

# Barotropic vorticity balance of the North Atlantic subpolar gyre in an eddy-resolving model

Mathieu Le Corre<sup>1</sup>, Jonathan Gula<sup>1</sup>, and Anne-Marie Tréguier<sup>1</sup>

<sup>1</sup>Univ. Brest, CNRS, IRD, Ifremer, Laboratoire d'Océanographie Physique et Spatiale (LOPS), IUEM, Brest, France

**Correspondence:** Mathieu Le Corre (mathieu.lecorre@univ-brest.fr)

**Abstract.** The circulation in the North Atlantic Subpolar gyre is complex and strongly influenced by the topography. The gyre dynamics is traditionally understood as the result of a topographic Sverdrup balance, which corresponds to a first order balance between the planetary vorticity advection, the bottom pressure torque and the wind stress curl. However, these dynamics have been studied mostly with non-eddy-resolving models and a crude representation of the bottom topography. Here we revisit the barotropic vorticity balance of the North Atlantic Subpolar gyre using a [high resolution simulation \(new eddy-resolving simulation \(with a grid space of  \$\approx 2\text{-km}\$ \)](#) with topography-following vertical coordinates to better represent the mesoscale turbulence and flow-topography interactions. Our findings highlight that, locally, there is a first order balance between the bottom pressure torque and the nonlinear terms, albeit with a high degree of cancellation between each other. However, balances integrated over different regions of the gyre – shelf, slope and interior – still highlight the important role played by nonlinearities and the bottom drag curls. In particular the [topographic](#)–Sverdrup balance cannot describe the dynamics in the interior of the gyre. The main sources of cyclonic vorticity are the non linear terms due to eddies generated along eastern boundary currents and the time-mean nonlinear terms [from in](#) the Northwest Corner. Our results suggest that a good representation of the mesoscale activity along with a good positioning of [the Northwest corner mean currents](#) are two important conditions for a better representation of the circulation in the North Atlantic Subpolar Gyre.

## 15 1 Introduction

The North Atlantic Subpolar Gyre (SPG) is a key region for the meridional overturning circulation (MOC). There, the North Atlantic surface waters coming from the subtropical gyre are transformed into denser waters that flow southward and form the lower limb of the MOC. The dynamics of the currents in the SPG is a result of strong buoyancy gradients, intense surface buoyancy and wind forcings, and exchanges of waters with the Nordic Seas through overflows. Understanding these complex dynamics is essential to better understand the mechanisms that drive the variability of the MOC.

The dynamics of wind-driven oceanic gyres is traditionally understood as the result of two distinct balances for the interior of the gyre and the boundary of the gyre, where currents flow along topography. In the interior, the flow follows a Sverdrup balance, which corresponds to a first order balance between the wind stress curl and a meridional transport in the barotropic (depth-integrated) vorticity balance. This balance has been shown to hold in the interior of subtropical gyres (Hughes and De Cuevas, 2001; Thomas et al., 2014; Yeager, 2015; Schoonover et al., 2016; Sonnewald et al., 2019; Le Bras

et al., 2019). Where the currents interact with the topography, another term becomes first order in the barotropic vorticity balance: the Bottom Pressure Torque (BPT). The BPT includes the impacts of the bottom topography on the barotropic currents, and derives from the interaction of the abyssal geostrophic flow with the sloping bottom bathymetry. Works by Hughes (2000); Hughes and De Cuevas (2001); Jackson et al. (2006); Schoonover et al. (2016) have demonstrated the prevalence of the BPT in the global barotropic vorticity balance. They have shown in particular that the BPT is the dominant term in western boundary currents, thus demonstrating that [bottom friction and](#) viscous effects were not required to close the vorticity budget of the gyres as hypothesized in the classical works of [Stommel \(1948\)](#) and [Munk \(1950\)](#). The SPG circulation is strongly shaped by the bottom topography. Due to the weak stratification, the currents have a strong barotropic component (Van Aken, 1995; Daniault et al., 2016; Fischer et al., 2004). They are thus strongly impacted by the steep topography around the gyre. The importance of the bottom topography in driving the SPG dynamics emerged quite early in the works of Luyten et al. (1985) and Wunsch (1985). The prevalence of the BPT in the SPG has also been demonstrated by [Hughes and De Cuevas \(2001\)](#); [Spence et al. \(2012\)](#); [Yeager \(2015\)](#)[Greatbatch et al. \(1991\)](#); [Hughes and De Cuevas \(2001\)](#); [Spence et al. Yeager \(2015\)](#). All studies also pointed out a failure of the flat [bottom bottomed](#) Sverdrup balance in this area.

The studies putting forward the importance of the BPT in the SPG have been using coarse resolution models. But currents in the SPG are also strongly influenced by eddies, which can modify the mean flow structure (McWilliams, 2008). Models then require resolutions able to resolve these effects. Eddy-permitting resolutions have been shown to improve the characteristics of the boundary currents of the SPG, including a better position of the currents, narrower lateral extensions and velocity amplitudes closer to observations (Treguier et al., 2005; Danek, 2019). The vertical structure of the currents is also improved with a more barotropic structure for the boundary currents around the SPG (Marzocchi, 2015). These changes, compared to coarser resolution models, allow the inertial effects to become more important and modify the interactions with the topography. Also, at higher resolution, the viscosity is reduced and the bottom topography and inertial effects become prevalent, allowing the flow to better match the observations (Spence et al., 2012; Schoonover et al., 2016).

Recently, Sonnewald et al. (2019) clustered regions dominated by different barotropic vorticity balances using a global  $1^\circ \times 1^\circ$  model. They retrieved the results of a SPG dominated by BPT effects, but also a part of the gyre dominated by Non-Linear (NL) effects, despite the relatively coarse resolution of the model. Yeager (2015) compared results from a  $1^\circ$  resolution model with an eddy-permitting  $1/10^\circ$  resolution model, and noticed an increase of the amplitude of the NL term by a factor 3 in some locations. However, it did not modify significantly the first order equilibrium between the wind, planetary vorticity and BPT. The impact of the NL term becomes clearer at higher resolution. With a  $1/20^\circ$  resolution simulation Wang et al. (2017) showed the importance of this term in the dynamics of recirculation gyres such as the Gulf Stream recirculation gyres [or the North-Western Corner, the Northwestern Corner or the recirculation in the Labrador Sea \(Lavender et al., 2000\)](#).

In addition to the horizontal resolution, the representation of the bottom topography has an impact on the structure of the flow. z-level coordinates have the tendency to create too shallow flows compared to partial step coordinates (Pacanowski and Gnanadesikan, 1998). Terrain following coordinates ( $\sigma$ -level) have proven effective in representing boundary currents (Schoonover et al., 2016; Ezer, 2016). The z-level types coordinates tend to have too much viscosity and/or diffusivity close to

60 the topography due to the presence of vertical walls. This effect is corrected when increasing the vertical resolution or using partial steps to converge to results obtained with  $\sigma$ -coordinates (Ezer and Mellor, 2004).

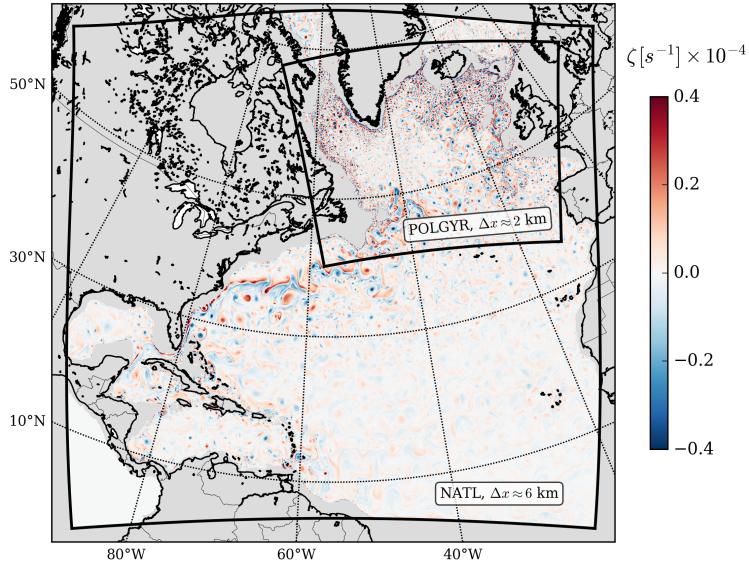
The aim of this paper is to investigate the dynamics of the SPG by analysing the barotropic vorticity balance in a truly eddy-resolving  $\sigma$ -level coordinate model. To our knowledge no study of the SPG dynamics has ever been conducted at this resolution with this kind of vertical coordinate. The switch in vertical coordinate combined with eddy-resolving resolution ~~might help to resolve smaller scale processes and allow a better representation of~~ will allow the model to resolve more non-linear processes and to better represent the flow-topography interactions overall, which are believed to be two essential ingredients for the circulation of the SPG. The paper is organised as follows: The simulation setup is presented in section 2. The mean currents characteristics and variability in the simulation are compared to observations in section 3. The barotropic vorticity balance is analyzed for the full SPG in section 4. The balances corresponding to the different parts of the gyre are further described in 70 section 5. To better understand what is hidden inside the non linear term we analyze it more in detail in section 6. Conclusions are presented and discussed in section 7.

## 2 Model and set-up

To investigate the impact of the topography on the circulation, it is essential to have a good representation of the flow-topography interactions. To do so, we use a terrain-following coordinate model: the Regional Oceanic Modelling System 75 (ROMS, ~~Shehepetkin and McWilliams (2009)~~ Shchepetkin and McWilliams (2005)) in its CROCO (Coastal and Regional Ocean Community) version (Debreu et al., 2012). It solves the hydrostatic primitive equations for velocity, temperature and salinity, using a full equation of state for seawater (Shchepetkin and McWilliams, 2009, 2011).

To achieve a kilometric resolution at a reasonable cost, we use a one way nesting approach by defining two successive horizontal grids with resolutions  $\Delta x \approx 6$  km for the parent grid covering the North Atlantic ocean (NATL) and  $\Delta x \approx 2$  km for 80 the child grid covering the SPG (POLGYR). The parent North Atlantic domain is identical to the one in Renault et al. (2016). It has  $1152 \times 1059$  points with a horizontal resolution of 6–7 km. The child grid has  $2000 \times 1600$  points and a horizontal resolution of 2 km. It allows the simulation to be truly eddy resolving in most of the area, as the first Rossby deformation radius ~~varies between 10 and 20 km over~~ remains below 10-km over most of the region (Chelton et al., 1998). The domains are shown in figure 1.

85 The bathymetry for both domains is constructed from the SRTM30 PLUS dataset (available online at [http://topex.ucsd.edu/WWW\\_html/srtm30\\_plus.html](http://topex.ucsd.edu/WWW_html/srtm30_plus.html)) based on the 1 min Sandwell and Smith (1997) global dataset and higher resolution data where available. A Gaussian smoothing kernel with a width 4 times the topographic grid spacing is used to avoid aliasing whenever the topographic data are available at higher resolution than the computational grid and to ensure the smoothness of the topography at the grid scale. Also, to avoid pressure gradient errors induced by terrain-following coordinates in shallow 90 regions with steep bathymetric slopes (Beckmann and Haidvogel, 1993), we locally smooth the bottom topography  $h$  to ensure that the steepness of the topography does not exceed a factor  $r = 0.2$ , where the local  $r$ -factor is defined in the  $x$  and  $y$  directions by  $r_x = \frac{h(i,j) - h(i-1,j)}{h(i,j) + h(i-1,j)}$  and  $r_y = \frac{h(i,j) - h(i,j-1)}{h(i,j) + h(i,j-1)}$ ,  $(i,j)$  representing the grid index.

