# THE MINIMAL SUPERSYMMETRIC STANDARD MODEL Part I: Theory

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Supersymmetry Seminar supervised by Prof. Jörg Jäckel

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## Outline

- 1. The Standard Model
- 2. The Minimal Supersymmetric Standard Model

## Outline

1 The Standard Model

Basics
The Lagrangian

Parameter Count

The Minimal Supersymmetric Standard Model

Basics

The Lagrangian — SUSY conserving

The Lagrangian — SUSY breaking

(Effective) Higgs potentia

Particle spectrum

Parameter Count

The gauge group of the Standard Model (SM) is

$$\mathcal{G}_{\mathrm{SM}} = \mathrm{SU}(3)_C \times \mathrm{SU}(2)_T \times \mathrm{U}(1)_Y.$$

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The SM fields transform in representations of this group:

$$s = 0: \quad (\mathbf{1}, \mathbf{2})_{\frac{1}{2}} \\ \ni \phi \\ s = \frac{1}{2}: \quad (\mathbf{3}, \mathbf{2})_{\frac{1}{6}} \oplus (\overline{\mathbf{3}}, \mathbf{1})_{\frac{1}{3}} \oplus (\overline{\mathbf{3}}, \mathbf{1})_{-\frac{2}{3}} \oplus (\mathbf{1}, \mathbf{2})_{-\frac{1}{2}} \oplus (\mathbf{1}, \mathbf{1})_{1} \\ \ni q_{L} \quad \ni (d_{R})^{c} \quad \ni (u_{R})^{c} \quad \ni \ell_{L} \quad \ni (e_{R})^{c} \\ s = 1: \quad (\mathbf{8}, \mathbf{1})_{0} \oplus (\mathbf{1}, \mathbf{3})_{0} \oplus (\mathbf{1}, \mathbf{1})_{0}. \\ \ni A_{\mu}^{a} \quad \ni W_{\mu}^{k} \quad \ni B_{\mu}$$

Beware! We only use lefthanded fields 
$$\psi_L = \begin{pmatrix} \psi_\alpha \\ 0 \end{pmatrix}$$
, righthanded fields are included via charge conjugation  $(\psi_R)^c = \begin{pmatrix} 0 \\ \bar{\psi}^{\dot{\alpha}} \end{pmatrix}^c = \begin{pmatrix} \psi_\alpha \\ 0 \end{pmatrix}$ .

The SU(2)-doublets are written as:

$$\phi = \begin{pmatrix} \phi_+ \\ \phi_0 \end{pmatrix} \qquad q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix} \qquad \ell_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}.$$

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# Standard Model — The Basics (Well, more or less...)

GEORGI-GLASHOW model: Using the breaking pattern  $SU(5) \to \mathcal{G}_{SM}$  the previous fields fit nicely into representations of SU(5):

$$\begin{split} &\bar{\mathbf{5}} = (\bar{\mathbf{3}},\mathbf{1})_{\frac{1}{3}} \oplus (\mathbf{1},\mathbf{2})_{-\frac{1}{2}} \\ &\mathbf{10} = (\mathbf{3},\mathbf{2})_{\frac{1}{6}} \oplus (\bar{\mathbf{3}},\mathbf{1})_{-\frac{2}{3}} \oplus (\mathbf{1},\mathbf{1})_{1} \end{split}$$

$$\mathbf{24} = (\mathbf{8}, \mathbf{1})_0 \oplus (\mathbf{1}, \mathbf{3})_0 \oplus (\mathbf{1}, \mathbf{1})_0 \oplus (\mathbf{3}, \mathbf{2})_{-\frac{5}{3}} \oplus (\bar{\mathbf{3}}, \mathbf{2})_{\frac{5}{3}} \,.$$

# Standard Model — The Lagrangian

The SM Lagrangian contains a variety of terms which roughly fall into three categories:

gauge terms

kinetic terms

Higgs sector

The gauge part is straightforward, albeit there being additional gauge configurations:

$$egin{aligned} \mathcal{L}_{\mathsf{gauge}} &\supset rac{1}{2g_i^2} \operatorname{tr}\left[F_{\mu
u}^{(i)}F^{(i)\mu
u}
ight] \ &\supset rac{ heta_{\mathrm{QCD}}}{16\pi^2g_{\mathrm{s}}^2} \epsilon^{\mu
u
ho\sigma} \operatorname{tr}\left[F_{\mu
u}^{(3)}F_{
ho\sigma}^{(3)}
ight]. \end{aligned}$$

