# 3D MODELLING OF MUSCLE MECHANICS USING FINITE ELEMENTS

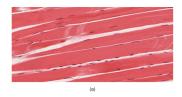
CUMC/CCÉM Saskatoon 2018

Megan Monkman  $^1$  Dr. Nilima Nigam  $^1$  Sebastian Dominguez  $^1$  Dr. Emma Hodson-Tole  $^2$  July 15, 2018

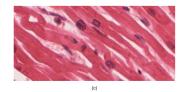
<sup>&</sup>lt;sup>1</sup>Simon Fraser University, Department of Mathematics

<sup>&</sup>lt;sup>2</sup>Manchester Metropolitan University

# INTRODUCTION

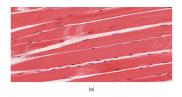


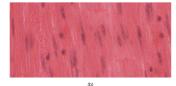


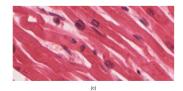


#### Three broad types of muscle:

- (a) **Skeletal**: most common very large multi-nucleated cells.
- (b) **Smooth**: contribute to the walls of blood vessels, and many visceral organs.
- (c) **Cardiac**: found in the walls of your heart.

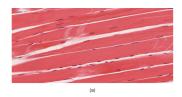


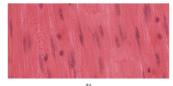


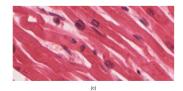


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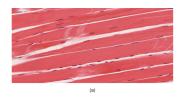




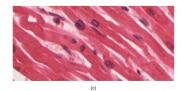
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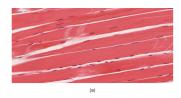




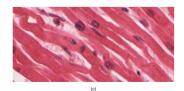


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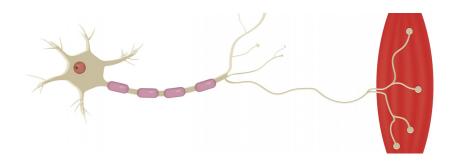




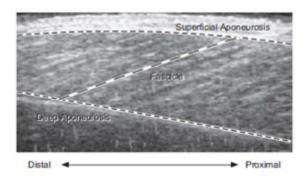
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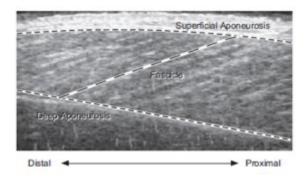
A **motor unit** consists of a motor neuron (located in the spinal cord), its axon, and the muscle fibers it innervates.

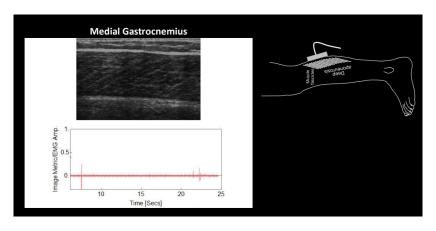


**aponeurosis:** white fibrous tissue that connects muscle and tendon to bone or other muscles.



**pennation angle:** angle of the fascicles within the muscle with respect to the aponeurosis.





Ultrasound of the medial gastrocnemius showing the pennate muscle fibres and aponeurosis. The medial gastrocnemius is one of the most popular muscles for study because of the easy access.

#### Muscle Architecture and Physiology



The classic 1D Hill-type muscle models were first fully and formally described in the 1980's. Since then, many similar formulations have been developed to incorporate different effects.



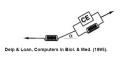




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- 2-dimensional models treat muscle as a panel with springs to either side, springs deform but area remains constant
- 3-dimensional continuum models hope to more accurately capture the complexity of biological tissue

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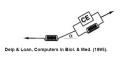




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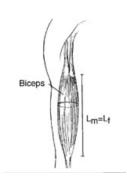
THE MATHEMATICAL PROBLEM

**GOAL:** Design a robust and accurate mathematical framework to answer fundamental questions about muscle mechanics

# Features of biological tissue:

#### Nearly incompressible

- Capable of finite, non-linear deformations
- Comprised of many materials
- Fibres can be activated



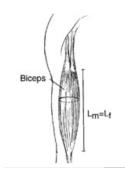
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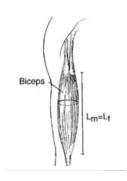
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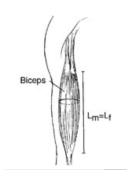
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# PROBLEM: PARTIAL DIFFERENTIAL EQUATION

Want to find displacement u(x,t) so that:

$$\nabla \cdot \sigma(u(x,t)) + F(x,t) = \rho(x) \frac{\partial^2 u}{\partial t^2}$$

All of the "biology" goes into  $\sigma$ 

In the first term,  $\sigma$  is the stress function. It describes the forces within the muscle (active, passive, elastic).

