#### **ORIGINAL ARTICLE**



## Comprehensive landscape of immune-checkpoints uncovered in clear cell renal cell carcinoma reveals new and emerging therapeutic targets

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Received: 26 June 2019 / Accepted: 18 February 2020 / Published online: 12 March 2020 © Springer-Verlag GmbH Germany, part of Springer Nature 2020

#### **Abstract**

Clear cell renal cell carcinoma (ccRCC) constitutes the most common renal cell carcinoma subtype and has long been recognized as an immunogenic cancer. As such, significant attention has been directed toward optimizing immune-checkpoints (IC)-based therapies. Despite proven benefits, a substantial number of patients remain unresponsive to treatment, suggesting that yet unreported, immunosuppressive mechanisms coexist within tumors and their microenvironment. Here, we comprehensively analyzed and ranked forty-four immune-checkpoints expressed in ccRCC on the basis of in-depth analysis of RNAseq data collected from the TCGA database and advanced statistical methods designed to obtain the group of checkpoints that best discriminates tumor from healthy tissues. Immunohistochemistry and flow cytometry confirmed and enlarged the bioinformatics results. In particular, by using the recursive feature elimination method, we show that HLA-G, B7H3, PDL-1 and ILT2 are the most relevant genes that characterize ccRCC. Notably, ILT2 expression was detected for the first time on tumor cells. The levels of other ligand-receptor pairs such as CD70:CD27; 4-1BB:4-1BBL; CD40:CD40L; CD86:CTLA4; MHC-II:Lag3; CD200:CD200R; CD244:CD48 were also found highly expressed in tumors compared to adjacent non-tumor tissues. Collectively, our approach provides a comprehensible classification of forty-four IC expressed in ccRCC, some of which were never reported before to be co-expressed in ccRCC. In addition, the algorithms used allowed identifying the most relevant group that best discriminates tumor from healthy tissues. The data can potentially assist on the choice of valuable immune-therapy targets which hold potential for the development of more effective anti-tumor treatments.

**Keywords** HLA-G · Transcriptome · Immune-checkpoints · RNAseq · TCGA · ccRCC

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**Electronic supplementary material** The online version of this article (https://doi.org/10.1007/s00262-020-02530-x) contains supplementary material, which is available to authorized users.

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#### **Abbreviations**

ILT4

ccRCC Clear cell renal cell carcinoma
HLA-G Human leukocyte antigen-G
IC Immune-checkpoints
ILT2 Immunoglobulin-like transcript 2 (LILRB1)

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Immunoglobulin-like transcript 4 (LILRB2)

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RFEM Recursive feature elimination method

SVM Support vector machine TCGA The Cancer Genome Atlas

#### Introduction

Clear cell renal cell carcinoma (ccRCC) is a renal tumor typically characterized by malignant epithelial cells with clear cytoplasm and a compact alveolar or acinar growth pattern interspersed with intricate, arborizing vasculature. Among kidney cancers, 70% are estimated to be ccRCC [1] constituting the most common renal cell carcinoma subtype. Patients cannot be treated by radiation or chemotherapy. Metastases at the diagnosis time are observed for 25–30% of the patients and less than 10% of these survive more than five years. Recurrence occurs in 20-30% of patients even after complete nephrectomy of primary tumors. Genetic evidence revealed that ccRCC originates from sequential losses of multiple tumor suppressor genes such as von Hippel-Lindau (VHL) gene. Other genes such as PBRM1 (Polybromo 1) and BAP1 (BRCA1-associated protein) have also been identified as renal cancer driver genes, mainly underexpressed in ccRCC [2]. These three genes are closely located on chromosome 3p. Remarkably, chromosome 3p loss occurs in more than 90% of sporadic ccRCCs [3].

ccRCC has long been recognized as an immunogenic cancer. As such, significant attention has been directed toward optimizing immune-checkpoints (IC)-based therapies. IC are defined as cell surface molecules that transduce positive or negative signals, into effector cells. When the same ligand interacts with an activating or an inhibitory receptor, inhibition is dominant and allows tumor cells to escape destruction by the immune system [4]. Therefore, blockade of inhibitory IC by antibody-based therapeutics constitutes a suitable strategy to restore an effective anti-tumor response [5, 6].

Clinical phase I/II trials have provided evidence that treatments with anti-CTLA-4 or PD-L1:PD-1 antibodies are capable of restoring suitable anti-tumor responses and that therapies using combinations of anti-CTLA-4 and PD-L1:PD-1 are more efficient than using each one individually [7–9]. Although these trials have helped to give a step forward in the treatment of some patients, others still remain unresponsive. Potential causes might be the complexity of IC pathways since several yet undescribed checkpoints, besides CTLA-4 and PD-1:PD-L1, might be expressed simultaneously and act concomitantly through non-overlapping, sometimes opposite, mechanisms. In addition, other causes of the inefficiency of the treatments might be the heterogeneity of expression within tumor cells or the toxicity due to their action on non-tumor tissues. Consequently, to achieve optimal specificity and limit potential side effects, IC targeted by

immune-therapies must have restricted expression in normal tissues and high expression upon cellular transformation.

In this context, the search for novel IC targets has been intensified. Ongoing trials include antibody-based protocols against LAG-3, TIM-3 and VISTA [10] or agonist antibody-based protocols for co-stimulatory molecules ICOS, OX40 and 4-1BB [11]. Some of these molecules are evaluated in mono or combined therapies. However, the uncomplete list of their side effects and the lack of knowledge about their mechanisms of action prevent their immediate clinical utilization.

The advent of next-generation sequencing technologies, particularly applied to RNAseq, has demonstrated its usefulness in classifying patients with similar pathologies, screening genes involved in carcinogenesis and in identifying prognostic factors in cancer [12–14]. This technique also revealed inter- and intra-tumor heterogeneity which challenges the precise diagnosis and selection of reliable therapeutic targets [15]. The full exploration of large and growing public databases such as The Cancer Genome Atlas (TCGA) data portal (https://tcga-data.nci.nih.gov/tcga/tcgaHome2.jspa) which covers RNAseq transcriptome data for more than 10,000 samples of human cancers including over 30 different cancer types, holds the potential to help identify suitable therapeutic targets.

Many statistical tools were developed to analyze RNA-seq data [16]. Comparison of these different tools 16 singled out DESeq2 as the most conservative [17]. However, several statistical challenges must still be faced in order to unravel molecular processes and interactions at stake for each cancer type.

Here, we provide a novel and comprehensible view on forty-four IC expressed in ccRCC and highlight the most relevant group of checkpoints that characterize ccRCC and the ones that best discriminate tumor from healthy tissues. The data can potentially assist on the choice of valuable immunetherapy targets which hold potential for the development and effectiveness of anti-tumor treatments.

#### **Materials and methods**

#### TCGA data collection and processing

RNA-sequencing profiles of ccRCC samples and their related clinical data obtained from The Cancer Genome Atlas (TCGA) data portal (https://tcga-data.nci.nih.gov/tcga/) were used to identify expressed IC. A set of 25 283 RNA-seq derived from the 539 patients with ccRCC was downloaded. These were normalized by the FPKM-UQ method that scales the number of reads of each gene compared to the total number of reads and the length of genes.



#### Statistical methods used for the differential analysis

The differential analysis was conducted on the RNA-seq data using DESeq2 [18] which is a statistical method implemented in an R software package. DESeq2 allows identifying differentially expressed genes using the standard comparison mode between two experimental conditions. A high variability between patients exists in RNA-seq data. Therefore, to take into account this variability and accurately analyze these data, it is mandatory to use a distribution that incorporates over-dispersion as does the negative binomial distribution. DESeq2 takes into account this variability by using Wald test based on a negative binomial distribution to test whether each model, tumor or healthy cells, differs significantly from zero. It models counts by a negative binomial distribution because counts are over-dispersed (the variance is higher than the mean), and the negative binomial distribution has two parameters called mean and dispersion which enable to model the mean-variance relationship. A scaling factor normalization procedure is performed to take into account the varying sequencing depths of the different samples. The generalized linear models (GLMs) with a logarithmic link are used to estimate coefficients that indicate the overall expression strength of the gene. The p-value adjustment for multiple tests was performed by the Benjamini-Höchberg procedure [19], which consists in controlling the false discovery rate (FDR). We considered differentially expressed genes those with an adjusted p value  $\leq$  to 0.05.

#### **Feature selection method**

Supervised learning is a powerful tool for mathematical analysis of biological data. Here, we consider the following classification task: "how well can I predict if a tissue is tumoral or not with gene expression data?" In this section, our goal is to rank IC genes according to their powers of prediction: We want to find the smallest and the best subset of genes that realizes this classification task. To achieve this, we consider the recursive feature elimination (RFE) algorithm [20] with a linear-support vector machine (linear-SVM). This algorithm selects features by recursively considering smaller and smaller sets of features and assigns weights to the features directly linked to the coefficients of the linear model. A subset of the ranked genes is selected according to the SVM-IC [21]. The details of the method are explained below.

#### **Dataset and tools**

Python and scikit-learn were used [22]. The features are normalized (FPKM-UQ normalization) gene expressions of the differentially expressed genes (d=41) in order to use well-known gene selection techniques for micro-array-based data

[23]. The data are scaled with zero mean and variance one for better performance with the linear-SVM (see below for details of this algorithm).

#### **Linear Support Vector Machine training**

We focused on a binary classification model. We want to build a classifier f:

$$f: \mathbb{R}^d \to \{-1, 1\}$$
$$(x_1, \dots, x_d) \to y$$

where  $(x_1, ..., x_d)$  is the gene expression data of a tissue sample and the target value is the type of the tissue: non-tumor adjacent or tumor.

Support vector machine with a linear kernel was chosen for the classification learning algorithm since the data are almost linearly separable. Also, linear decision functions capture very well the underlying distributions in micro-array classification tasks [23–25]. The goal is to find the optimal parameters of a classifier function that as the form:

$$f: \mathbb{R}^d \to \{-1, 1\}$$
$$x \to \operatorname{sign}(w^t x + b)$$

We define the dataset as  $\{(x_i, y_i)\}_{\{1 \le i \le n\}}$  where  $x_i = (x_{i1}, \dots, x_{id})$  is the gene expression data of the sample  $\mathbf{i}$  and  $y_i$  its label (non-tumor adjacent tissue or tumor tissue). For each gene  $j \in \{1, \dots, d\}$ , a weight  $w_j$  is involved in the classification task. This weight is used for the ranking of genes. The linear-SVM learning algorithm can be defined as an optimization problem:

minimize 
$$\frac{1}{2} \|w\|^2 + C \sum_{i=1}^n \xi_i$$
  
subject to 
$$\forall i \in \{1, \dots, n\}, y_i(w^t x_i + b) \ge 1 - \xi_i$$
  
$$\forall i \in \{1, \dots, n\}, \xi_i \ge 0.$$

#### Recursive feature elimination (RFE) algorithm

The RFE method recursively deletes the genes that are the less important in the classification task. At an iteration  $k \in \{1, ..., d\}$ , d minus k genes are left to rank. At each iteration, we train the linear SVM classifier used in the RFE method over the whole dataset. Each gene has a weight associated to this classifier in the decision making whether to distinguish if a tissue is tumoral or not. The square of this weight is the importance of a gene: It shows how the value of the gene expression is important in the decision making. The linear-SVM is trained over these genes, and the gene that has the least importance cj is deleted in the classification task  $(cj = Wj^2)$ . Let X be the matrix of the dataset



 $\left\{\left(x_{i},y_{i}\right)\right\}_{\left\{1\leq i\leq n\right\}}$  (where **i** is the patient) so that  $X[i,:]=x_{i}$  (the vector of gene expression data of patient **i**) and X[:,j] the vector of expression data of gene **j** among all the patients. Let  $y=\left(y_{i}\right)_{i}$  be the vector of the labels. The RFE algorithm is detailed below.

Adjacent non-tumor renal parenchyma was removed simultaneously. All patients participating in this study gave their informed written consent. The study was approved by the institutional review boards of Saint-Louis Hospital, Paris.

