THE MINIMAL SUPERSYMMETRIC STANDARD MODEL

Part II: Phenomenology

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Supersymmetry Seminar supervised by Prof. Jörg Jäckel

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Outline

- 1. Overview
- 2. Phenomenology of the MSSM
- 3. A Top-Down Approach to Low-Energy Phenomenology: mSUGRA
- 4. Grand Unification and SUSY
- 5. Going Beyond the MSSM
- 6. Summary and Outlook

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What have we learned so far and what needs to be discussed?

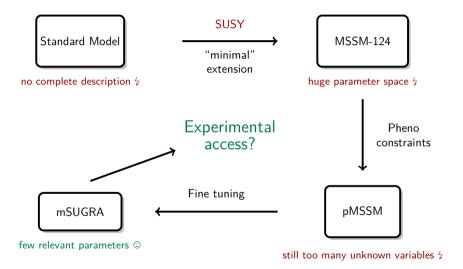
- State of the Art: We promoted the SM to the MSSM-124 and found a variety of new degrees of freedom that need to be taken into account in further investigations.
- Now we want to understand how to make sense of a theoretical model with $\mathcal{O}(100)$ parameters.
- Central Question: Is it possible to reduce this huge number of parameters to a reasonable number that may be tested in future experiments?¹
- Phenomenology of the MSSM: Focus on the "pMSSM" and Gauge Coupling Unification.
- Which problems are still present? Why might the "minimal" SSM not be enough?

¹Experimental details \rightarrow talk next week!

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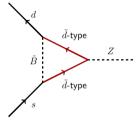
How to test the MSSM?



Some Observations

This huge additional parameter space in general comes with some severe problems :

- The respective lepton numbers L_e , L_μ and $L_ au$ are not conserved $\mbox{\em 4}$
- Flavor-changing neutral currents (FCNCs) are unsuppressed \$
- New sources of CP-violation are present 4



For all of the above mentioned problems we have rather strict experimental bounds, for example:

Want to avoid contributions to electric dipole moments \implies complex phases of the gaugino mass parameters, A-parameters and $|\mu| \lesssim 10^{-2} - 10^{-3}$ for TeV-ish sfermion and gaugino masses [12].

General Requirements

We use these phenomenological constraints to define the phenomenological MSSM (pMSSM) [11]:

- ullet No additional sources of CP-violation \Longrightarrow all phases in the soft-SUSY-breaking potential zero
- No FCNCs ⇒ simple, diagonal structure of the sfermion and trilinear coupling matrices
- First and second generation universality \implies soft-SUSY-breaking scalar masses + trilinear couplings² A^u , A^d and A^ℓ are the same for the first two generations

In addition, for different regions of the parameter space, one can use even more severe constraints³!

²Usually they are just set to zero for the first two generations

³In actual experiments only very simplified models with two or three parameters are tested.

This already reduces the number of relevant parameters by a large amount, a summary is given below:

• $\tan \beta = v_u/v_d$, the ratio of the VEVs in the two-Higgs doublet model

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- $m_{\tilde{Q}}$, $m_{\tilde{t}_R}$, $m_{\tilde{b}_R}$, $m_{\tilde{L}}$ and $m_{\tilde{ au}_R}$, the third generation sfermion masses

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- A^t , A^b and A^τ , the third generation trilinear couplings

In total we are left with 19 additional parameters in the pMSSM.

What about SUSY-breaking?

- The MSSM-124 fails to explain the fundamental origin of the SUSY-breaking parameters.
- Last talks: Gauge- and gravity-mediated SUSY breaking may provide a way around!
- The phenomenon of gauge coupling unification hints at a simpler structure of the MSSM at high energies.



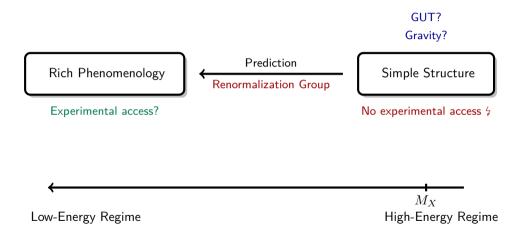
Figure: Gravity-mediated SUSY-breaking in the hidden sector⁴.

