# Section 6.4 — Finding Values of a Normally Distributed Random Variable

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# Outline

Standard Normal Distribution

Applications

Standard Normal Distribution

• What z value has an area of 0.7291 to the left?

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- What z value has an area of 0.1949 to the left?

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- What z value has an area of 0.1949 to the left?
- What is the z value that has an area of 0.2500 to the left?

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- What z value has an area of 0.1949 to the left?
- What is the z value that has an area of 0.2500 to the left?
- What is the z value that has an area of 0.90 to the left?

- What z value has an area of 0.7291 to the left?
- What z value has an area of 0.1949 to the left?
- What is the z value that has an area of 0.2500 to the left?
- What is the z value that has an area of 0.90 to the left?
- What z value represents the 95th percentile?

# Area to the right

• What is the z value with an area of 0.3936 to the right?

# Area to the right

- What is the z value with an area of 0.3936 to the right?
- What is the z value with an area of 0.5600 to the right?

# Area in between

• Find z so that the area between -z and z is 0.99.

#### Area in between

- Find z so that the area between -z and z is 0.99.
- Find z so that the area between -z and z is 0.75.

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- Find z so that the area between -z and z is 0.99.
- Find z so that the area between -z and z is 0.75.
- Find z so that the area between -z and z is 0.6827.

# **Applications**

# Water Temperature

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# **Water Temperature**

In region of the Caribbean Seas, daily water temperatures are normally distributed with a mean of 77.9°F and a standard deviation of 2.4°F.

- What is the cutoff for the first quartile of water temperatures?
- Let's say that the water temperature is unusually high if it is in the top 5% of temperatures. What is the minimum temperature to qualify as unusually high?

# Body temperature

Assume that healthy human body temperatures are normally distributed with a mean of 98.20°F and standard deviation 0.62°F.

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• If 100.6°F is the lowest temperature to be considered a fever, what percentage of healthy persons would be considered to have a fever?

# Body temperature

Assume that healthy human body temperatures are normally distributed with a mean of 98.20°F and standard deviation 0.62°F.

- If 100.6°F is the lowest temperature to be considered a fever, what percentage of healthy persons would be considered to have a fever?
- What should the cutoff be so that only 5% of healthy people have a temperature that is considered a fever?