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Algorithm 1 RFE algorithm

Require: X, y

Ensure: A set of ranked genes G = [\text{gene}_1, \dots, \text{gene}_d]

Initialization: S \leftarrow [1, \dots, d], G \leftarrow \emptyset

while S \neq \emptyset do

X_{\text{current}} \leftarrow X[:, S]

Get w from linear-SVM training on the dataset X_{\text{current}}, y

\forall j \in [1, \dots, d], c_j \leftarrow w_j^2

j_{\min} \leftarrow \arg \min_j c_j

S \leftarrow S \setminus \{j_{\min}\}

G \leftarrow \operatorname{concat}(j_{\min}, G)

end while
```

The set of ranked genes G is then obtained. We want to compare the classifiers trained on a subset of features  $G_k$  in order to get the best subset of genes:

$$G_k = [\text{gene}_1, \dots, \text{gene}_k], \quad \forall k \in \{1, \dots, d\}$$

where gene<sub>1</sub> is the most important gene and gene<sub>d</sub> the least important one. To compare these classifiers, an information criterion is performed [21] which can be seen as an equivalent of Akaike's information criterion for linear-SVM. In the framework of the linear-SVM learning algorithm, one can define the SVM information criteria as: SVMIC( $G_k$ ) =  $\sum_{i=1}^n \xi_i + 2\text{Card}(G_k)$  where the  $\xi_i$  are the coefficients learned by the linear-SVM algorithm over  $X[:, G_k]$  and Card( $G_k$ ) is the length of the subset. In this case, Card( $G_k$ )=k. The smaller this criterion is, the better the classifier is. So, we chose the best subset of features with:  $G_{k_{\text{best}}} = \min_{G_k} \text{SVMIC}(G_k)$ . This subset is the best compromise between classification performance and smallness of the subset in order to get the most significant genes.

#### **Recovery of tumors from ccRCC patients**

Tumors were obtained from patients who underwent a radical nephrectomy for ccRCC as first therapeutic intervention in the Urology Department of Saint-Louis Hospital (Paris, France). Renal tumors were classified as ccRCC by an experienced uropathologist according to the World Health Organization (WHO) classification of tumors of the kidney [26].

#### Immunohistochemistry (IHC)

Immunohistochemistry was performed for each pair of tumor and normal renal parenchyma on 4-µm-thick, formalin-fixed and paraffin-embedded or on snap-frozen tissue sections according to technical specificities of each antibody. The following murine antibodies were used: CD70, B7H4, HVEM, B7H5 (VISTA), CD40, CD163, HLA-G (clone 4H84) and PD-L1. Staining was performed on automated slide stainers from Roche (BenchMark ULTRA system, Tucson, AZ) using the OptiView DAB IHC Detection Kit (Roche), Cell Conditioning 1 (CC1) standard antigen retrieval, an antibody incubation time of 32 min at 37 °C, ultraWash procedure, counterstaining with Hematoxylin II for 4 min, and bluing reagent for 8 min. Isotype-matched immunoglobulins were used for negative controls simultaneously. The immunohistochemical analyses were finally realized by an uropathologist using a BX51 microscope (Olympus France S.A.S, Rungis).

#### **Primary tumor cell culture**

Tumor tissues were cultured in RPMI1640 supplemented with 20% fetal bovine serum, 20  $\mu$ g/mL insulin, 10  $\mu$ g/mL transferrin, 25 nM sodium selenite, 50 nM hydrocortisone, 1 ng/mL epidermal growth factor, 10  $\mu$ M ethanolamine, 10  $\mu$ M phosphorylethanolamine, 100 pM triiodothyronine, 2 mg/mL bovine serum albumin, 2 mM glutamine, 0.5 mM sodium pyruvate. After 21 days, medium was removed, tumor cells detached with EDTA 2 mM solution and analyzed by flow cytometry.



#### Flow cytometry analysis

Flow cytometry analyses were performed on tumor and tumor-infiltrating cells. Tumor-infiltrating cells were phenotyped immediately after isolation, whereas tumor cells were phenotyped after 3-week culture. This culture step was necessary to ensure sufficient cell numbers for flow cytometry analysis, even though some phenotype modifications by the in vitro culture might arise. Acquisition was performed on a MACSQuant 10 flow cytometer (Miltenyi Biotec), and analysis was performed using MACSQuantify (Miltenyi Biotec) and Flowjo softwares. Antibodies were CD45 VioGreen, CD3 PerCP, CD4 VioBright FITC, CD8 APC-Vio770, HLA-DR PerCP, CD28 PE-Vio770, CD137 PE-Vio770, B7-H3 VioBlue, ILT4 APC, CD70 APC, PD-L1 APC, CD137L PE from Miltenyi Biotec; HLA-G PE (clone MEM-G/09), ILT2 APC and ILT2PE (clone HP-F1) from eBioscience. PD-1 BV421 from Biolegend and CD27 PE, CD40 PE, CD86 FITC from Beckman Coulter.

#### Results

#### Landscape of IC expressed in ccRCC

To provide a global landscape of IC expressed in ccRCC patients, we analyzed the TCGA database which contains RNAseq information for 539 patients with ccRCC. To avoid selecting biased expression thresholds, we further focused on patients for whom data included tumor and adjacent non-tumor tissues. This information was available for 72 patients and is depicted in Table 1. A total of forty-four IC were chosen on the basis of a previously report [27]. To test our methodology, three tumor suppressor genes expressed at very low levels in most ccRCC were added as controls: the von Hippel-Lindau (*VHL*), the Polybromo 1 (*PBRM1*) and the BRCA1-associated protein (*BAP1*).

Expression ratios for tumor versus healthy adjacent tissues were first analyzed for each of the forty-four IC by biclustering genes for each of the 72 patients individually. The results are represented on a heatmap, a colored representation of a matrix of numbers that helps the visualization of gene expression data (Fig. 1). In this representation, each column represents a gene, each row a patient. The standardized expression levels are depicted by the color gradients. The results show perceptible differences between patients even though a global pattern emerges. Notably, the ratio of expression of tumor to adjacent non-tumors for B7H4 was found extremely low except for 2 out of 72 samples. The three control genes *PBRM1*, *VHL* and *BAP1* that are mostly down-regulated in ccRCC were grouped together, and their low expressions in ccRCC samples were confirmed (Fig. 1).

#### Statistically modulated IC in ccRCC

To establish statistically robust results, we chose to conduct a differential analysis to compare the expression levels of IC in ccRCC samples versus the adjacent non-tumor tissues using the DESeq2. A set of 1264 genes were found up-regulated and 1194 genes down-regulated, by considering a *p*-value of 0.05. The similar numbers of induced and repressed genes is consistent with an absence of methodological biases. From these, we extracted expression information for the forty-four IC simultaneously. The results obtained are represented by bar plots (Fig. 2). The x-axis represents the value of the log fold change and the y-axis the genes. A gradient of color is used in order to show the significance of genes in the study. The redder the bar, the more differentially expressed the gene.

Moreover, the genes on the *y*-axis are ranked according to their adjusted *p*-values. The lower the adjusted *p*-value, the lower the position of the associated gene on the axis, and the more significant the differential expression. If the value of the log fold change is negative, the gene is underexpressed, and if it is positive, the gene is overexpressed. Values representing the mean of normalized counts for all samples, the log2 FoldChange, the *p* values and the adjusted *p*-values of the test are represented in supplementary Table 1.

Notably, among the most significantly differentially over-expressed genes in tumor cells we found those encoding ligand-receptor pairs such as: CD70:CD27; HLA-G:ILTs; 4-1BB:4:1BBL, CD40:CD40L; CD86:CTLA4; MHC-II:Lag3; CD200:CD200R; CD244:CD48. In contrast, adjacent non-tumor cells express significantly higher levels of B7-H4 compared to tumor cells. As expected, the expression levels of the three control genes: *PBRM1*, *VHL* and *BAP1*, were lower in tumors than in adjacent non-tumor tissues, which further confirms the robustness of our statistical analysis.

## Localization of representative IC within tumor compartments.

To deepen the results of the TCGA analysis, we aimed at identifying more precisely the nature of the IC-expressing cells. To this end, we performed IHC analysis on different samples derived from a new cohort of ccRCC patients that underwent a radical nephrectomy at the Urology Department of Saint-Louis Hospital (Paris, France).

Tumor and normal renal parenchyma of ten patients were assessed simultaneously. We focused on B7-H4, the most significantly down-regulated gene and three up-regulated genes in tumor: CD70, CD40 and B7-H5 (VISTA). When samples were analyzed with the antibody directed against B7H4, strong labeling of the normal renal parenchyma of all renal tubular epithelial cells was observed in all cases. On



Table 1 ID and clinical information obtained from The Cancer Genome Atlas (TCGA) for the 72 patients for whom data included tumor and adjacent non-tumor tissues

Patient ID	Case ID	Sex	Year of birth	Year of death	Tumor stage	Age at diagnosis (days)	Days to death	Days to last follow up
TCGA-CW-5581	2d0f6d4f-acb9-4b45-a69d- c9a3f68c3732	Male	1959	_	Stage I	16,195	_	2799
TCGA-CZ-4865	305eaef4-4644-46e3-a696- d2e4a972f691	Female	1936	2006	Stage I	25,709	166	_
TCGA-B0-5691	31a0dd95-8199-4d25-b40d- 4b353644af46	Female	1936	-	Stage I	24,120	-	3431
TCGA-CW-6088	4100b960-7963-4a1e-ba24- 0a6526387e06	Male	1943	_	Stage I	22,020	-	3222
TCGA-CW-6090	4dd51edf-05d1-445a-b43c- 6fce29eb21d4	Male	1935	_	Stage I	24,909	_	2552
TCGA-B0-5703	576ea0ef-3abb-479d-adb7- ba646cee344e	Male	1936	_	Stage I	26,897	-	2246
TCGA-CW-5589	58ef1a13-a549-4043-b66c- 5327bfcbd2e6	Male	1952	_	Stage I	19,312	-	2378
TCGA-B0-5705	62cf9546-b932-4a5e-bc9b- 4103506d296d	Female	1937	_	Stage I	23,746	-	4537
TCGA-CJ-6030	6ab00314-5228-43ba-9880- 9d5177b64c61	Male	1938	2009	Stage I	24,096	2299	-
TCGA-B8-4619	78ec8bc9-e502-4f5b- b0f6-893,718,650,352	Male	1952	_	Stage I	21,206	_	523
TCGA-B0-5690	794aeb92-205f-4c75-bb1a- 0b2c6db99fea	Female	1951	-	Stage I	19,685	-	3392
TCGA-CZ-5986	883c37e2-c723-45d7-9e25- 082d1bec34e2	Male	1945	_	Stage I	22,456	_	373
TCGA-A3-3358	8a575e00-5dc5-416d-a8f5- 2cdfb8e62c31	Female	1948	_	Stage I	21,087	-	1307
TCGA-B8-5549	98dea82b-46f9-4b77-be8a- 06669bcf731b	Male	1957	_	Stage I	19,561	-	194
TCGA-A3-3387	9dc7812b-c7a2-4de4-bf6d- 4c7261384a62	Male	1957	_	Stage I	17,920	-	617
TCGA-CZ-5982	a43401ae-14cd-4f57-946b- 9a9c073f2a47	Female	1946	-	Stage I	21,592	-	2439
TCGA-B2-5641	a682a2a3-dc53-4b7e-8929- 07215737ec5e	Male	1931	_	Stage I	28,953	-	656
TCGA-B0-5699	c814c26c-ee8e-4fd8-a3d3- 441b302ead3b	Male	1950	_	Stage I	19,647	-	3841
TCGA-B0-5697	dfd2c288-5054-4fc1-9cae- f437779dc2de	Male	1957	_	Stage I	18,486	-	2630
TCGA-B8-5552	e58f2c7b-d1cc-48f3-a0c9- dcd2b27c37f6	Female	1969	_	Stage I	15,219	-	1046
TCGA-CJ-5689	e865d40a-9989-436c-8426- 88cc84c863e8	Male	1915	2009	Stage I	32,872	1620	-
TCGA-CZ-5984	ea26d89f-2843-489b-8627- 3d5ed0cabc2a	Male	1954	_	Stage I	18,775	-	2067
TCGA-B2-5636	ed2e9354-5ee1-4fcf-92ec- a1b507818b91	Male	1931	-	Stage I	28,901	-	919
TCGA-CJ-5672	eee108d6-bb11-4369-b776- 0f524afef6f3	Male	1920	2010	Stage I	30,900	2190	-
TCGA-CZ-5988	f2806652-1d7b-4c46-bb4e- ac7a2c96c68d	Male	1968	-	Stage I	14,131	-	693
TCGA-CZ-5989	13e25128-9be1-4f67-a43f- a8744a619203	Male	1946	-	Stage II	22,170	-	1905



 Table 1 (continued)

Patient ID	Case ID	Sex	Year of birth	Year of death	Tumor stage	Age at diagnosis (days)	Days to death	Days to last follow up
TCGA-B0-5706	3b2b492b-94af-4540-b283- 3b9ef98d5b2f	Male	1959	_	Stage II	16,442	_	3205
TCGA-CZ-5456	467bf226-a646-4217-bce6- 8d0f11c756eb	Male	1949	_	Stage II	21,164	-	2422
TCGA-CZ-5985	4c474c70-1d72-49e8-a8cc- a4145c5ab607	Male	1948	-	Stage II	21,242	-	1997
TCGA-CZ-5453	577847b9-f9b6-4954-868f- 3d5ab2b4f694	Male	1939	_	Stage II	24,640	2419	25
TCGA-CZ-5469	6205c2d8-d431-4c4c-8ac6- ee407170e833	Male	1966	2009	Stage II	15,242	946	-
TCGA-CZ-4864	7fc6b44d-ae66-409c-98e1- c1a518c33e95	Male	1916	2009	Stage II	31,557	2830	2830
TCGA-CZ-5463	8e9e684c-20e5-48b1-9e40- 970037fe959f	Male	1931	_	Stage II	27,911	-	662
TCGA-CZ-5470	99f59583-2728-4c1d-b98c- 8fbc3bb0a819	Female	1936	_	Stage II	26,494	_	386
TCGA-CZ-5451	9cdda9fa-d492-4902-afc1- eb2244e70c1b	Male	1932	_	Stage II	27,312	_	1929
TCGA-CZ-5452	e9faa588-d45a-450a-81a2- 949eb2834bc0	Male	1937	-	Stage II	25,486	-	1789
TCGA-CW-5584	09c4ea05-928d-49b7-b7fb- 30cff3481b14	Male	1929	2003	Stage III	27,352	164	-
TCGA-B0-5694	11111b58-c7df-4291-ad8a- 4baec9ff7d1f	Male	1937	2009	Stage III	26,060	480	-
TCGA-B0-5696	1d176c53-6cbb-4a39-9a6f- 669b4f1cb575	Male	1938	_	Stage III	25,552	-	2609
TCGA-CJ-5676	310c31bf-91ce-40b4-99e4- a10242296de9	Male	1957	_	Stage III	17,170	_	4067
TCGA-CJ-5679	3fa6c93e-e7fe-402c-9526- c81411aa0920	Male	1930	2004	Stage III	26,858	679	-
TCGA-CZ-5466	5722df9f-5631-476d-a11b- b3c1e9a40fbf	Male	1940	_	Stage III	24,669	_	685
TCGA-CZ-5465	5e248b21-e69d-4dee-a1e8- 029ade80d0eb	Female	1931	_	Stage III	27,838	2564	1446
TCGA-CW-5587	73fc6ae6-7c5e-44de-a9a0- 17292cbb01cc	Female	1941	_	Stage III	22,693	-	2226
TCGA-B0-5711	88c91a7b-5c41-4361-85d0- da759ab94204	Male	1954	_	Stage III	18,444	-	3989
TCGA-CZ-4863	88e7ce26-5b3f-4e4e-89b7- f706063fc467	Female	1955	_	Stage III	18,730	-	1928
TCGA-B0-5701	8f8a632d-7fbd-4c86-b909- afb7edb9ad28	Male	1942	_	Stage III	23,915	-	2461
TCGA-CZ-5467	b602a73b-809c-44c6-a787- d496705e7ae8	Female	1921	2007	Stage III	31,473	73	-
TCGA-B0-5709	bf768635-b809-4df4-a4e6- 7495e66aa227	Female	1941	_	Stage III	22,843	-	3974
TCGA-CZ-5458	c4247ccb-8201-428e-a2e7- b5104f095588	Male	1963	_	Stage III	15,790	-	2789
TCGA-B8-4620	eda2b871-8a18-4854-92d8- d8d66fb127d8	Female	1940	-	Stage III	25,786	-	777
TCGA-CZ-5457	f00b7956-73a9-4e4b-85d2- 60b3ba13f4a4	Male	1944	-	Stage III	22,763	-	2754



Table 1 (continued)

Patient ID	Case ID	Sex	Year of birth	Year of death	Tumor stage	Age at diagnosis (days)	Days to death	Days to last follow up
TCGA-CJ-5681	2939c03a-6f3f-4f7b-b246- 34361baadeb9	Female	1959	2004	Stage IV	16,121	552	_
TCGA-CZ-5461	393abcf7-1155-4b32-85ca- cd44d259e4b4	Male	1954	2006	Stage IV	19,030	330	330
TCGA-B0-4712	3f72d63f-ad48-4500-baf6- 897b1d6dda7d	Male	1930	2009	Stage IV	28,095	1337	-
TCGA-CJ-6033	4edff57f-4b0e-4770-beac- 590da7d7232c	Female	1950	2004	Stage IV	19,919	224	-
TCGA-B0-5712	514af471-31d2-43fa-88dc- 8639a5e97181	Female	1936	_	Stage IV	24,988	-	2722
TCGA-CJ-5680	5db69ebe-38db-4ef3-b825- 674b4a6ddaee	Female	1938	2005	Stage IV	23,778	768	-
TCGA-CZ-5455	74749fe8-f5d0-4d0d-8c7a- e56eba6503b3	Male	1943	2007	Stage IV	23,150	561	-
TCGA-CJ-5678	822cf6c1-dd65-4814-94b1- 0c335208ad9b	Male	1941	2004	Stage IV	22,944	574	-
TCGA-CZ-5468	878d1caa-c4d8-4864-888c- 310a0c1ee898	Male	1923	2007	Stage IV	30,729	59	59
TCGA-CW-5580	88fc4bc4-32cf-4d92-8c29- 20d920b8f719	Female	1930	2008	Stage IV	26,696	1964	_
TCGA-B8-4622	b125ff14-4fb4-4f90-8622- fed49bdfe954	Male	1953	-	Stage IV	21,135	-	1525
TCGA-CW-6087	bbdaa931-e922-49be-bfbf-fa0c2ae27d7a	Male	1942	2003	Stage IV	22,438	41	_
TCGA-CJ-5677	d2664fde-ce3b-45e6-9a23- 4a07980f7bac	Female	1950	2006	Stage IV	19,849	782	_
TCGA-B0-5402	d7ab7ec0-3de7-4ffd-a5ac- f75579355b2a	Male	1946	-	Stage IV	23,477	-	1290
TCGA-CZ-5462	e0127e51-43ba-4536-bc9d- 004591f9c627	Male	1924	2007	Stage IV	30,659	311	_
TCGA-B0-4700	e33dff22-5bf1-4dd8-bed7- 063cb555677c	Male	1944	2009	Stage IV	22,034	1980	_
TCGA-CW-5591	f1ae0181-74f8-47fd-83be- 83a7d01101cc	Male	1948	-	Stage IV	20,712	-	2271
TCGA-CZ-5454	f2801b21-5444-4cc3-a642- c60c6d82cd3d	Male	1943	2007	Stage IV	23,083	722	-
TCGA-CZ-5987	f5759059-c0e3-4f1a-af96- 5c7197d3c33c	Male	1946	2007	Stage IV	21,928	445	-
TCGA-CW-5585	0487fc41-386c-4d76-9084- daf959bf5e98	Male	1952	-	Stage IV	18,898	-	2609

the other hand, a very heterogeneous labeling was observed within and between ccRCC samples. In the majority of ccRCC tumors, no labeling was noted in both tumor and tumor-infiltrating inflammatory cells. In the other cases, a slight labeling was noted in tumor cells and/or tumor-infiltrating inflammatory cells. This confirms further the down-regulation of B7H4 highlighted in the RNAseq analysis. A representative example is illustrated in Fig. 3. When antibodies directed against the three up-regulated genes CD70, CD40 and B7-H5 (VISTA) were used, tumors were strongly stained when compared to normal renal parenchyma which

further confirms the transcriptome results. Nevertheless, the supplementary information given by the morphologic analysis concerns the nature of cells that highly express these checkpoints. Indeed, IHC results showed that tumor cells themselves expressed high levels of CD70 whereas only rare parietal cells of Bowman's capsule, some interstitial fibrous areas and glomerular capillary vessels were labeled with anti-CD70 in normal renal parenchyma. In sharp contrast, CD40 and B7-H5 (VISTA) antibodies intensely labeled numerous inflammatory cells in contact with tumor cells



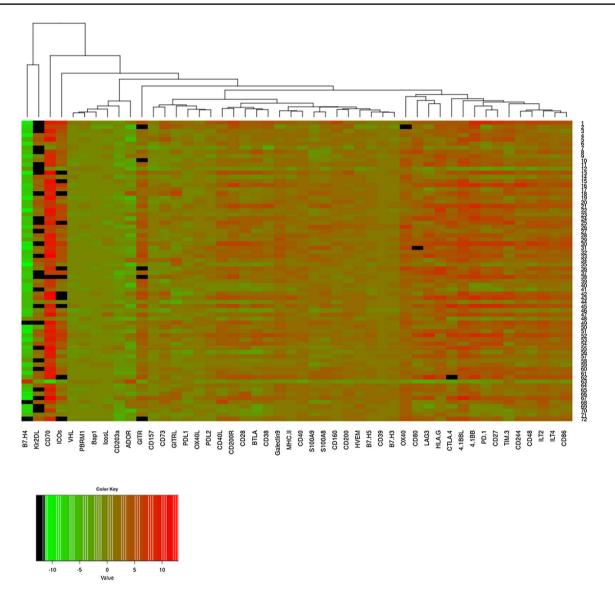


Fig. 1 Heatmap representation of the logarithm of the ratio of gene expression between tumor and non-tumor adjacent tissues. In this representation, each column represents a gene, and each row a patient.

The standardized expression levels are depicted by the color gradient: green, low expression ratio in ccRCC samples; red, high expression ratio. Values in black represent a ratio equals to 0 (whose log is  $-\infty$ )

such as CD163-labeled macrophages representative stains are illustrated in Fig. 3.

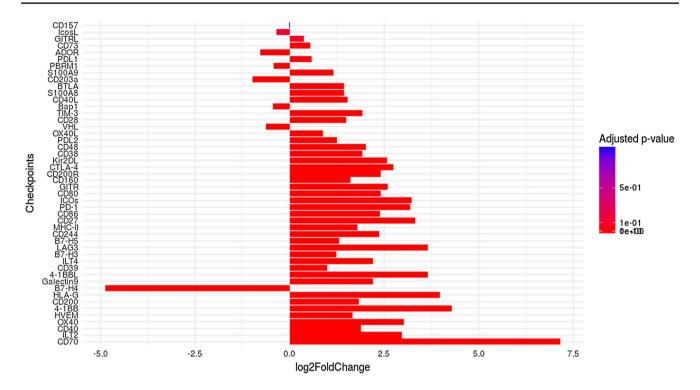
Altogether, IHC results confirmed and extended those obtained by the analysis of RNAseq data showing for the first time the down-regulation of B7H4 and overexpression of CD70, CD40 and B7-H5 (VISTA) in ccRCC.

The ID of each patient included in the TCGA database (Table 1) allows to gain further insight into IHC results which are digitalized and made available on https://cancer.digitalslidearchive.org.

### Most relevant IC expressed in tumors of ccRCC patients

Our survey of IC expressed in ccRCC reveals the overexpression of 38 IC at different levels. To find out which of them are the most important representatives of this type of cancer, we considered the recursive feature elimination (RFE) algorithm with a linear-SVM. The model eliminates the least important features, one by one iteratively until all features in the dataset are exhausted. Features are then ranked according to when they were eliminated. As such, it is a robust method for finding the best performing subset of features and owns the advantage that it can be applied to the whole dataset without fixing a threshold beforehand.





**Fig. 2** Categorization of forty-four differentially expressed IC. Numbers on the *x*-axis represent the value of the logarithm fold change. If this value is negative, then the gene is underexpressed, and if this one is positive, then the gene is overexpressed. The higher the value is,

the more the gene is affected by the condition (tumor). To represent differentially expressed genes, we used a color gradient. More red the bar is, more the IC is considered as differentially expressed

The RFE algorithm was therefore applied to the 539 patients included in the TCGA database followed by the linear-SVM model. The results, named SVMIC, revealed that the optimal number of features is 7. The accuracy is visible on the plot represented in Fig. 4a and was estimated by tenfold cross-validation over the whole dataset. The dataset was separated in ten parts, for each part we trained the model on the nine others and computed the accuracy on the singled-out part. Finally, we took the mean of the ten computed accuracies. The output of the whole algorithm is the ranked subset of the following genes: 'HLA-G' 'HVEM' 'PD-L1' 'B7-H3' 'ILT2' 'CD40' 'B7-H5'. The importance of each gene, defined as the square of its weight (see Materials and Methods for more details), shows how the value of the gene expression is important in the decision making. It is depicted by a graphical representation in Fig. 4b. The x-axis represents the selected genes, and the y-axis the importance of the genes in the linear-SVM model. Although HLA-G has been identified as the most significant gene, the graph shows that its bar plot is smaller. This would mean that HLA-G shares information with one or several of the other selected genes. This interesting feature should be the aim of future work.

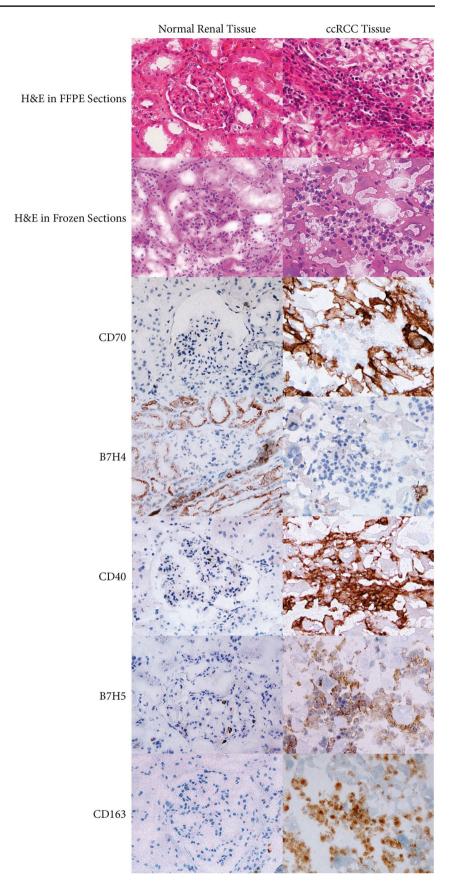
#### **Checkpoints expression in tumor cells**

To validate the RFE algorithm results, we analyzed ten additional tumors derived from ccRCC patients. The results obtained by immunohistochemistry for six representative samples are illustrated in Fig. 5. A constant labeling of tumor cells and more rarely tumor-infiltrating inflammatory cells was noted in all ccRCC tumors with the antibody directed against HVEM. Nevertheless, this antibody also labeled renal tubular epithelial cells of the normal renal parenchyma. Immunostaining with HLA-G and PD-L1 antibodies revealed high and heterogeneous inter- and intratumor labeling. In sharp contrast, no staining was observed in normal renal parenchyma.

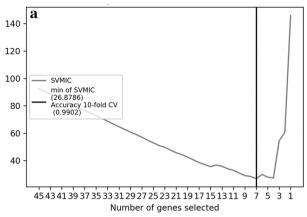
To better quantify the cell populations that express the IC, we analyzed tumor cells individually by flow cytometry. We focus on the most significant checkpoints revealed by the RFE algorithm: HLA-G:ILT2 and HLA-G:ILT4, 4-1BBL:4-1BB (CD137L:CD137), PD-L1:PD-1, and B7-H3, to which we added CD70, one of the most overexpressed IC in ccRCC. Thus, ten additional ccRCC tumors were more thoroughly analyzed (Fig. 6a) and a representative example, expressing the majority of the IC is shown in Fig. 6b. Consistent with the results of the RFE model, PD-L1, HLA-G and CD137L were expressed in all tumors studied. CD70

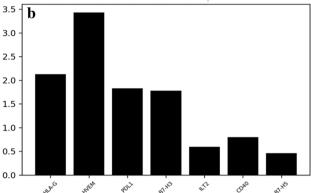


Fig. 3 IHC illustration of the localization of differentially expressed IC within tumor compartments of a representative ccRCC patient. Protein products of the selected genes CD70, B7H4, CD40, HVEM, B7H5 and CD163 were assessed in normal renal tissue and tumor tissue (H&E and immunoperoxidase stains are also shown)









**Fig. 4** A. Plot of the SVM information criteria as a function of the subsets generated by the RFE algorithm. *x*-axis: number of selected genes; *y*-axis: cross-validations score (number of correct classifications). B. Barplot showing the importance of each of the seven features selected. The *x*-axis represents the selected genes and the *y*-axis the importance of the genes in the linear-SVM model

and B7-H3 were found in 6/7 and 5/8 tumors studied, respectively (Fig. 6c). There was a high inter-individual variability with respect to the proportion of tumor cells expressing a given checkpoint. For instance, the proportion of tumor cells expressing PD-L1 varied from 27% in patient #1 to 100% in patient #3. Similarly, this range was 17-74% for 4-1BB (CD137L) and 5–97% for HLA-G (Fig. 6c). Notably, ILT2 expression was observed in tumor cells from six out of ten patients, and particularly significant in three of them (16%, 20% and 30%). Similarly, ILT4 expression was also observed in tumor cells from six out of ten patients, and particularly significant (from 28 to 79%). This is noteworthy since ILT2 and ILT4 are usually considered as being expressed only by leukocytes [28]. All the values are represented in Fig. 6c. These results are thus consistent with those derived from the RNAseq analysis and the RFE model and reveal for the first time the expression of ILT2 on tumor cells. In addition, a very important conclusion that follows from culturing individual tumors is that a particular tumor expresses several IC simultaneously, and this has to be taken into account for optimizing future IC-based future therapies, since the treatment with a single checkpoint does not seem to be efficient enough.

#### **Discussion**

Immune-checkpoint blockade by antibodies that target specific ligand–receptor interactions has emerged as one of the most promising therapeutic options for patients with ccRCC. Despite the success of these therapies, a considerable proportion of patients remain unresponsive to treatment suggesting that multiple non-redundant immunosuppressive mechanisms coexist within tumor and its microenvironment.

In this study, we comprehensibly analyzed forty-four IC expressed in tumors derived from patients with ccRCC in terms of gene and protein expression differences between tumor and non-tumor-adjacent tissues and ranked them according to their relevances to characterize ccRCC. Among the ligand-receptor pairs identified in this study, some are involved in inhibitory pathways, whereas others are implicated in stimulatory pathways and might be expressed in the same tumor cells or the microenvironment.

One of the most highly differentially expressed RNA in ccRCC is CD70, a type II integral membrane protein that belongs to the tumor necrosis factor superfamily. This result was confirmed at the protein level by IHC analysis and is consistent with previous report [29] adding arguments in favor of the robustness of our analysis.

Our TCGA survey also revealed high expression of CD40 in ccRCC samples compared to adjacent non-tumor tissues. Using IHC, we have confirmed this and further show that CD40 is expressed in the abundant CD163-labeled macrophage population surrounding tumor cells. Clinical trials using CD40 agonists are still ongoing even though its administration is associated with particular toxicities [30]. Another ligand-receptor pair found highly overexpressed in ccRCC samples is 4-1BB (CD137) and 4-1BBL (CD137L). These are co-stimulatory molecules that are involved in multiple steps during the progression of inflammation and hematopoiesis. High expression of 4-1BB has also been noted on a number of cancer cell lines such as liver or leukemia cell lines [31]. Clinical trials with two agonist antibodies, urelumab and utomilumab, are ongoing. Despite initial signs of efficacy, clinical development of urelumab has been hampered by inflammatory liver toxicity [32]. To our knowledge, the presence of high levels of 4-1BBL in ccRCC is reported here for the first time. The presence of co-stimulatory molecules would provide a "second" signal that activates T-cell and promote anti-tumor response following the blockage of the negative IC [33]. In agreement with this, blockade of CTLA-4 (inhibitory IC) together with



**Fig. 5** IHC illustration of the localization of the three more important selected IC obtained by the linear-SVM model



engagement of ICOS (stimulatory IC) enhanced anti-tumor responses and significantly improved tumor rejection [34].

