

THE MINIMALLY SUPERSYMMETRIC STANDARD MODEL

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2. The Standard Model
3. The MSSM

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Standard Model — The Basics

The gauge group of the Standard Model (SM) is

$$\mathcal{G}_{\text{SM}} = \text{SU}(3)_C \times \text{SU}(2)_T \times \text{U}(1)_Y. \quad (1)$$

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The SM fields transform in representations of this group:

$$s = 0 : \quad (\mathbf{1}, \mathbf{2})_{\frac{1}{2}} \quad (2)$$

$\ni \phi$

$$s = \frac{1}{2} : \quad (\mathbf{3}, \mathbf{2})_{\frac{1}{6}} \oplus (\bar{\mathbf{3}}, \mathbf{1})_{\frac{1}{3}} \oplus (\bar{\mathbf{3}}, \mathbf{1})_{-\frac{2}{3}} \oplus (\mathbf{1}, \mathbf{2})_{-\frac{1}{2}} \oplus (\mathbf{1}, \mathbf{1})_1 \quad (3)$$

$\ni q_L \qquad \ni (d_R)^c \qquad \ni (u_R)^c \qquad \ni \ell_L \qquad \ni (e_R)^c$

$$s = 1 : \quad (\mathbf{8}, \mathbf{1})_0 \oplus (\mathbf{1}, \mathbf{3})_0 \oplus (\mathbf{1}, \mathbf{1})_0. \quad (4)$$

$\ni A_\mu^a \qquad \ni W_\mu^k \qquad \ni B_\mu$

Standard Model — The Basics

Beware! We only use lefthanded fields $\psi_L = \begin{pmatrix} \psi_\alpha \\ 0 \end{pmatrix}$, righthanded fields are included via charge conjugation $(\psi_R)^c = \begin{pmatrix} 0 \\ \bar{\psi}^{\dot{\alpha}} \end{pmatrix}^c = \begin{pmatrix} \psi_\alpha \\ 0 \end{pmatrix}$.

The $SU(2)$ -doublets are written as:

$$\phi = \begin{pmatrix} \phi_+ \\ \phi_0 \end{pmatrix} \quad q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix} \quad \ell_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}.$$

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Standard Model — The Lagrangian

The SM Lagrangian contains a variety of terms which roughly fall into three categories:

gauge terms kinetic terms Higgs sector

The gauge part is straightforward albeit there being additional gauge configurations:

$$\mathcal{L}_{\text{gauge}} \supset \frac{1}{2g_i^2} \text{tr} \left[F_{\mu\nu}^{(i)} F^{(i)\mu\nu} \right] \quad (5)$$

$$\supset \frac{\theta_{\text{QCD}}}{16\pi^2 g_s^2} \epsilon^{\mu\nu\rho\sigma} \text{tr} \left[F_{\mu\nu}^{(3)} F_{\rho\sigma}^{(3)} \right]. \quad (6)$$

Kinetic terms for the fermions are constructed with the covariant derivative

$$\mathcal{L}_{\text{kin}} \supset \bar{\psi}_i i \not{D} \psi_i \quad (7)$$

$$D_\mu = \partial_\mu - iq A_\mu^k \mathcal{R}(T_k) \quad (8)$$

Standard Model — Higgs sector

The Higgs part is made of a scalar kinetic term, the quartic potential and the Yukawa couplings:

$$\mathcal{L}_{\text{Higgs}} \supset - (D^\mu \phi)^\dagger (D_\mu \phi) + \mu \phi^\dagger \phi - \lambda (\phi^\dagger \phi)^2 - \lambda^\psi [\overline{\psi} \phi \psi]_1. \quad (9)$$

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The fermions gain masses $m_\psi = v\lambda^\psi$ when the Higgs field acquires its vacuum expectation value (VEV):

$$\langle \phi \rangle = \begin{pmatrix} 0 \\ v \end{pmatrix} \quad (\text{shorthand: } \langle \phi_0 \rangle = v).$$

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For our three types of massive fermions (electron, up-quark, down-quark) the corresponding singlets look like:¹

$$\lambda^u [\bar{q}_L \tilde{\phi} u_R]_1 \quad \lambda^d [\bar{q}_L \phi d_R]_1 \quad \lambda^e [\bar{\ell}_L \phi e_R]_1. \quad (10)$$

¹Careful, since $\tilde{\phi} = \epsilon \phi^*$ to account for the u-type quarks.