Kinetic terms for the fermions are constructed with the covariant derivative

$$\mathcal{L}_{kin} \supset \bar{\psi}_i i \not \!\! D \psi_i$$
$$D_{\mu} = \partial_{\mu} - i q A_{\mu}^k \mathcal{R}(T_k).$$

The Higgs part is made of a scalar kinetic term, the quartic potential and the Yukawa couplings:

$$\mathcal{L}_{\text{Higgs}} \supset -\left(D^{\mu}\phi\right)^{\dagger} \left(D_{\mu}\phi\right) + \mu\phi^{\dagger}\phi - \lambda \left(\phi^{\dagger}\phi\right)^{2} - \left(\lambda^{\psi} \left[\bar{\psi}\phi\psi\right]_{1} + \text{h.c.}\right).$$

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The fermions gain masses  $m_{\psi}=v\lambda^{\psi}$  when the Higgs field acquires its vacuum expectation value (VEV):

$$\langle \phi \rangle = \left( \begin{array}{c} 0 \\ v \end{array} \right)$$
 (shorthand:  $\langle \phi_0 \rangle = v$ ),

while the Higgs mass becomes  $m_h = 2\sqrt{\lambda}v$ .

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For our three types of massive fermions (electron, up-quark, down-quark) the corresponding singlets look like:<sup>1</sup>

$$\lambda^u \left[ \bar{q}_L \tilde{\phi} u_R \right]_1, \qquad \lambda^d \left[ \bar{q}_L \phi d_R \right]_1, \qquad \lambda^e \left[ \bar{\ell}_L \phi e_R \right]_1.$$

<sup>&</sup>lt;sup>1</sup>Careful, since  $\tilde{\phi} = \epsilon \phi^*$  to account for the u-type quarks.

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Furthermore, the SM fermion fields consists of three generations, thus promoting the  $\lambda^{\psi}$  to complex 3x3 matrices  $\lambda^{e}_{mn}$ ,  $\lambda^{d}_{mn}$  and  $\lambda^{u}_{mn}$ . These  $\lambda^{f}_{mn}$  can be diagonalised via bi-unitary transformations:

$$V_f^{\dagger} \lambda^f U_f \propto \operatorname{diag}\left(m_f^{(1)}, m_f^{(2)}, m_f^{(3)}\right) / v.$$

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#### Standard Model — Parameter count

Count parameters and gauge redundancies:

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- ullet 3 couplings g, g' and  $g_{
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- Higgs parameters v,  $\lambda$  (2 parameters)
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- Quark flavour symmetry  $\mathrm{U}(3)_{q_L} \times \mathrm{U}(3)_{u_R} \times \mathrm{U}(3)_{d_R}/\mathrm{U}(1)_B$  (3x9-1 parameters)
- Lepton flavour symmetry  $U(3)_{\ell_L} \times U(3)_{e_R}/U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau}$  (2x9-3 parameters)

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The Standard Model of Particle Physics has 19 free parameters with v being the only one carrying a physical dimension.<sup>2</sup>

<sup>&</sup>lt;sup>2</sup>14 real parameters, 3 mixing angles, 2 CP-violating phase.

## Outline

 The Standard Model Basics
 The Lagrangian Parameter Count

2 The Minimal Supersymmetric Standard Model Basics The Lagrangian — SUSY conserving The Lagrangian — SUSY breaking (Effective) Higgs potential Particle spectrum Parameter Count

## MSSM — The fields

First of all we promote all our previous fields to real (chiral) superfields resulting in our renewed table:

