCC TAA GGA CCC CTG AAA GTC CTG ATA GAT GTC TTT TTA ATT ACC ACA GCA CAG
dere GTG AGC ATT GCA TTT CCT AGA GGA TCC GAT GGT GGT TTC AAA GGG CTG ATA GAT TGC TTT TTA ATT ACC ACA GCA CAG
dana GTG AGC ATT GCA TTT ACT AGA GCA TCT AGC AGG TGG CCC AAA AAC CTG ATG GAT TGC TTT TTA ATT ACC ACA GAG TCG
dpse GTG TCG ACT GCA TTT AGC CCC AGG CCC AGC AGG ACT CTG CAC GCA CTG ATA GAT TGC TTT TTA ATT ACC ACA GAG AGA
dper GTG TCG ACT GCA TTT ACC CCC AGG CCC AGC AGG AGT CTG CAC GCA CTG ATA GAT TGC TTT TTA ATT ACC ACA GAG AGA
dwil GTG GCG AGT GCA TTA AAA AGA AGA GTT GAT TTT AGT GGA GAG GGT CTG ATT ATT TGC TTT TTA ATT ACC ACT AGT TAA
dvir GTG GCG AGT GCA TGT CGG GCA TCG TTT GGT CGG CAA CTG GGT TAG CTG ATA AAT TGC TTT TTA ATT ACC ATA CGG CAG
dmoj GTG GCG ACT GCA ATT GCA GGT CGT GTT GGC CGG GCT TCG GGT CAG CTG ATG GAT GAC TTT TTA ATT AGT ATA CGG CAG
dgri GTG GCG AGT GCA TCT CGG GCA TGT GTT GGT CAG CGG CTG GGT TGC CTG ATA AAT GGT TTT TTA ATT ACC CTA CGG CAG
```

$$\Pr(\text{Leaves}; \mathbf{Q}_C, \underline{t}) = \frac{1}{10^{117}}$$

$$\Pr(\text{Leaves}; \mathbf{Q}_N, \underline{t}) = \frac{1}{10^{152}}$$

$$\Pr(\text{Leaves}; \mathbf{Q}_C, \underline{t}) = \frac{1}{10^{275}}$$

$$\Pr(\text{Leaves}; \mathbf{Q}_N, \underline{t}) = \frac{1}{10^{254}}$$

```

ancestor ATG AGC TCA TTC CTC ATG GGT TAT CCG CAT GCC CCA CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT
dmel ATG AGC TCT TTG CTC ATG GGT TAT CCG CAT CGA CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTG GAC
dsim ATG AGC TCT TTG CTC ATG GGT TAT CCG CAT CGA CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTG GAC
dsec ATG AGC TCT TTG CTC ATG GGT TAT CCG CAT CGA CCA CAT CAT GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC TTG GAC
dyak ATG AGC TCT TTG CTC ATG GGT TAT CCG CAT CGT GAA AGT CCC ATG TCC ATG GGC AAT GGC TTG GAC
dere ATG AGC TCT TTG CTC ATG GGT TAT CCG CAT CGT CAA AGT CCC ATG TCC ATG GGC AAT GGT TTG GAC
dana ATG AGC TCC TTC CTC ATG GGT TAT CCA CAT CGC CCC CAT CAC GTC CAG AGC CCC ATG TCC ATG GGC AAT GGC CTG GAT
dpse ATG AGC TCA TTC CTC ATG GGT TAT CGA CAT CGC CCC CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT
dper ATG AGC TCA TTC CTC ATG GGT TAT CGA CAT CGC CCC CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGC CTG GAT
dwil ATG AGC TCA TTC CTC ATG GGT TAT CGC CAT CGC CCC CAT CAC GTC CAG AGT CCC ATG TCC ATG GGC AAT GGA CTC GAT
dvir ATG AGC TCA TTC CTC ATG GGT TAT CGA CAT CGC CCC CAT CAC GTC CAG AGC CCC ATG TCC ATG GGT ATT AAT GGC CTA GAT
dmoj ATG AGC TCA TTC CGA ATG GGT TAT CGA CAT CGC CCC CAT CAC GTC CAG AGC CCC ATG TCC ATG GGC AAT GGA CTG GAA
dgrt ATG AGC TCA TTC CTC ATG GGT CGC CGA CAT CGC CCC ATG TCC ATG GGC AAT GGC CTG GAT

```

$$\frac{\Pr(\text{Leaves}; \mathbf{Q}_C, \underline{t}) = \frac{1}{10^{117}}}{\Pr(\text{Leaves}; \mathbf{Q}_N, \underline{t}) = \frac{1}{10^{152}}} = 10^{35}$$

This alignment is  $10^{35}$  times more probable under the coding model than the non-coding model.

```

ancestor GTG GCG AGT GCA TTT CCC AGA GGA GTT GAT AGG AGT CTG AAA CTA CTG ATA AAT TGC TTT TTA ATT AGC ACA GAG CAG
dmel GTG ACC AAT CGC TTT CCC AGA GGA TCC GAT CGA GGT CTG AAC CTA CTG ATA CGT TGC TTT TTA ATT AGC ACA CGA CAG
dsim GTG ACG AAT CGC TTT CCC AGA GGA TCC GAT CGA GGT CTG AAC CTA CTG ATA CGT TGC TTT TTA ATT AGC ACA CGA CAG
dsec GTG ACG AAT CGC TTT CCC AGA GGA TCC GAT CGA GGT CTG AAC CTA CTG ATA CGT TGC TTT TTA ATT AGC ACA CGA CAG
dyak GTG ACG AAT CGC TTT CCT AGAGGA TCC GAT CGT GGT TTG AAA CGG CTG ATA CGT TGC TTT TTA ATT AGC ACA CGA CAG
dere GTG ACG AAT CGC TTT CCT AGAGGA TCC GAT CGT GGT TTG AAA CGG CTG ATA CGT TGC TTT TTA ATT AGC ACA CGA CAG
dana GTG ACG AAT CGC TTT ACT AGA CGA TCT AGC AGG TGG CGG AAA AAC CTG ATG CGT TGC TTT TTA ATT AGC ACA GAG TCG
dpse GTG TCC ACT CGC TTT ACC CGG ACC CGC ACC AGG AGT TGC CGC CTG ATA CGT TGC TTT TTA ATT AGC ACA GAG CGA
dper GTG TCC ACT CGC TTT ACC CGG AGG CGC ACC AGG AGT TGC CGC CTG ATA CGT TGC TTT TTA ATT AGC ACA GAG CGA
dwil GTG GCG AGT CGA TTA AAA AGA ACA GTT TGG TTT AGT CGA GAG CGG CTG ATT AAT TGC TTT TTA ATT AGC ACT AGT TAA
dvir GTG GCG AGT CGA TGT CGC CGA TGG CCT CGT CGG CGA CTG GGT TAG CTG ATA ATT TGC TTT TTA ATT AGC ATA CGC CAG
dmoj GTG GCG ACT CGA ATT CGA CGG GTT CGT CGG CGA CTG CGT CGA CTG ATG GAT GAC ATT TTA ATT AGT ATA CGC CAG
dgrt GTG CGC AGT CGA TCT CGC CGA TGT GGT CGT CGG CGA CTG CGT CGT CGT ATA ATT AGC CGT TGC ATA ATT AGC CTA CGG CAG

```

$$\frac{\Pr(\text{Leaves}; \mathbf{Q}_C, \underline{t}) = \frac{1}{10^{275}}}{\Pr(\text{Leaves}; \mathbf{Q}_N, \underline{t}) = \frac{1}{10^{254}}} = 10^{-21}$$

This alignment is  $10^{21}$  times less probable under the coding model than the non-coding model.

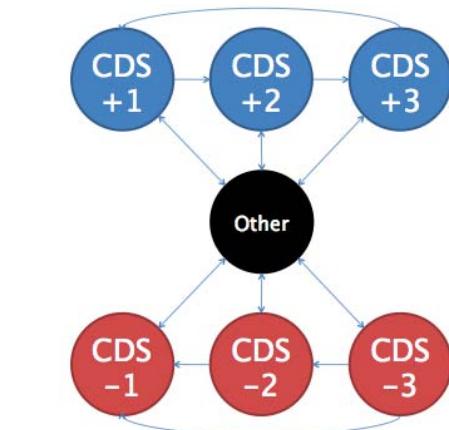
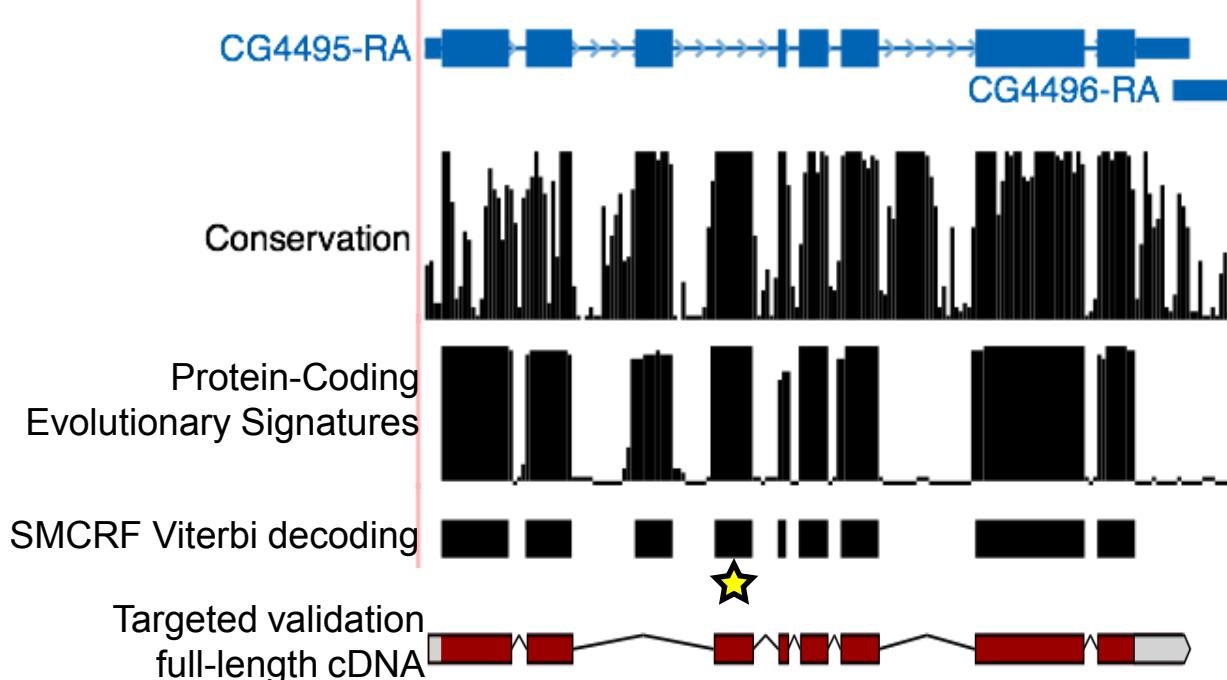
**This likelihood ratio**  $\frac{\Pr(\text{Leaves}; \mathbf{Q}_C, \underline{t})}{\Pr(\text{Leaves}; \mathbf{Q}_N, \underline{t})}$  is our measure of confidence that the alignment is protein-coding.