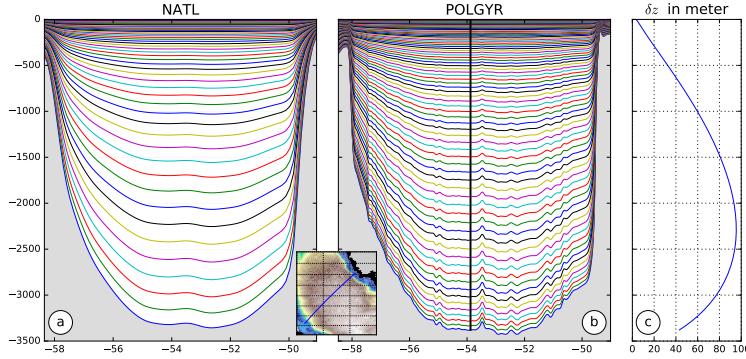


**Figure 1.** Snapshot of the relative vorticity at 500 m depth in the North Atlantic in the NATL simulation. The NATL grid ( $\Delta x \approx 6$  km) covers most the North Atlantic, and the POLGYR grid (smaller rectangle,  $\Delta x \approx 2$  km) covers the subpolar gyre.

Initial and lateral boundary data for the largest domain are taken from the Simple Ocean Data Assimilation (SODA, Carton and Giese (2008)). The NATL simulation is run from January 1st, 1999 to December 31st, 2009–2008. It is spun up for 2 years, 95 and the following 8 years are used to generate boundary conditions for the child grid. Our focus is the barotropic vorticity dynamics, characterized by time scales on the order of months, such that a year of spin up is sufficient for the kinetic energy (both for barotropic and baroclinic modes) to reach a state of quasi-equilibrium in POLGYR (not shown). The study is carried on the 7 remaining years between 2002 and 2009–2008. The surface forcings are daily ERA-INTERIM data for the parent grid and 12-hourly ERA-INTERIM data for the child grid.

100 The North Atlantic and subpolar gyre simulations have 50 and 80 vertical levels, respectively. Vertical levels are stretched at the surface and bottom (Lemarié et al., 2012) to have a better representation of the surface layer dynamics at the top and flow-topography interactions at the bottom. The depth of the transition between flat  $z$  levels and terrain-following  $\sigma$  levels is  $h_{cline} = 300$  m. The two parameters controlling the bottom and surface refinement of the grid are  $\sigma_b = 2$ ,  $\sigma_s = 7$  for the parent grid and  $\sigma_b = 3$ ,  $\sigma_s = 6$  for the child grid, corresponding to strongly stretched levels at the surface and bottom (Figure Fig. 2).

105 The vertical mixing of tracers and momentum is done by a  $k-\epsilon$  model (GLS, Umlauf and Burchard (2003)). The effect of bottom friction is parameterized through a logarithmic law of the wall with a roughness length  $Z_0 = 0.01$  m. We use no explicit horizontal viscosity or diffusivity and rely on third-order upwind-biased advection schemes, which include an implicit hyperdiffusivity at the grid scale.



**Figure 2.** Depths of the model vertical  $\sigma$ -levels along a section in the [Irminger Basin](#)-[Labrador Sea](#) for (a) the 6-km simulation (NATL), and (b) the 2-km simulation (POLGYR) [and \(c\) the vertical grid spacing with depth along the black line shown in \(b\)](#).

### 3 Mean Currents and variability

#### 110 3.0.1 Mean circulation

Before investigating what is driving the SPG dynamics, we first need to validate the mean circulation in our simulations. Mean velocities from the two simulations (NATL and POLGYR) at the surface and 1000-m depth are shown in figure 3. We present at the bottom of figure 3 (e,f) the amplitudes of the currents from the NOAA drifter climatology (Laurindo et al., 2017) at the surface and from the ARGO-based ANDRO dataset at 1000-m depth (Ollitrault and Rannou, 2013; Lebedev et al., 2007). The  
115 ANDRO data have been binned on a  $0.25^\circ \times 0.25^\circ$  grid and cells with less than 10 data points have been removed.

The North Atlantic Current (NAC) represents a boundary between the subtropical and the subpolar gyres. Oceanic models have difficulties in reproducing its dynamics and particularly its Northern extension known as the [NorthWest](#)[Northwest](#) Corner (Bryan et al., 2007; Hecht and Smith, 2008; Drews et al., 2015), which is centered at  $50^\circ$  N,  $48^\circ$  W (Lazier, 1994). These difficulties lead to the apparition of the so called "cold-bias", which can reach up to  $10^\circ$  C (Griffies et al., 2009; Drews  
120 et al., 2015), and which plays a role in the Atlantic low frequency variability (Drews and Greatbatch, 2017). The [NorthWest](#)[Northwest](#) Corner is well reproduced in our simulations, and the temperature bias at this location is less than a degree.

After turning eastward, the NAC splits into three branches, which are strongly constrained by topography (Bower, 2008). They cross the Mid Atlantic Ridge (MAR) through three deep fracture zones: the Charlie-Gibbs Fracture Zone (CGFZ,  $52.5^\circ$  N), the Faraday fracture zone ( $50^\circ$  N) and the Maxwell fracture zone ( $48^\circ$  N) (Bower et al., 2002). In both surface and [1000 m](#)[1000-m](#) observations (Fig. 3(e),(f)), the Northern branch of the NAC is more intense and corresponds to the main pathway across the MAR. The three branches are well represented in the simulations with, at the surface, an overestimation of the southern branch and an underestimation of the northern branch. At depth, ANDRO data depict an intense branch crossing the MAR at the CGFZ while the amplitude of the two Southern branches is smaller. This feature might be related to the Labrador Sea Water passing into the Eastern Basin through the CGFZ in this depth range, while in the Faraday and Maxwell Fracture

130 zones the flow is more surface intensified. The circulation in POLGYR is closer to the observations with a better representation of the flow in the CGFZ at ~~1000-m~~1000-m.

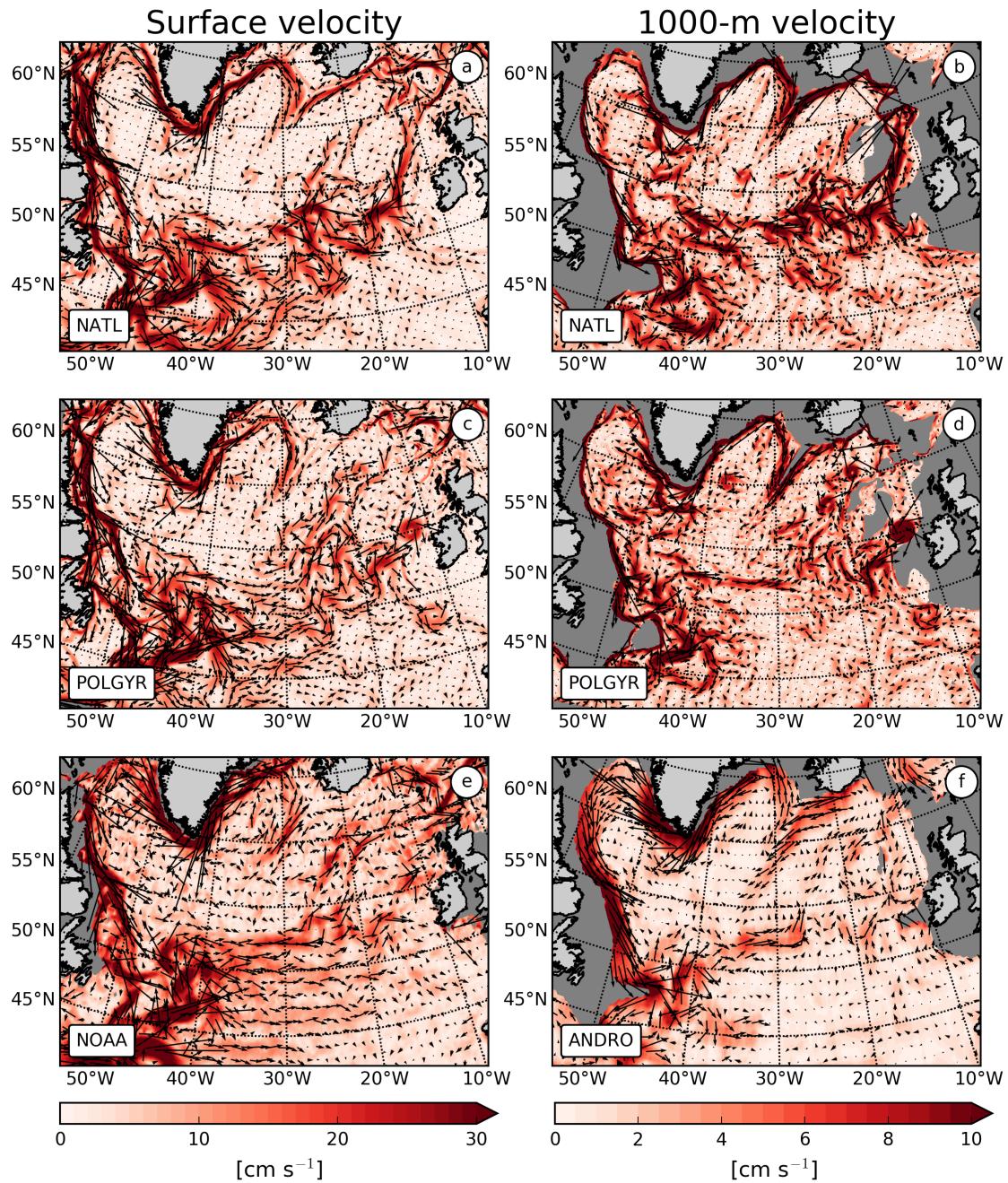
After crossing the MAR, the three branches head North with the two Northern ones feeding the interior of the Iceland basin and the Rockall Trough (RT) (Daniault et al., 2016). The water coming from the Maxwell fracture zone recirculates southward in the West European Basin (Paillet and Mercier, 1997). As most of the models (Treguier et al., 2005; Deshayes et al., 2007),  
135 NATL and POLGYR are consistent with observations for the circulation in the Eastern Basin with a good positioning of the two main branches passing respectively in the Maury channel (deepest part of the Iceland Basin west of Hatton Bank) and the RT.

A deep permanent anticyclonic eddy is found in Rockall Trough (Fischer et al., 2018; Smilanova et al., to be submitted; Le Corre et al., 2019). This structure is detectable in the ANDRO dataset around  $55^{\circ}$  N,  $12^{\circ}$  W (Fig. 3(f)). It is not present in  
140 NATL while it appears in POLGYR, albeit with too intense velocities. In NATL at depth, there is a strong southward flow in the western part of the RT due to the wrong representation of the Faroe Bank channel. As the topography is strongly smoothed, the channel is not properly represented and does not allow the dense water coming from the Nordic Seas to pass through it and feed the Iceland Scotland Overflow Water properly (Hansen et al., 2016; Kanzow and Zenk, 2014). Thus, the water is recirculating in the western part of the RT, creating a spurious pattern (Fig. 3(b)). The problem is solved by increasing the  
145 horizontal resolution and improving the representation of the topography, which corresponds to a wider opening of the channel and allows a more realistic circulation in the RT.

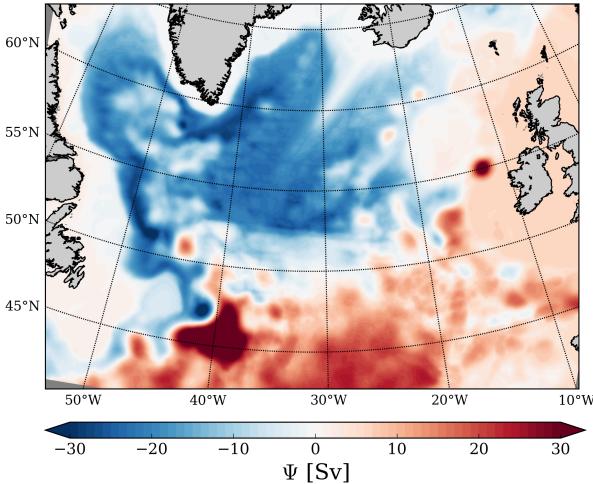
Further north, part of the flow continues to the Nordic Seas (Rossby and Flagg, 2012), while the other part follows the Reykjanes Ridge (RR). A common bias in models east of RR is a too intense southward flow at the surface (Treguier et al., 2005). This bias is present in NATL but disappears at higher resolution in POLGYR, which is closer to the circulation observed  
150 by the drifters. On the western side of the RR the signal of the strong northward Irminger current visible in observations is well resolved by the simulations (Fig. 3).