Several members of the B7 family were also found modulated in ccRCC. A hallmark of the B7 family is the capability to co-stimulate or co-inhibit T cell responses in the presence of peptide/MHC complex-mediated TCR signaling [35]. The B7 co-stimulatory ligands are important for full activation of naïve T cells in the lymphoid organs. In contrast, B7 co-inhibitory ligands are crucial for the termination of over activated T cell response and maintenance of self-tolerance [36]. The analysis of the TCGA data highlighted members of the B7 family that are differentially modulated in ccRCC, mainly B7H3, B7-H4 and B7H5/VISTA.

The levels of B7H4 were highly decreased in ccRCC. This correlates with results of our protein expression analysis performed by IHC on our cohort of ccRCC patients but sharply contrast with studies performed in other cancer types such as pancreatic or hepatocellular carcinoma, in which the overexpression of the B7-H4 protein constitute a negative prognostic marker for patient's survival [37]. This emphasizes the need to assess the expression of each IC in the different cancer types.

Another member of the B7 family, CD276/B7-H3, was found overexpressed at mRNA and protein levels. Given its immunomodulatory capacities and its overexpression on both, cancer cells and tumor-infiltrating blood vessels [38, 39], CD276/B7-H3 may be considered a more general



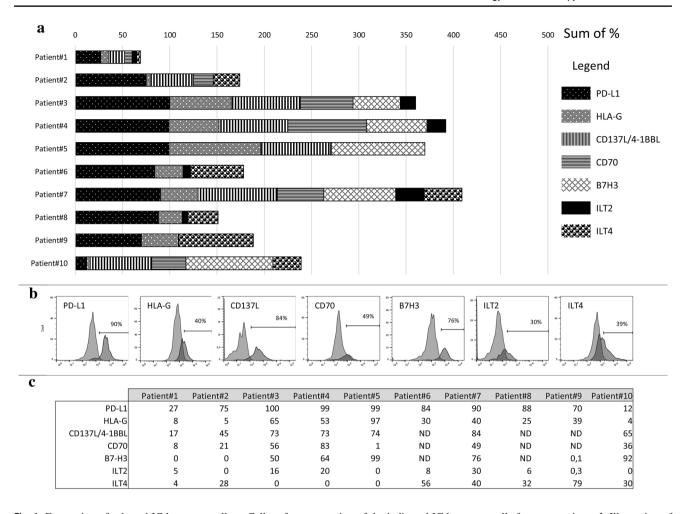


Fig. 6 Expression of selected IC by tumor cells. a Cell surface expression of the indicated IC by tumor cells from ten patients. b Illustration of cell surface profiles of all the IC expressed in tumor of patient 7. c Percentage of cell surface IC expression for the ten ccRCC patients studied

target in cancer's treatment. However, its therapeutic use awaits more information due to its dual activity, either as stimulatory effect on the proliferation of both CD4+ and CD8+-T cells or as co-inhibitory molecule. Moreover, since B7-H3 is broadly expressed, especially in peripheral healthy tissues, B7-H3's blockade by specific antibodies might be associated with severe adverse effects. In addition, B7H3 seems to share a yet unidentified receptor with B7H4. Considering that levels of B7H3 and B7H4 are highly increased and decreased respectively in ccRCC, it would be necessary to determine which of the two will work and in what circumstances.

This may also be the case of B7H5/VISTA, which is a molecule with dual activity. It behaves as a stimulatory ligand for antigen presenting cells (APCs) causing immune activation and as a negative ligand for T-cells, suppressing activation and proliferation [40]. In this study, the mRNA and protein levels of this molecule were found increased in ccRCC samples. In particular, IHC clearly showed that B7H5/VISTA is expressed on abundant macrophage

surrounding tumor cells. It is likely that given the multiple binding partners of these molecules and their bidirectionality with regard to signaling, their molecular mechanisms of action have to be clarified more thoroughly before therapeutic application.

The recursive method pointed out HLA-G and PD-L1 as highly relevant IC expressed in tumor cells of ccRCC patients. These confirmed recent reports show high expression of HLA-G in ccRCC which may coexist with PD-L1 [41, 42]. This was also demonstrated here by in vitro culture of tumor cells derived from ccRCC patients. If PD-L1 is already used for therapeutic purposes, HLA-G still is not. We have previously made the proof of concept that anti-HLA-G antibodies can be used in immunotherapy protocols [43]. In addition, HLA-G offers a significant therapeutic window for targeted therapy since: (1) HLA-G has a restricted expression in normal tissues, (2) HLA-G has broad immune-inhibitory functions through binding to its receptors ILT2 and ILT4 present on immune cells. Indeed, HLA-G/ILTs can block all stages of an immune response,



from APC activation and effector priming to the function of fully activated CTLs, NK or B cells [44]. Therefore, developing strategies to block this pathway would offer the advantage of exerting extended effects with less prominent systemic toxicities. We propose that simultaneously engaging PD-L1 and HLA-G blockade would constitute a promising new therapeutic opportunity. Moreover, the demonstration that ILT4 [41, 45] and for the first time in this study, ILT2, are expressed not only by tumor infiltrating cells but also by CD45-negative tumor cells themselves, adds supplementary interest of this checkpoint as a therapeutic target.

In conclusion, the approach adopted in this study, which couples transcriptome stringent data analyses and protein measurement by IHC and flow cytometry, highlighted key IC, some of which were never reported before to be expressed in ccRCC. In particular, the ranking of these checkpoints and the demonstration that each tumor express several IC simultaneously emphasize the importance that exists to expand the potential therapeutic targets to treat ccRCC. Targeting HLA-G/ILT in HLA-G-positive tumors, either concomitantly or in case of non-responsiveness to anti-PD1/PD-L1, would be one strategy to be tested. The remaining challenges include the understanding of fundamental mechanisms of IC action in pathological conditions and the identification of optimal combinations of IC for ccRCC patient's benefit.

Acknowledgements The authors are particularly grateful to Dr. Nathalie Rouas-Freiss for very instructive discussions and critical reading of the manuscript. We are also thankful to Dr. Marcela Garcia and Santiago Miriuka for their enlightened suggestions on tumor culture procedures. We kindly appreciate the experimental assistance of Alix Jacquier on cytometric assays and Jerome Delmotte on immunochemistry. The results shown are based upon data generated by the TCGA Research Network: https://www.cancer.gov/tcha.

Authors contributions DTLR was involved in conceptualization, formal analysis, writing original draft, supervision; MS helped in methodology, software, formal analysis, writing original draft; MB contributed to methodology, software, formal analysis, writing original draft; JV performed experiments, formal analysis and diagnosis; MBP contributed to methodology, performed experiments; MD performed experiments and analysis; FB performed experiments; JLM contributed to methodology, formal analysis, writing original draft; FD provided samples; S.L. contributed to formal analysis, writing original draft; PHC helped in formal analysis, methodological supervision, writing-original draft, funding; EDC was involved in research design, funding.

**Funding** This work was funded by the Commissariat à l'Energie Atomique et aux Energies Alternatives (CEA) and Ecole CentraleSupélec, Université Paris-Saclay.

#### Compliance with ethical standards

Conflict of interest The authors declare no potential conflicts of interest

**Ethical approval** The study was approved by the institutional ethics committee of Saint-Louis Hospital, Paris.

**Informed consent** Patients provided written informed consent before sampling.

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# SMM: An R Package for Estimation and Simulation of Discrete-time semi-Markov Models

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**Abstract** Semi-Markov models, independently introduced by Lévy (1954), Smith (1955) and Takacs (1954), are a generalization of the well-known Markov models. For semi-Markov models, sojourn times can be arbitrarily distributed, while sojourn times of Markov models are constrained to be exponentially distributed (in continuous time) or geometrically distributed (in discrete time). The aim of this paper is to present the R package **SMM**, devoted to the simulation and estimation of discrete-time multi-state semi-Markov and Markov models. For the semi-Markov case we have considered: parametric and non-parametric estimation; with and without censoring at the beginning and/or at the end of sample paths; one or several independent sample paths. Several discrete-time distributions are considered for the parametric estimation of sojourn time distributions of semi-Markov chains: Uniform, Geometric, Poisson, Discrete Weibull and Binomial Negative.

#### Introduction

Semi-Markov models, independently introduced by Lévy (1954), Smith (1955) and Takacs (1954), are a generalization of the well-known Markov models. For semi-Markov models, sojourn times can be arbitrarily distributed, while sojourn times of Markov models are constrained to be exponentially distributed (in continuous time) or geometrically distributed (in discrete time). For this reason, semi-Markov processes are more general and more adapted for applications than the Markov processes.

Semi-Markov processes have become important tools in probability and statistical modeling with applications in various domains like survival analysis, biology, reliability, DNA analysis, insurance and finance, earthquake modeling, meteorology studies, etc.; see, e.g., Heutte and Huber-Carol (2002), Ouhbi and Limnios (2003), Chryssaphinou et al. (2008), Janssen and Manca (2006), Votsi et al. (2012), D'Amico et al. (2013), Votsi et al. (2014), D'Amico et al. (2016b), Barbu et al. (2016), D'Amico et al. (2016a) for semi-Markov processes in continuous or discrete time with various applications and Sansom and Thomson (2001), Bulla and Bulla (2006), Barbu and Limnios (2008), for hidden semi-Markov models and applications in climatology, finance and DNA analysis.

Note that the semi-Markov theory is developed mainly in a continuous-time setting, while utterly less works address the discrete-time case. We refer the reader to Limnios and Oprisan (2001) for continuous-time framework and to Barbu and Limnios (2008) and references therein for discrete-time framework. The R package SMM that we present in this paper is developed in discrete time. Note that undertaking works also in discrete time (modeling stochastic tools, associated estimation procedures, corresponding software, etc.) is an important issue for several reasons. In our opinion, the most relevant of these reasons is that the time scale is intrinsically discrete in several applications. For instance, in DNA studies, when modeling a nucleotide or protein sequence by means of a stochastic process, the "time" of that process is in fact the position along the sequence, so it is discrete. Other examples can be found in some reliability/survival analysis applications where the time represents the number of cycles of a system or the counting of days/hours/etc. We can argue further for the importance of developing works also in discrete time, in parallel to their analogous ones developed in continuous time. For instance, we can mention the simplicity of computations in discrete time, the fact that a discrete-time stochastic process does not explode, the potential use of discrete processes after the discretization of continuous ones, etc.

Few R packages have been developed to handle semi-Markov models or hidden semi-Markov models. For semi-Markov models we have the recent **semiMarkov** R package (Król and Saint-Pierre, 2015) that performs maximum likelihood estimation for parametric continuous-time semi-Markov processes, where the distribution can be chosen between Exponential, Weibull or exponentiated Weibull. That package computes associated hazard rates; covariates can also be taken into account through the Cox proportional hazard model. Two R packages are also dedicated to hidden semi-Markov models, implementing estimation and prediction methods: the hsmm R package (Bulla et al., 2010) and the mhsmm R package (O'Connell and Højsgaard, 2011).

Note that there is no R package developed for discrete-time multi-state semi-Markov models. Thus the purpose of this paper is to present an R package that we have developed, called **SMM**, which performs parametric and non-parametric estimation and simulation for multi-state discrete-time semi-Markov processes. For the parametric estimation, several discrete distributions are considered

for the sojourn times: Uniform, Geometric, Poisson, Discrete Weibull and Negative Binomial. The non-parametric estimation concerns the sojourn time distributions, where no assumptions are made on the shape of distributions. Moreover, the estimation can be done on the basis of one or several trajectories, with or without censoring. The aim of this paper is to describe the different possibilities of this package. To summarize, the package **SMM** that we present deals with different problems:

- Parametric estimation for sojourn time distributions (Uniform, Geometric, Poisson, Discrete Weibull and Negative Binomial) or non-parametric estimation;
- One or several sample paths;
- Four different types of sojourn times: a general one depending on the current state and on the next state to be visited, one depending only on the next state, one depending only on the current state, and one depending neither on the current state nor on the next state;
- Four different types of censoring: censoring at the beginning of sample paths, censoring at the
  end of sample paths, censoring at the beginning and at the end of sample paths or no censoring
  at all.

Let us make some remarks about these points.

First, concerning the censoring, the simplest situation is the one when all the sojourn times are completely observed (non censored). A more complicated and realistic framework is when the last sojourn time is not completely observed, thus being right censored; in most practical situations this case occurs. An analogous situation is when the first sojourn time is not completely observed, thus being also right censored. In practice, this last case occurs when one does not know the beginning of a phenomenon modeled by a semi-Markov chain. Note that this censoring at the beginning of the sample path is a right censoring (not a left censoring); indeed, when the first sojourn time is censored as in our paper, the available information is that the real sojourn time (that is not observed) is greater than this censored observed time. Thus we are clearly in a right censoring framework, although this happens at the beginning (i.e., left) of the trajectory, which could seem confusing. The most complete framework is when both the first and the last sojourn times are right censored.

Second, when considering estimation starting from several independent sample paths of a semi-Markov chain, it is assumed that all the trajectories are censored in the same way; note that this is not a real constraint, but we imposed this condition only in order to avoid useless technical notations that would make the comprehension more difficult.

Third, note that it is important for the four types of models (of sojourn times) to be considered separately because: (i) in practical situations, one model could be more adapted than some other; (ii) different models will yield specific parameter estimators, so it is important to study them separately.

The paper is organized as follows. The next section **Semi-Markov models** describes the semi-Markov models used in this package. Section **The SMM package** illustrates the different functions of the **SMM** package. We end the paper by presenting some concluding remarks on this R package.

#### Semi-Markov models

Let us consider a random system with finite state space  $E = \{1, \ldots, s\}$ ,  $s < \infty$ . Let  $(\Omega, \mathcal{A}, \mathbb{P})$  be a probability space and assume that the time evolution of the system is governed by a stochastic process  $Y = (Y_k)_{k \in \mathbb{N}^*}$ , defined on  $(\Omega, \mathcal{A}, \mathbb{P})$  with values in E; that is to say that  $Y_k$  gives the state of the system at time k. Let  $T = (T_m)_{m \in \mathbb{N}^*}$ , defined on  $(\Omega, \mathcal{A}, \mathbb{P})$  with values in  $\mathbb{N}$ , be the successive time points when state changes in  $(Y_k)_{k \in \mathbb{N}^*}$  occur (the jump times) and let also  $J = (J_m)_{m \in \mathbb{N}^*}$ , defined on  $(\Omega, \mathcal{A}, \mathbb{P})$  with values in E, be the successively visited states at these time points. The relation between the process Y and the process Y of the successively visited states is given by  $Y_k = J_{N(k)}$ , or, equivalently,  $J_m = Y_{T_m}$ ,  $m, k \in \mathbb{N}$ , where  $N(k) := \max\{m \in \mathbb{N} \mid T_m \leq k\}$  is the discrete-time counting process of the number of jumps in  $[1, k] \subset \mathbb{N}$ .

In this paper we consider four different semi-Markov models corresponding to the following four types of sojourn times.

• Sojourn times depending on the current state and on the next state:

$$f_{ij}(k) = \mathbb{P}(T_{m+1} - T_m = k | J_m = i, J_{m+1} = j);$$

• Sojourn times depending only on the current state:

$$f_{i\bullet}(k) = \mathbb{P}(T_{m+1} - T_m = k | J_m = i);$$

• Sojourn times depending only on the next state to be visited:

$$f_{\bullet i}(k) = \mathbb{P}(T_{m+1} - T_m = k | J_{m+1} = j);$$

• Sojourn times depending neither on the current state nor on the next state:

$$f(k) = \mathbb{P}(T_{m+1} - T_m = k).$$

Note that the sojourn times of the type  $f_{i\bullet}(\cdot)$ ,  $f_{\bullet j}(\cdot)$  or  $f(\cdot)$  are particular cases of the general type  $f_{ij}(\cdot)$ . Nonetheless, in some specific applications, particular cases can be important because they are adapted to the phenomenon under study; that is the reason why we investigate these cases separately.

#### General case: sojourn times of the type $f_{ij}(.)$

Definition 1 (semi-Markov chain SMC and Markov renewal chain MRC). If we have

$$\mathbb{P}(J_{m+1}=j,T_{m+1}-T_m=k|J_m=i,J_{m-1},\ldots,J_1,T_m,\ldots,T_1)=\mathbb{P}(J_{m+1}=j,T_{m+1}-T_m=k|J_m=i),$$

(1)

then  $Y = (Y_k)_k$  is called a semi-Markov chain (SMC) and  $(J, T) = (J_m, T_m)_m$  is called a Markov renewal chain (MRC).

All along this paper we assume that the MRC or SMC are homogeneous with respect to the time in the sense that Equation (1) is independent of m.

Note that if (J, T) is a MRC, then it can be proved that  $J = (J_m)_{m \in \mathbb{N}^*}$  is a Markov chain with state space E, called the *embedded Markov chain* of the MRC (J, T) (or of the SMC Y).

**Definition 2.** For a semi-Markov chain we define:

• *the* semi-Markov kernel  $(q_{ij}(k))_{i,j\in E,k\in\mathbb{N}}$ ,

$$q_{ij}(k) = \mathbb{P}(J_{m+1} = j, T_{m+1} - T_m = k | J_m = i);$$

• *the* initial distribution  $(\mu_i)_{i \in F}$ ,

$$\mu_i = \mathbb{P}(J_1 = i) = \mathbb{P}(Y_1 = i);$$

• the transition matrix  $(p_{ij})_{i,j\in E}$  of the embedded Markov chain  $J=(J_m)_m$ ,

$$p_{ij} = \mathbb{P}(J_{m+1} = j | J_m = i);$$

• *the* conditional sojourn time distributions  $(f_{ij}(k))_{i,j\in E,k\in\mathbb{N}}$ ,

$$f_{ij}(k) = \mathbb{P}(T_{m+1} - T_m = k | J_m = i, J_{m+1} = j).$$

Note that

$$q_{ij}(k) = p_{ij}f_{ij}(k). (2)$$

Clearly, a semi-Markov chain is uniquely determined a.s. by an initial distribution  $(\mu_i)_{i\in E}$  and a semi-Markov kernel  $(q_{ij}(k))_{i,j\in E,k\in\mathbb{N}}$  or, equivalently, by an initial distribution  $(\mu_i)_{i\in E}$ , a Markov transition matrix  $(p_{ij})_{i,j\in E}$  and conditional sojourn time distributions  $(f_{ij}(k))_{i,j\in E,k\in\mathbb{N}}$ .

Other assumptions we make are: (i) We do not allow transitions to the same state, i.e.,  $p_{ii}=0$  for all  $i \in E$ , or equivalently  $q_{ii}(k)=0$ , for all  $i \in E$ ,  $k \in \mathbb{N}$ ; (ii) We assume that there are not instantaneous transitions, that is  $q_{ij}(0) \equiv 0$  or equivalently  $f_{ij}(0) \equiv 0$  for all  $i, j \in E$ ; note that this implies that T is a strictly increasing sequence.

For the conditional sojourn time distributions, one can consider the associated cumulative distribution function defined by

$$F_{ij}(k) := \mathbb{P}(T_{m+1} - T_m \le k | J_m = i, J_{m+1} = j) = \sum_{k=1}^{k} f_{ij}(t).$$

For any distribution function  $F(\cdot)$  we can consider the associated survival/reliability function defined by

$$\overline{F}(k) := 1 - F(t).$$

Consequently we have

$$\overline{F}_{ij}(k) := \mathbb{P}(T_{m+1} - T_m > k | J_m = i, J_{m+1} = j) = 1 - \sum_{t=1}^{k} f_{ij}(t) = \sum_{t=k+1}^{\infty} f_{ij}(t).$$

#### Particular cases: sojourn times of the type $f_{i.}(.)$ , $f_{.j}(.)$ and f(.)

We have considered up to here general semi-Markov models with the semi-Markov kernel of the type given in (2). Particular types of this semi-Markov model can be taken into account, by considering particular cases of holding time distributions  $f_{ij}(k)$ , where these distributions depend only on the current state i, or only on the next state j, or neither on i nor on j. For each case, let us define the semi-Markov kernel and the distribution function associated to the sojourn time distribution.

• Sojourn times depending only on the current state:

$$q_{ij}(k) := p_{ij} f_{i\bullet}(k), \text{ where}$$

$$f_{i\bullet}(k) = \mathbb{P}(T_{m+1} - T_m = k | J_m = i) = \sum_{v \in E} p_{iv} f_{iv}(k),$$

$$F_{i\bullet}(k) := \mathbb{P}(T_{m+1} - T_m \le k | J_m = i) = \sum_{t=1}^k f_{i\bullet}(t) = \sum_{t=1}^k \sum_{v \in E} p_{iv} f_{iv}(t).$$
(3)

• Sojourn times depending only on the next state:

$$q_{ij}(k) := p_{ij} f_{\bullet j}(k), \text{ where}$$

$$f_{\bullet j}(k) = \mathbb{P}(T_{m+1} - T_m = k | J_{m+1} = j),$$

$$F_{\bullet j}(k) := \mathbb{P}(T_{m+1} - T_m \le k | J_{m+1} = j) = \sum_{t=1}^{k} f_{\bullet j}(t).$$
(4)

• Sojourn times depending neither on the current state nor on the next state:

$$q_{ij}(k) := p_{ij}f(k), \text{ where}$$

$$f(k) = \mathbb{P}(T_{m+1} - T_m = k).$$

$$F(k) := \mathbb{P}(T_{m+1} - T_m \le k) = \sum_{t=1}^{k} f(t).$$
(5)

We also denote the associated survival/reliability functions respectively by  $\overline{F}_{i\bullet}(k)$ ,  $\overline{F}_{\bullet i}(k)$ ,  $\overline{F}(k)$ .

#### The SMM package

The **SMM** R package is mainly devoted to the simulation and estimation of discrete-time semi-Markov models in different cases by the two following functions:

- simulSM() for the simulation of sequences from a semi-Markov model:
  - One or several trajectories
  - According to classical distributions for the sojourn times (Uniform, Geometric, Poisson, Discrete Weibull and Negative Binomial) or according to distributions given by the user
  - Four different types of censoring mechanisms: censoring at the beginning of sample paths, censoring at the end, censoring at the beginning and at the end, no censoring
  - Four different types of sojourn times: depending on the current state and on the next state, depending only on the current state, depending only on the next state, depending neither on the current state nor on the next state
- estimSM() for the estimation of model parameters:
  - One or several trajectories
  - Parametric (Uniform, Geometric, Poisson, Discrete Weibull and Negative Binomial) or non-parametric distributions for the sojourn times
  - Four different types of censoring mechanisms: censoring at the beginning of sample paths, censoring at the end, censoring at the beginning and at the end, no censoring

 Four different types of sojourn times: depending on the current state and on the next state, depending only on the current state, depending only on the next state, depending neither on the current state nor on the next state

As the Negative Binomial distribution and the Discrete Weibull distribution can have several different parameterizations, note that we have considered the following ones in our package:

- Discrete Weibull of type I with the density  $f(x) = q^{(x-1)^{\beta}} q^{x^{\beta}}$  for x = 1, 2, ..., n with n > 0, q is the first parameter, 0 < q < 1, and  $\beta$  is the second parameter,  $\beta > 0$ ;
- Negative Binomial with the density  $f(x) = \frac{\Gamma(x+\alpha)}{\Gamma(\alpha)x!} \left(\frac{\alpha}{\alpha+\mu}\right)^{\alpha} \left(\frac{\mu}{\alpha+\mu}\right)^{x}$  for  $x=0,1,\ldots,n$  with n>0,  $\Gamma$  is the Gamma function,  $\alpha$  is the parameter of overdispersion,  $\alpha>0$ , and  $\mu$  is the mean,  $\mu\in\mathbb{R}$ .

In order to avoid any confusion, note also that the expressions of the different densities considered in this package are also provided in the corresponding manual.

The **SMM** R package is also devoted to the simulation and estimation of discrete-time Markov models by the two following functions:

- simulMk() for the simulation of sequences from a *k*th order Markov model;
- estimMk() for the estimation of the parameters of the model.

All the different possibilities of the package are illustrated in Figure 1.

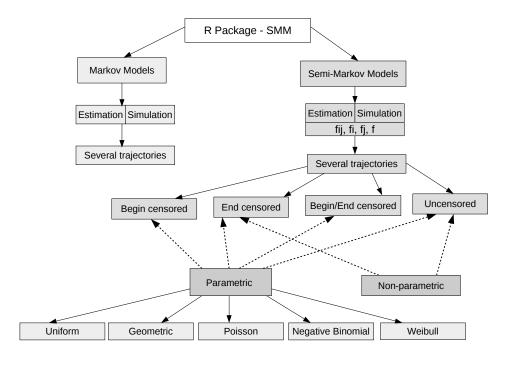


Figure 1: Schema of the SMM package.

#### Simulation of semi-Markov models

#### Parametric simulation: according to classical distributions

In this part, we will consider the simulation according to classical distributions.

**Parameters:** This simulation is carried out by the function simulSM(). The different parameters of the function are:

- E: Vector of state space of length *S*
- NbSeq: Number of simulated sequences

- lengthSeq: Vector containing the lengths of each simulated sequence
- TypeSojournTime: Type of sojourn time; it can be "fij", "fi", "fj" or "f" according to the four cases previously discussed
- init: Vector of initial distribution of length S
- Ptrans: Matrix of transition probabilities of the embedded Markov chain  $J = (J_m)_m$  of size  $S \times S$
- distr: Sojourn time distributions:
  - is a matrix of distributions of size  $S \times S$  if TypeSojournTime is equal to "fij",
  - is a vector of distributions of size *S* if TypeSojournTime is equal to "fi" or "fj",
  - is a distribution if TypeSojournTime is equal to "f",

where the distributions to be used can be one of "uniform", "geom", "pois", "weibull" or "nbinom".

- param: Parameters of sojourn time distributions:
  - is an array of parameters of size  $S \times S \times 2$  if TypeSojournTime is equal to "fij"
  - is a matrix of parameters of size  $S \times 2$  if TypeSojournTime is equal to "fi" or "fj"
  - is a vector of parameters if TypeSojournTime is equal to "f"
- cens.beg: Type of censoring at the beginning of sample paths; 1 (if the first sojourn time is censored) or 0 (if not). All the sequences must be censored in the same way.
- cens. end: Type of censoring at the end of sample paths; 1 (if the last sojourn time is censored) or 0 (if not). All the sequences must be censored in the same way.
- File.out: Name of fasta file for saving the sequences; if File.out = NULL, no file is created. A fasta file is a simple text file containing sequences only described by one description line beginning by a ">": an example is given in Figure 2.

Figure 2: Example of a fasta file.

The R commands below generate three sequences of size 1000, 10000 and 2000 respectively with the finite state space  $E = \{a, c, g, t\}$ , where the sojourn times depend on the current state and on the next state.