# **Comparative genomics I: Evolutionary signatures**

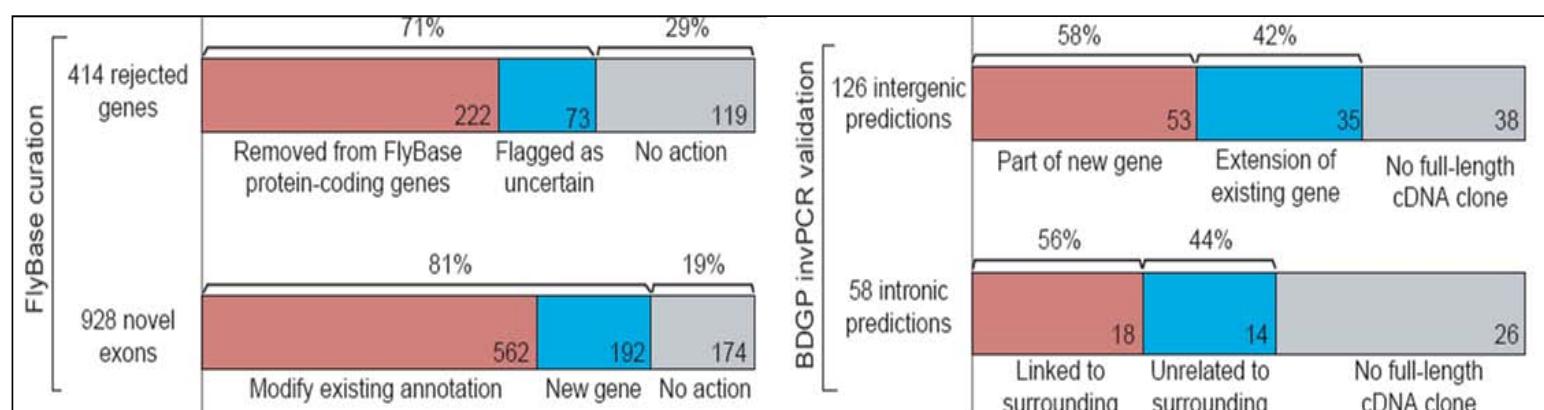
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  - Sense/anti-sense miRNAs, mature/star arm cooperation

# Evolutionary signatures can predict new genes and exons



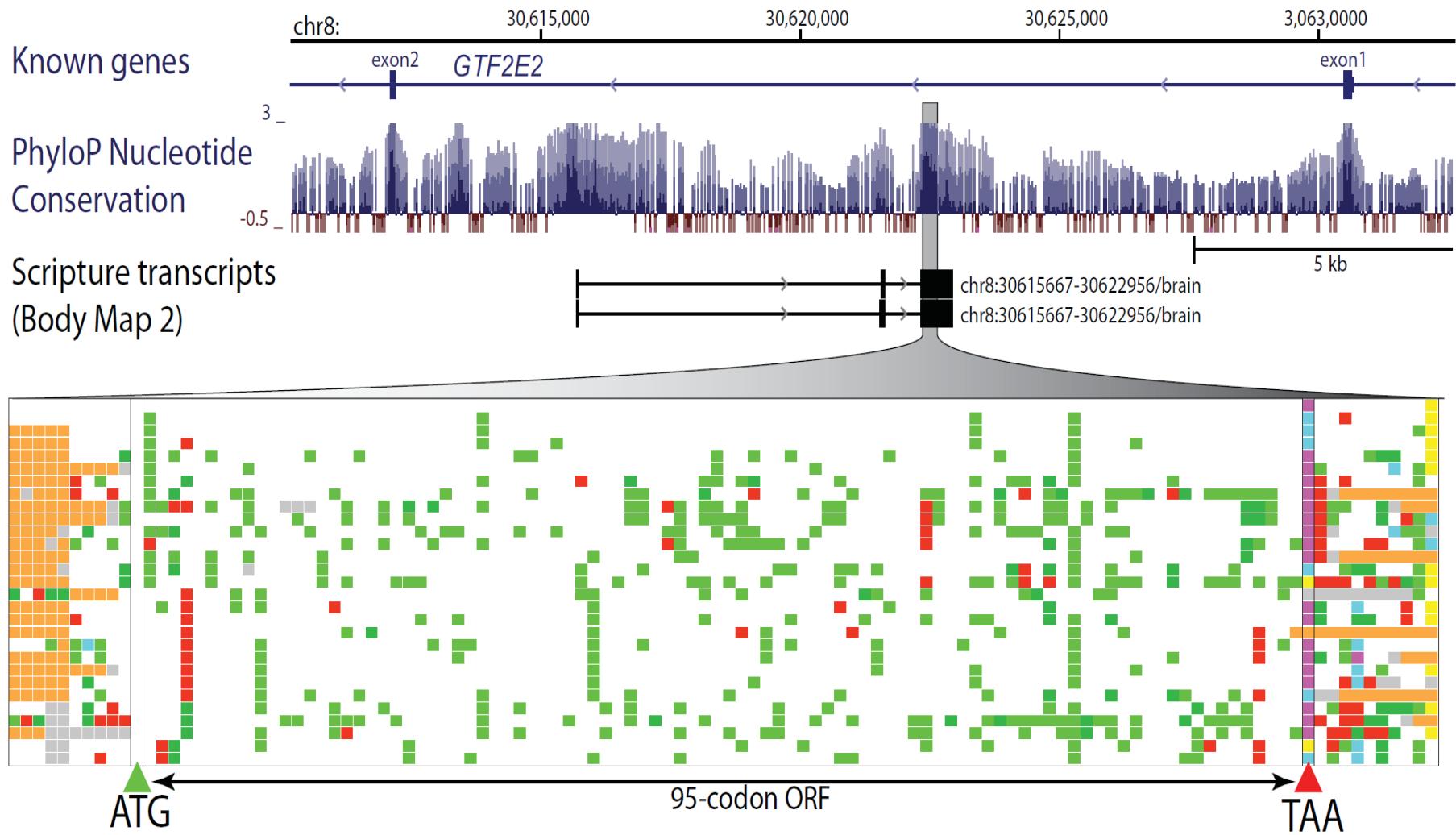
*Evolutionary signatures built into a semi-Markov conditional random field to predict protein-coding exons*



Courtesy of Macmillan Publishers Limited. Used with permission.

Source: Stark, Alexander et al. "Discovery of functional elements in 12 Drosophila genomes using evolutionary signatures." Nature 450, no. 7167 (2007): 219-232.

# New protein-coding genes

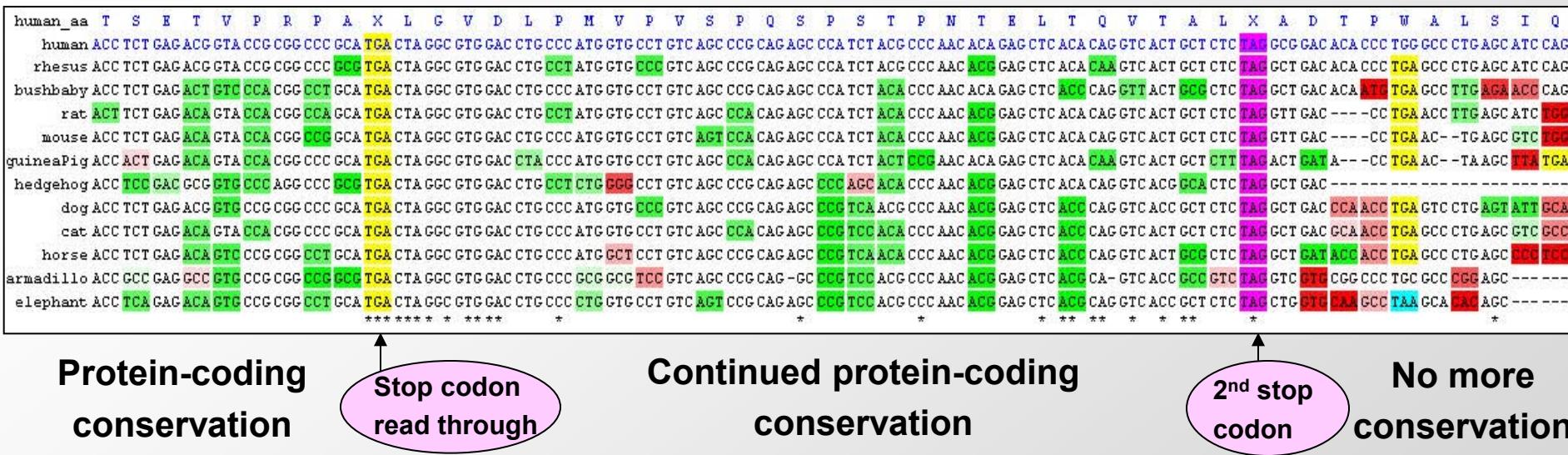


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New genes supported by Illumina BodyAtlas transcripts  
Submitted to GENCODE for validation / manual curation

# Translational read-through in flies and mammals

## One of four novel candidates in the human genome: OPRL1 neurotransmitter



- **New mechanism of post-transcriptional regulation?**
    - Conserved in both mammals (4 candidates) and flies (350 candidates)
    - Strongly enriched for neurotransmitters, brain-expressed proteins, TF regulators
    - After correcting for gene length: TF enrichment remains
  - **Evidence suggestive of regulatory control**
    - Read-through stop codon perfectly conserved in 93% of cases (24% at bkgrnd)
    - Upstream bases show increased conservation. Downstream is TGAC.
    - GCA triplet repeats
    - Increased RNA secondary structure

Lin et al, Genome Research 2007  
Jungreis et al, in preparation 45

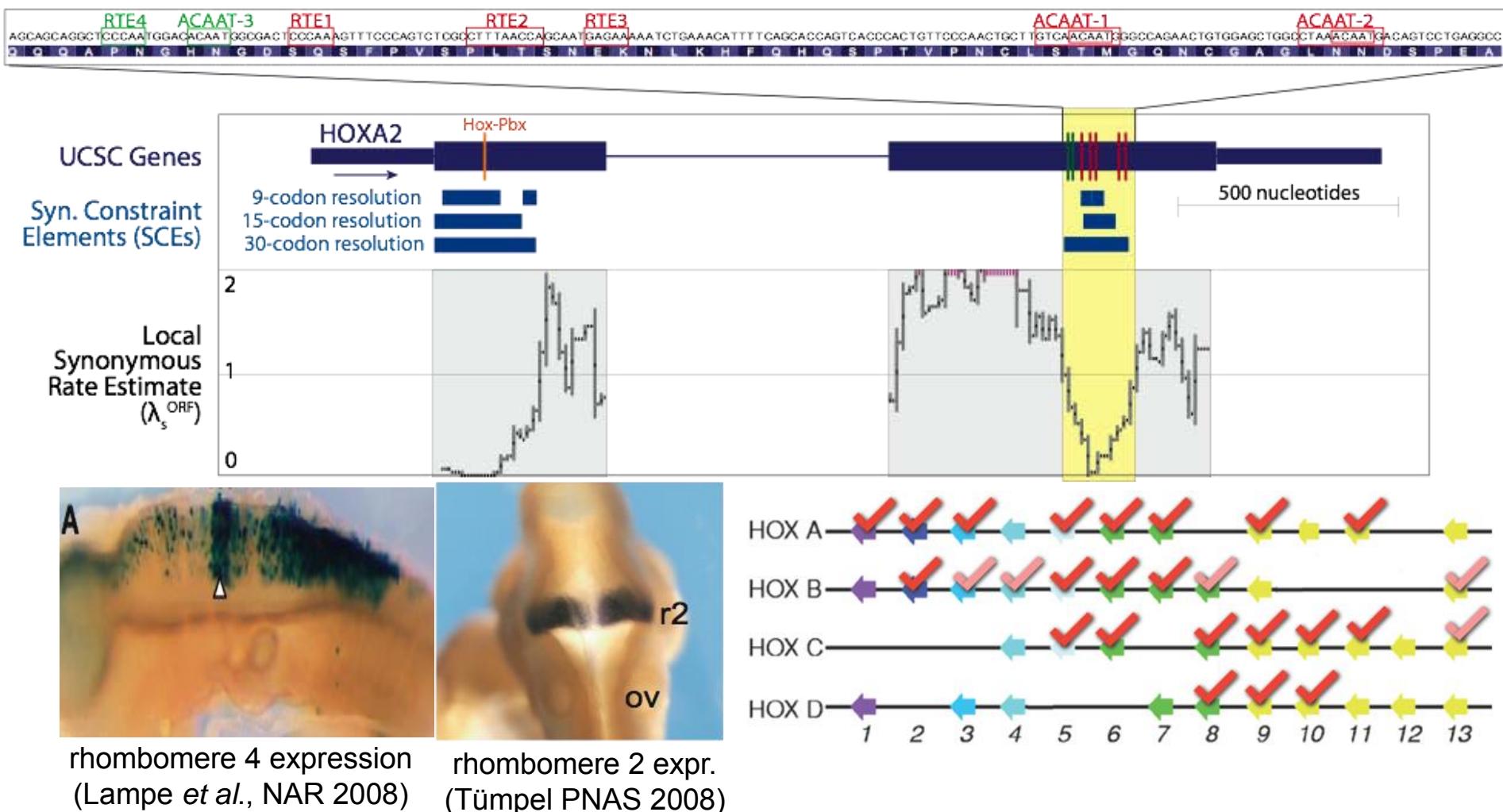
# Discover of translational readthrough genes



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## Discovery of 4 readthrough genes, abundant in many animal genomes

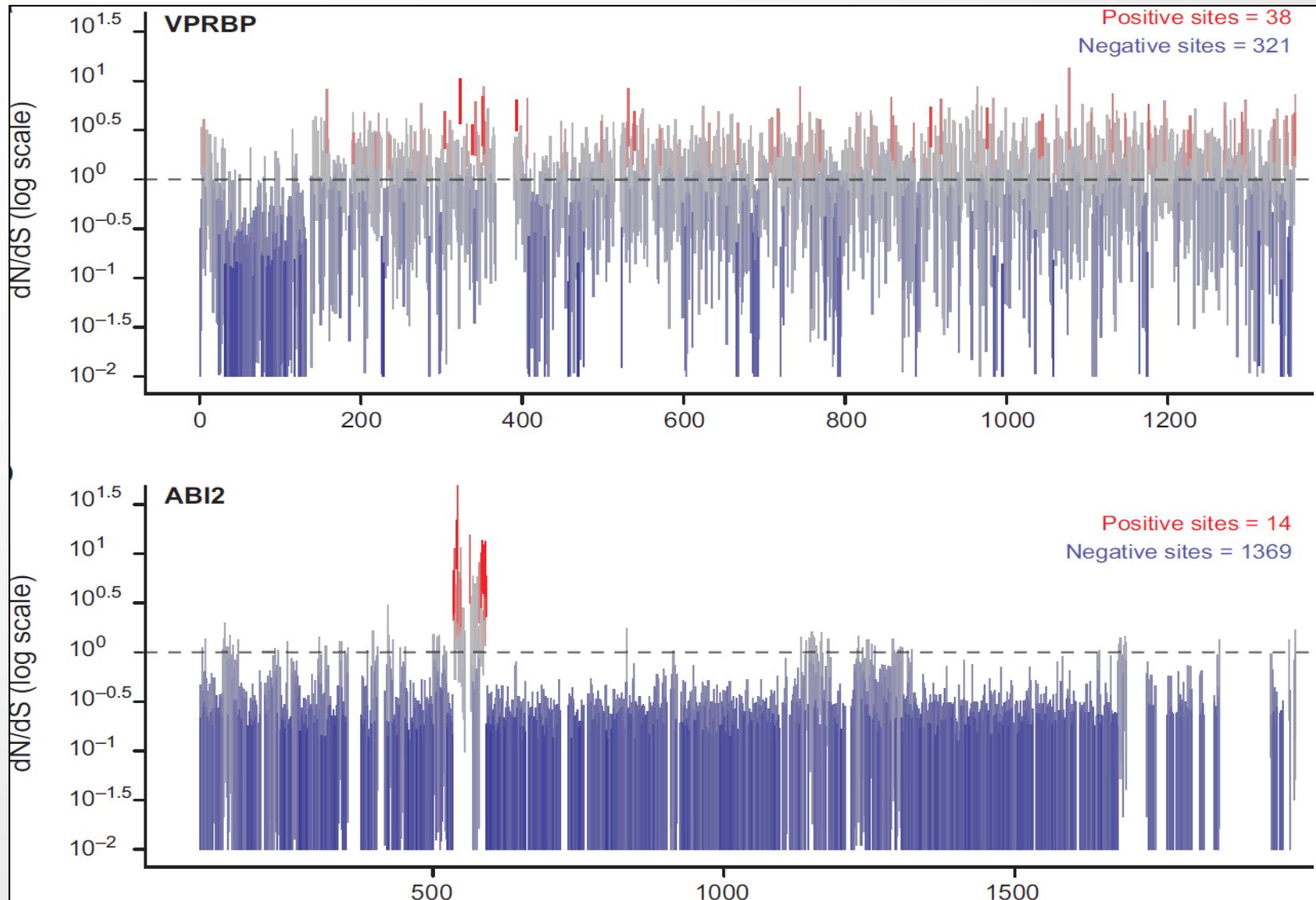
# Overlapping selection in protein-coding exons



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10,000 overlapping synonymous constrained elements  
Roles in splicing, translation, regulation

# Codon-specific measures of positive selection



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Gene-wide vs. punctate regions of exons positive selection

# **Comparative genomics I: Evolutionary signatures**

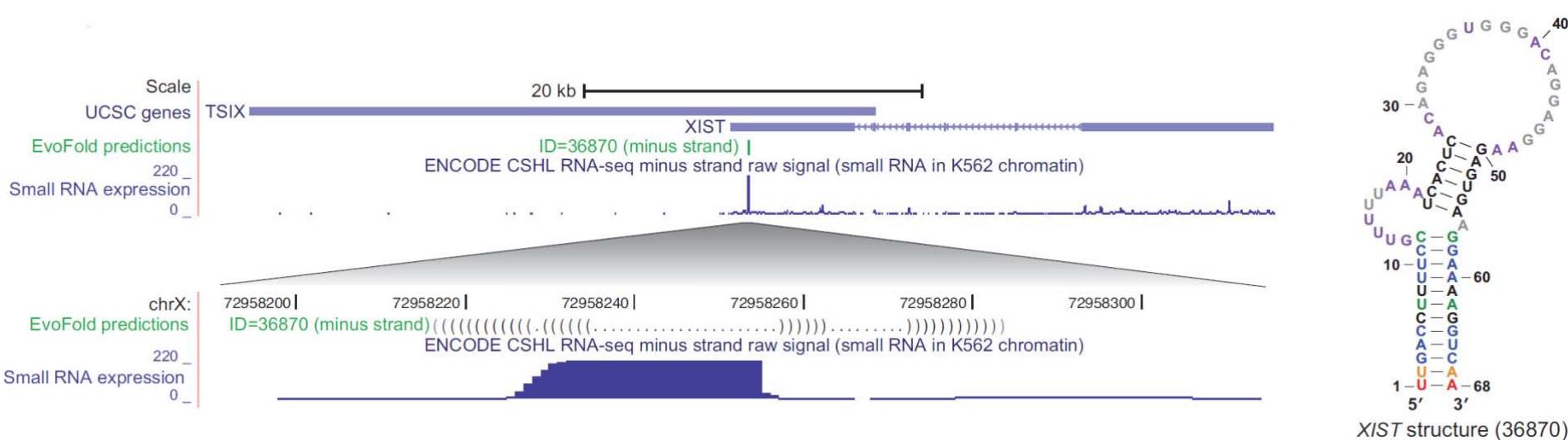
