# Section 5.2 - Binomial Probability Distributions

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## Outline

Introduction

Examples

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## Definition (Binomial Probability Distribution)

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A binomial probability distribution results from a procedure that meets the following requirements:

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- 2. The trials must be independent.
- 3. Each trial must have all outcomes classified into *two categories* (usually called success and failure).
- 4. The probability must remain the same for all trials.
- 5. The random variable *X* counts the number of successes in *n* trials.

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- P(X = x) is the probability of getting exactly x successes.
- P(X < x) is the probability of getting fewer than x successes.

#### Formula

## Theorem (Binomial Probability Formula)

$$P(X = x) = {}_{n}C_{x} \cdot p^{x} \cdot (1-p)^{n-x}$$

## Mean and Standard Deviation

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#### Standard Deviation

The standard deviation of a binomial probability distribution is

$$\sigma = \sqrt{np(1-p)}$$

# Examples

You are in the middle of a nightmare and have to take an exam for which you haven't studied. Fortunately, it's a multiple choice test with 10 question. Each question as 4 choices.

• What is *p*?

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- What is P(X = 7)?
- What is E(X)?
- What is the probability that the student gets at least 7 correct?

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- What is the probability that no more than 3 out of 8 people have blood in Group O?
- What is the probability that exactly 16 out of 21 people have blood in Group O?