⁴Figure inspired by the visualization in: https://www.thphys.uni-heidelberg.de/-plehn/includes/bad_honnef_12/kribs_2.pdf (13.02.15)

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The mSUGRA Framework I



The mSUGRA framework II

- Want to naturally include gravity, or more precisely local SUGRA.
- SUGRA is broken at some high energy scale, usually at around $M_{\rm Planck} \sim 10^{19} \ {\rm GeV}.$
- Assume gravity-mediated SUSY breaking, i. e. $m_{
 m soft} \sim \frac{\langle F \rangle}{M_{
 m Planck}}$

The general idea is now to assume a "minimal" normalization of the kinetic terms in the SUGRA Lagrangian, i. e.

$$\mathcal{L}_{\text{SUGRA}} \supset -\frac{1}{M_{\text{Planck}}} F\left(\frac{1}{2} \alpha \lambda \lambda + \frac{1}{6} \beta \phi \phi \phi + \frac{1}{2} \gamma \phi \phi\right) + \text{h.c.} - \frac{1}{M_{\text{Planck}}^2} F F^* \delta \phi \phi^*$$

Comparison with initial $\mathcal{L}_{\mathrm{soft}} \implies$ Simple relations for the input parameters!

Finding the correct initial Conditions

The relatively simple form of the kinetic terms allows to simplify the structure of the relevant couplings at the initial scale as follows:

scalar squared-masses are flavor-diagonal and universal:

$$\begin{split} m_{\tilde{q}}^2(M_X) &= m_{\tilde{u}}^2(M_X) = m_{\tilde{d}}^2(M_X) = m_0^2 \mathbb{1} \\ m_{\tilde{\ell}}^2(M_X) &= m_{\tilde{e}}^2(M_X) = m_0^2 \mathbb{1} \\ m_1^2(M_X) &= m_2^2(M_X) = m_0^2 \end{split}$$

• the same is true for the A-parameters:

$$A^{U}(M_X) = A^{D}(M_X) = A^{E}(M_X) = A_0^2 \mathbb{1}$$

Additionally we assume unification of the (tree level) gaugino masses:

$$M_1(M_X) = M_2(M_X) = M_3(M_X) = m_{1/2}$$

Renormalization Group Equations

This allows us to compute the low-energy MSSM parameters with the help of standard renormalization group techniques!

Reminder: The beta function $\beta(g) = \frac{\partial g}{\partial \ln M}$ is the rate of change of the renormalized coupling at the scale M, where the bare coupling is fixed [17].

For example, we get the following result for the low-energy gaugino mass parameters:

$$M_{i} = \frac{\alpha_{i}\left(M_{Z}\right)}{\alpha_{\mathrm{GUT}}} m_{1/2} \longrightarrow M_{3}\left(M_{Z}\right) = \frac{\alpha_{3}\left(M_{Z}\right)}{\alpha_{2}\left(M_{Z}\right)} M_{2}\left(M_{Z}\right) = \frac{\alpha_{3}\left(M_{Z}\right)}{\alpha_{1}\left(M_{Z}\right)} M_{1}\left(M_{Z}\right)$$

This results in the well known relation:

$$M_1 = \frac{5}{3} \tan^2 \theta_W M_2 \sim \frac{1}{2} M_2$$

Solution of the RGEs for mSUGRA

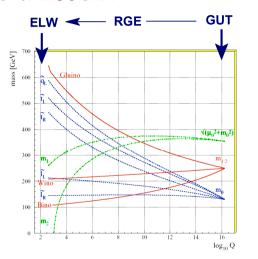


Figure: Running of the mSUGRA parameters⁵.

 $^{^{5}} Figure \ taken \ from: \ {\tt https://www.physi.uni-heidelberg.de/-uwer/lectures/ParticlePhysics/Vorlesung/Lect-10b.pdf} \ (10.02.21)$

Parameter Count in the mSUGRA Framework

This means in total we are left with only the following four continuous and one discrete free parameters in the mSUGRA model:

- $\tan \beta$, the ratio of the VEVs in the two-Higgs doublet model
- $m_{1/2}$, the universal gaugino mass
- m_0 , the universal scalar (sfermion/Higgs) mass
- A₀, the universal trilinear coupling
- $sign(\mu)$, the sign of the Higgs-higgsino mass parameter

The relations for $\tan \beta$ and $|\mu|$ come from the two minimum conditions for the Higgs potential.

Remark: Additional requirements such as the unification of the top, bottom and tau Yukawa couplings at the GUT scale further restricts the possible values of $\tan \beta$ and A_0 .

Map of the mSUGRA Parameter Space

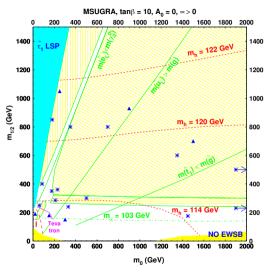


Figure: Map of the mSUGRA parameter space for different values of the universal mass parameters, slightly adapted from [10].