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# New RNA structures and families

	No. of structures	No. of novel structures	No. of families	No. of novel families	EvoFold score	RNAz overlap enrichment (x)	DNase hypersensitivity overlap (%)	Avg. correlation of tissue-specific expression within families
EvoFold all (no CDS)	27,012	26,643	n/a	n/a	14	13.5	25 ( $P \leq 5e-3$ )	n/a
Unfiltered families	3293	3081	1254	1215	18	17.3	25 ( $P \leq 7e-3$ )	0.14 ( $P \leq 1e-3$ )
Filtered families	725	526	220	181	18	29	32 ( $P \leq 4e-3$ )	0.15 ( $P \leq 1e-3$ )

New structs fall in families, supported by evolut/energy



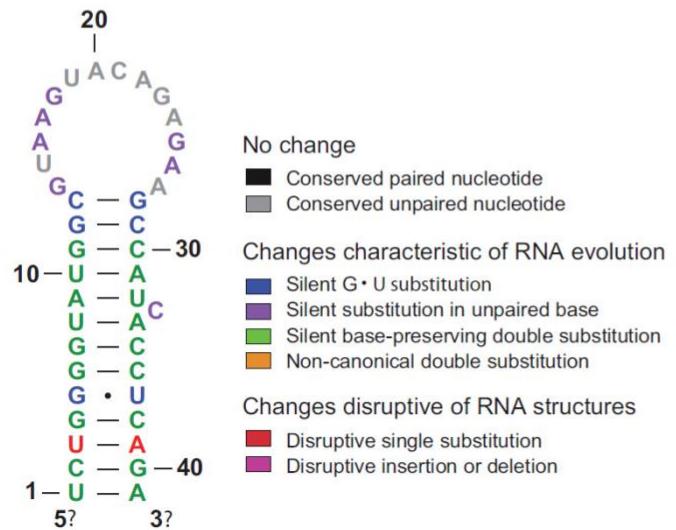
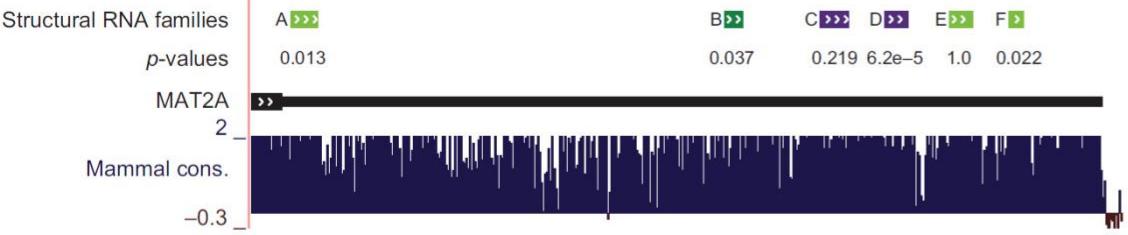
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Ex: new struct in XIST long non-coding RNA

Known function in X-chromosome inactivation

Possible functional domain of XIST?

# RNA families: orthologous/paralogous conservation



Human  
Guinea Pig  
Squirrel  
Rabbit  
Hedgehog  
Tenrec  
Sloth  
Opossum  
*Lizard*  
*X. tropicalis*  
Tetraodon  
Fugu  
Stickleback  
Medaka  
Zebrafish

D 4 2 1 10 20 30 3 40 4  
UCUGGGGUAGGC GUAAGUACAGAGAA GCCAUCCUCAGA  
A UC<sup>CC</sup>AGACU<sup>U</sup>GGC GUAGGUACAGAGAA AGCC<sup>A</sup>GCUCUGAGA  
B ..... UUGUGAUGUCA-UACAGAGAA AGUCACCGG.....  
C UCUGA<sup>A</sup>AGCUGGU GUAGCUACAGAGAA ACCAGC<sup>U</sup>UUUCAGA  
E ..... GGCA<sup>A</sup>GGGU GUCC-UACAGAAAA ACCUUGGUU....  
F ..... UGGUGUG-GUACAGAGAA AGCCA.....  
(((((((((.....))))))).)))))  
abcdefghijklmn nmlki hgfedcba

UCUGGGGUAGGC GUAAGUACAGAGAA GCCAUCCUCAGA  
UCUGGGGUAGGC GUAAGUACAGAGAA GCCAUCCUCAGA  
UCUG<sup>AG</sup>GUAGGU GUAAGUACAGAGAA GCCAUCCUCAGA  
UCUGGGGG<sup>G</sup>AUGGC GUAAGUACAGAGAA GCCAUCCUCAGA  
UCUG<sup>AG</sup>GUAGGC GUAAGUACAGAGAA GCCAUCCUCAGA  
U-GGGGUAGGC UUAAGUACAGAGAA GCCCUCACCUCAGA  
UCUGGGGUAGGU GUAAGUACAGAGAA CCCGUACCCUCAGA  
UCUGGGGU<sup>G</sup>GGC GUGAGUACAGAGAA CCUAUCACCUCAGA  
U-UGGGACC<sup>GGG</sup>U GUGAGUACAGAGAA GCCCUUGUCUCAA  
UCUAGGC<sup>U</sup>GGG GUAAGUACAGAGAA GCCUUUGCCU---  
UCUGAGGCC<sup>GG</sup>C GUGGAUACAGAGAA GUCGGGCUUUCAGG  
UCUGAGGCC<sup>GG</sup>C GUGGAUACAGAGAA GUCGGGCUUGUCAGG  
UCUGAGACGCC<sup>GG</sup>C GUGGAUACAGAGAA GCUGUGGUUUCAGA  
UCUGGAA<sup>C</sup>CGC GUGGAUACAGAGAA GCCGAUGUUUCAGA  
CUUGAGCCU<sup>GG</sup>C GUCGGUACAGAAA GCCGGGAUCUCAAG  
\* \*\*\*\*\* \*  
(((((((((.....))))))).)))))  