```
## state space
E = c("a","c","g","t")
S = length(E)
## sequence sizes
lengthSeq3 = c(1000, 10000, 2000)
## creation of the initial distribution
vect.init = c(1/4, 1/4, 1/4, 1/4)
## creation of transition matrix
Pij = matrix(c(0,0.2,0.3,0.4,0.2,0,0.5,0.2,0.5,0.3,0,0.4,0.3,0.5,0.2,0)),
             ncol=4)
## creation of the distribution matrix
distr.matrix = matrix(c("dweibull", "pois", "geom", "nbinom",
                         "geom", "nbinom", "pois", "dweibull",
                         "pois", "pois", "dweibull", "geom",
                         "pois", "geom", "geom", "nbinom"),
                      nrow = S, ncol = S, byrow = TRUE)
## creation of an array containing the parameters
param1.matrix = matrix(c(0.6, 2, 0.4, 4, 0.7, 2, 5, 0.6,
                                                   2,3,0.6,0.6,4,0.3,0.4,4),
                                           nrow = S, ncol = S, byrow = TRUE)
param2.matrix = matrix(c(0.8,0,0,2,0,5,0,0.8,
                         0,0,0.8,0,4,0,0,4),
```

First, note that in this simulation, the parameters cens.beg and cens.end are equal to 0, that is to say the simulated sequences are not censored.

Second, note also that the parameters of the distributions are given in the following way: for example,  $f_{13}(\cdot)$  is Geometric distribution with parameter 0.4, while  $f_{14}(\cdot)$  is Negative Binomial with parameters 4 and 2. In other words, the parameters of  $f_{13}(\cdot)$  are given in the vector param. array[1,3,] that is equal to (0.4, 0) and the parameters of  $f_{14}(\cdot)$  are given in the vector param. array[1,4,] that is equal to (4, 2); that means that if a distribution has only 1 parameter, the corresponding vector of parameters will have 0 on the second position.

**Values:** The function simulSM() returns a list of simulated sequences. These sequences can be saved in a fasta file by using the parameter File.out.