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Gauge Couplings in the Standard Model

The Standard Model is described as the most general renormalizable field theory with gauge group

$$\mathcal{G}_{SM} = SU(3) \times SU(2) \times U(1),$$

with associated gauge couplings α_3 , α_2 and α_1 , three generations of fermions and a scalar [4].

The couplings are larger for the larger component of the gauge group, i. e.

$$\alpha_3(m_Z) > \alpha_2(m_Z) > \alpha_1(m_Z)$$

- Interesting observation: Values of the running couplings come close together at some high energy scale $\Lambda_{\rm GUT} \sim 10^{16}~{\rm GeV}$ (cf. next slide).
- Georgi-Glashow [13]: Embed \mathcal{G}_{SM} in larger gauge group, i.e. $SU(5) \implies GUT$?

One Loop Running of the SM Gauge Couplings I

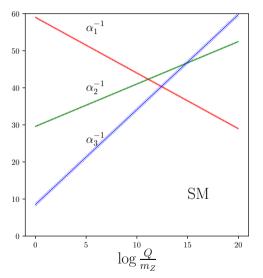
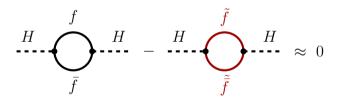


Figure: Running of the (inverse) SM gauge couplings, plot inspired by [15].

One Loop Running of the SM Gauge Couplings II

- In the Georgi-Glashow model, we need $-\mu^2 \sim -(100 \text{ GeV})^2$ to reproduce the correct W and Z masses \implies Gauge hierarchy problem! [17]
- SUSY provides way out: If SUSY breaking works such that the mass differences between the superpartners are large enough, one can reproduce the correct Higgs mass ⇒ superpartners influence the running of the (MS)SM gauge couplings (cf. next slide)



• In the end it remains a complicated fine tuning task!

Comparison: SM vs. MSSM

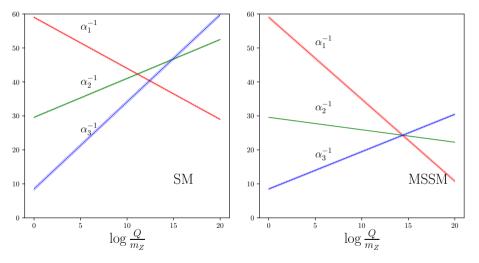


Figure: Running of the (inverse) gauge couplings in the SM and the MSSM, plots inspired by [15].

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Are all Problems solved now?

The MSSM as introduced in the first part of our talk still fails to answer some of the key questions:

- How do we explain the value of the μ parameter in the MSSM?
- What about the "total" particle content?
- Is there a "natural" way to implement SUSY-breaking?
- What is \mathcal{G}_{MSSM} ?
- and (many) more ...

To conclude our talk we want to have a look at some ideas concerning the first mentioned problem, the value of the μ parameter.

- **General Problem:** μ is a SUSY-preserving parameter, but from phenomenology we know that it must be of the order of the SUSY-breaking scale.
- "Natural" solution: Symmetry enforcing $\mu=0$, and a small SUSY-breaking parameter that generates a value of μ which is not parametrically larger than the SUSY-breaking scale.

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In proposed extensions of the MSSM, some other approaches have been presented, for example:

1 Replace μ by the VEV of a new $SU(3) \times SU(2) \times U(1)$ scalar singlet \implies NMSSM

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- 4 Possible connection to the strong CP problem? ⇒ PQ symmetry ⇒ Axion Physics?
- 6 Higher-dimensional Higgs multiplets?

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What have we learned today?

- The SM can be promoted to the MSSM using the concepts and methods introduced in the scope of this seminar.
- In addition to the 19 parameters of the SM we get $\mathcal{O}(100)$ new ones, which complicates the experimental access to the MSSM a lot!
- Phenomenological models of the MSSM allow for a drastic reduction of the number of independent parameters that have to be measured experimentally.
- SUSY may lead to a better understanding of the connection between Gravity and the SM.
 Additionally SUGRA helps us to further reduce the number of dof's in the MSSM.
- In the MSSM the unification of the SM gauge couplings at some high-energy scale M_X can be realized due to the effect of loop-corrections arising from the additional superpartners.
- There are still plenty of problems where the MSSM fails to explain the experimental results.
 - → The MSSM is not the "ultimate" model to describe our Universe.

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[2]

[3]

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