abcdefghijklmn mlkji hgfedcba

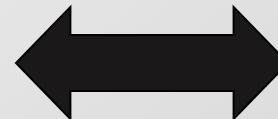
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Example of new structural 3'UTR family in MAT2A gene  
likely role in detecting S-adeosyl-methionine (SAM) level

# Computational challenge of miRNA discovery

760,355  
miRNA-like hairpins

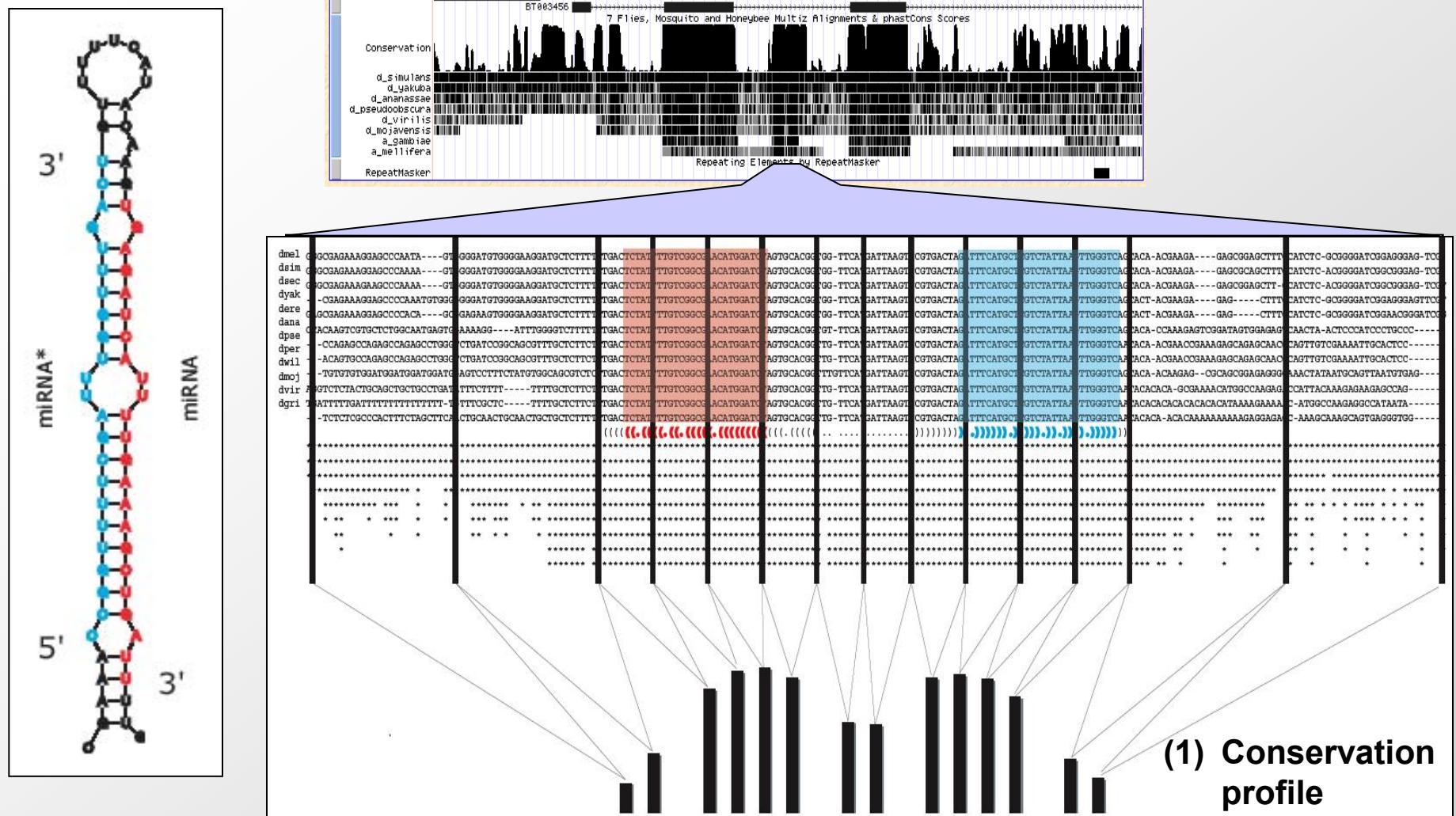
60-100  
true miRNAs



A false positive rate of 0.5% → 3800 spurious hairpins.

Need 99.99% specificity (>5,000-fold enrichment)

# Evolutionary signatures for microRNA genes

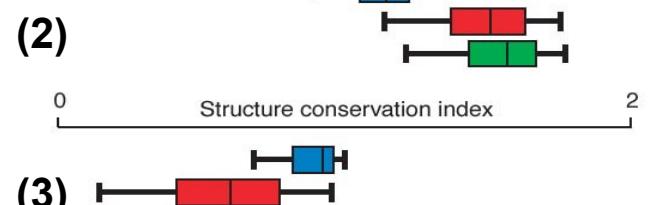
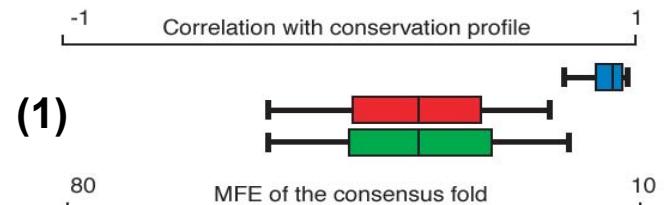


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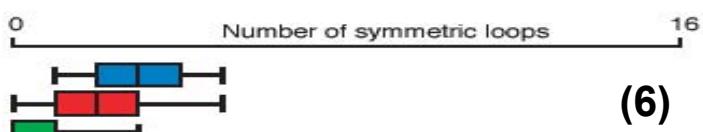
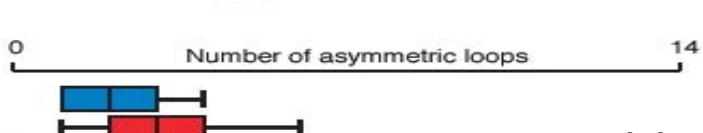
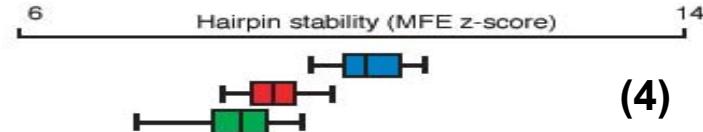
miRNAs show characteristic conservation properties

# Distinguishing true miRNAs from random hairpins

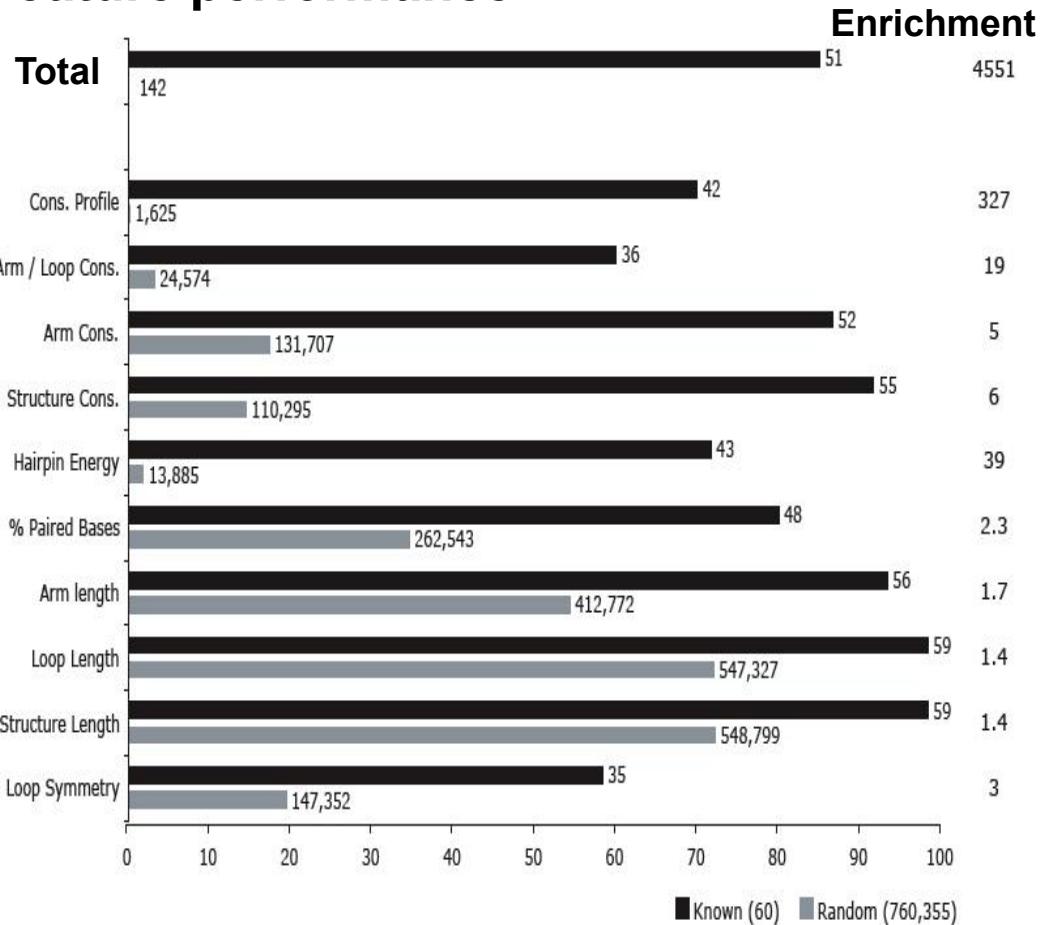
## Evolutionary features



## Structural features



## Feature performance



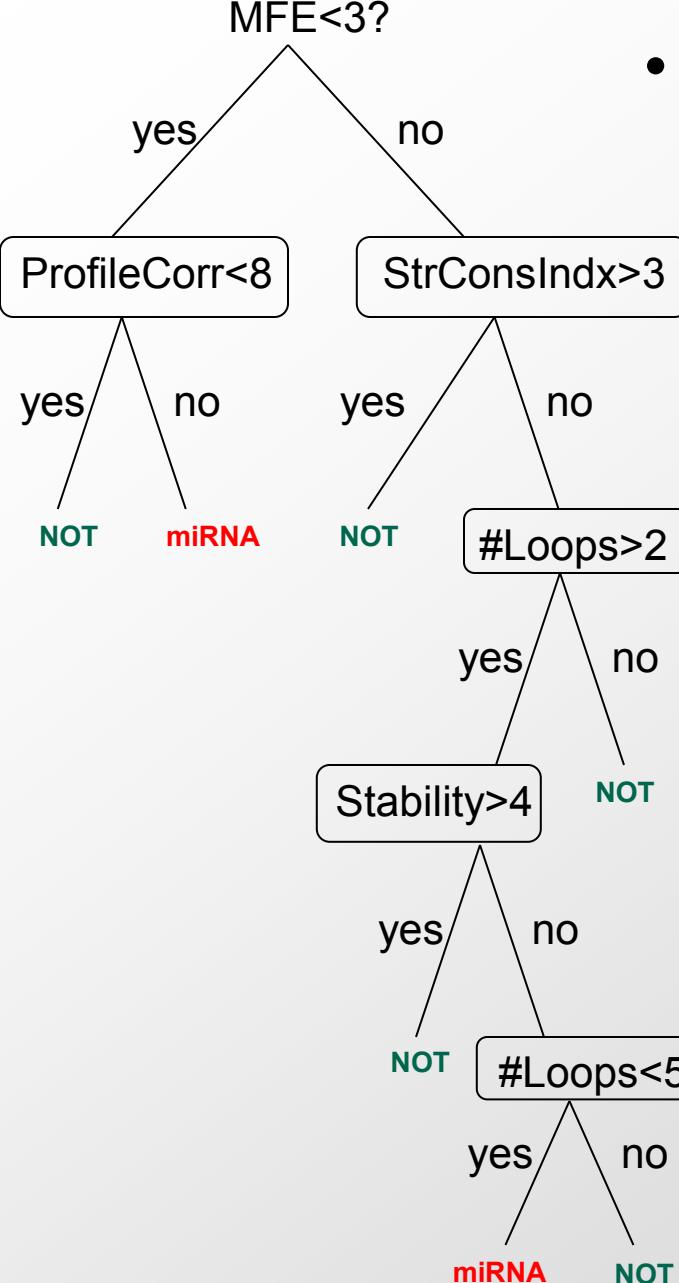
Combination of features:  
> 4,500-fold enrichment

# **Comparative genomics I: Evolutionary signatures**

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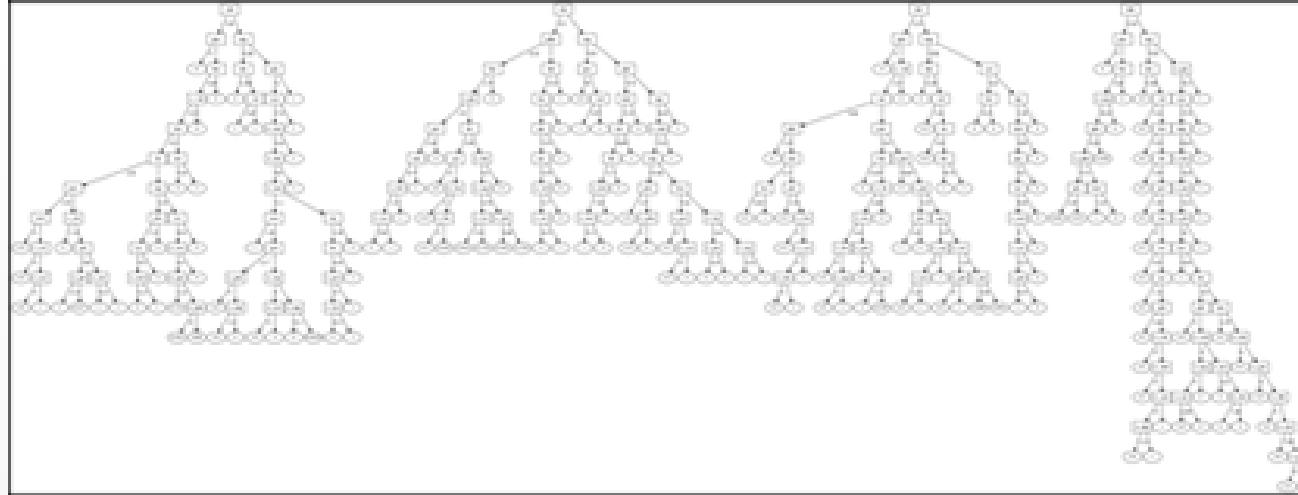
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# miRNA detection using many decision trees



- For each tree:
  - Randomly select:
    - Subset of features to base classification on
    - Subset of +/- training examples
    - Remainder of testing examples
  - Use to train a decision tree classifier:
    - Select a feature and cutoff at each level
    - Continue with feature/cutoff at next level
    - (...)