```
seq3[[1]][1:15]
[1] "g" "g" "g" "g" "c" "c" "c" "a" "a" "a" "c" "c" "c" "g" "g"
```

#### Non-parametric simulation: according to distributions given by the user

Now we will consider the simulation according to distributions given by the user.

**Parameters:** This simulation is carried out by the function simulSM(). The different parameters of the function are:

- E: Vector of state space of length S
- NbSeq: Number of simulated sequences
- lengthSeq: Vector containing the lengths of each simulated sequence
- TypeSojournTime: Type of sojourn time; it can be "fij", "fi", "fj" or "f" according to the four cases previously discussed
- init: Vector of initial distribution of length *S*
- Ptrans: Matrix of transition probabilities of the embedded Markov chain  $J = (J_m)_m$  of size  $S \times S$
- laws: Sojourn time distributions introduced by the user:
  - is an array of size  $S \times S \times Kmax$  if TypeSojournTime is equal to "fij",
  - is a matrix of size  $S \times Kmax$  if TypeSojournTime is equal to "fi" or "fj",
  - is a vector of length *Kmax* if TypeSojournTime is equal to "f",

where *Kmax* is the maximum length for the sojourn times.

- cens.beg: Type of censoring at the beginning of sample paths; 1 (if the first sojourn time is censored) or 0 (if not). All the sequences must be censored in the same way.
- cens. end: Type of censoring at the end of sample paths; 1 (if the last sojourn time is censored) or 0 (if not). All the sequences must be censored in the same way.
- File.out: Name of fasta file for saving the sequences; if File.out = NULL, no file is created.

The R commands below generate three sequences of size 1000, 10000 and 2000 respectively with the finite state space  $E = \{a, c, g, t\}$ , where the sojourn times depend only on the next state.