At 1000-m depth, Argo floats reveal a continuous current following the Eastern RR flank until reaching the CGFZ, with some of the flow crossing the ridge North of  $57.3^{\circ}$  N and some crossing at the Bright Fracture Zone ( $56\text{--}57^{\circ}$  N). This is consistent with the results from Petit et al. (2018), who observed that water at this depth (their layer 3) was more likely to cross the  
155 ridge North of  $56^{\circ}$  N. This southwestward flow is present in our simulations, with too intense velocity amplitudes in NATL, but realistic amplitudes at higher resolution in POLGYR. In both cases, we clearly see the flow crossing the ridge north of  $56^{\circ}$  N. On the western side of RR, the velocity in the simulations is too strong compared to observations. The mean subpolar gyre intensity in the model (Fig. 4), computed as the cumulative transport from Iceland to  $53.15^{\circ}$  N along the crest of the RR, is equal to -25 Sv and compares well with the  $-21.9 \pm 2.5$  Sv monthly average in Petit et al. (2018).

160 Numerous recirculations are present in the SPG, many of them occurring near the intense boundary currents along Greenland and around the Labrador sea (Reverdin, 2003; Flatau et al., 2003; Cuny et al., 2002). The recirculation cells are present in the Labrador sea (Lavender et al., 2000; Cuny et al., 2002) and extend to the Irminger basin (Holliday et al., 2009). ~~These features are mainly driven by Käse et al. (2001) and Spall and Pickart (2003) suggested that both the topography and the wind as described in Käse et al. (2001); Spall and Pickart (2003), and are driving these features, which~~ are stable in time (Palter



**Figure 3.** Mean velocity averaged over 2002-2008 at the surface (left) and 1000-m (right) in NATL (a,b), POLGYR (c,d) and observations, NOAA drifters and ANDRO (e,f).



**Figure 4.** Time mean barotropic stream function over 2002-2008

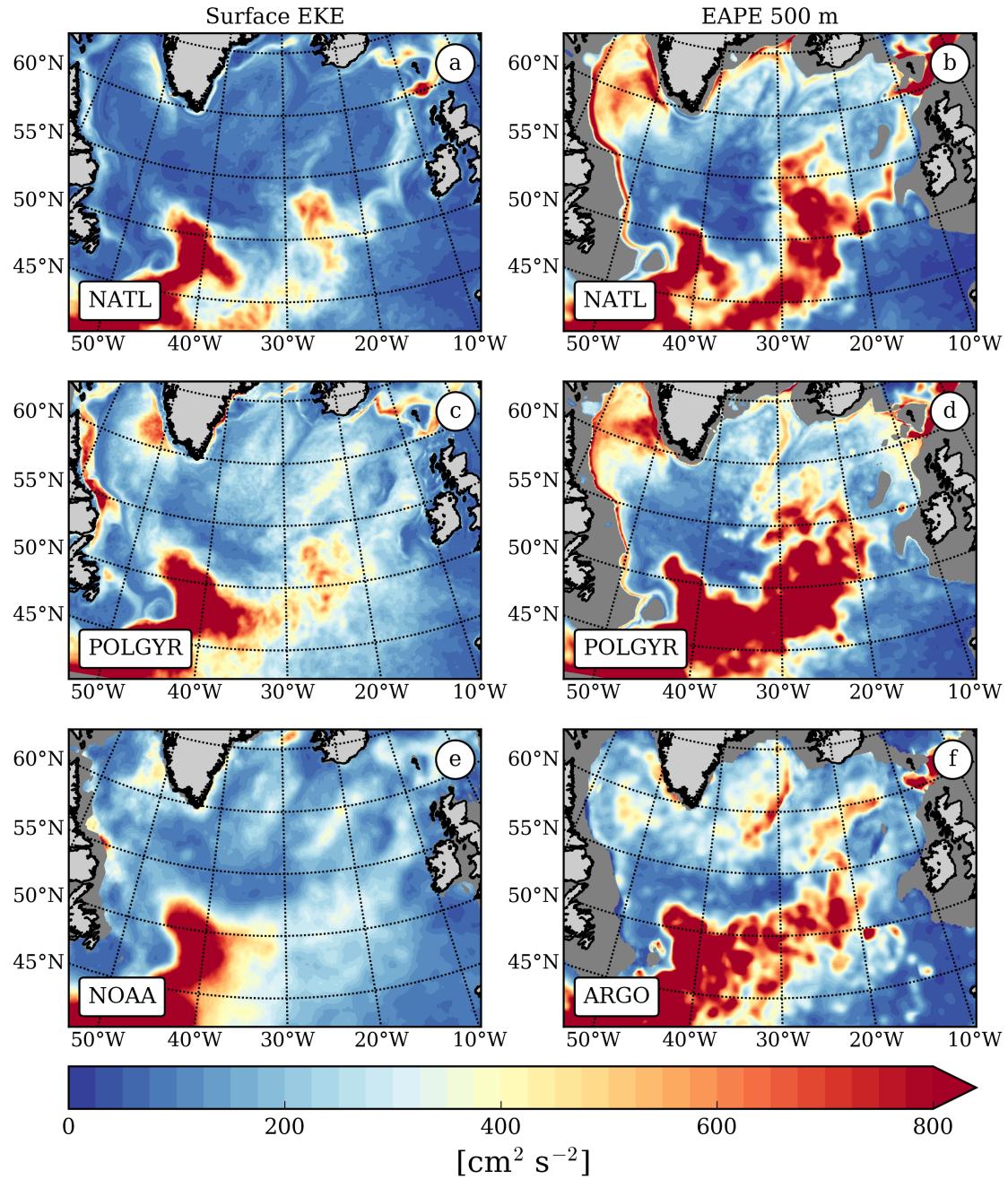
et al., 2016). [More recently Wang et al. \(2017\) showed the importance of the mean flow advection in these circulations.](#) Some models are unable to reproduce correctly the recirculation cells, especially the one in the centre of the Labrador Sea (Treguier et al., 2005). In our case, this recirculation is well represented (Figure 3(a),(b),(c),(d)). The counter current flows offshore the Labrador continental slope, with a northward extension at 60° N, which matches observations from Lavender et al. (2005). At the tip of Greenland, this counter current separates in two to form a branch flowing inside the Irminger Basin while the other branch is redirected southward. This second branch is relatively intense in our simulation but is also present in ANDRO data (Fischer et al. (2018), their Figures 3 and 5a).

### 3.1 The mesoscale activity

The mesoscale activity plays a big role in redistributing water masses properties in the SPG ([de Jong et al., 2016; Zhao et al., 2018](#))[\(Brandt, 2018\)](#). The presence of mesoscale eddies can be inferred by their signatures on the Eddy Kinetic Energy (EKE). From the surface EKE signal extracted from NOAA drifters on a  $0.25^\circ \times 0.25^\circ$  grid (Fig. 5(e)), we retrieve the main hot spots described by Flatau et al. (2003) in the SPG: the Labrador Sea, the Irminger and Iceland basins. Those signals are mainly due to generation of mesoscale eddies through baroclinic and barotropic instabilities of the boundary currents.

EKE amplitudes in the NATL simulation are weaker than in observations, but the eddy activity is enhanced when the resolution is increased. The POLGYR simulation displays similar EKE patterns than observational data in every basins (Labrador, Irminger and Iceland) with close amplitudes over most of the SPG. The EKE patterns corresponding to the generation of Irminger Rings have higher magnitudes in POLGYR than in the NOAA drifters data.

A way to quantify the mesoscale activity at depth is to look at the vertical isopycnal displacements. When referenced to a mean, it represents the Eddy Available Potential Energy (EAPE) or the amount of energy stored in the potential energy reservoir



**Figure 5.** Mean Surface Eddy Kinetic Energy (left) and Mean Eddy Available Potential Energy between 2002 and 2008 (right) in NATL (a,b), POLGYR (c,d). There are compared with result from the NOAA database (e) and the EAPE Atlas from Roullet&al (f)

due to mesoscale activity (Lorenz, 1955). This quantity is a proxy of the baroclinic activity in the interior of the ocean and is

185 computed following Roullet et al. (2014) formulation:

$$\text{EAPE} = -\frac{g}{2\rho_0} \langle z' \rho' \rangle \quad (1)$$

where  $z'$  is the vertical isopycnal displacement,  $\rho'$  the density anomaly associated with this displacement and  $\langle \cdot \rangle$  is the time average.

We compare EAPE from the simulations with the atlas of Roullet et al. (2014) constructed from Argo data (Fig. 5(f)).

The atlas presented here is an update of the original product, which uses virtual density instead of potential density

190 and includes more recent data up to July 2015. In NATL (at 6 km resolution) most of the baroclinic activity already seems

well resolved. However, observations highlight an EAPE maximum on the western flank of the RR that is missing in NATL,

but appears only in POLGYR (at 2 km resolution). On the contrary, strong patches of EAPE are visible along the boundary

currents of the western half of the SPG in NATL, but are not visible in observations. Interestingly these patterns weaken in

POLGYR, potentially pointing to a change in the vertical structure of the currents at higher resolution. Another factor to take

195 into consideration is the lack of Argo measurements close to the boundaries, which might cause an underestimation of EAPE

at these locations.

## 4 Vorticity balance of the subpolar gyre at high resolution

### 4.1 An overall view of the subpolar gyre vorticity balance

The barotropic vorticity equation is obtained by Two barotropic vorticity equations can be obtained depending on the choice of

200 vertically averaging or integrating the momentum equations in the vertical and before cross-differentiating them. While

the former helps to quantify the barotropic flow across f/h contour, the latter defines the main barotropic forcing on the flow.

Our main focus being to defines the main forcing of the SPG, the last definition will be used in the following and can be written

as (Gula et al., 2015):

$$\underbrace{\frac{\partial \Omega}{\partial t}}_{\text{rate}} = - \underbrace{\nabla \cdot (f \bar{\mathbf{u}})}_{\text{planet. vort. adv}} + \underbrace{\frac{J(P_b, h)}{\rho_0}}_{\text{BPT}} + \underbrace{\mathbf{k} \cdot \nabla \times \frac{\tau_{wind}}{\rho_0}}_{\text{wind curl}} - \underbrace{\mathbf{k} \cdot \nabla \times \frac{\tau_{bot}}{\rho_0}}_{\text{BDC}} + \underbrace{D_\Sigma}_{\text{horiz. diffusion}} + \underbrace{A_\Sigma}_{\text{NLA}} \quad (2)$$

205 where the vorticity  $\Omega$  is the curl of the vertically integrated components of the velocity between the bottom and the surface:

$\Omega = \mathbf{k} \cdot \nabla \times \bar{\mathbf{u}}$ , with  $\mathbf{u} = (u, v)$  the velocities in the  $(x, y)$  direction. The overbar defines a vertically integrated quantity:

$$\bar{u} = \int_{-h}^{\eta} u \, dz \quad (3)$$

with  $\eta(x, y, t)$  the free surface height and  $h(x, y)$  the topography. It is possible to decompose the planetary vorticity advection  $-\nabla \cdot (f\bar{u}) = -\beta V - f \frac{\partial \eta}{\partial t} \approx -\beta V$ , with  $V$  the vertically integrated meridional component of velocity, if we consider a mean over a long enough time period such that  $\frac{\partial \eta}{\partial t} \approx 0$ .