  - Evaluate performance on test set:
    - Push each element down the decision tree
    - Leaf label gives classification decision
- To combine trees:
  - Average prediction class across trees
  - Report class with maximum # of votes

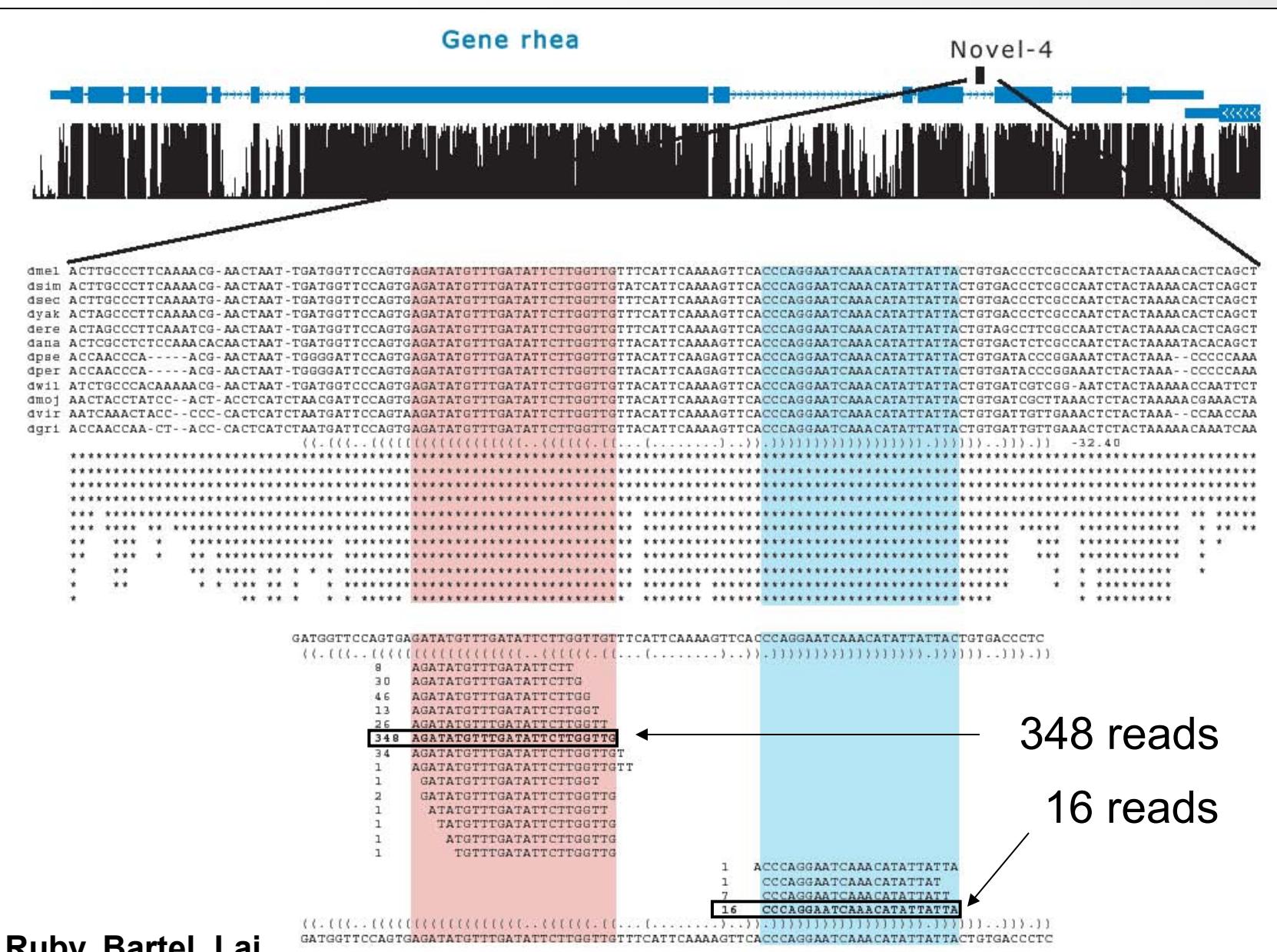
# Random Forests: Combine many decision trees



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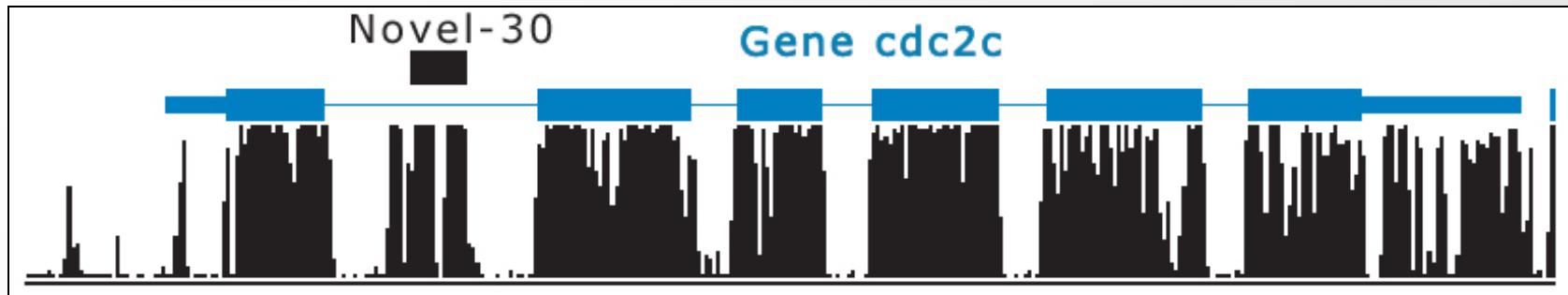
- **Many decision trees:**
  - Each can select cutoffs and direction of cutoff
  - Each feature can be reused multiple times
  - Used serially (AND) and in parallel (OR)
- **Ensemble classifier**
  - Bagging: model averaging, combines predictions
  - Can take median of predictions
- **Advantages: Robustness, Feature importance**

## **Evidence 1: Novel miRNAs match sequencing reads**

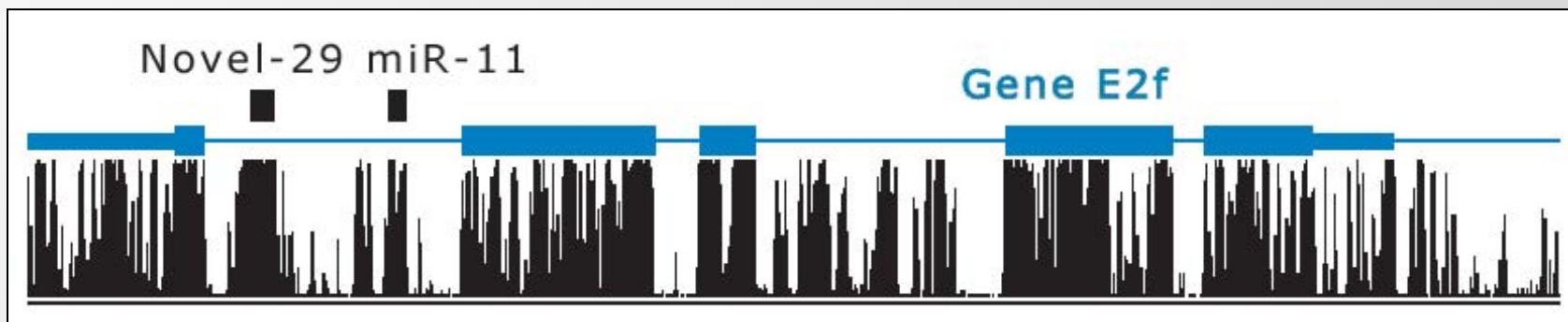


Ruby, Bartel, Lai

## Evidence 2: Genomic properties typical of miRNAs



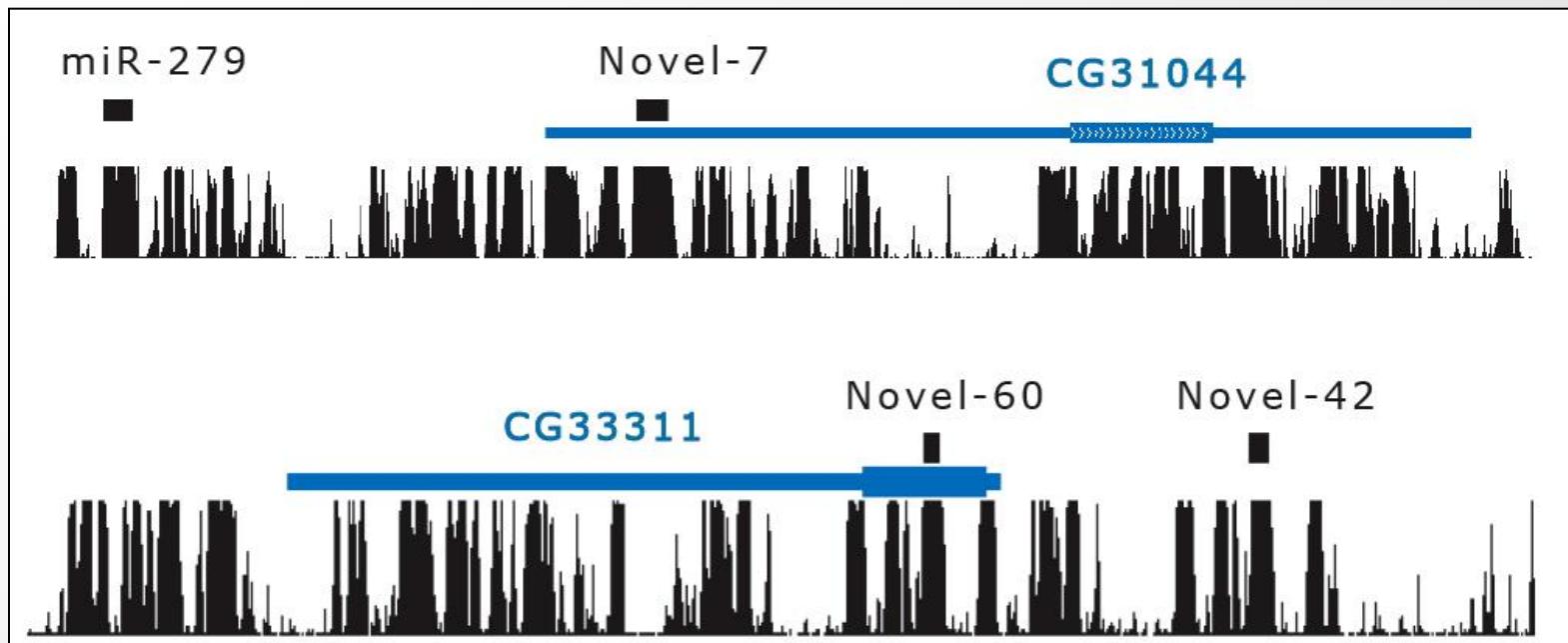
- Novel miRNAs in introns of known genes
- Preference for + strand, transcription factors



- Genomic clustering with novel / known miRNAs
- Same family, common origin / same precursor

# Two ‘dubious’ protein-coding genes are in fact miRNAs

Two novel miRNAs overlap exons (5'UTR and coding!)