```
## state space
E = c("a","c","g","t")
S = length(E)
## sequence sizes
lengthSeq3 = c(1000, 10000, 2000)
```

```
## creation of the initial distribution
vect.init = c(1/4, 1/4, 1/4, 1/4)
## creation of transition matrix
Pij = matrix(c(0,0.2,0.3,0.4,0.2,0,0.5,0.2,0.5,0.3,0,0.4,0.3,0.5,0.2,0),
             ncol=4)
## creation of a matrix corresponding to the conditional
## sojourn time distributions
nparam.matrix = matrix(c(0.2,0.1,0.3,0.2,0.2,0.0.4,0.2,0.1,
                                                  0,0.2,0.1,0.5,0.3,0.15,0.05,0,0,
                                                  0.3, 0.2, 0.1, 0.2, 0.2, 0),
                       nrow = S, ncol = Kmax, byrow = TRUE)
## for the reproducibility of the results
set.seed(2)
## simulation of 3 sequences with censoring at the beginning
seqNP3_begin = simulSM(E = E, NbSeq = 3, lengthSeq = lengthSeq3,
TypeSojournTime = "fj", init = vect.init, Ptrans = Pij,
                                 laws = nparam.matrix, File.out = "seqNP3_begin.txt",
                                 cens.beg = 1, cens.end = 0)
## simulation of 3 sequences with censoring at the end
seqNP3_end = simulSM(E = E, NbSeq = 3, lengthSeq = lengthSeq3,
                                 TypeSojournTime = "fj", init = vect.init, Ptrans = Pij,
                                 laws = nparam.matrix, File.out = "seqNP3_end.txt",
                                 cens.beg = 0, cens.end = 1)
## simulation of 3 sequences censored at the beginning and at the end
seqNP3_begin_end = simulSM(E = E, NbSeq = 3, lengthSeq = lengthSeq3,
                                 TypeSojournTime = "fj", init = vect.init, Ptrans = Pij,
                                 laws = nparam.matrix, File.out = "seqNP3_begin_end.txt",
                                 cens.beg = 1, cens.end = 1)
## simulation of 3 sequences without censoring
seqNP3_no = simulSM(E = E, NbSeq = 3, lengthSeq = lengthSeq3,
                                 TypeSojournTime = "fj", init = vect.init, Ptrans = Pij,
                                 laws = nparam.matrix, File.out = "seqNP3_no.txt")
## for the reproducibility of the results
seqNP3_begin = read.fasta("seqNP3_begin.txt")
seqNP3_end = read.fasta("seqNP3_end.txt")
seqNP3_begin_end = read.fasta("seqNP3_begin_end.txt")
seqNP3_no = read.fasta("seqNP3_no.txt")
seqNP3_begin[[1]][1:15]
```

Note that in this simulation all the different censoring mechanisms are considered.

**Values:** The function simulSM() returns a list of simulated sequences. These sequences can be saved in a fasta file by using the parameter File.out.

#### Estimation of semi-Markov models

In this subsection we explain and illustrate the estimation of a semi-Markov model in the parametric and non-parametric cases.

#### Parametric estimation of semi-Markov models

We will consider the distributions  $f_{ij}(k) = f_{ij}(k;\theta_{ij})$  depending on unknown parameters  $\theta_{ij} \in \mathbb{R}^{m_{ij}}$ , where the dimension of parameters set  $m_{ij}$  is known; no assumptions are made on  $\left(p_{ij}\right)_{ij}$ . From the data, we want to estimate  $p_{ij}$  and  $\theta_{ij}$ ,  $i,j \in E$ . Let us assume that we have at our disposal several independent sample paths of a semi-Markov chain, say L, each of them of length  $n_l$ ,  $l=1,\ldots,L$ , censored at the beginning and at the end of the trajectory, i.e.,

$$y_1^l, y_2^l, \ldots, y_{n_l}^l,$$

or, equivalently,

$$j_0^l, k_0^l, j_1^l, k_1^l, j_2^l, k_2^l, \cdots, j_{t^l}^l, k_{t^l}^l, j_{t^l+1}^l, k_{t^l+1}^l$$

with  $\sum_{i=0}^{l^l+1} k_i^l = n_l$ , where  $j_0^l, \ldots, j_{l^l+1}^l$  are the successive distinct visited states,  $k_0^l$  is the first sojourn time, assumed to be right censored,  $k_{l^l+1}^l$  is the last sojourn time, assumed also to be right censored, while  $k_1^l, \ldots, k_{l^l}^l$  are the other successive sojourn times, assumed to be complete (observed, non censored).

To estimate the parameters of model, we use the maximum likelihood estimation:

$$\underset{p_{uv},\theta_{uv};u,v\in E}{\operatorname{argmax}} \left( l(p_{uv},\theta_{uv};u,v\in E) \right) \\
= \left( \underset{p_{uv},\theta_{uv};v\in E}{\operatorname{argmax}} \left( \sum_{v\in E} N_{uv}(L,n_{1:L}) \log(p_{uv}) + \sum_{v\in E} \sum_{k=1}^{\max_{l}(n_{l})} N_{uv}(k;L,n_{1:L}) \log(f_{uv}(k;\theta_{uv})) \right) \\
+ \sum_{v\in E} \sum_{k=1}^{\max_{l}(n_{l})} \overline{N}_{uv}^{b}(k;L) \log(\overline{F}_{uv}(k;\theta_{uv})) \\
+ \sum_{k=1}^{\max_{l}(n_{l})} \overline{N}_{u\bullet}^{b}(k;L) \log\left(1 - \sum_{m=1}^{k} \sum_{v\in E} p_{uv} f_{uv}(m;\theta_{uv})\right) \right)_{u\in E} , \tag{6}$$

where we introduced the following counting processes

$$\begin{split} N_{ij}(L,n_{1:L}) &= \sum_{l=1}^{L} \sum_{m=1}^{N^{l}(n_{l})-1} \mathbb{1}_{\left\{J_{m}^{l}=i;J_{m+1}^{l}=j\right\}}, \\ N_{ij}(k;L,n_{1:L}) &= \sum_{m=1}^{N^{l}(n_{l})-1} \mathbb{1}_{\left\{J_{m}^{l}=i;J_{m+1}^{l}=j;T_{m+1}^{l}-T_{m}^{l}=k\right\}}, \\ \overline{N}_{ij}^{b}(k;L) &= \sum_{l=1}^{L} \mathbb{1}_{\left\{J_{0}^{l}=i;J_{1}^{l}=j;T_{1}^{l}-T_{0}^{l}>k\right\}}, \\ \overline{N}_{i\bullet}^{e}(k;L) &= \sum_{l=1}^{L} \mathbb{1}_{\left\{J_{N^{l}(n_{l})}^{l}=i,X_{N^{l}(n_{l})+1}^{l}>k\right\}}, \end{split}$$

where

$$N^l(n_l) = \max\{m \in \mathbb{N} \mid T_m^l \le n_l\}$$

is the counting process of jump number in  $[1; n_l]$  of the trajectory l.

Note that:

- $N_{ij}(L, n_{1:L})$  represents the number of transitions from state i to state j along the L sample paths;
- $N_{ij}(k; L, n_{1:L})$  represents the number of transitions from state i to state j along the L sample paths, with sojourn time of length k in state i;
- $\overline{N}_{ij}^b(k;L)$  represents the number of trajectories starting in state i, with a next transition to state j and censored sojourn time in state i greater than k;
- $-\overline{N}_{i\bullet}^{e}(k;L)$  represents the number of trajectories ending in state i with a censored sojourn time in state i greater than k.

Note also that in the expression (6) of the log-likelihood, the first two terms correspond to the transition probabilities and the observed (non censored) sojourn times, the third term is the contribution to the likelihood of the first sojourn times, assumed to be right censored, while the last term is the contribution to the likelihood of the last sojourn times, assumed to be right censored.

Up to here we presented the estimation for the general case, taking into account the censoring at the beginning and at the end and the sojourn times depending on the current state and on the next state. Thus the maximization problem (6) is written with the sojourn times depending on the current state and on the next state (the general model of the type  $q_{ij}(k) = p_{ij}f_{ij}(k)$  given in (2)), but the

different cases of sojourn times are written and coded in the package. Note also that different types of censoring are also written and coded in the package.

**Parameters:** The estimation is carried out by the function estimSM(). The different parameters of the function are:

- · file: Path of the fasta file which contains the sequences from which to estimate
- seq: List of the sequence(s) from which to estimate
- E: Vector of state space of length *S*
- TypeSojournTime: Type of sojourn time; it can be "fij", "fi", "fj" or "f" according to the four cases previously discussed
- distr: Sojourn time distributions:
  - is a matrix of distributions of size  $S \times S$  if TypeSojournTime is equal to "fij",
  - is a vector of distributions of size *S* if TypeSojournTime is equal to "fi" or "fj",
  - is a distribution if TypeSojournTime is equal to "f",

where the distributions to be used can be one of "uniform", "geom", "pois", "weibull" or "nbinom".

- cens.beg: Type of censoring at the beginning of sample paths; 1 (if the first sojourn time is censored) or 0 (if not). All the sequences must be censored in the same way.
- cens. end: Type of censoring at the end of sample paths; 1 (if the last sojourn time is censored) or 0 (if not). All the sequences must be censored in the same way.

Note that the sequences from which we estimate can be given either as an R list (seq argument) or as a file in fasta format (file argument).

Here, we estimate simulated sequences with no censoring. The estimation performed will correspond to the likelihood given in (6), without the third and forth terms.

**Values:** The function estimSM() returns a list containing:

• init: Vector of size *S* with estimated initial probabilities of the semi-Markov chain