The non linear term can be written as:

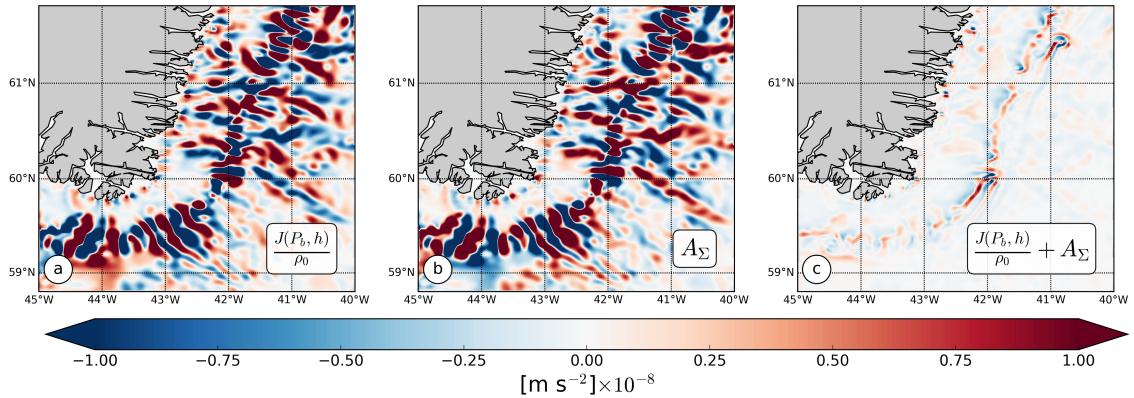
$$A_{\Sigma} = -\frac{\partial^2(\bar{v}\bar{v} - \bar{u}\bar{u})}{\partial x \partial y} - \frac{\partial^2 \bar{u}\bar{v}}{\partial x \partial x} + \frac{\partial^2 \bar{u}\bar{v}}{\partial y \partial y} \quad (4)$$

The expression for  $A_{\Sigma}$  is similar to the one shown in Schoonover et al. (2016) (their equation (2)) but in our case, the integration between  $-h$  and  $\eta$  allows their last term to cancel out with a residue from the inversion of the time derivative and the vertical integral in the rate term. The bottom pressure torque  $J(P_b, h)$  is the Jacobian of the bottom pressure and the depth of the topography. It encompasses the effects of the varying topography on the flow, and is known to play a key role in the barotropic vorticity balance of the SPG. In an idealized case of a geostrophic current flowing along a topography in free-slip condition, the BPT can be written  $\frac{J(P_b, h)}{\rho_0} = f u_b \cdot \nabla h$  where  $\rho_0$  is the mean reference density and the subscript  $b$  denotes a field at the bottom. Given the kinematic condition at the bottom:  $-u_b \cdot \nabla h = w_b$ , the BPT can be written  $\frac{J(P_b, h)}{\rho_0} = -f w_b$ , which highlights the relation between the BPT and vortex stretching when the flow crosses an isobath.

The barotropic vorticity terms have already been computed for the North Atlantic using different models ([OCCAM Ocean Circulation and Climate Advanced Modelling- OCCAM](#), [University of Victoria Earth System Climate Model- UVic](#), [ECCO](#), [UVicESCM](#), [Estimating the Circulation and Climate of the Ocean- ECCO](#), [Parallel Ocean Program- POP](#)) at different resolutions ( $1.8^\circ \times 3.6^\circ$ ,  $1^\circ$ ,  $0.25^\circ$ , [Hughes and De Cuevas, 2001](#);  $0.2^\circ \times 0.4^\circ$ , [Spence et al., 2012](#);  $1^\circ$  [Sonnewald et al., 2019](#);  $0.1^\circ$  [in Hughes and De Cuevas \(2001\), Spence et al. \(2012\), Sonnewald et al. \(2019\), and Yeager \(2015\)](#) [Yeager, 2015](#)). Their major result is that the barotropic vorticity balance in the subtropical and subpolar gyres is at first order a balance between  $\beta V$ ,  $\nabla \times \frac{\tau_{wind}}{\rho_0}$ , and  $\frac{J(P_b, h)}{\rho_0}$ .

In the subtropical gyre, the barotropic vorticity balance is close to a Sverdrup balance away from the boundaries ( $\beta V \approx \nabla \times \frac{\tau_{wind}}{\rho_0}$ ), while the closure of the northward branch of the gyre at the western boundary is done primarily through BPT ( $\beta V \approx \frac{J(P_b, h)}{\rho_0}$ ) (Schoonover et al., 2016).

The barotropic vorticity balance in the SPG is slightly more complex due to the strong impact of the topography. Along the northern and western boundaries of the SPG, the first order balance is between meridional advection and BPT ( $\beta V \approx \frac{J(P_b, h)}{\rho_0}$ ) (e.g. Hughes and De Cuevas (2001), their Figure 4; Yeager (2015), their Figure 1), with a significant impact of the wind only in the northern part of the gyre along the Greenland coast. When the resolution of the model is increased from  $1^\circ$  to  $0.1^\circ$  in Yeager (2015), the main balances stay qualitatively similar, showing a modest effect of the eddies. Using a shallow water model with higher resolution ( $1/20^\circ$ ), Wang et al. (2017) illustrates the importance of the NL term in the dynamics of specific regions such as the Gulf Stream and the [recirculation gyres](#) [Labrador recirculation in the SPG](#). The viscous torque decreases in the boundary currents due to the lower viscosity of their model.



**Figure 6.** Time mean (a) bottom pressure torque, (b) non-linear terms, and (c) sum of the two for Eastern Greenland in the 2-km North Atlantic subpolar gyre simulation.

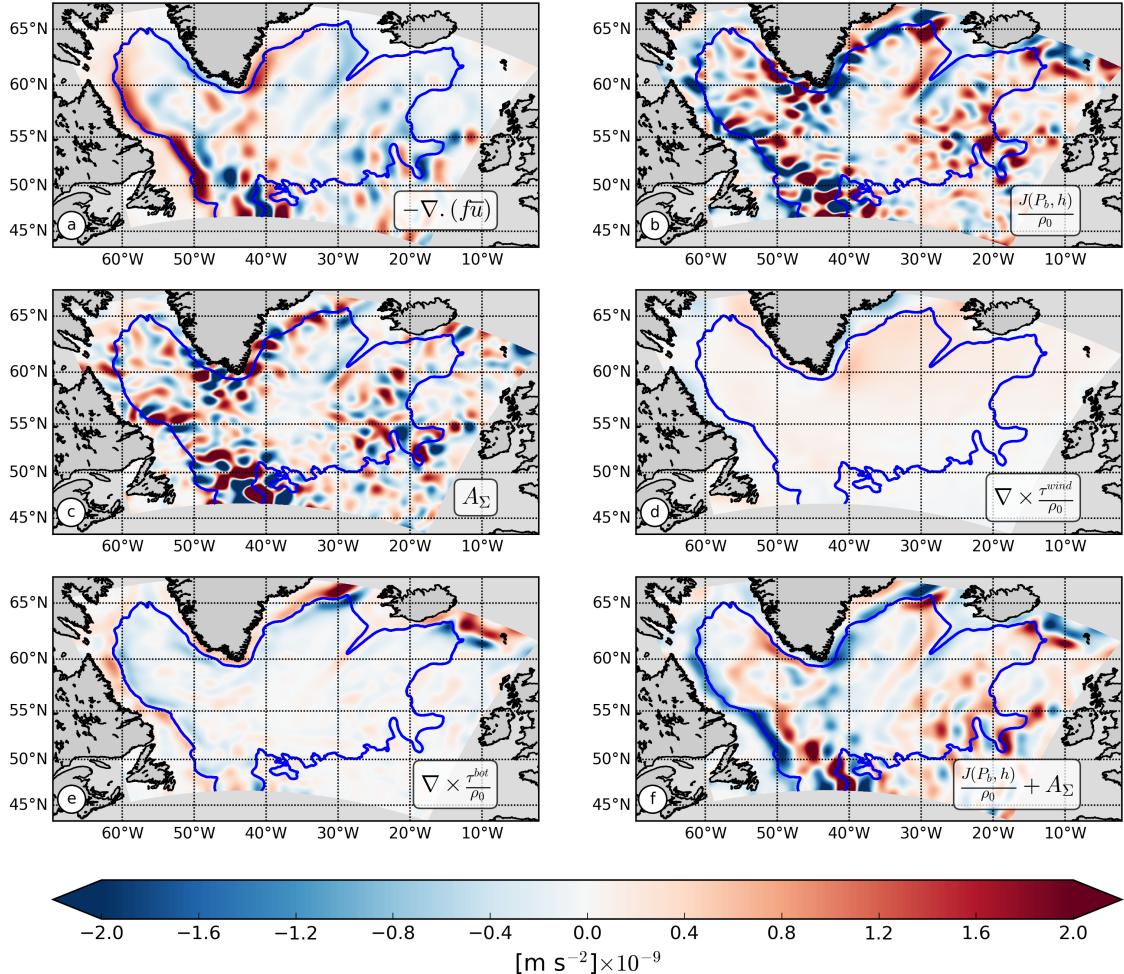
#### 4.2 Spatial scales of the vorticity balance

240 In our simulations, the BPT balances the [advection of vorticity nonlinear term](#) at leading order everywhere in the domain (Fig. 6). This is qualitatively different from the vorticity balances shown in Yeager (2015), but it is similar to the results of Gula et al. (2015) in the Gulf Stream region with the same ocean model and a similar horizontal resolution. This highlights the fact that locally the flow is able to follow isobaths due to an equilibrium between the NL term (making the flow cross isobaths) and the bottom pressure anomaly.

245 Both terms exhibit small scales related to topographic features, but with a high degree of cancellation between each other. The sum of the BPT and NL terms (Fig. 6 (c)) is often an order of magnitude smaller than the amplitude of the terms considered individually and exhibits patterns and amplitudes matching the advection of planetary vorticity. This cancellation is also clear in Wang et al. (2017), their Figure 3, where the transport driven by mean flow advection balances the one driven by the BPT, both having amplitudes larger than the wind stress curl-driven transport.