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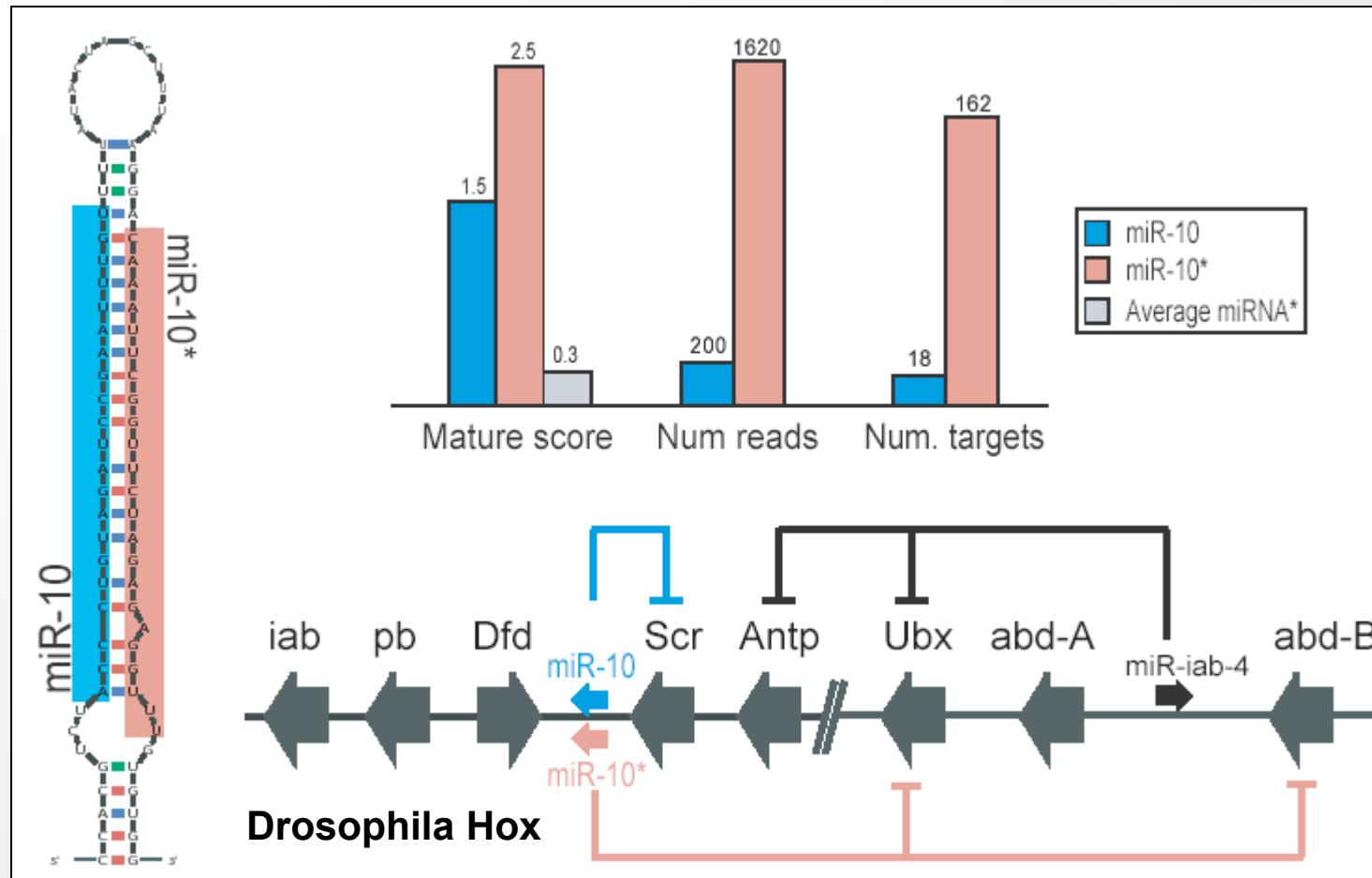
- Both CG31044 and CG33311 were independently rejected as *dubious* based on their non-protein-coding conservation patterns (Lin *et al.*)
- Novel miRNA genes provide explanation for their transcripts, as their precursor miRNA

# **Comparative genomics I: Evolutionary signatures**

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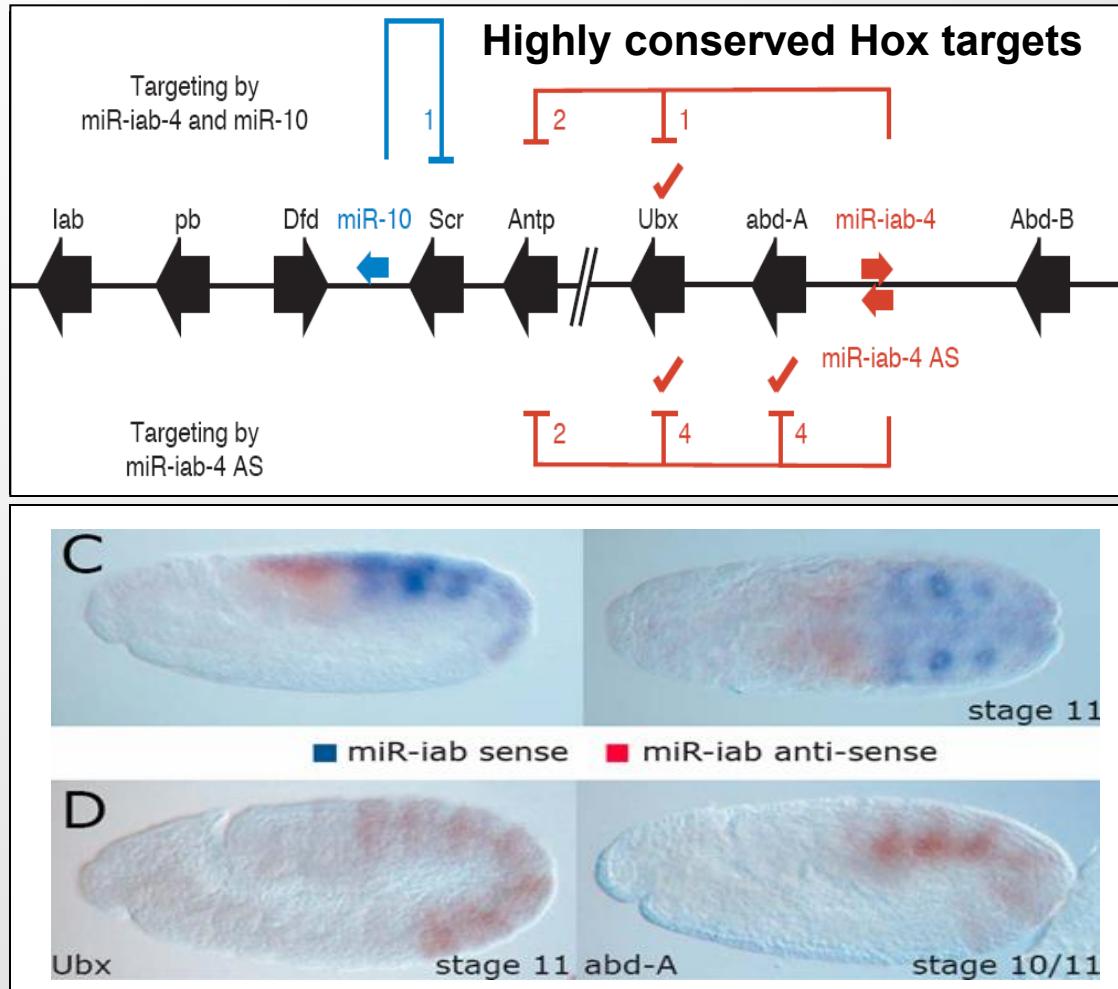
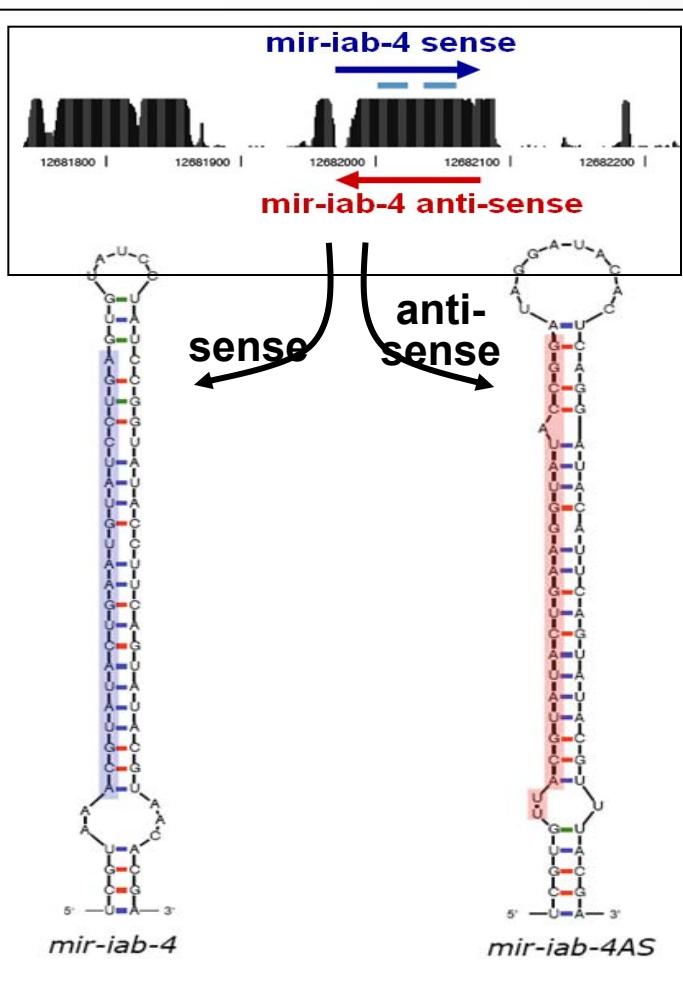
# Surprise 1: microRNA & microRNA\* function



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- Both hairpin arms of a microRNA can be functional
  - High scores, abundant processing, conserved targets
  - Hox miRNAs miR-10 and miR-iab-4 as master Hox regulators

# Evidence of miR-iab-4 anti-sense (AS) function

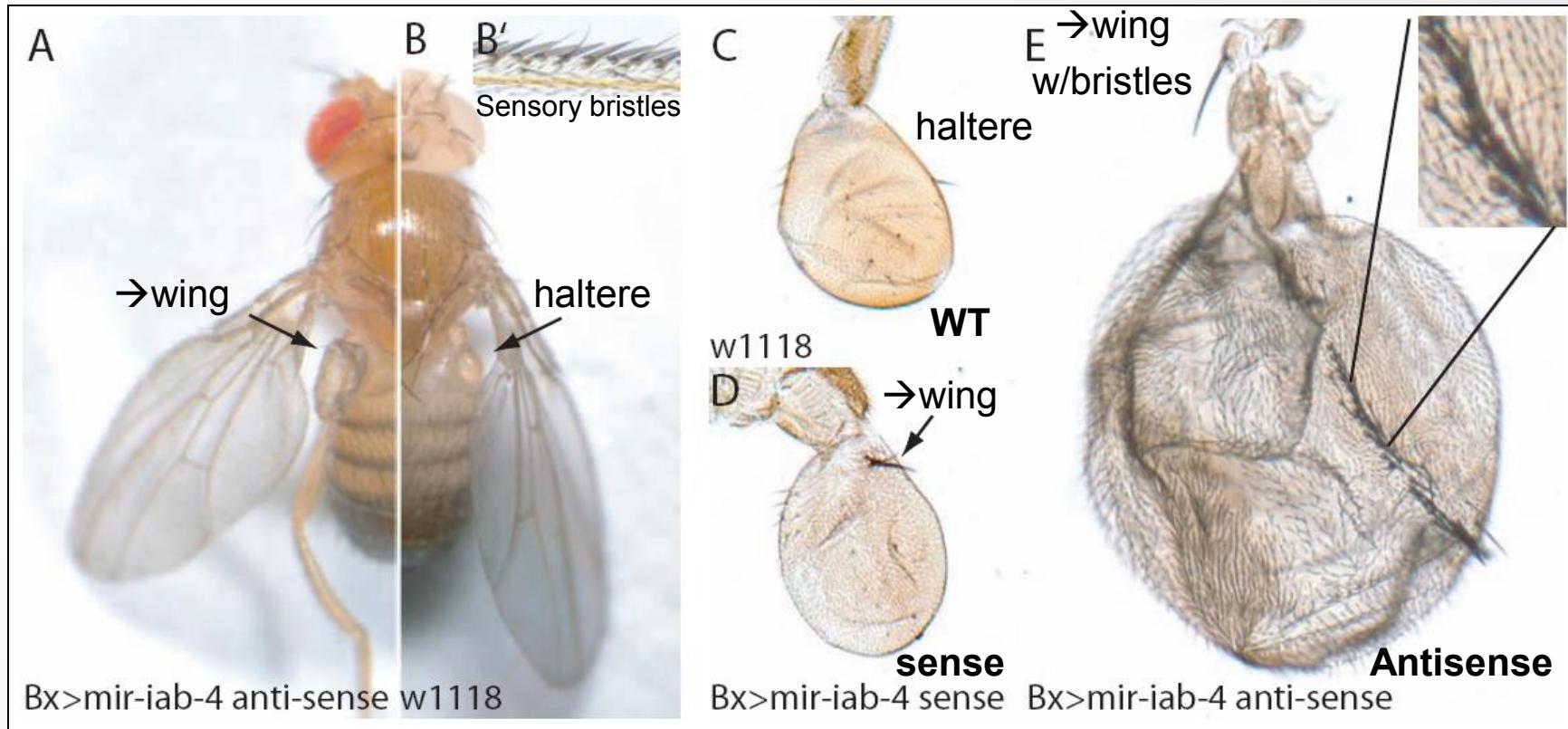


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Source: Stark, Alexander et al. "A single Hox locus in Drosophila produces functional microRNAs from opposite DNA strands." *Genes & development* 22, no. 1 (2008): 8-13.