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Furthermore, the SM consists of three generations of fermions thus promoting the λ^ψ to complex 3x3 matrices λ_{mn}^e , λ_{mn}^d and λ_{mn}^u . The λ_{mn}^f can be diagonalised via bi-unitary transformations:

$$V_f^\dagger \lambda^f U_f \propto \text{diag} \left(m_f^{(1)}, m_f^{(2)}, m_f^{(3)} \right). \quad (11)$$

¹Careful, since $\tilde{\phi} = \epsilon \phi^*$ to account for the u-type quarks.

Standard Model — Parameter count

Count parameters and gauge redundancies:

+

- 3 couplings g , g' and g_s , one vacuum angle θ_{QCD} (4 parameters)
- Higgs parameters v , λ (2 parameters)
- 3 (complex) mass matrices λ^f (3x18 parameters)

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- Quark flavour symmetry $\text{U}(3)_{q_L} \times \text{U}(3)_{u_R} \times \text{U}(3)_{d_R}/\text{U}(1)_B$ (3x9-1 parameters)
- Lepton flavour symmetry $\text{U}(3)_{\ell_L} \times \text{U}(3)_{e_R}/\text{U}(1)_{L_e} \times \text{U}(1)_{L_\mu} \times \text{U}(1)_{L_\tau}$ (2x9-3 parameters)

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The Standard Model of Particle Physics has 19 free parameters with v being the only one carrying a physical dimension.²

²15 real parameters, 3 mixing angles, 1 CP-violating phase.

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③ The MSSM

- The Lagrangian — SUSY conserving

- The Lagrangian — SUSY breaking

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MSSM — The fields

First of all we promote all our previous fields to real (chiral) superfields resulting in our renewed table:

super field	bosonic field	fermionic field	representation
\hat{V}_8	g	\tilde{g}	$(\mathbf{8}, \mathbf{1})_0$
\hat{V}	W^0, W^\pm	$\tilde{W}^0, \tilde{W}^\pm$	$(\mathbf{1}, \mathbf{3})_0$
\hat{V}'	B	\tilde{B}	$(\mathbf{1}, \mathbf{1})_0$
\hat{L}	$(\tilde{\nu}_e, \tilde{e})$	(ν_L, e_L)	$(\mathbf{1}, \mathbf{2})_{-\frac{1}{2}}$
\hat{E}^c	\tilde{e}_R^c	e_R^c	$(\mathbf{1}, \mathbf{1})_1$
\hat{Q}	$(\tilde{u}_L, \tilde{d}_L)$	(u_L, d_L)	$(\mathbf{3}, \mathbf{1})_{\frac{1}{6}}$
\hat{U}^c	\tilde{u}_R^c	u_R^c	$(\mathbf{3}, \mathbf{1})_{-\frac{2}{3}}$
\hat{D}^c	\tilde{d}_R^c	d_R^c	$(\mathbf{3}, \mathbf{1})_{\frac{1}{3}}$
\hat{H}_u	(H_u^+, H_u^0)	$(\tilde{H}_u^+, \tilde{H}_u^0)$	$(\mathbf{1}, \mathbf{2})_{\frac{1}{2}}$
\hat{H}_d	(H_d^0, H_d^-)	$(\tilde{H}_d^0, \tilde{H}_d^-)$	$(\mathbf{1}, \mathbf{2})_{-\frac{1}{2}}$

MSSM — SUSY terms

For the gauge part the usual field strength super fields $\mathcal{W}_{i,\alpha}$ are constructed and included in the Lagrangian:

$$\mathcal{L}_{\text{gauge}}^{\text{MSSM}} \supset \frac{1}{2g_i^2} \text{tr} \left[\int d^2\theta (\mathcal{W}_i)^\alpha (\mathcal{W}_i)_\alpha + \text{h.c.} \right]. \quad (12)$$

The kinetic terms for the fields read:

$$\mathcal{L}_K^{\text{MSSM}} \supset \int d^2\theta d^2\bar{\theta} \left[\hat{\Phi}_i^\dagger e^{2V_i} \hat{\Phi}_i \right]_1 \quad (13)$$

$$V_i = \hat{V}_8^a \mathcal{R}_i(T_a) + \hat{V}^k \mathcal{R}_i(T_k) + Y_i \hat{V}'. \quad (14)$$

MSSM — Superpotential

The superpotential term is simply:

$$\mathcal{L}_W^{\text{MSSM}} = \int d^2\theta W + \text{h.c.} \quad (15)$$

What terms are contained in W ?