250 To facilitate the interpretation of maps of NL and BPT terms, the impact of small topographic scales has to be reduced by smoothing with a large enough length scale. NL terms in particular are expected to be smoothed out on scales larger than 1-2° (Hughes and De Cuevas, 2001). Figure 7 shows all terms smoothed with a Gaussian kernel of 1° radius. Even with such smoothing, the BPT and NL terms are still significantly larger than the corresponding results from the 0.1° simulation of Yeager (2015). However, their sum  $\frac{J(P_b, h)}{\rho_0} + A_\Sigma$  (Fig. 7 (f)) is of the same order of magnitude than the  $\beta V$  (Fig. 7 (a)) and the  
255 Bottom Drag Curl (BDC, Fig. 7 (e)). [More precisely, the  \$\beta V\$  term balances the sum  \$\frac{J\(P\_b, h\)}{\rho\_0} + A\_\Sigma\$  over most of the domain, while the BDC locally plays a role in the shallow areas.](#)

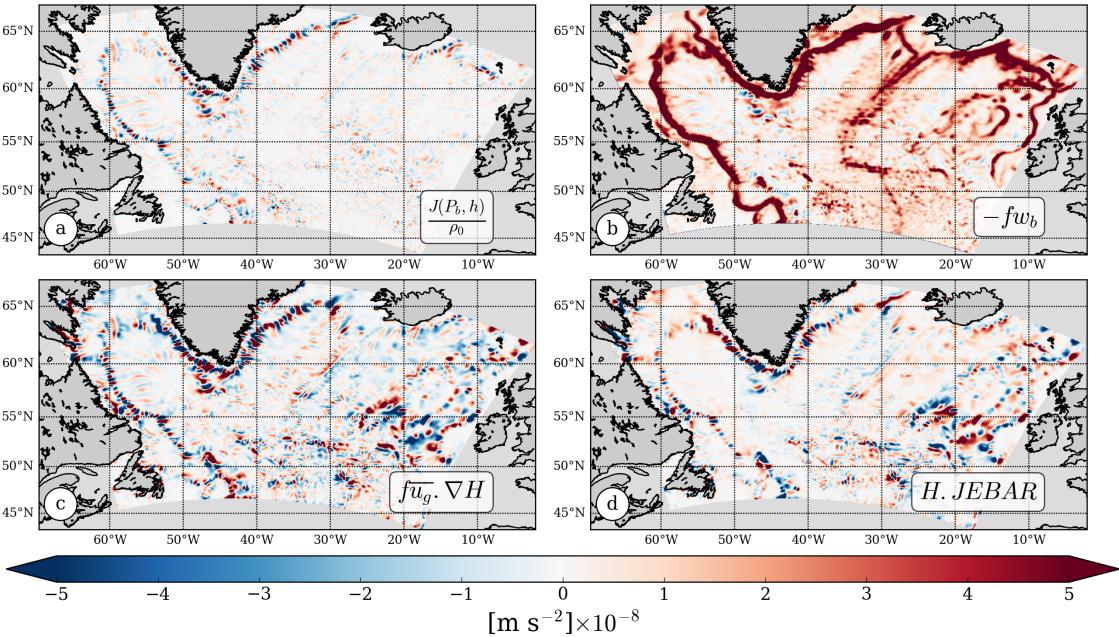
The curl of the wind stress in POLGYR has the same pattern and amplitude as in Yeager (2015). It is mostly positive with the strongest signal on the Eastern coast of Greenland. The amplitude of the  $\beta V$  term is slightly stronger in our model than in coarser resolution simulations. In the simulations of Hughes and De Cuevas (2001) and Yeager (2015), the patterns of the



**Figure 7.** Time mean of the planetary vorticity (a), bottom pressure torque (b), non linear terms (c), wind stress curl (d), and bottom drag curl (e). As bottom pressure torque and non-linear terms are canceling each other their sum is plotted in (f). The fields have been smoothed using a kernel of  $1^\circ$  radius. The blue contour represents the limit of our shelf area and is the  $-3$  Sv barotropic streamline

260  $\beta V$  term seems to indicate much wider currents. Here, the patterns correspond to thinner and more intense currents, closely following the continental slopes, in agreement with the observations.

In our simulations, the amplitude of the viscous torque, due to the implicit horizontal viscosity of the model ( $D_\Sigma$ ), is very small, while compared with the amplitude of the BDC is comparable to the  $\beta V$ . This is opposite to the results of the 0.1° POP simulation of Yeager (2015). In fact, their viscous term is qualitatively similar in pattern to the bottom drag curl 265 in our simulation. The boundary conditions near the topography are quite different in the two models due to the different vertical coordinates. The z-levels coordinates have vertical walls between each level, with parameterized lateral viscosity, which explains the pattern in Yeager (2015). The  $\sigma$ -levels coordinates have no lateral boundary conditions and friction on the



**Figure 8.** (a) Bottom Pressure Torque, (b)  $-f w_b$ , (c)  $\frac{f}{h} \bar{u}_g \cdot \nabla H$ , and (d)  $H \cdot \text{JEBAR}$  for the 2-km North Atlantic subpolar gyre simulation smoothed with a 25 km Gaussian Kernel .

topographic slopes is only parameterized as a bottom drag. The amplitude of the BDC is however stronger in our simulation than the viscous term in Yeager (2015) and seems to play ~~a-an~~ an important role in balancing the BPT and  $\beta V$  terms over the shelf and on the upper part of the continental slope along the northern and western boundaries of the gyre.

270

#### 4.3 Link between barotropic vorticity balance and bottom velocities

As explained previously, the bottom pressure torque  $J(P_b, h)$  can be identified with a bottom vortex stretching term:  $\frac{J(P_b, h)}{\rho_0} = f u_{gb} \cdot \nabla h = -f w_{gb}$ , where  $u_{gb}$  is the horizontal geostrophic bottom flow.

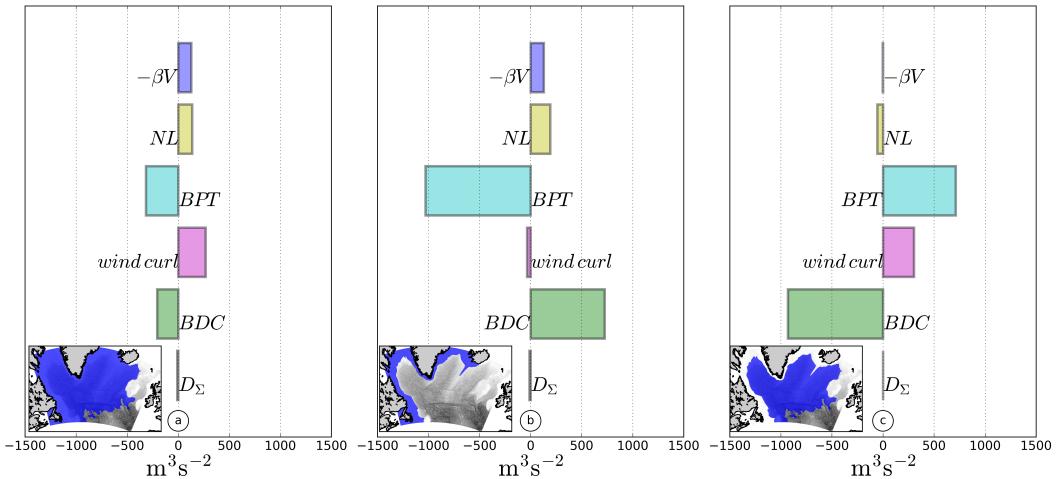
275

The computation of the BPT in Spence et al. (2012) is performed by directly estimating the term  $-f w_b$ , where  $w_b$  is the vertical velocity at the bottom. However this estimation does not take into account the presence of an ageostrophic component of the velocity at the bottom, in particular the Ekman component of the velocity due to the bottom drag. The same computation in our model leads to the results of Fig. 8(b), which are very different from the actual bottom pressure torque (Fig. 8 (a)). It gives results quite similar to Spence et al. (2012) with positive signals - implying downwelling of bottom currents - over most of the boundaries of the gyre. But this downwelling is a result of the Ekman currents oriented to the left of the main bottom geostrophic currents, which are flowing with the shallower topography on their right around the gyre.

280

Following Mertz and Wright (1992) and Yeager (2015), the BPT can be further decomposed into:

$$\frac{J(P_b, h)}{\rho_0} = f u_{gb} \cdot \nabla h = \frac{f}{h} \bar{u}_g \cdot \nabla h + h(JEBAR) \quad (5)$$



**Figure 9.** Integration of the barotropic vorticity terms over the SPG including or excluding the shelf area (respectively (a) and (c)). The Subpolar gyre area without the shelf corresponds to the -3 Sv contour. The shelf balance is plotted in (b).

which illustrates that the bottom geostrophic currents that appears in the expression of BPT are the sum of a vertically averaged part and a baroclinic part directly related to the JEBAR term. The term  $\frac{f}{h} \bar{u}_g \cdot \nabla h$  highlights regions where the depth-averaged flow is crossing isobaths, and the  $h(JEBAR)$  term where the baroclinic effects are playing a role to decouple the bottom flow from the barotropic flow through the geostrophic shear. In Fig. 8 (c) the geostrophic velocity has been computed from the thermal wind balance referenced at the surface.

Along the continental slopes, on the western and northern part of the gyre, the flow is close to barotropic and the  $\frac{f}{h} \bar{u}_g \cdot \nabla H$  term has similar patterns and amplitudes than the BPT. This contrasts with results from Yeager (2015), who found that the  $h(JEBAR)$  term was almost an order of magnitude larger than the BPT in these regions. However over the southern and eastern part of the gyre, it is clear that the structure of the flow is much more baroclinic and the  $\frac{f}{h} \bar{u} \cdot \nabla h$  and  $h(JEBAR)$  terms are both an order of magnitude larger than the BPT.

## 5 Integrated vorticity balance for the shelf, slope and interior of the gyre

### 5.1 Gyre integrated barotropic vorticity balances

The maps of the barotropic vorticity terms, with various degrees of smoothing, can help identify the locally dominant terms, but do not enable us to identify the important balances at the gyre scale. Spatial integrations are performed inside different gyre contours (Fig. 9) to better understand the main contributions to the circulation of the subpolar gyre.

We distinguish the shelf area from the gyre using a contour of barotropic streamfunction of -3 Sv. This contour is chosen because it corresponds to the largest possible closed contour of the barotropic streamfunction. We can check that the term

300  $-\nabla \cdot (f\bar{u}) \approx -\beta V$  integrates to zero over-within such a contour (Fig. 9 (c)). The shelf thus defined corresponds to an area with a mean depth of 290 meter and is extending from the South of Iceland to Flemish cap (blue area in Fig. 9 (b)).

When integrated inside the -3 Sv contour (which means excluding the shelf area, Fig. 9 (c)), the main sources for the cyclonic circulation of the gyre are the wind and the BPT. They are balanced by the BDC. The wind input does not contribute much locally (Fig. 7), but becomes significant when integrated spatially over the whole gyre. The BPT is the major source of positive vorticity and helps the flow move cyclonically around the gyre. The BDC and NL terms act as sinks of vorticity, but the NL term is much smaller than the BDC. The BDC is very intense where the current flows close to a steep topography, as in the case of the Labrador Current (LC) and the West Greenland Current.

When integrated over the whole gyre (Fig. 9 (a)), the balance is slightly different. The wind is still a major contributor for the cyclonic circulation and the BDC still represents the major sink of vorticity. However, the NL term replaces the BPT as a source of cyclonic vorticity for the gyre. In this interpretation, both the wind and the NL term forces the gyre cyclonically, while the BDC and BPT balance this input.

The difference between the two balances is highlighted by looking at the balance in the region in-between the two contours, which covers the upper slope and the shelf. It corresponds to a balance between BPT, NL and bottom drag. The NL term is only significant around the Greenland shelf and is related to eddy interactions between the shelf and the open ocean. Otherwise, the vorticity is negative on the shelf, thus explaining the positive sign of the bottom drag. The main source of anticyclonic vorticity is related to the BPT. This balance is close to the one described in Csanady (1978) and Csanady (1997) and evokes a buoyancy driven flow in this area (Chapman and Beardsley, 1989). Indeed, with a switch to  $(n,s)$  coordinates system with  $n$  the right handed coordinates (here oriented toward shallower water) and  $s$  the distance along flow, the BPT can be written  $\frac{J(P_b, h)}{\rho_0} = -\frac{\partial P_b}{\partial s} \frac{\partial h}{\partial n}$ . A negative value of BPT then means  $\frac{\partial P_b}{\partial s} < 0$  corresponding to a buoyancy driven current (Chapman et al., 1986; Chapman and Beardsley, 1989).