```
estSeq3$init
[1] 0.0000000 0.0000000 0.3333333 0.6666667
```

 Ptrans: Matrix of size S × S with estimated transition probabilities of the embedded Markov chain J = (J<sub>m</sub>)<sub>m</sub>

• param: Array with estimated parameters of the sojourn time distributions

```
estSeq3$param
, , 1
         [,1]
                   [,2] [,3]
[1,] 0.0000000 1.7867299 0.411398 4.1358797
[2,] 0.6920415 0.0000000 4.745387 0.6131806
[3,] 2.0123457 3.0722433 0.000000 0.5729614
[4,] 3.8088235 0.3068702 0.392237 0.0000000
, , 2
     [,1] [,2] [,3]
                 0 2.1043710
[1,]
           0
                 0 0.8425902
            0
[2,]
                 0 0.0000000
            0
[3,]
       0
                 0 0.0000000
[4,]
```

Note that, for example, estSeq3param[1,3,] is the vector containing the parameters of the distribution  $f_{13}(\cdot)$ .

• q: Array of size  $S \times S \times Kmax$  with estimated semi-Markov kernel

```
estSeq3$q[,,1:3]
, , 1
                     [,2]
           [,1]
[1,] 0.00000000 0.03792273 0.20393336 0.05070777
[2,] 0.14771431 0.00000000 0.00251382 0.19237763
[3,] 0.03877405 0.02181093 0.00000000 0.13695675
[4,] 0.00911087 0.06211573 0.15168076 0.00000000
, , 2
           [,1]
                     [,2]
                               [,3]
[1,] 0.00000000 0.06775768 0.12003558 0.07072333
[2,] 0.04548987 0.00000000 0.01192905 0.09806611
[3,] 0.07802680 0.06700849 0.00000000 0.05848582
[4,] 0.03470170 0.04305426 0.09218596 0.00000000
, , 3
           [,1]
                     [,2]
                               [,3]
[1,] 0.00000000 0.06053233 0.07065318 0.06124460
[2,] 0.01400899 0.00000000 0.02830398 0.06214172
[3,] 0.07850845 0.10293320 0.00000000 0.02497570
[4,] 0.06608632 0.02984219 0.05602722 0.00000000
```

Note that, for example,  $q_{13}(2) = \mathbb{P}(J_{m+1} = 3, T_{m+1} - T_m = 2 | J_m = 1) = 0.12192187.$ 

#### Non-parametric estimation of semi-Markov models

Here we will consider two types of estimation for semi-Markov chains: a direct estimation, obtaining thus empirical estimators (in fact, approached MLEs), cf. Barbu and Limnios (2006), Barbu and Limnios (2008) and an estimation based on a couple Markov chain associated to the semi-Markov chain (see Trevezas and Limnios, 2011).

#### No censoring: direct estimation

Let  $\{Y_1, Y_2, \dots, Y_n\}$  be a trajectory of a semi-Markov chain  $Y = (Y_n)_{n \in \mathbb{N}}$ , censored at an arbitrary fixed time n.

• The case  $q_{ij}(k) = p_{ij}f_{ij}(k)$ : The maximum likelihood estimators are

$$\widehat{p_{ij}}(n) = \frac{N_{ij}(n)}{N_{i\bullet}(n)}, \quad \widehat{f_{ij}}(k;n) = \frac{N_{ij}(k;n)}{N_{ii}(n)}, \quad \widehat{q_{ij}}(k;n) = \frac{N_{ij}(k;n)}{N_{i\bullet}(n)}.$$

where 
$$N_{ij}(n) = \sum_{m=1}^{N(n)-1} \mathbb{1}_{\{J_m=i;J_{m+1}=j\}}, N_{i\bullet}(n) = \sum_{m=1}^{N(n)-1} \mathbb{1}_{\{J_m=i\}}, N_{ij}(k;n) = \sum_{m=1}^{N(n)-1} \mathbb{1}_{\{J_m=i;J_{m+1}=j;T_{m+1}-T_m=k\}}.$$

• The case  $q_{ii}(k) = p_{ii}f_{i\bullet}(k)$ : The maximum likelihood estimators are

$$\widehat{p_{ij}}(n) = \frac{N_{ij}(n)}{N_{i\bullet}(n)}, \quad \widehat{f_{i\bullet}}(k;n) = \frac{N_{i\bullet}(k;n)}{N_{ij}(n)}, \quad \widehat{q_{ij}}(k;n) = \frac{N_{i\bullet}(k;n)}{N_{i\bullet}(n)},$$

where 
$$N_{i\bullet}(k;n) = \sum_{m=1}^{N(n)-1} \mathbb{1}_{\{J_m=i;T_{m+1}-T_m=k\}}$$
.

• The case  $q_{ij}(k) = p_{ij} f_{\bullet j}(k)$ : The maximum likelihood estimators are

$$\widehat{p_{ij}}(n) = \frac{N_{ij}(n)}{N_{i\bullet}(n)}, \quad \widehat{f_{\bullet j}}(k;n) = \frac{N_{\bullet j}(k;n)}{N_{ii}(n)}, \quad \widehat{q_{ij}}(k;n) = \frac{N_{\bullet j}(k;n)}{N_{i\bullet}(n)},$$

where 
$$N_{\bullet j}(k;n) = \sum_{m=1}^{N(n)-1} \mathbb{1}_{\{J_{m+1}=j;T_{m+1}-T_m=k\}}$$
.

• The case  $q_{ij}(k) = p_{ij}f(k)$ : The maximum likelihood estimators are

$$\widehat{p_{ij}}(n) = \frac{N_{ij}(n)}{N_{i\bullet}(n)}, \quad \widehat{f}(k;n) = \frac{N(k;n)}{N_{ij}(n)}, \quad \widehat{q_{ij}}(k;n) = \frac{N(k;n)}{N_{i\bullet}(n)},$$

where 
$$N(k; n) = \sum_{m=1}^{N(n)-1} \mathbb{1}_{\{T_{m+1} - T_m = k\}}$$
.

**Censoring: couple Markov chain** For a semi-Markov chain  $Y = (Y_n)_{n \in \mathbb{N}}$ , let  $U = (U_n)_{n \in \mathbb{N}}$  be the backward recurrence time of the SMC, defined by

$$U_n := n - T_{N(n)}. \tag{7}$$

We can show (cf. Limnios and Oprisan, 2001) that the chain  $(Y, U) = (Y_n, U_n)_{n \in \mathbb{N}}$  is a Markov chain with state space  $E \times \mathbb{N}$ . We will denote its transition matrix by  $\widetilde{\mathbf{p}} := (p_{(i,t_1)(j,t_2)})_{i,j \in E,t_1,t_2 \in \mathbb{N}}$ .

The maximum likelihood estimators of  $q_{ij}(k)$  (Trevezas and Limnios, 2011) are given by

$$\widehat{q_{ij}}(k;n) = \widehat{p}_{(i,k-1)(j,0)}(n) \prod_{t=0}^{k-2} \widehat{p}_{(i,t)(i,t+1)}(n), \tag{8}$$

where  $\hat{p}_{(i,t_1)(j,t_2)}(n)$  represents the classical MLE of the transition probability  $p_{(i,t_1)(j,t_2)}$ . Thus we obtain the corresponding estimator of  $p_{ij}$ 

$$\widehat{p}_{ij} = \sum_{k=0}^{\infty} \widehat{q}_{ij}(k). \tag{9}$$

In order to compute the estimators of the sojourn times, we consider the four different types of semi-Markov kernels defined in Equations (2), (3), (4) and (5).

**Parameters:** The estimation is carried out by the function estimSM() and several parameters must be given.

- file: Path of the fasta file which contains the sequences from which to estimate
- seq: List of the sequence(s) from which to estimate
- E: Vector of state space of length *S*
- TypeSojournTime: Type of sojourn time; always equal to "NP" for the non-parametric estimation
- cens.beg: Type of censoring at the beginning of sample paths; 1 (if the first sojourn time is censored) or 0 (if not). All the sequences must be censored in the same way.
- cens. end: Type of censoring at the end of sample paths; 1 (if the last sojourn time is censored) or 0 (if not). All the sequences must be censored in the same way.

Note that the sequences from which we estimate can be given either as an R list (seq argument) or as a file in fasta format (file argument). The parameter distr is always equal to "NP".

```
## data
seqNP3_no = read.fasta("seqNP3_no.txt")
```

```
E = c("a","c","g","t")
## estimation of simulated sequences
estSeqNP3= estimSM(seq = seqNP3_no, E = E, TypeSojournTime = "fj",
                    distr = "NP", cens.end = 0, cens.beg = 0)
```

Here, we estimate simulated sequences with no censoring.

**Values:** The function estimSM() returns a list containing:

- init: Vector of size *S* with estimated initial probabilities of the semi-Markov chain estSeqNP3\$init [1] 0.0000000 0.6666667 0.3333333 0.0000000
- Ptrans: Matrix of size  $S \times S$  with estimated transition probabilities of the embedded Markov chain  $J = (J_m)_m$

```
estSeqNP3$Ptrans
          [,1]
                    [,2]
                              [,3]
[1,] 0.0000000 0.2051948 0.5090909 0.2857143
[2,] 0.1938179 0.0000000 0.3107769 0.4954052
[3,] 0.3010169 0.4874576 0.0000000 0.2115254
[4,] 0.3881686 0.1936791 0.4181524 0.0000000
```

• laws: Array of size  $S \times S \times Kmax$  with estimated values of the sojourn time distributions

[,4]

```
, , 1
          [,1]
                    [,2]
                               [,3]
[1,] 0.0000000 0.3941423 0.4728997 0.2939271
```

estSeqNP3\$laws[,,1:2]

[2,] 0.1896104 0.0000000 0.4728997 0.2939271 [3,] 0.1896104 0.3941423 0.0000000 0.2939271 [4,] 0.1896104 0.3941423 0.4728997 0.0000000

, , 2

```
[,4]
          [,1]
                    [,2]
                              [,3]
[1,] 0.0000000 0.1949791 0.3089431 0.1959514
[2,] 0.1073593 0.0000000 0.3089431 0.1959514
[3,] 0.1073593 0.1949791 0.0000000 0.1959514
[4,] 0.1073593 0.1949791 0.3089431 0.0000000
```

• q: Array of size  $S \times S \times Kmax$  with estimated semi-Markov kernel

```
estSeqNP3$q[,,1:3]
, , 1
```

```
[,1]
                      [,2]
                                [,3]
                                           [,4]
[1,] 0.00000000 0.07792208 0.2562771 0.06753247
[2,] 0.03508772 0.00000000 0.1378446 0.15956558
[3,] 0.05559322 0.18576271 0.0000000 0.06372881
[4,] 0.07698541 0.08670989 0.1920583 0.00000000
```

, , 2

```
[,2]
           [,1]
                                [,3]
[1,] 0.00000000 0.04329004 0.1411255 0.05627706
[2,] 0.01670844 0.00000000 0.1019215 0.10025063
[3,] 0.03796610 0.09762712 0.0000000 0.03864407
[4,] 0.03889789 0.03160454 0.1385737 0.00000000
, , 3
```

```
[,1]
                                            [,4]
                      [,2]
                                 [,3]
[1,] 0.00000000 0.02770563 0.07965368 0.04069264
[2,] 0.07101086 0.00000000 0.05179616 0.03926483
[3,] 0.09152542 0.05423729 0.00000000 0.02440678
[4,] 0.10940032 0.01782820 0.05591572 0.00000000
```

#### Supplementary functions

In this package, others functions are available. These functions enable to compute the initial distribution for a semi-Markov model, the log-likelihood of a semi-Markov model and the AIC and BIC of a semi-Markov model.

■ InitialLawSM(): Estimation of initial distribution for a semi-Markov model

#### Parameters:

• q: Array of size  $S \times S \times Kmax$  with estimated semi-Markov kernel

Values: The function InitialLawSM() returns a list containing a vector of the initial distribution.

■ LoglikelihoodSM (): Computation of the log-likelihood

#### Parameters:

- E: Vector of state space of length *S*
- seq: List of the sequence(s) from which to estimate
- mu: Vector of initial distribution of length S
- Ptrans: Matrix of transition probabilities of the embedded Markov chain  $J = (J_m)_m$  of size  $S \times S$
- TypeSojournTime: Type of sojourn time; it can be "fij", "fi", "fj" or "f" according to the four cases previously discussed
- distr: Sojourn time distributions:
  - is a matrix of distributions of size  $S \times S$  if TypeSojournTime is equal to "fij",
  - is a vector of distributions of size *S* if TypeSojournTime is equal to "fi" or "fj",
  - is a distribution if TypeSojournTime is equal to "f",

where the distributions to be used can be one of "uniform", "geom", "pois", "weibull" or "nbinom".

- param: Parameters of sojourn time distributions:
  - is an array of parameters of size  $S \times S \times 2$  if TypeSojournTime is equal to "fij"
  - is a matrix of parameters of size  $S \times 2$  if TypeSojournTime is equal to "fi" or "fj"
  - is a vector of parameters if TypeSojournTime is equal to "f"
- laws: Sojourn time distributions introduced by the user:
  - is an array of size  $S \times S \times Kmax$  if TypeSojournTime is equal to "fij",
  - is a matrix of size  $S \times Kmax$  if TypeSojournTime is equal to "fi" or "fj",
  - is a vector of length *Kmax* if TypeSojournTime is equal to "f",

where *Kmax* is the maximum length for the sojourn times.