MSSM — Superpotential

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In general, the superpotential contains a great variety of different terms, under them the Yukawa couplings:

$$\begin{aligned} W = & \lambda_d [H_d Q U]_1 + \lambda_d [H_d L E]_1 - \lambda_u [H_u Q U]_1 + \mu [H_u H_d]_1 \\ & + a [\hat{L} \hat{H}_u]_1 + b [\hat{Q} \hat{L} \hat{D}]_1 + c [\hat{U} \hat{U} \hat{D}]_1 + d [\hat{L} \hat{L} \hat{E}]_1. \end{aligned} \quad (16)$$

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The terms in the last line introduce B -number violation via proton decay as well as lepton number violation, but by imposing R -parity

$$R = (-1)^{3(B-L)+2s}, \quad (17)$$

we can get rid of them. Beware! This is not obligatory!

R -conservation implies the existence of a lightest supersymmetric particle (LSP) thus providing us with a dark matter candidate.

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We could use **matter parity**

$$P_m = (-1)^{3(B-L)}, \quad (17)$$

instead and see directly how the lower line gets thrown out.

MSSM — Soft SUSY breaking terms

Introduce explicitly SUSY breaking terms to generate masses and additional interactions

$$\begin{aligned} -\mathcal{L}_{\text{soft}}^{\text{MSSM}} \supset & \frac{1}{2} M_i \tilde{\lambda}_i \tilde{\lambda}_i + M_{\tilde{F}}^2 \tilde{f}^\dagger \tilde{f} \\ & + m_1^2 H_d^\dagger H_d + m_2^2 H_u^\dagger H_u + m_{12}^2 (H_u H_d + \text{h.c.}) \\ & + T_U H_u Q U + T_D H_d Q D + T_E H_d L E + \text{h.c.} \end{aligned} \quad (18)$$

Often, a parametrisation $m_{12}^2 = \mu B$ (and $T_F = \lambda_f A_F$) is chosen. Therefore, the corresponding terms are called A and B-terms.

MSSM — Note on the Higgs sector

Repeat the SM steps: In the MSSM the quartic coupling is generated by the kinetic and soft SUSY breaking terms leading to an effective Higgs potential.

$$\begin{aligned} V_{\text{Higgs}} = & (m_1^2 + |\mu|^2) H_d^\dagger H_d + (m_2^2 + |\mu|^2) H_u^\dagger H_u + m_{12}^2 (H_u \cdot H_d + \text{h.c.}) \\ & + \frac{g^2 + g'^2}{8} (H_d^\dagger H_d - H_u^\dagger H_u)^2 + \frac{1}{2} g^2 |H_d^\dagger H_u|^2, \end{aligned} \quad (19)$$

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The two doublets acquire separate VEVs:

$$\langle H_f^0 \rangle = v_f, \quad (20)$$

related to the previous v via:

$$\sqrt{v_u^2 + v_d^2} = v, \quad (21)$$

by convention the angle β is defined as

$$\tan \beta = \frac{v_u}{v_d}. \quad (22)$$

MSSM — Mixing in the particle spectrum

The SM particle spectrum looks like:

$$\begin{array}{ccccc} u & c & t & B & W^0 \\ d & s & b & g & W^\pm \\ & & & & \\ e & \mu & \tau & h^0 & \\ \nu_e & \nu_\mu & \nu_\tau & & \end{array}$$

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The SM particle spectrum looks like:

u	c	t	B	W^0
d	s	b	g	W^\pm
e	μ	τ	H_d^-	H_d^0
ν_e	ν_μ	ν_τ	H_u^0	H_u^+

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u	c	t	γ	Z^0
d	s	b	g	W^\pm
e	μ	τ	h^0	H^0
ν_e	ν_μ	ν_τ	A^0	H^\pm