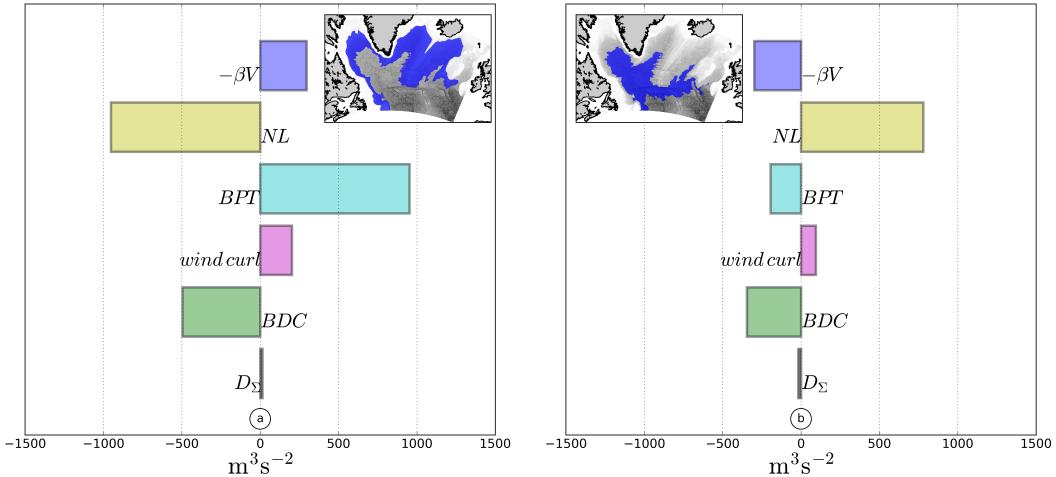
## 5.2 Barotropic vorticity balance in the interior of the gyre

It is clear from the patterns of the different terms of the barotropic vorticity balance that the local balances over the boundary currents are very different than what is happening in the interior of the gyre. The classical picture of a gyre interior (far from the boundaries) in a quasi-Sverdrup balance that applies in the subtropical gyre, does not seem to apply anywhere in the SPG.

325 To better understand what drives the interior part of the subpolar gyre, we further divide the domain into an interior and a boundary part, as represented in Fig. 10. The two domains are defined using the -3 Sv line as previously, and the 3000 m isobath. What is between the -3 Sv line and the 3000 m isobath is considered as the slope region and the rest is considered as the interior area. The choice of the 3000 m isobath is somehow subjective but the results are not sensitive to the choice of a specific isobath.

330 In the slope region, the main source of cyclonic vorticity is the BPT. The curl of the wind and the  $\beta V$  are also positive. The strongly negative NL term indicates advection of cyclonic vorticity outside of this domain toward the shelf or the gyre interior.

In the interior, the NL term represents the major contribution to the cyclonic circulation. It is balanced by the BDC, the BPT and the  $\beta V$  terms. Contributions from the BDC are of similar magnitude in the interior and the slope area. The wind input of



**Figure 10.** Integration of the barotropic vorticity terms in the slope area (a, defined between the barotropic streamfunction contour -3 Sv and the 3000-m isobath) and interior (b).

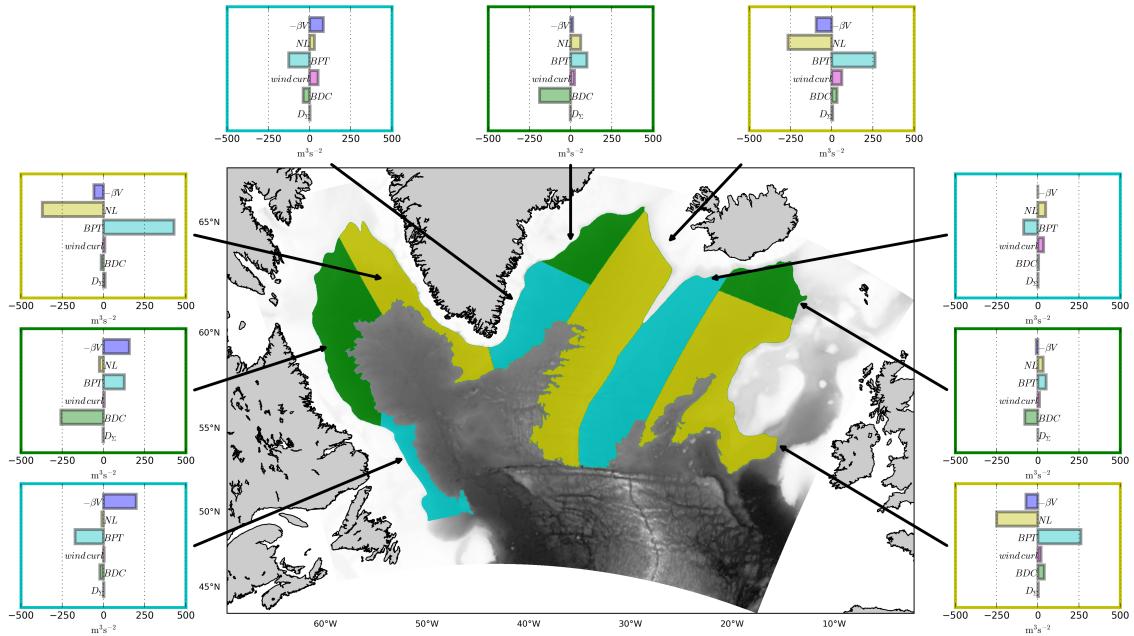
vorticity is smaller than in the slope region, as the major wind source of vorticity is located near Greenland (Fig. 7 (d)) and not uniformly distributed over the gyre. It confirms that the gyre interior is not in Sverdrup balance at the first order, which would imply a dominant balance between a negative  $\beta V$  and a positive input from the curl of the wind stress, but is driven instead by nonlinear effects. The comparison between balances in the interior and slope regions indicates that the NL term helps to redistribute vorticity from the boundary toward the interior of the gyre.

### 5.3 Balance in the slope area

The main source of cyclonic vorticity inside the gyre is related to the NL term, which helps transfer the vorticity from the boundary toward the inside. But which boundary regions are the main contributors of vorticity to the interior?

Several type of regions can be identified by looking at the dominant terms in the barotropic vorticity balance (Fig. 11): The western boundary areas in cyan, which include the Western Labrador Sea (WLS), Eastern Greenland (EG) and Eastern Reykjanes Ridge (ERR); the eastern boundary regions in yellow, which include the Western Greenland (WG), the Western Reykjanes Ridge (ERR) and the eastern part of the Iceland Basin; and the Northwest regions in green, which include the extension of the Denmark Strait and Iceland Scotland overflows, and the northwestern part of the Labrador Sea.

The barotropic vorticity balance in the western boundary areas (cyan in Fig. 11) is close to the typical equilibrium of Western Boundary Currents (WBC) (Schoonover et al., 2016; Gula et al., 2015) with an equilibrium between the planetary vorticity and the BPT. For the WLS, the deviation from WBC dynamics is small and is related to a bottom drag signal. We excluded the Southern part near Flemish Cap ( $48^\circ N, 46^\circ W$ ) (not shown) where the dynamics is driven by a positive input of planetary vorticity and BPT balanced by the NL term. The case of the ERR is slightly different with no net meridional transport in this area. The main input of vorticity is provided by the NL term, which is related to inertial effects from the current following



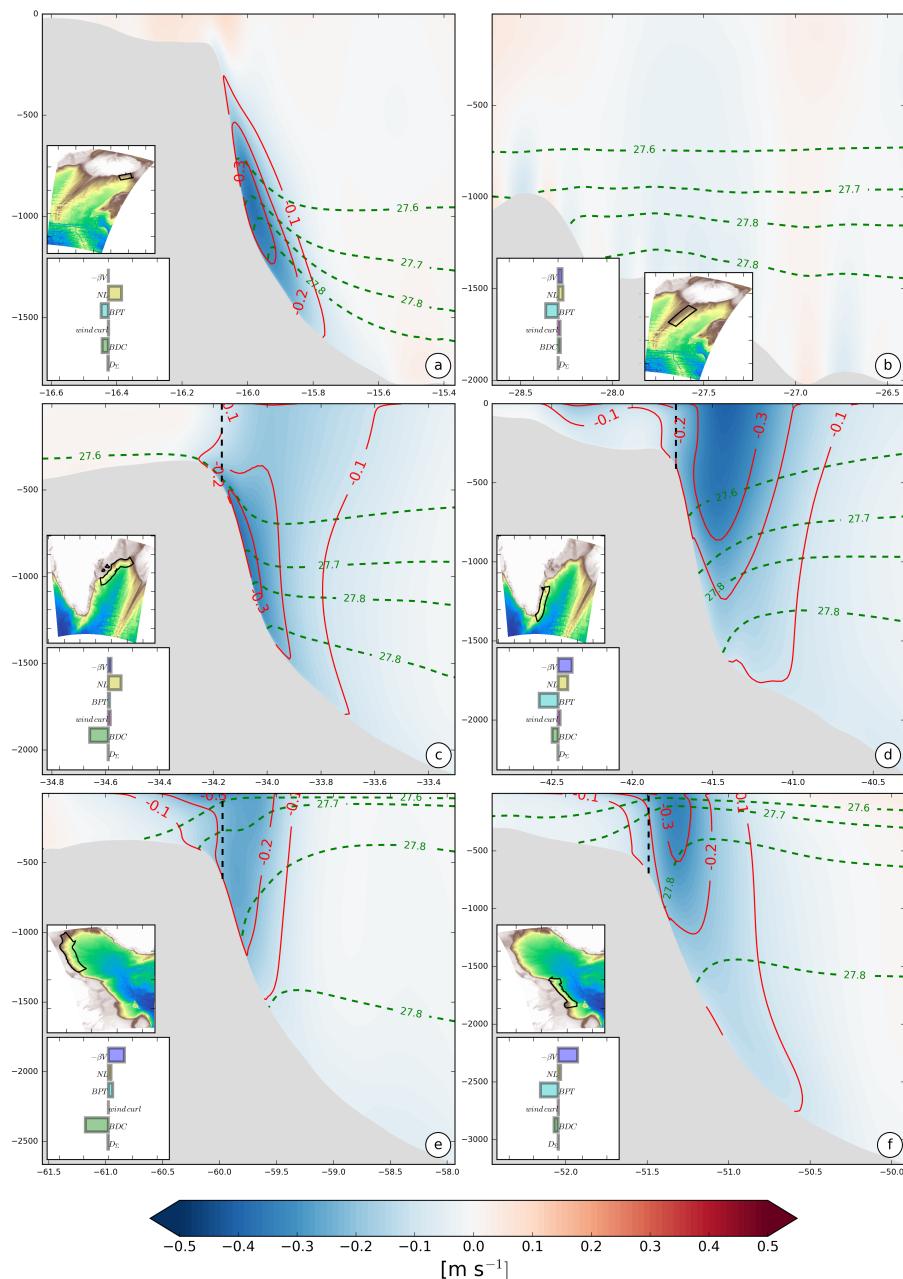
**Figure 11.** Barotropic vorticity balance integrated over different parts of the gyre along the slope

the Iceland Shelf. In this area the input of positive vorticity is mainly balanced by topography and the drag corresponding to a local dissipation of vorticity. From this we can infer that western boundary areas do not provide cyclonic vorticity to the gyre interior.

Three regions (green in Fig. 11) have in common a dominant contribution from the bottom drag. Vertical sections of the mean along-stream current (Fig. 12 (a),(c),(e)) in these areas reveal strong intensified bottom current (especially near the Iceland shelf and the Denmark Strait). In comparison, WBCs have a more surface intensified structure with reduced amplitudes near the bottom (Fig. 12 (b),(d),(f)). In Fig. 12, vorticity balances are indicated. They differ from Fig. 11 because the integration is restricted to the boundary current, excluding recirculations. In Fig. 12 (a),(c),(e) the BPT amplitudes are reduced (and even change sign) compared to Fig. 11. This reflects the sensitivity of the vorticity balance on the location of the boundary on the continental slope. The -3 Sv contour used in Fig. 11 does not coincide everywhere with the top of the continental slope used in Fig. 12.

The dynamics in the extension of the Denmark Strait and Iceland Scotland overflows is a balance between the NL term and BDC, while in the Northwestern Labrador sea, the BDC balances the  $\beta$ -effect. As the BDC is the main sink of vorticity and only acts locally, no advection of positive vorticity toward the inside of the gyre can come from these locations.