- A single miRNA locus transcribed from both strands
- The two transcripts show distinct expression domains (mutually exclusive)
- Both processed to mature miRNAs: *mir-iab-4*, *miR-iab-4AS* (anti-sense)

# miR-iab-4AS leads to homeotic transformations

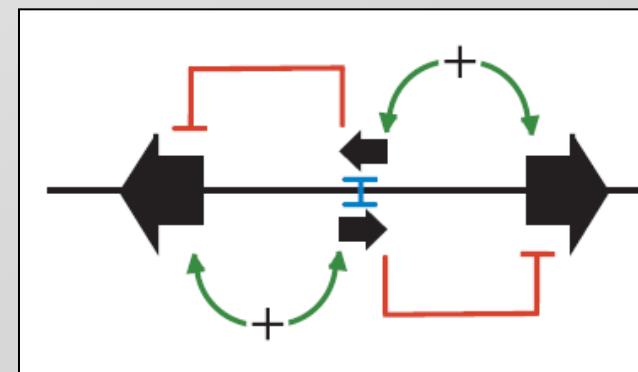


Note: C,D,E same magnification

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Source: Stark, Alexander et al. "A single Hox locus in *Drosophila* produces functional microRNAs from opposite DNA strands." *Genes & development* 22, no. 1 (2008): 8-13.

- **Mis-expression of miR-iab-4S & AS: alteres → wings homeotic transform.**
- **Stronger phenotype for AS miRNA**
- **Sense/anti-sense pairs as general building blocks for miRNA regulation**
- **10 sense/anti-sense miRNAs in mouse**

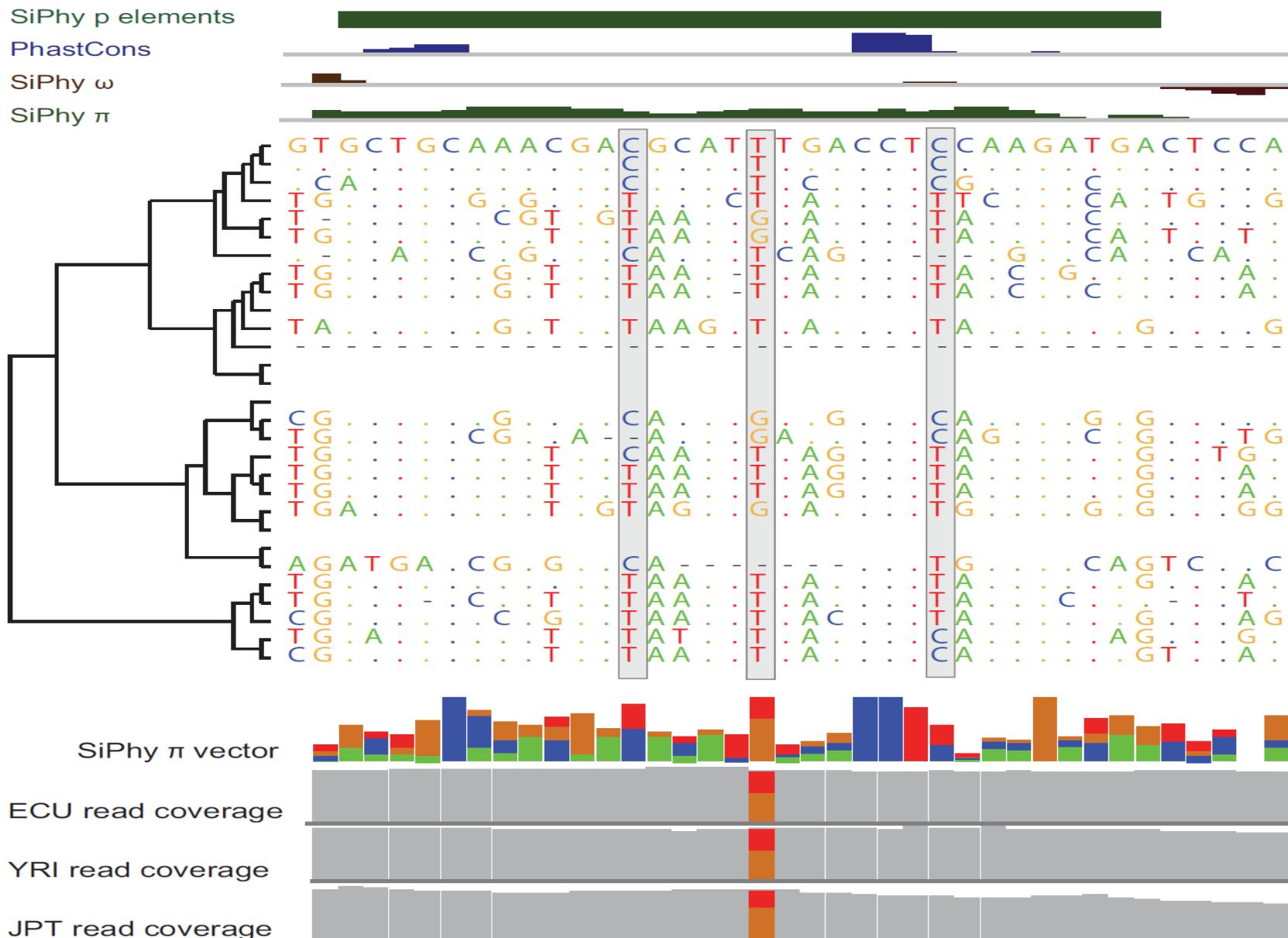


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- **Measuring selection within the human lineage**

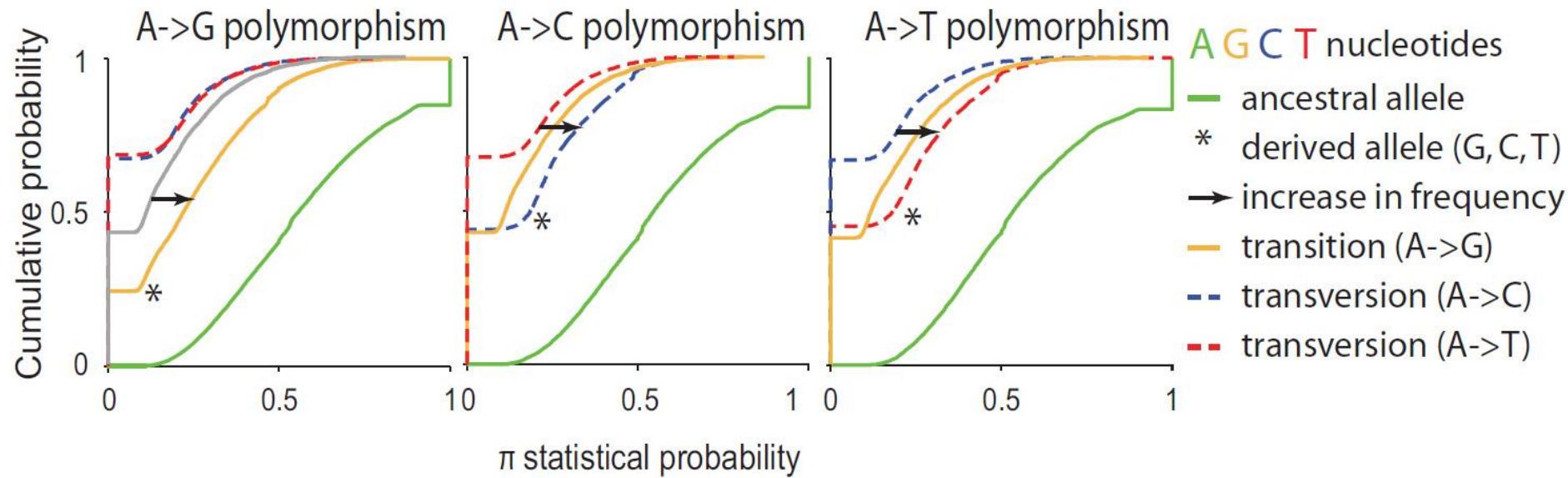
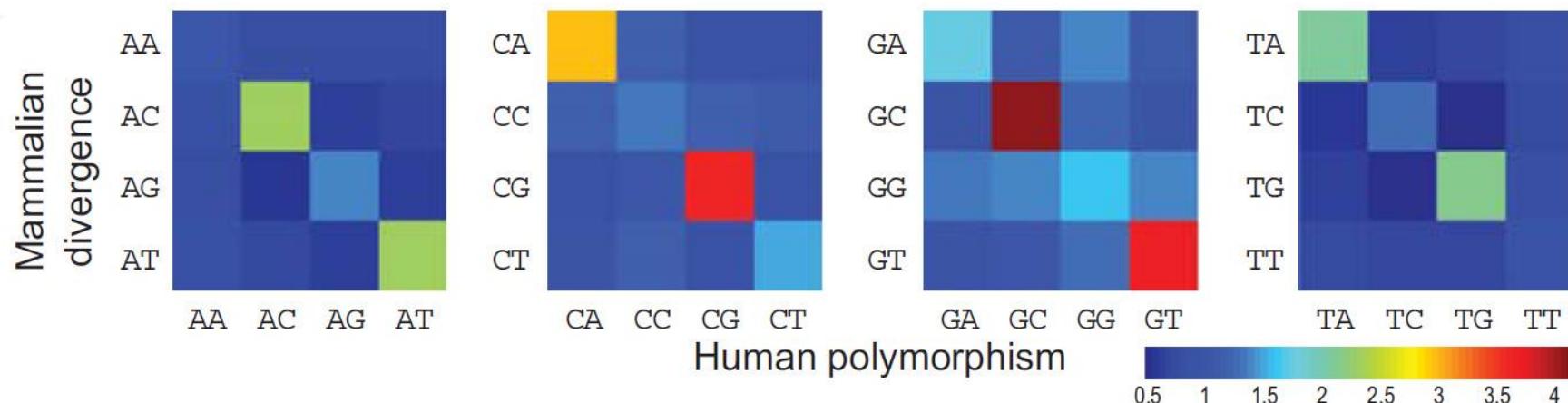
# Mammalian constraint matches Human SNPs



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Human SNPs match mammalian-wide twofold constraint<sup>66</sup>

# Mammalian constraint matches Human SNPs



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# Human constraint outside conserved regions



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## Active regions

5.9

Conserved

4.0

4.8

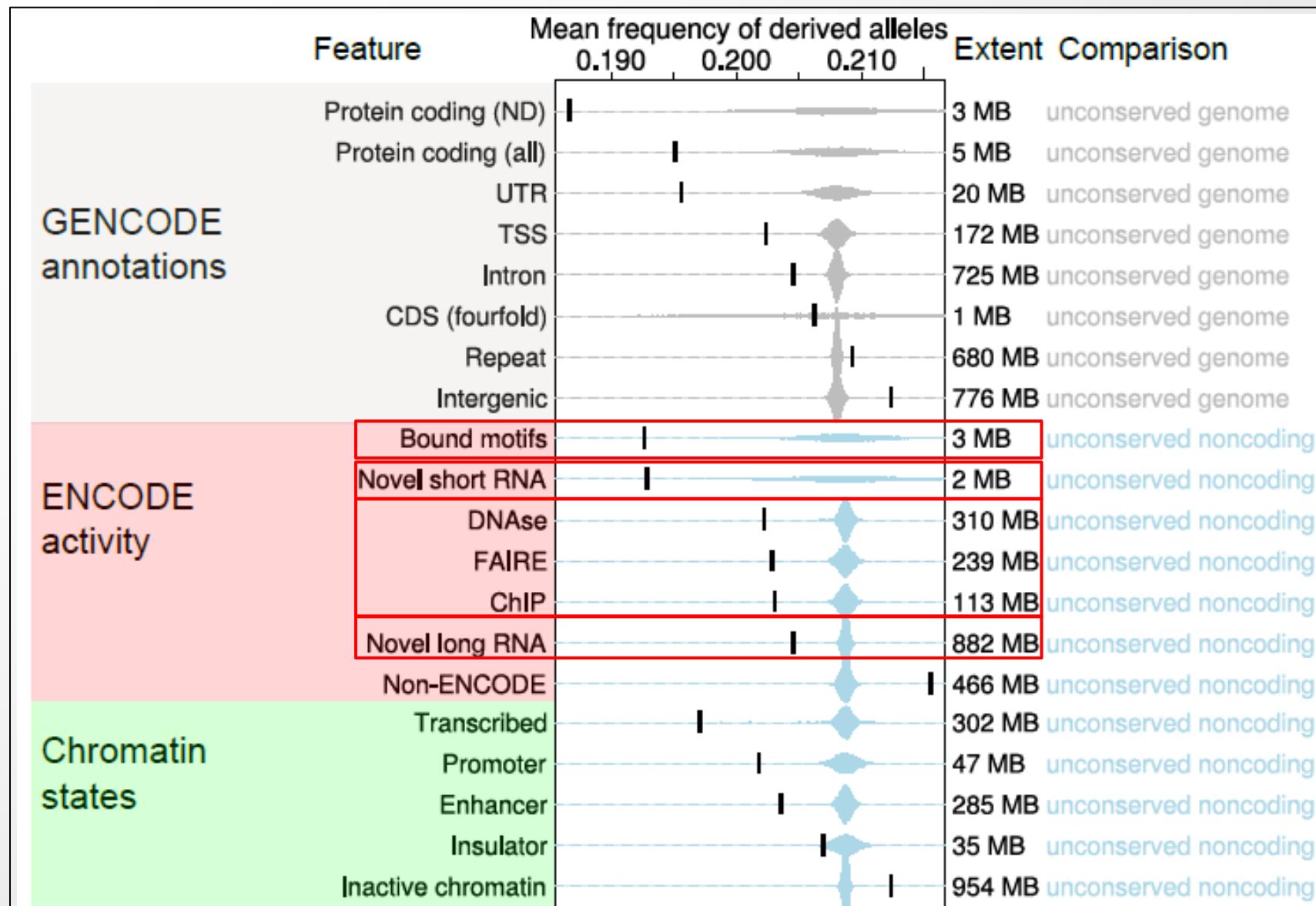
6.8

Average  
diversity  
(heterozygosity)

Aggregate over  
the genome

- **Non-conserved regions:**
  - ENCODE-active regions show reduced diversity
- Lineage-specific constraint in biochemically-active regions
- **Conserved regions:**
  - Non-ENCODE regions show increased diversity
- Loss of constraint in human when biochemically-inactive<sub>68</sub>

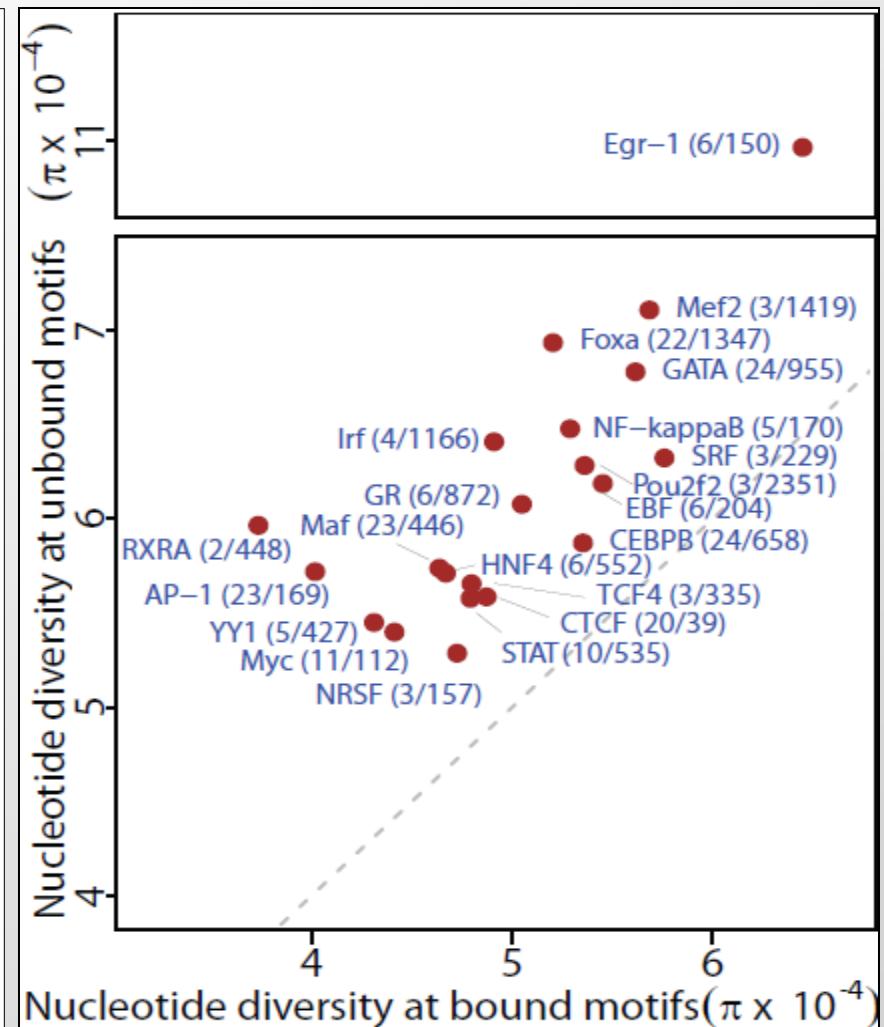
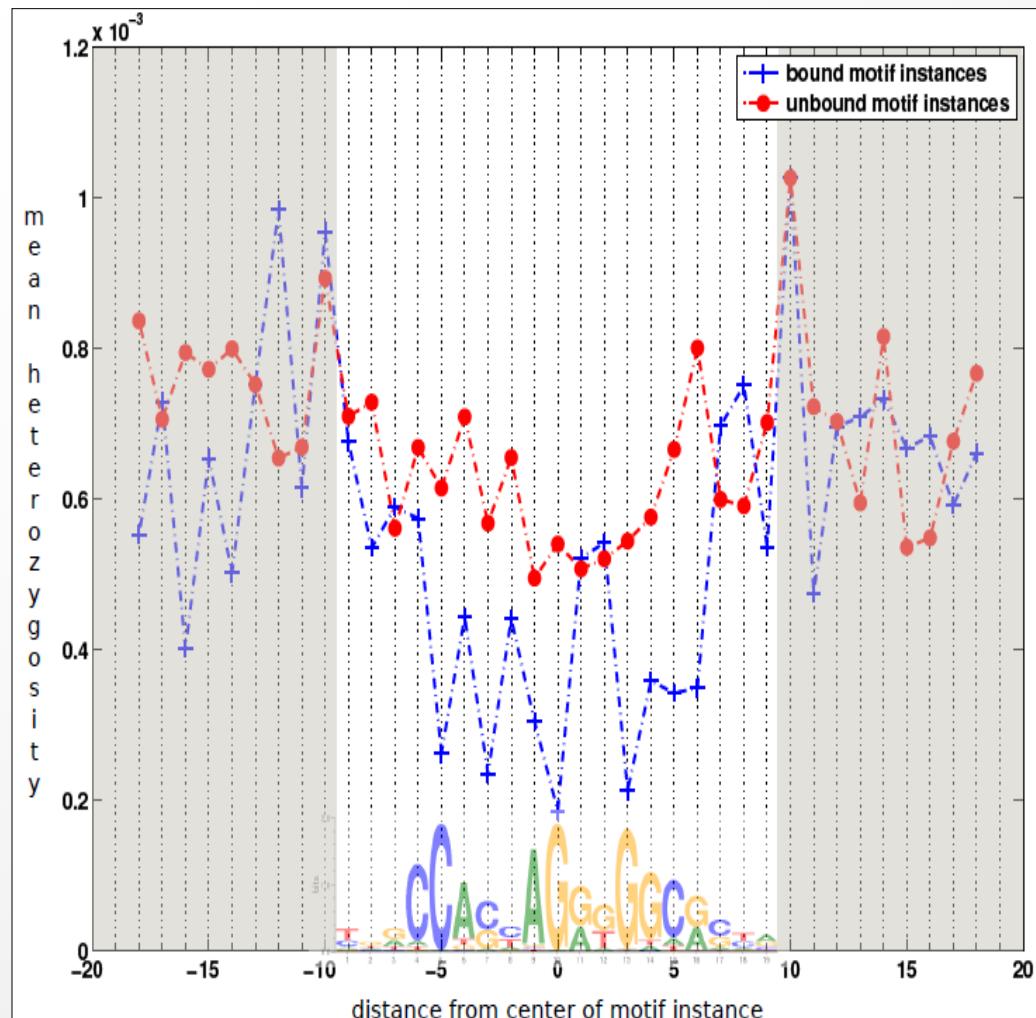
# Strongest: motifs, short RNA, Dnase, ChIP, lncRNA



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- Significant derived allele depletion in active features

