

B₁-Sensitivity Analysis of qMT

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INTRODUCTION: B₁ mapping is an important measurement used in quantitative magnetization transfer (qMT) imaging, particularly at high field strengths (≥ 3.0 T) where B₁ can vary by $\pm 30\%$ in a human brain (Fig. 1). For pulsed spoiled gradient echo (SPGR) qMT imaging experiments, B₁ maps are used as a corrective factor for the excitation flip angle ($\sim 5^\circ$ to 15°) and MT saturation power (flip angles $\sim 150^\circ$ to 700°). Additional measurements necessary for qMT (e.g. T₁ mapping) may also require B₁ maps as a corrective factor; variable flip angle (VFA) T₁ mapping requires B₁ maps, while inversion recovery (IR) or Look-Locker typically do not¹. Thus, local (e.g. artifacts) or global (e.g. systemic biases) inaccuracies in B₁ mapping² will propagate to the fitted qMT parameters differently, depending on the chosen T₁ mapping method.

We recently reported that the qMT pool-size ratio (F), an important myelin biomarker, is insensitive to a large range of B₁ inaccuracies when using VFA for T₁ mapping³ (Fig. 1). Here we present a simulation-based analysis of the B₁ sensitivity of qMT, comparing how different T₁ mapping methods (VFA vs. IR) propagate the B₁ error to the qMT parameters. We show that the F parameter is very robust and insensitive to B₁ inaccuracies when VFA T₁ mapping is used, but this comes at the expense of a substantial increase in error of kf.

METHODS: The Bloch-McConnell equations for magnetization exchange were solved using MATLAB (MATLAB2011a, The Mathworks Inc.) for a pulsed SPGR experiment by decomposing the pulse sequence into periods of instantaneous saturation of the free pool, constant irradiation of the restricted pool, and free precession⁴. Healthy white matter tissue parameters were fixed to the following values: $F = 0.122$, $k_f = 3.97 \text{ s}^{-1}$, $R_{1f} = 1.11 \text{ s}^{-1}$, $R_{1r} = 1.0 \text{ s}^{-1}$, $T_{2f} = 27.2 \text{ ms}$, $T_{2r} = 10.96 \mu\text{s}$. The MT signal was simulated from the solution of the Bloch-McConnell equation for the following MT protocol: TR = 25 ms, $\alpha_{\text{excitation}} = 7^\circ$, Gaussian-Hanning MT pulses with a pulse duration of 10.2 ms, $\alpha_{\text{MT}} = 142^\circ$ and 426° , logarithmically spaced off-resonance frequencies = 423.9 Hz, 1,087.5 Hz, 2,731.6 Hz, 6,861.6 Hz, and 17,235.4 Hz. The MT signal was subsequently fitted using the Sled and Pike method⁵ for a linear range of 100 B₁ and 100 T₁ values (10,000 points in total); T₁ varied independently of B₁ for this step, and without any assumptions on the measurement method. B₁ ranged from 0.5 to 2 (B_{1,true} = 1), and T₁ ranged from 0.1 s to 4 s (T_{1,true} = 0.9 s). VFA signals were also simulated from the analytical SPGR equation¹: TR = 25 ms, $\alpha = 3^\circ$ and 20° , T₁ = T_{1,true}. T₁ values were fitted from the VFA data for the B₁ error range. The fitted T₁ values were subsequently used in conjunction with their respective B₁ values to fit the MT signal.

RESULTS: Figure 2 shows the error (%) of the fitted qMT pool-size ratio, F, in the presence of a wide range of B₁ and T₁ inaccuracies (B_{1,true} = 1, T_{1,true} = 0.9 s). The superimposed lines show the range of errors expected from an experiment using a B₁ independent T₁ method like IR (solid line), and from VFA T₁ mapping (dashed line). Figure 3 plots the errors in qMT fitted parameters (F, kf, T_{2f}, T_{2r}) using B₁-independent (IR) and VFA measured T₁ (see lines in Fig. 2), for a range of B₁ inaccuracies typically observed in vivo. Errors in F induced by B₁ errors were greatly reduced using VFA T₁ mapping (Fig. 3a). A substantial increase in errors in kf occurs for VFA relative to IR (Fig. 3b), while T_{2r} remains insensitive to B₁ inaccuracies for both cases.