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 \end{array}$$

The MSSM particle spectrum looks like:

$$\begin{array}{ccccccccc}
 \tilde{u}_L & \tilde{u}_R & \tilde{c}_L & \tilde{c}_R & \tilde{t}_L & \tilde{t}_R & \tilde{B} & \tilde{W}^0 \\
 \tilde{d}_L & \tilde{d}_R & \tilde{s}_L & \tilde{s}_R & \tilde{b}_L & \tilde{b}_R & \tilde{g} & \tilde{W}^\pm \\
 \\
 \tilde{e}_L & \tilde{e}_R & \tilde{\mu}_L & \tilde{\mu}_R & \tilde{\tau}_L & \tilde{\tau}_R & \tilde{H}_d^- & \tilde{H}_d^0 \\
 \tilde{\nu}_e & & \tilde{\nu}_\mu & & \tilde{\nu}_\tau & & \tilde{H}_u^0 & \tilde{H}_u^+
 \end{array}$$

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e	μ	τ	h^0	H^0
ν_e	ν_μ	ν_τ	A^0	H^\pm

The MSSM particle spectrum³ looks like:

\tilde{q}_1	\tilde{q}_2	\tilde{q}_3	\tilde{q}_4	\tilde{q}_5	\tilde{q}_6	$\tilde{\chi}_1^\pm$	$\tilde{\chi}_2^\pm$
\tilde{q}'_1	\tilde{q}'_2	\tilde{q}'_3	\tilde{q}'_4	\tilde{q}'_5	\tilde{q}'_6	\tilde{g}	
$\tilde{\ell}_1$	$\tilde{\ell}_2$	$\tilde{\ell}_3$	$\tilde{\ell}_4$	$\tilde{\ell}_5$	$\tilde{\ell}_6$	$\tilde{\chi}_1^0$	$\tilde{\chi}_2^0$
$\tilde{\nu}_1$		$\tilde{\nu}_2$		$\tilde{\nu}_3$		$\tilde{\chi}_3^0$	$\tilde{\chi}_4^0$

³Worst case scenario.

MSSM — Mixing in the particle spectrum

Summary of mixed states:

- The charged gauginos (\tilde{W}^{\pm} , \tilde{H}_u^{+} , \tilde{H}_d^{-}) form the charginos $\tilde{\chi}_i^{\pm}$.
- The neutral gauginos (\tilde{B} , \tilde{W}^0 , \tilde{H}_u^0 , \tilde{H}_d^0) form the neutralinos $\tilde{\chi}_i^0$.
- The squarks ($\tilde{q}_{i,L}$, $\tilde{q}_{i,R}$) form mass eigenstates labeled \tilde{q}_i .
- The sleptons ($\tilde{e}_{i,L}$, $\tilde{e}_{i,R}$) form eigenstates $\tilde{\ell}_i$.
- The Higgs bosons (H_d^{-} , H_d^0 , H_u^0 , H_u^{+}) form: a charged pair H^{\pm} , two CP-even neutral scalars h^0 , H^0 and a CP-odd A^0 .

Only for certain ranges of the parameters the particle spectrum will resemble a 'double-SM'.

MSSM — Parameter count

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- 3 couplings g_i , one vacuum angle θ_{QCD} (4 parameters)
- 3 (complex) gaugino masses M_i (6 parameters)
- 2 Higgs mass parameters v, β (2 parameters)
- 2 (complex) Higgs/ino mass parameters μ, B (4 parameters)
- 5 hermitian scalar mass matrices $M_{\tilde{F}}^2$ (5x9 parameters)
- 3 mass matrices λ^f (3x18 parameters)
- 3 trilinear couplings T_F (3x18 parameters)

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- Flavour symmetry $U(3)^5/U(1)^2$ (5x9-2 parameters)

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The full Minimal Supersymmetric Standard Model has 124 free parameters³ (MSSM-124).

³Consisting of 3 couplings, 37 real masses, 39 mixing angles and 45 CP-violating phases.

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