```
## state space
E = c("a","c","g","t")
S = length(E)
## creation of transition matrix
Pij = matrix(c(0,0.2,0.3,0.4,0.2,0,0.5,0.2,0.5,0.3,0,0.4,0.3,0.5,0.2,0), ncol=4)
## for the reproducibility of the results
set.seed(3)
## simulation
seq5000 = simulSM(E = E, NbSeq = 1, lengthSeq = 5000,
                                  TypeSojournTime = "f", init = c(1/4, 1/4, 1/4, 1/4),
                                   Ptrans = Pij, distr = "pois", param = 2, File.out =
                                         "seq5000.txt")
## computation of the log-likelihood
LoglikelihoodSM(seq = seq5000, E = E, mu = rep(1/4,4),
                                  Ptrans = Pij, distr = "pois", param = 2,
                                   TypeSojournTime = "f")
$L
$L[[1]]
[1] -1748.431
$Kmax
[1] 10
```

Values: The function likelihoodSM() returns a list containing:

- L: List with the value of the likelihood for each sequence
- Kmax: Maximal sojourn time

We also consider model selection criteria in order to evaluate and choose among candidate models; the Akaike information criterion (AIC) and the Bayesian information criterion (BIC) are considered.

■ AIC\_SM(): computation of the AIC

$$AIC(M) = -2\log \mathcal{L} + 2M,$$

where  $\mathcal{L}$  is the log-likelihood, M is the number of parameters involved in the model

#### Parameters:

- E: Vector of state space of length *S*
- seq: List of the sequence(s) from which to estimate
- mu: Vector of initial distribution of length S
- Ptrans: Matrix of transition probabilities of the embedded Markov chain  $J=(J_m)_m$  of size  $S\times S$
- TypeSojournTime: Type of sojourn time; it can be "fij", "fi", "fj" or "f" according to the four cases previously discussed
- distr: Sojourn time distributions:
  - is a matrix of distributions of size  $S \times S$  if TypeSojournTime is equal to "fij",
  - is a vector of distributions of size S if TypeSojournTime is equal to "fi" or "fj",
  - is a distribution if TypeSojournTime is equal to "f",

where the distributions to be used can be one of "uniform", "geom", "pois", "weibull" or "nbinom".

- param: Parameters of sojourn time distributions:
  - is an array of parameters of size  $S \times S \times 2$  if TypeSojournTime is equal to "fij"
  - is a matrix of parameters of size  $S \times 2$  if TypeSojournTime is equal to "fi" or "fj"
  - is a vector of parameters if TypeSojournTime is equal to "f"
- laws: Sojourn time distributions introduced by the user:
  - is an array of size  $S \times S \times Kmax$  if TypeSojournTime is equal to "fij",
  - is a matrix of size  $S \times Kmax$  if TypeSojournTime is equal to "fi" or "fj",

– is a vector of length *Kmax* if TypeSojournTime is equal to "f", where *Kmax* is the maximum length for the sojourn times.

```
## state space
E = c("a","c","g","t")
S = length(E)
lengthSeq3 = c(1000, 10000, 2000)
## creation of the initial distribution
vect.init = c(1/4, 1/4, 1/4, 1/4)
## creation of transition matrix
Pij = matrix(c(0,0.2,0.3,0.4,0.2,0,0.5,0.2,0.5,0.3,0,0.4,0.3,0.5,0.2,0), ncol=4)
## creation of the distribution matrix
distr.matrix = matrix(c("dweibull", "pois", "geom", "nbinom",
                                                     "geom", "nbinom", "pois", "dweibull",
                                                     "pois", "pois", "dweibull", "geom",
"pois", "geom", "geom", "nbinom"),
                                                     nrow = S, ncol = S, byrow = TRUE)
## creation of an array containing the parameters
param1.matrix = matrix(c(0.6, 2, 0.4, 4, 0.7, 2, 5, 0.6, 2, 3, 0.6,
                                                      0.6,4,0.3,0.4,4), nrow = S,
                                                    ncol = S, byrow = TRUE)
param2.matrix = matrix(c(0.8,0,0,2,0,5,0,0.8,0,0,0.8,
                                                    0,4,0,0,4), nrow = S, ncol = S,
                                                   bvrow = TRUE)
param.array = array(c(param1.matrix, param2.matrix), c(S,S,2))
## for the reproducibility of the results
set.seed(4)
## simulation of 3 sequences
seq.crit = simulSM(E = E, NbSeq = 3, lengthSeq = lengthSeq3,
                                   TypeSojournTime = "fij", init = vect.init,
                                  Ptrans = Pij, distr = distr.matrix,
                                  param = param.array, File.out = "seq.crit.txt")
## computation of the AIC
AIC_SM(seq = seq.crit, E = E, mu = rep(1/4,4), Ptrans = Pij,
                 distr = distr.matrix, param = param.array,
                  TypeSojournTime = "fij")
[[1]]
[1] 1692.061
[[2]]
[1] 16826.28
[[3]]
[1] 3334.314
```

Values: The function AIC\_SM() returns a list with the value of AIC for each sequence.

■ BIC\_SM(): computation of the BIC

$$BIC(M) = -2\log \mathcal{L} + \log(n)M$$

where  $\mathcal{L}$  is the log-likelihood, M is the number of parameters involved in the model and n is the sample size.

#### Parameters:

- E: Vector of state space of length *S*
- seq: List of the sequence(s) from which to estimate
- mu: Vector of initial distribution of length S
- Ptrans: Matrix of transition probabilities of the embedded Markov chain  $J = (J_m)_m$  of size  $S \times S$
- TypeSojournTime: Type of sojourn time; it can be "fij", "fi", "fj" or "f" according to the four cases previously discussed

- distr: Sojourn time distributions:
  - is a matrix of distributions of size  $S \times S$  if TypeSojournTime is equal to "fij",
  - is a vector of distributions of size *S* if TypeSojournTime is equal to "fi" or "fj",
  - is a distribution if TypeSojournTime is equal to "f",

where the distributions to be used can be one of "uniform", "geom", "pois", "weibull" or "nbinom".

- param: Parameters of sojourn time distributions:
  - is an array of parameters of size  $S \times S \times 2$  if TypeSojournTime is equal to "fij"
  - is a matrix of parameters of size  $S \times 2$  if TypeSojournTime is equal to "fi" or "fj"
  - is a vector of parameters if TypeSojournTime is equal to "f"
- laws: Sojourn time distributions introduced by the user:
  - is an array of size  $S \times S \times Kmax$  if TypeSojournTime is equal to "fij",
  - is a matrix of size  $S \times Kmax$  if TypeSojournTime is equal to "fi" or "fj",
  - is a vector of length *Kmax* if TypeSojournTime is equal to "f",

where *Kmax* is the maximum length for the sojourn times.

Values: The function BIC\_SM() returns a list with the value of BIC for each sequence.

#### The Markov case

In the SMM R package, we have also implemented the estimation and the simulation of discrete-time multi-state Markov models. As in the semi-Markov case, other functions are available, enabling to estimate the initial distribution, to compute the log-likelihood and also the AIC and BIC of a Markov model.

 $\blacksquare$  simulMk(): Simulation of a Markov chain of order k

 $\blacksquare$  estimMk(): Estimation of a Markov chain of order k

```
## state space
E <- c("a","c","g","t")
## for the reproducibility of the results
seq.markov = read.fasta("seq.markov.txt")
## estimation of simulated sequences
res.markov = estimMk(seq = seq.markov, E = E, k = 2)</pre>
```

**Values:** The function estimMk() returns a list containing:

• init: Vector of initial probabilities of the Markov chain

```
res.markov$init
[1] 0.2513810 0.2491905 0.2519048 0.2475238
```

• Ptrans: Matrix of transition probabilities of the Markov chain

```
res.markov$Ptrans
```

```
[,3]
           [,1]
                     [,2]
 [1,] 0.2845283 0.2498113 0.2188679 0.2467925
 [2,] 0.2479645 0.2361214 0.2709104 0.2450037
 [3,] 0.2640625 0.2507813 0.2515625 0.2335937
 [4,] 0.2577475 0.2448980 0.2433862 0.2539683
 [5,] 0.2371988 0.2454819 0.2402108 0.2771084
 [6,] 0.2458629 0.2584712 0.2450749 0.2513790
 [7,] 0.2435897 0.2533937 0.2624434 0.2420814
 [8,] 0.2457887 0.2258806 0.2710567 0.2572741
 [9,] 0.2300296 0.2692308 0.2684911 0.2322485
[10,] 0.2767584 0.2194190 0.2484709 0.2553517
[11,] 0.2542248 0.2578986 0.2549596 0.2329170
[12,] 0.2377567 0.2535545 0.2440758 0.2646130
[13,] 0.2527473 0.2590267 0.2417582 0.2464678
[14,] 0.2448196 0.2578665 0.2509593 0.2463546
[15,] 0.2617602 0.2276176 0.2594841 0.2511381
[16,] 0.2390469 0.2790161 0.2559570 0.2259800
```

■ InitialLawMk(): Estimation of the initial distribution of a Markov chain of order k

```
seq = list(c("a","c","c","g","t","a","a","a","a","g","c","t","t","t","g"))
res = estimMk(seq = seq, E = c("a","c","g","t"), k = 1)
Warning message:
In estimMk(seq = seq, E = c("a", "c", "g", "t"), k = 1):
    missing transitions
p = res$Ptrans

InitialLawMk(E = c("a","c","g","t"), seq = seq, Ptrans = p, k = 1)
$init
[1] 0.2205882 0.2205882 0.2058824 0.3529412
```

■ LoglikelihoodMk(): Computation of the log-likelihood

#### Parameters:

- mu: Initial distribution
- Ptrans: Probability transition matrix
- k: Order of the Markov chain

```
## state space
E = c("a","c","g","t")
S = length(E)
## creation of transition matrix
p = matrix(rep(1/4,S*S),ncol=4)
## for the reproducibility of the results
set.seed(6)
## simulation of two sequences of length 20 and 50 respectively
seq.markov2 = simulMk(E = E, nbSeq = 2, lengthSeq = c(20,50),
```

**Values:** The function likelihoodSM() returns a list containing the value of the likelihood for each sequence.

 $\blacksquare$  AIC\_Mk(): Computation of the AIC for a Markov chain of order k

#### **Parameters:**

- mu: Initial distribution
- Ptrans: Probability transition matrix
- k: Order of the Markov chain

```
## for the reproducibility of the results
seq.markov2 = read.fasta("seq.markov2.txt")

## computation of the AIC
AIC_Mk(seq = seq.markov2, E = E, mu = rep(1/4,4), Ptrans = p, k = 1)
[[1]]
[1] 79.45177

[[2]]
[1] 162.6294
```

Values: The function AIC\_Mk() returns a list containing the value of the AIC for each sequence.

■ BIC\_Mk(): Computation of the BIC for a Markov chain of order k

#### Parameters:

- mu: Initial distribution
- Ptrans: Probability transition matrix
- k: Order of the Markov chain

```
## for the reproducibility of the results
seq.markov2 = read.fasta("seq.markov2.txt")

## computation of the AIC
BIC_Mk(seq = seq.markov2, E = E, mu = rep(1/4,4), Ptrans = p, k = 1)
[[1]
[1] 91.40056

[[2]]
[1] 185.5737
```

Values: The function BIC\_Mk() returns a list containing the value of the BIC for each sequence.

#### Concluding remarks

In this paper we have presented the **SMM**, an R package for the simulation and the estimation of discrete-time multi-state semi-Markov models. The conditional sojourn time can be modeled by an arbitrary distribution for a semi-Markov model, which enables a generalization with respect to Markov

models, where the sojourn time is only modelled by a Geometric distribution (in discrete time) or an Exponential distribution (in continuous time). The **SMM** package offers a variety of conditional sojourn time distributions (Poisson, Uniform, Negative Binomial, Geometric and Discrete Weibull). This package provides also non-parametric estimation and simulation and takes into account censored data of several types.

To summarize, the importance and interest of the R package  $\mathbf{SMM}$  that we have developed come from:

- considering versatile tools, namely discrete-time multi-state semi-Markov processes, that are of use in a variety of applied fields, like survival analysis, biology, reliability, DNA analysis, insurance and finance, earthquake modeling, meteorology studies, etc. An example of application can be the description of DNA sequences by using a 2-state process to distinguish between coding and non-coding regions in DNA sequences. It is well known that the length of such regions generally does not follow a Geometric distribution. Thus semi-Markov chains can represent adapted tools for this type of modeling.
  - implementing parametric and non-parametric estimation/simulation;
  - considering several censoring schemes, that important in various applications;
  - taking into account one or several independent sample paths;
- considering different types of semi-Markov kernels: either of the general type  $q_{ij}(k) = p_{ij}f_{ij}(k)$  with the holding time distributions  $f_{ij}(k)$  depending on the current state and on the next state to be visited, or with the holding time distributions depending only on the current state,  $q_{ij}(k) := p_{ij}f_{i\bullet}(k)$ , or with the holding time distributions depending only on the next state to be visited,  $q_{ij}(k) := p_{ij}f_{\bullet j}(k)$ , or with the holding time distributions depending neither on the current, nor on the future state,  $q_{ij}(k) := p_{ij}f(k)$ . As already mentioned, it is important that these four types of models be considered separately.

In conclusion, the R package **SMM** that we have developed deals with an important and versatile tool, useful for researchers, practitioners and engineers in various fields.

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