The second term  ${\cal F}$  describes any external forces

 $\rho(x)$  is the local mass density

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- 3. We end up with a non-linear system of equations

13

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- 4 6 1 ... 6 ... 11 ... 1
- 4. Solution of the discrete problem, and computer implementation

# TOOLS: DIFFERENTIAL EQUATIONS ANALYSIS LIBRARY



dealii is an open source finite element library

C++ program library targeted at the computational solution of partial differential equations using adaptive finite elements.

Current model based on the step 44 tutorial on nonlinear solid mechanics

Within each sub-grid lie a finite number of quadrature points, at which we store  $\approx$ 27 important values such as:

#### location in space (x,y,z) coordinates

- components of velocity in the (x,y,z) directions
- type of tissue (muscle or tendon)
- activation level
- modulus of compression (tells us how the compressive force is changing the volume per unit)
- constants related to tissue mechanical properties (e.g. bulk modulus)
- local mass density  $\rho$
- the orientation of the fibro

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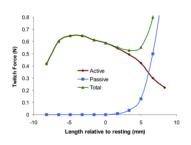
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**CURRENT EXPERIMENTS AND PROBLEMS** 





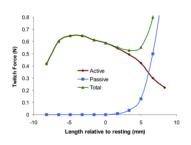
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**Ryan:** Adapting code to simulate an external weight on the muscle, changing length and then activating.

**Cassidy:** Adapting code to apply pressure to the "top" of the muscle, observing how compression effects force output.

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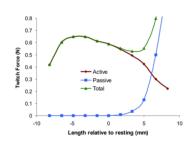
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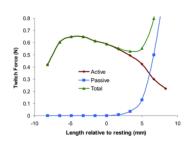
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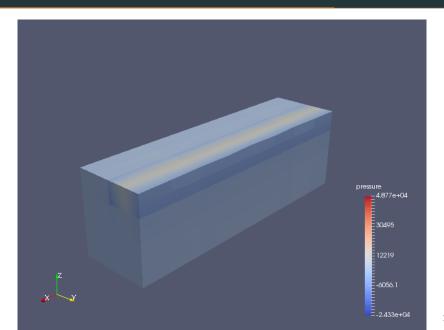
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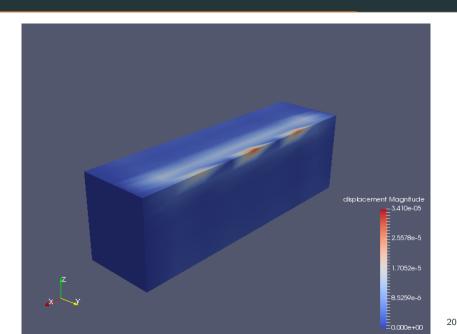
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# RESULTS

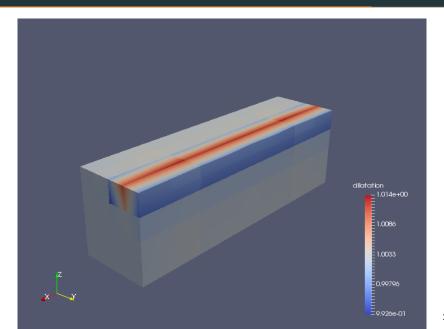
#### **EXAMPLE 1: PRESSURE OUTPUT**



#### **EXAMPLE 1: DISPLACEMENT OUTPUT**



### **EXAMPLE 1: DILATION OUTPUT**



#### **EXAMPLE 2: DISPLACEMENT MOVIE!**

In this simulation, we are activating the top 5 percent of fibres in the z-direction.



For ALS, can we simulate motor neuron death? This would change the base properties of the material, as fibres degenerate into fat and other substances.

Time delay between activation of fibres within a single motor unit. i.e. "jitters"

Changing the function used to ramp up activation. (generalized norma distribution)

How does not being at optimal length affect "twitches"?

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We want to add the aponeurosis tissue, and observe how the visual output of "twitches" changes.

ALS probes are most commonly used in the bicep and gastrocnemius muscles. The bicep has parallel fibres, while the gastrocnemius is pennate. Adapt geometries to these two specific muscles for most accurate and helpful results.

How does the distribution of the muscle fibres associated with a single motor unit effect the result? (i.e. clumped close together, spread across mesh)

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