super field	bosonic field	fermionic field	representation
$\hat{V}_8$	g	$ ilde{g}$	$({\bf 8},{\bf 1})_0$
$\hat{V}$	$W^0$ , $W^\pm$	$ ilde{W}^0$ , $ ilde{W}^\pm$	$\left(1,3 ight)_{0}$
$\hat{V}'$	B	$ ilde{B}$	$\left(1,1 ight)_{0}$
$\hat{L}$	$( ilde{ u}_L, ilde{e}_L)$	$(\nu_L,e_L)$	$({f 1},{f 2})_{-rac{1}{2}}$
$\hat{E}^c$	$ ilde{e}_R^c$	$e_R^c$	$(1,1)_1$
$\hat{Q}$	$( ilde{u}_L, ilde{d}_L)$	$(u_L,d_L)$	$(3,1)_{\frac{1}{6}}$
$\hat{U}^c$	$ ilde{u}_R^c$	$u_R^c$	$({f 3},{f 1})_{-rac{2}{3}}$
$\hat{D}^c$	$ ilde{d}_R^c$	$d_R^c$	$(3,1)_{\frac{1}{3}}$
$\hat{H}_u$	$\left(H_u^+,H_u^0\right)$	$\left( ilde{H}_{u}^{+}, ilde{H}_{u}^{0} ight)$	$({f 1},{f 2})_{rac{1}{2}}$
$\hat{H}_d$	$(H_d^0,H_d^-)$	$(\tilde{H}_d^0, \tilde{H}_d^-)$	$({f 1},{f 2})_{-{1\over 2}}$

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$\hat{H}_d$	$(H_d^0,H_d^-)$	$(\tilde{H}_d^0, \tilde{H}_d^-)$	$({f 1},{f 2})_{-rac{1}{2}}$

Beware! We need a second Higgs doublet to cancel the gauge anomaly introduced by the Higgsinos!

#### MSSM — SUSY terms

For the gauge part the ususal field strength super fields

$$\mathcal{W}_{i,\alpha} = -\frac{1}{4}\bar{D}^2 e^{-\hat{V}} D_{\alpha} e^{\hat{V}},$$

are constructed and included in the Lagrangian:

$$\mathcal{L}_{\mathrm{gauge}}^{\mathrm{MSSM}} \supset \frac{1}{2g_i^2} \operatorname{tr} \left[ \int \mathrm{d}^2 \theta \left( \mathcal{W}_i \right)^{lpha} \left( \mathcal{W}_i \right)_{lpha} + \mathrm{h.c.} \right].$$

The kinetic terms for the fields read:

$$\mathcal{L}_K^{\text{MSSM}} \supset \int d^2\theta d^2\bar{\theta} \left[ \hat{\Phi}_i^{\dagger} e^{2V_i} \hat{\Phi}_i \right]_1$$
$$V_i = \hat{V}_8^a \mathcal{R}_i(T_a) + \hat{V}^k \mathcal{R}_i(T_k) + Y_i \hat{V}'.$$

The superpotential term is simply:

$$\mathcal{L}_W^{ ext{MSSM}} = \int d^2 \theta W + \text{h.c.}$$

What terms are contained in W?

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In general, the superpotential contains a great variety of different terms, under them the Yukawa couplings:

$$\begin{split} W = & \lambda_d \left[ \hat{H}_d \hat{Q} \hat{D} \right]_1 + \lambda_e \left[ \hat{H}_d \hat{L} \hat{E} \right]_1 - \lambda_u \left[ \hat{H}_u \hat{Q} \hat{U} \right]_1 + \mu \left[ \hat{H}_u \hat{H}_d \right]_1 \\ & + a \left[ \hat{L} \hat{H}_u \right]_1 + b \left[ \hat{Q} \hat{L} \hat{D} \right]_1 + c \left[ \hat{U} \hat{U} \hat{D} \right]_1 + d \left[ \hat{L} \hat{L} \hat{E} \right]_1. \end{split}$$

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$$+ a \left[ \hat{L} \hat{H}_u \right]_1 + b \left[ \hat{Q} \hat{L} \hat{D} \right]_1 + c \left[ \hat{U} \hat{U} \hat{D} \right]_1 + d \left[ \hat{L} \hat{L} \hat{E} \right]_1.$$

The terms in the last line introduce B-number violation via proton decay as well as lepton number violation, but by imposing R-parity

$$R = (-1)^{3(B-L)+2s}.$$

we can get rid of them. Beware! This is not obligatory!

R-conservation implies the existance of a lightest supersymmetric particle (LSP) thus providing us with a dark matter candidate.

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We could use matter parity

$$P_{\rm m} = (-1)^{3(B-L)},$$

instead and see directly how the lower line gets thrown out.