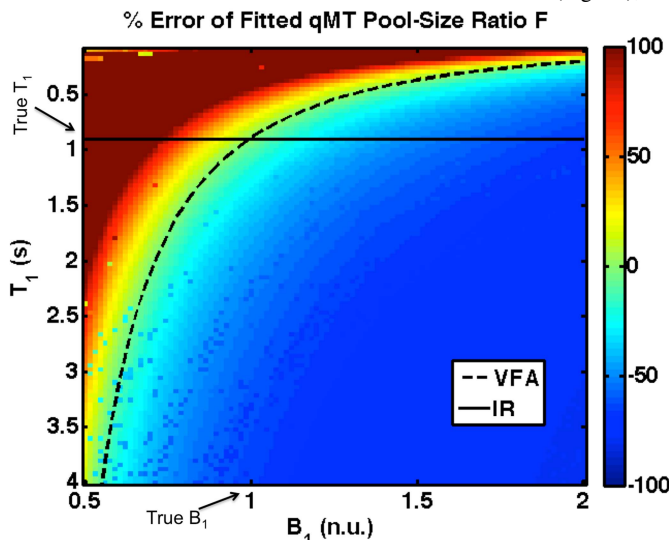


Figure 2. Percent error in fitted qMT F values in the presence of a wide range of B₁ and T₁ errors (B_{1,true} = 1 n.u., T_{1,true} = 0.9 s). The superimposed lines plot the T₁ distribution for a B₁-independent T₁ mapping method (IR, solid line) and VFA (dashed line).

DISCUSSION: The qMT pool size ratio F was shown to be nearly B₁-error insensitive when using VFA T₁ mapping (Fig. 3a - blue). Using a B₁-independent T₁ measure such as IR produces large qMT F errors (from $>100\%$ to -45% for B₁ errors ranging from -30% to 30% , Fig 3a - red), while VFA T₁ mapping kept qMT F errors within a moderate range (7% to -3% , Fig. 3a - blue). The B₁ errors for the case of VFA were mostly absorbed by the kf parameters (Fig. 3b), in agreement with observations from previous in vivo work³. These results suggest that qMT imaging using B₁-independent T₁ measurement, and qMT methods that fixes qMT model parameters, may have increased sensitivity to B₁-inaccuracies. However, for applications where kf may be the biomarker of interest (e.g. cartilage imaging⁶, systemic inflammation⁷), a B₁-independent measure of T₁ may be preferred instead of the VFA method. Further analytical sensitivity analysis of the qMT equations for different qMT measurement protocols could help determine optimal qMT protocols for reduced B₁-inaccuracy sensitivity.

REFERENCES: [1] Stikov, n. et al, MRM, doi: 10.1002/mrm.25135 (2014) [2] Boudreau, M. et al, Proc. of ISMRM, #3207 (2014) [3] Boudreau, M. et al, Proc. of ISMRM, #3167 (2014) [4] Sled J. and Pike G. B., JMR, 145:24-36 (2000) [5] Sled J. and Pike G. B., MRM, 46:923-931 (2001) [6] Stikov, N. et al, MRM, 66:725-734 (2011) [7] Harrison, N. et al, Biological Psychiatry, DOI: 10.1016/j.biopsych.2014.09.023 (2014)

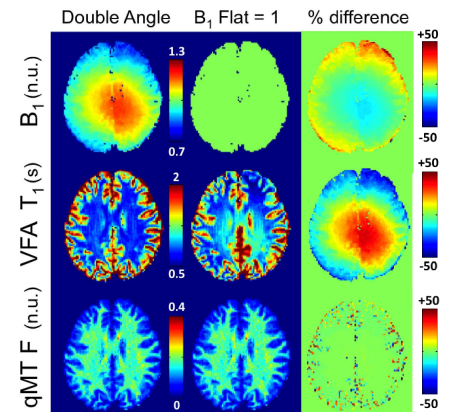


Figure 1. Comparison of VFA T₁ and qMT F maps using measured and nominal (B₁ flat = 1) B₁ maps at 3T³.

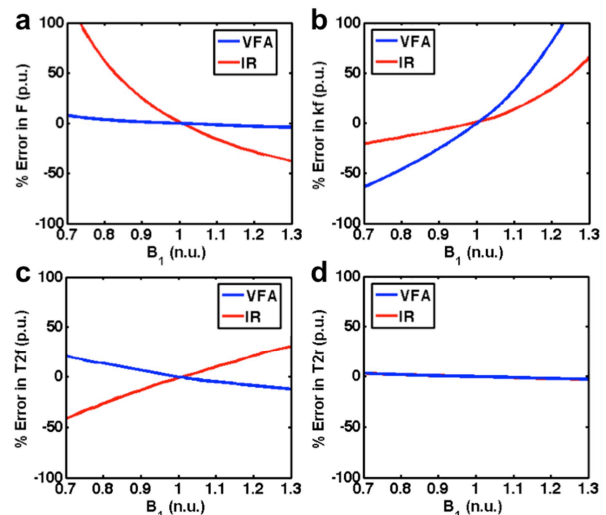


Figure 3. Percent error in fitted qMT parameters for a range of B₁ errors (a – pool size ratio (F), b – magnetization exchange rate (kf), c – free pool T₂ (T_{2f}), d – restricted pool T₂ (T_{2r})). Fits using a B₁-independent T₁ measure (IR) are shown in red, and those using VFA T₁ mapping are shown in blue. See solid and dashed lines in Fig. 2 for B₁ dependence of IR and VFA T₁.