In Eastern boundary regions (yellow in Figure 12), most of the cyclonic vorticity is provided by flow-topography interactions through the BPT and is balanced by the NL term. These regions are located where a strong eddy activity is observed (Figure 5), which might be responsible for the high amplitude of the NL term. This negative NL signal implies an export of positive vorticity toward either the shelf or the gyre interior.



**Figure 12.** Vertical section of the mean along-stream current near Iceland shelf (a), Eastern Reykjanes Ridge (b), Denmark Strait (c), Eastern Greenland (d), Northern Labrador Current (e), and Southern Labrador Current (f). Red solid lines and green dashed lines are velocity and isopycnal surface referenced potential density contours, respectively, while the black dashed line is the limit of integration near the shelf. The black contour on the topography map represents the area on which barotropic vorticity terms are integrated

## 6 Characterisation of the nonlinear term

The NL term is locally important and balances the bottom pressure torque at small scales (Fig. 6). When integrated over the gyre it plays a role in exporting cyclonic vorticity from the boundary toward the interior of the gyre. The NL term is however quite difficult to interpret as many processes are hidden inside the vertical and time integrals.

375 By decomposing the velocity in a barotropic and baroclinic part ( $u = \bar{u} + u'$ ) the NL advection term can be written as:

$$A_{\Sigma}(u, v) = \underbrace{A(\bar{u}, \bar{v})}_{A_{\Sigma}^{bt}} + \underbrace{A(u', v')}_{A_{\Sigma}^{bc}} \quad (6)$$

where the barotropic part can be written as  $A(\bar{u}, \bar{v}) = \bar{u}\Omega_x + \bar{v}\Omega_y$  which is the advection of the barotropic vorticity by the barotropic flow.

We show these terms integrated over the slope area and interior (same as Fig. 10) in Fig. 13. Over the slope area, both terms  
380 are negative and contribute to export cyclonic vorticity. The barotropic part is much larger than its baroclinic counterpart and  
export most of the vorticity, as can be expected from the barotropic structure of the currents over the slope. In the interior,  
both terms are positive, corresponding to an input of cyclonic vorticity for the interior (Fig. 13), but the NL term is evenly  
divided between its barotropic and baroclinic contributions. The North-West While defining our gyre interior with the 3000-m  
isobath and the -3 Sv barotropic streamfunction (in the South-East boundary), we include a part of the subtropical gyre with the  
Northwestern Corner. The Northwest corner provides about half of this baroclinic NL input, while the remaining part comes  
mostly from the South-Eastern boundary. The exchange of barotropic vorticity between the slope region and the interior is only  
385 due to the barotropic NL termbetween the slope region and the interior.

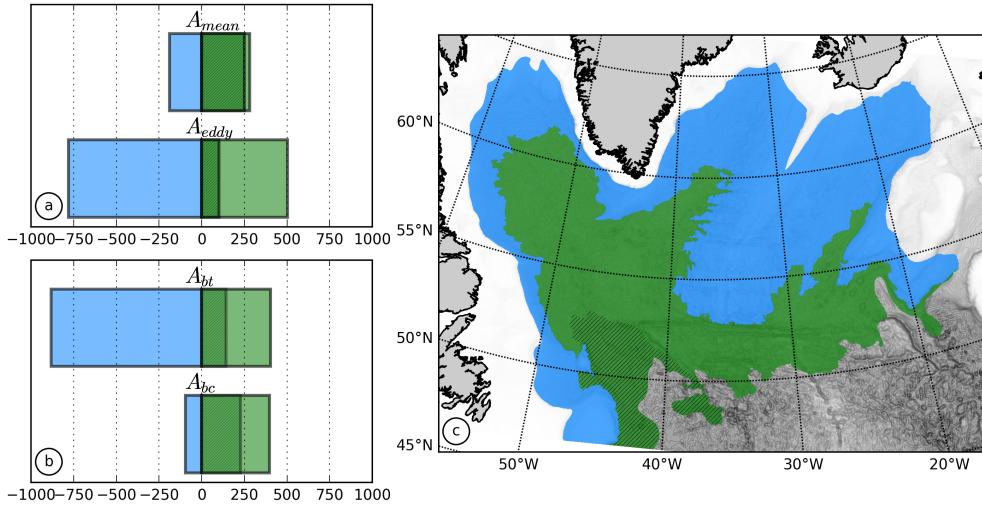
It is also possible to decompose the NL term into a time mean and eddy part by writing  $u = \langle u \rangle + u^*$  where  $\langle \bullet \rangle$  is the time average and the star denotes the fluctuation part. By putting this in the non linear operator  $A_{\Sigma}$  we have:

$$390 A_{\Sigma}(u, v) = \underbrace{A_{\Sigma}(\langle u \rangle, \langle v \rangle)}_{A_{\Sigma}^{mean}} + \underbrace{A_{\Sigma}(u^*, v^*)}_{A_{\Sigma}^{eddy}} + \underbrace{\left( 2 \frac{\partial^2 \langle v \rangle v^* - \langle u \rangle u^*}{\partial xy} + \frac{\partial^2 \langle u \rangle v^* + \langle v \rangle u^*}{\partial xx} - \frac{\partial^2 \langle u \rangle v^* + \langle v \rangle u^*}{\partial yy} \right)}_{\varepsilon} \quad (7)$$

The  $\varepsilon$  part is the residue of the cross product and its value is negligible compared to both the mean and eddy parts.

When integrated over the slope area (Fig. 13), the eddy component dominates over the mean one. In the interior area, the supply of barotropic vorticity is also mainly due to the eddy component but the mean component contributes about a third of the total. Almost all of this mean signal is coming from the North-West Northwest corner, consistent with Wang et al. (2017),  
395 while the eddy part is dominant over the rest of the interior.

We can identify several processes providing cyclonic barotropic vorticity to the subpolar gyre. The most important is the eddy contribution coming from the boundary area that is associated with a barotropic contribution. Barotropic vorticity is also provided through a mean-baroclinic signal coming from the NWC in the NWC region. Our definition of the subpolar gyre, based on a barotropic streamfunction contour, includes a part of the NWC, which is a complex transition region between the subtropical and the subpolar gyre. In comparison, in the lower resolution simulation (not shown) most of the vorticity is advected inside the gyre by mean-barotropic processes but the amplitude of the NL term is cut by half.  
400



**Figure 13.** Integration of the Non linear term in the slope (c,blue) and interior area (c,green) for the mean-eddy decomposition (a)and the barotropic-baroclinic decomposition (b). The hatches are the contribution from the [North Western Northwestern Corner](#) .

## 7 Summary and Conclusions

We have studied the dynamics of the North Atlantic Subpolar gyre in a numerical model with, for the first time, terrain following coordinates and a mesoscale-resolving resolution ( $\Delta x \approx 2$  km). The combination of the high resolution with  $\sigma$ -levels allows us to better resolve the effects of the mesoscale turbulence and of the complex bottom topography. The representation of the 405 mean currents and their variability is improved compared to previous simulations with coarser resolution. In particular, the simulations produce realistic levels of mesoscale turbulence at the surface and in the interior, as seen from comparisons of eddy potential and kinetic energy with observations from Argo floats and surface drifters.

The role of the topography is essential in the SPG. This impact is reflected in the barotropic vorticity balance of the gyre 410 through the Bottom Pressure Torque. The Bottom Pressure Torque is sometimes interpreted as the effect of the vortex stretching due to the bottom flow over topography, as expected for a predominantly geostrophic flow. However, we show here that the ageostrophic effects, in particular due to the viscous bottom drag, are predominant at the bottom and the BPT cannot be estimated from the bottom vertical velocity.

Barotropic vorticity balances are opposite in the shelf region compared to the interior of the gyre. The main balance in the 415 shelf region is between a negative bottom pressure torque and a positive bottom drag, which is typical of a buoyancy driven current. Inside the gyre, the inputs of positive vorticity from the BPT and the wind curl, are balanced by the bottom drag curl. The important role played by the bottom drag and the weak role played by the viscous torque, compared to other models, is related to the choice of  $\sigma$ -level coordinates and high horizontal resolution.

The bottom pressure torque has a large amplitude where boundary currents flow along the steep continental slope. It is the  
420 main term balancing the meridional transport of water in western boundary currents, except for some regions with dense water overflows where the bottom drag curl can become predominant. On the eastern (northward flowing) boundary currents, the strong input of positive vorticity by the bottom pressure torque is balanced by the non linear term. The nonlinearities, which are essentially due to the eddying activity, allow advection of the positive vorticity from the boundary toward the interior of the gyre. ~~The North Western Corner is also instrumental in feeding positive vorticity to the gyre interior through its southern~~  
425 ~~boundary, A positive input of vorticity is also related to the presence of the Northwestern Corner~~ mostly through time-mean baroclinic fluxes.

The nonlinear term is the main forcing for the interior part of the gyre, overcoming the effects of the wind curl and bottom pressure torque. This is putting forward the failure of the classical Sverdrup balance or even of a topographic Sverdrup balance in the interior of the Subpolar gyre, and emphasizing the importance of the inertial effects to obtain a more realistic Subpolar  
430 gyre circulation.

*Data availability.* The datasets ANDRO and NOAA are respectively available online at <https://www.umr-lops.fr/Donnees/ANDRO> and <https://www.aoml.noaa.gov/phod/gdp/interpolated/data/subset.php>.

*Author contributions.* MLC designed the setup and carried out the experiment. MLC and JG analysed the output of the simulation. All authors participated in the writing and editing of the article.

435 *Competing interests.* The authors declare that they have no conflict of interest.

*Acknowledgements.* M Le Corre is supported by UBO and Région Bretagne through ISblue, Interdisciplinary graduate school for the blue planet (ANR-17-EURE-0015) and co-funded by a grant from the French government under the program "Investissements d'Avenir". JG is supported by UBO and AM Treguier by CNRS. Simulations were performed using HPC resources from GENCI-TGCC (grant 2018-A0050107638) and from DATARMOR of "Pôle de Calcul Intensif pour la Mer" at Ifremer, Brest, France. Model outputs are available upon  
440 request. We are grateful for comments provided by two anonymous referees that helped to improve the paper.

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## Response to Referee #1

We would like to thank the Referee for his/her constructive comments. We have taken into account all the points that were raised and we document the changes below.

### Major comment :

*Abstract and elsewhere: The authors claim that the Northwest Corner is a source of vorticity through the non-linear terms for driving the subpolar gyre in the North Atlantic. But I do not see how this is possible dynamically. The problem is that information propagates westwards along potential vorticity contours – either lines of latitude, as in the formulation of the barotropic vorticity balance given by equation (1), or along f/H contours as in the formulation used by Wang et al. (2017) (see comment 10. below). In either case, it is not possible for a vorticity forcing applied at the northwest corner to influence the gyre interior. It seems to me, therefore, that it is the eastern boundary regions that are important for driving the gyre and not the Northwest corner. Unfortunately, one cannot appeal to non-linear advection to get around this problem. To be influential, the non-linear term must be important in the eastern part of the gyre or in the gyre interior itself.*

We thank the reviewer for this comment. The confusion comes from our definition of the gyre interior with the 3000-m isobath and the -3-Sv barotropic streamfunction contour (along the South Eastern edge). Due to baroclinicity, this region includes the Northwestern Corner (NWC) which can also be viewed as part of the subtropical gyre.

It is true there is no vorticity flux from the NWC to the subpolar gyre interior (excepted maybe by a small eddy component). However the vorticity balance of the region we have defined as subpolar (based on the barotropic streamfunction) is influenced by the NWC.