## MSSM — Soft SUSY breaking terms

Introduce explicitly SUSY breaking terms to generate masses and additional interactions

$$-\mathcal{L}_{\text{soft}}^{\text{MSSM}} \supset \frac{1}{2} M_i \tilde{\lambda}_i \tilde{\lambda}_i + M_{\tilde{F}}^2 \tilde{f}^{\dagger} \tilde{f}$$
$$+ m_1^2 H_d^{\dagger} H_d + m_2^2 H_u^{\dagger} H_u + m_{12}^2 \left( H_u \cdot H_d + \text{h.c.} \right)$$
$$+ T_U H_u \tilde{Q} \tilde{U} + T_D H_d \tilde{Q} \tilde{D} + T_E H_d \tilde{L} \tilde{E} + \text{h.c.}$$

Often, a parametrisation  $m_{12}^2 = \mu B$  (and  $T_F = \lambda_f A_F$ ) is chosen. Therefore, the corresponding terms are called A and B-terms.

#### Repeat the SM steps:

In the MSSM the quartic coupling is generated by the D-terms of the Kähler potential, and the SUSY breaking terms, leading to an effective Higgs potential.

$$\begin{split} V_{\rm Higgs} &= \left(m_1^2 + |\mu|^2\right) H_d^{\dagger} H_d + \left(m_2^2 + |\mu|^2\right) H_u^{\dagger} H_u + m_{12}^2 \left(H_u \cdot H_d + \text{h.c.}\right) \\ &+ \frac{g^2 + {g'}^2}{8} \left(H_d^{\dagger} H_d - H_u^{\dagger} H_u\right) + \frac{1}{2} g^2 \left|H_d^{\dagger} H_u\right|^2, \end{split}$$

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The two doublets acquire separate VEVs

$$\left\langle H_f^0 \right\rangle = v_f,$$

related to the previous v via

$$\sqrt{v_u^2 + v_d^2} = v,$$

by convention, the angle  $\beta$  is defined as

$$\tan \beta = \frac{v_u}{v_d}.$$

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$$+ \frac{g^2 + g'^2}{8} (H_d^{\dagger} H_d - H_u^{\dagger} H_u) + \frac{1}{2} g^2 |H_d^{\dagger} H_u|^2,$$

At tree level this implies an upper bound on the mass of the lightest Higgs:

$$m_h^2 \le m_Z^2 \cos^2 2\beta.$$

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The SM particle spectrum looks like:

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The MSSM particle spectrum<sup>3</sup> looks like:

<sup>&</sup>lt;sup>3</sup>Worst case scenario.

#### Summary of mixed states:

- The Higgs bosons  $(H_d^-, H_d^0, H_u^0, H_u^+)$  form: a charged scalar pair  $H^\pm$ , two neutral scalars  $h^0$ ,  $H^0$ , and a neutral pseudoscalar  $A^0$ .
- The charged bosinos  $(\tilde{W}^{\pm},\,\tilde{H}_u^+,\,\tilde{H}_d^-)$  form the charginos  $\tilde{\chi}_i^{\pm}.$
- The neutral bosinos  $(\tilde{B},\,\tilde{W}^0,\,\tilde{H}_u^0,\,\tilde{H}_d^0)$  form the neutralinos  $\tilde{\chi}_i^0.$
- The squarks  $(\tilde{q}_{i,L}, \, \tilde{q}_{i,R})$  form mass eigenstates labeled  $\tilde{q}_i$ .
- The charged sleptons  $(\tilde{e}_{i,L}, \tilde{e}_{i,R})$  form eigenstates  $\tilde{\ell}_i$ .
- The sneutrinos  $\tilde{\nu}_i$  form eigenstates  $\tilde{\nu}_i$ .

Only for certain ranges of the parameters the particle spectrum will resemble a 'double-SM'.

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- 3 couplings  $g_i$ , one vacuum angle  $\theta_{QCD}$  (4 parameters)
- 3 (complex) gaugino masses  $M_i$  (6 parameters)
- 2 Higgs mass parameters v,  $\beta$  (2 parameters)
- 2 (complex) Higgs/ino mass parameters  $\mu$ , B (4 parameters)
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- 3 mass matrices  $\lambda^f$  (3x18 parameters)
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The full Minimal Supersymmetric Standard Model has 124 free parameters<sup>3</sup> (MSSM-124).

<sup>&</sup>lt;sup>3</sup>Consisting of 3 couplings, 37 real masses, 39 mixing angles and 45 CP-violating phases.