# Bound motifs show increased human constraint



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Position-specific reduction in bound motif heterozygosity  
Aggregate across thousands of CTCF motif instances

# Most constrained human-specific enhancer functions

Transcription initiation from Pol2 promoter

Transcription coactivator activity

Transcription factor binding

Chromatin binding

Negative regulation of transcription, DNA-dependent

Transcription factor complex

Protein complex

Protein kinase activity

Nerve growth factor receptor signaling pathway

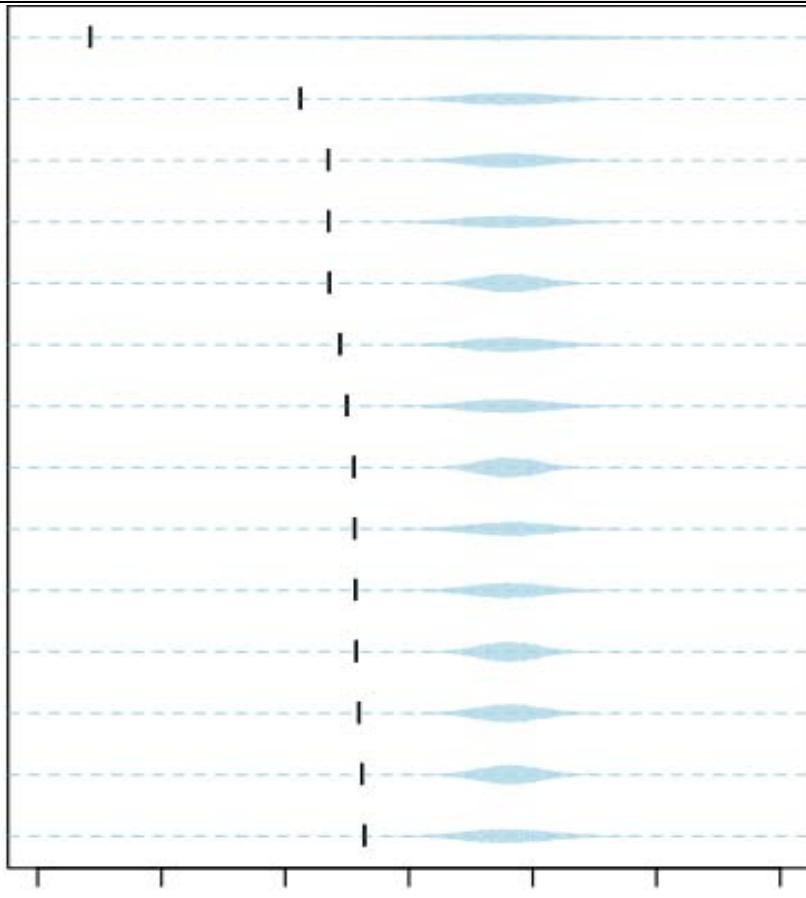
Signal transducer activity

Protein serine/threonine kinase activity

Negative regulation of transcription from Pol2 prom

Protein tyrosine kinase activity

In utero embryonic development



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Regulatory genes: Transcription, Chromatin, Signaling.

Developmental enhancers: embryo, nerve growth

# **Comparative genomics I: Evolutionary signatures**

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- **Nucleotide conservation: evolutionary constraint**
  - Purifying selection, neutral branch length, discovery power
  - Detect constrained elements: nucleotides, windows, HMM
  - Estimate fraction constrained: signal vs. background
- **Evolutionary signatures: focus on pattern of change**
  - Different functions  $\Leftrightarrow$  Characteristic patterns of evolution
- **Signatures of protein-coding genes**
  - Reading-frame conservation, codon-substitution frequency
  - Likelihood ratio framework: Estimating  $Q_C Q_N$ , scoring
  - Revise genes, read-through, excess constraint regions
- **Signatures of microRNA genes**
  - Structural and evolutionary features of microRNAs
  - Combining features: decision trees, random forests
  - Sense/anti-sense miRNAs, mature/star arm cooperation
- **Measuring selection within the human lineage**

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