This is now made clear in (l.387-390) :

« Barotropic vorticity is also provided through a mean-baroclinic signal located in the NWC. Our definition of the subpolar gyre, based on a barotropic streamfunction contour, includes a part of the NWC which is a complex transition region between the subtropical and the subpolar gyre. »

Minor comments :

1. Line 31: Why mention Munk (1950) but not Stommel (1948)? I would refer to both.

A reference to Stommel (1948) was added on l.31

2. Line 35: An important role for the bottom pressure torque is also anticipated in the early, diagnostic model of Greatbatch et al. (1991) – their Figure 6.

A reference to Greatbatch (1991) was added on l.35

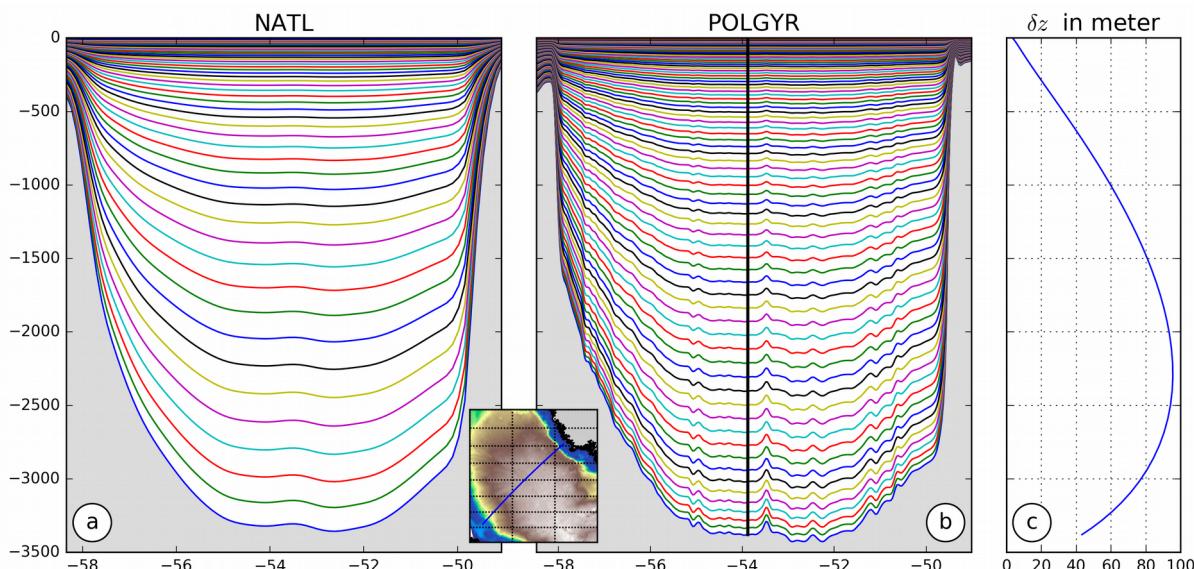
3. Lines 51-52: Wang et al. also showed the importance of the nonlinear terms in the subpolar gyre for driving the so-called Lavender recirculation – see their Figure 2c.

The case of the Lavender recirculation was added to the list of locations where the NL term is important (l.54)

4. Line 80: From Chelton et al., I would say that the radius of deformation for the 1 st baroclinic mode has trouble exceeding 10 kms and certainly does not reach 20 kms – see their Figure 6.

On the Southern edge of the domain the first radius of deformation is close to 20-km. To nuance our words we are now saying « first Rossby deformation radius remains below 10-km over most of the region » (l.80)

5. Line 97: From Figure 2, the vertical grid does not look to be particularly bottom intensified? We replaced the section in the Irminger basin by one in the Labrador Sea where we think it is clearer. We also added the variation of the grid spacing with depth along the vertical black line in (b).



*6. Figure 3: It is not easy to see all the details in this figure – although I do not have specific suggestions for improvement.*

We tried to improve the figure by changing the colormap to make the arrows more visible (p.6)

*7. Line 156-157: As noted above, Wang et al. find an important role for what they call “mean flow advection” for driving the Lavender recirculation along the slope around the Labrador Sea.*

Thank you for pointing this oversight. The following was added : « More recently Wang (2017) showed the importance of the mean flow advection in these circulations. ». (l.161)

*8. Paragraph beginning on line 165: Could refer to Brandt et al. (2004, JGR).*

Thank you for suggesting Brandt et al. (2004), the reference was added. (l.169)

*9. Line 175: How is EAPE defined? This should be given somewhere.*

The definition of EAPE is now added in the new equation (1) :

$$\text{EAPE} = \frac{-g}{2\rho_0} \langle z' \rho' \rangle$$

Where  $z'$  is the vertical isopycnal displacement,  $\rho'$  the density anomaly associated with this displacement and  $\langle . \rangle$  is the time average.

Also precisions on the EAPE version of Roullet et al. (2014) were added. (l.180-186)

*10. Line 186 and equation (1): Should mention that this is the vorticity equation for the vertically integrated flow. There is also an equivalent vorticity equation for the vertically averaged flow.*

We are now mentionning the two different versions for the barotropic equations and commenting their differences in the text. (l.195-199)

*11. Lines 205-206: Do the acronyms for these different models get defined somewhere?*

Acronyms are now defined along with references to previous studies using these models. (l.216-218)

12. Line 218: ...also the subpolar North Atlantic, as noted above (point 3).

Same as in point 3 (l.231-232)

13. Line 221: I would not say the “advection of vorticity” when you are referring to the nonlinear term. It is easy to confuse with the “advection of planetary vorticity”.

In order to avoid confusion « advection of vorticity » was changed by « nonlinear term » (l.233)

14. Line 280: Should “over” be replaced by “within”? Actually, the integral of this term should be very close to zero by construction.

« Over » was replaced by « within ». Because of model discretisation the integral is not exactly zero but very close. (l.293)

15. Line 294: My only objection here is that the Csanady paper uses dynamics linearized about a state of rest which means that the NL term plays no role, as could, perhaps, be made clearer. However, the comparison with the arrested topographic wave is certainly illuminating.

A reference to Csanady (1997) about JEBAR effect on the shelf has been added. The NL term is only important along the Greenland shelf and is related to eddy-barotropic component suggesting eddy interaction between the shelf and the open ocean. On the Canadian shelf the NL term is small and is barely contributing to the dynamics, thus the use of linearized dynamics seems valid there. The part with the coordinate changes has been removed for clarity. (l.305-310)

16. Figure 12: The dashed lines show isopycnal surfaces but which density is this? From the labelling, it must be a potential density of some kind. Please make clear.

Indeed, we are talking about potential density referenced at the surface. This precision was added in the caption. (p.19)

Typos and language issues :

Typos and language issues were corrected.

## Response to Referee #2

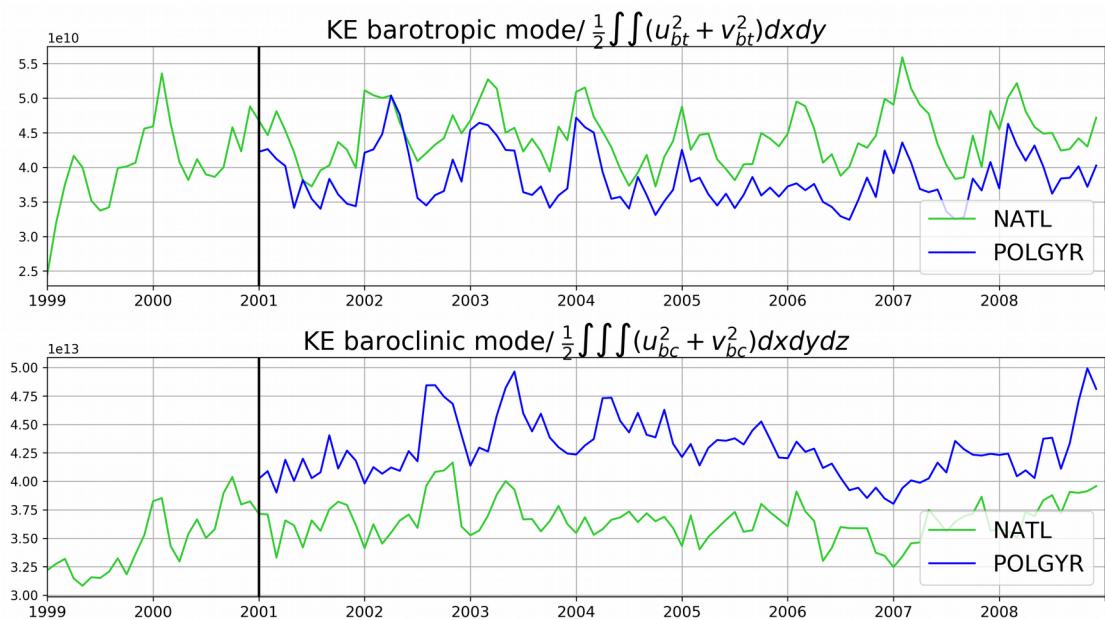
We would like to thank the Referee for his/her constructive comments. We have taken into account all the points that were raised and we document the changes below.

### Major comment :

*1) Like the rest of the paper, the introduction is thorough and well-written. I think it could do a better job of emphasising the novelty of the paper a little more strongly, particularly with regard to the vertical coordinate/nested domain and thorough analysis/breakdown of the barotropic vorticity equation.*

We have slightly modified the abstract (l. 1.5-6) and introduction (l. 63-65) to further emphasize the main novelty of the study.

*2) The model run is relatively short, although page 3 does discuss the spinup. Whilst this is probably sufficient to equilibrate the barotropic mode, there is a link to the baroclinic mode via the JEBAR term. Is the baroclinic mode properly spunup? If it isn't, the authors should discuss any impact this might have on their argument.*



To evaluate the equilibration of the model, we show the time series of the barotropic (top) and baroclinic energies (bottom) for NATL (green) and POLGYR (blue). The area of integration is the same and corresponds to the entire POLGYR domain. We can see that the amount of energy in the barotropic mode reaches a statistical equilibrium pretty fast, over about a year.

By 2001, the baroclinic mode is also close to equilibration in NATL. One additional year of spin up for the POLGYR nest from 2001 to 2002 allows the dynamics to adjust to the increase in resolution. The text has been modified to refer to both barotropic and baroclinic energies (l.94)

Minor comments :

Typos issues as in line 3- 18- 132- 303- 317- Fig13 were corrected

*lines 9-10 : "the topographic Sverdrup balance cannot describe the dynamics in the interior". which it probably shouldn't. I'd expect the flat bottomed Sverdrup balance to dominate here.*

We changed « topographic Sverdrup balance » to «Sverdrup balance » in the abstract (l.10)

*line 31 : It would also be appropriate to mention bottom friction and Stommel (1948) here, as bottom friction is discussed later, e.g. Fig. 7e.*

In addition to viscous effects, bottom friction was added along with a reference to Stommel (1948) (l.30-31)

*Section 2 : No mention of horizontal viscosity or diffusivity, although the rest of the section is very thorough.*

We have added the following in the model description : « We use no explicit horizontal viscosity or diffusivity and rely on third-order upwind-biased advection schemes, which include an implicit hyperdiffusivity at the grid scale. » (l.103-105)

*line 235 & 243 : There's really only a few locations where the BDC is large. It seems largely the case that betaV balances the residual of the NL and BPT terms.*

l.235 : We have added a sentence to make this more explicit in the text (l .248 in the revised version of the manuscript) : « More precisely, the  $\beta V$  term balances the sum  $\frac{J(P_b, h)}{\rho_0} + A_\Sigma$  over most of the domain, while the BDC locally plays a role in the shallow areas. »

l.243 : The sentence has been modified to avoid any misunderstanding (l.255)

*line 292-297 : This goes past a little too quickly for me. Without further reading, or a more in depth description, I find it difficult to make the link between the gradient of the bottom pressure and the nature of the flow's driving force.*

We have modified this part and removed the explanation based on the coordinate change to make the interpretation clearer. (l.305-310)