

$$3. (a) E(Y) = E(2.4X - 5) = 2.4 E(X) - 5 = (2.4)(19) - 5 = 40.6$$

$$(b) \text{Var}(Y) = \text{Var}(2.4X - 5) = \text{Var}(2.4X) = (2.4)^2 \text{Var}(X) \\ = (2.4)^2(5.3) = 30.528$$

$$4. V = \frac{\sqrt{3}}{2} h b^2 \Rightarrow V(b + \Delta b, h + \Delta h) \approx V(b, h) + \frac{\partial V}{\partial b}(b, h) \Delta b + \frac{\partial V}{\partial h}(b, h) \Delta h$$

$$u_v = \sqrt{\frac{3}{4} b^4 u_h^2 + 3 h^2 b^2 u_b^2}$$

$$\text{At } (b, h) = (4.8, 8.5), \quad V = \frac{\sqrt{3}}{2} (4.8)^2 (8.5) = 169.6024$$

$$\text{and } u_v = \sqrt{\frac{3}{4} (4.8)^4 (0.4)^2 + 3 (8.5)^2 (4.8)^2 (0.3)^2} = 22.65$$

$$\Rightarrow \boxed{V = 170 \pm 20 \text{ cm}^3}$$

5. (a) A 94% CI for μ is constructed from

$$\bar{x} \pm qt(0.97, df=11) \cdot \frac{s}{\sqrt{n}}.$$

That is,

$$21.6 \pm (2.096) \frac{5.14}{\sqrt{12}} \Rightarrow (18.49, 24.71).$$

(b) Option (iii) offers a correct interpretation of this confidence interval.

6. (a) Since X, Y are independent and both normal, $Y - X$ is normal as well.

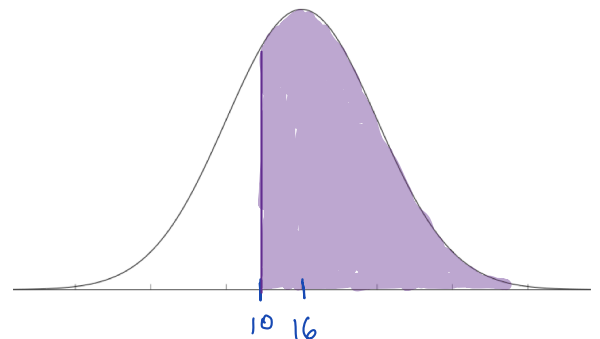
$$E(Y - X) = E(Y) - E(X) = 53 - 37 = 16.$$

$$\text{Var}(Y - X) = \text{Var}(Y) + \text{Var}(X) \quad (\text{by independence}) \\ = 25^2 + 7^2 = 674$$

$$\Rightarrow Y - X \sim \text{Norm}(16, \sqrt{674})$$

$$(b) 1 - \text{pnorm}(10, 16, 25.96)$$

$$\text{since } \sqrt{674} \doteq 25.96$$



How code for Problem 1 solutions might look

```
c(alpha1, lambda1, lambda2, alpha2, beta1)
```

```
## [1] 2.2800000 7.1600000 0.1061571 7.5100000 6.3400000
```

(a)

```
f = makeFun(dgamma(x, alpha1, lambda1) ~ x)
xF = antiD(x * f(x) ~ x)
xxF = antiD(x^2 * f(x) ~ x)
```

The expected value:

```
eX = xF(Inf) - xF(-Inf); eX
```

```
## [1] 0.3184358
```

The variance:

```
eXsq = xxF(Inf) - xxF(-Inf); eXsq
```

```
## [1] 0.1458756
```

```
aVar = eXsq - eX^2
```

mean	E(X^2)	variance
0.3184358	0.1458756	0.0444743

(b)

```
qexp(.7, lambda2)
```

```
## [1] 11.34142
```

(c)

```
manySums <- do(5000) * sum(~rbeta(50, alpha2, beta1))
mu = alpha2 / (alpha2 + beta1)
myVar = alpha2*beta1/((alpha2+beta1)^2*(alpha2+beta1+1))
```

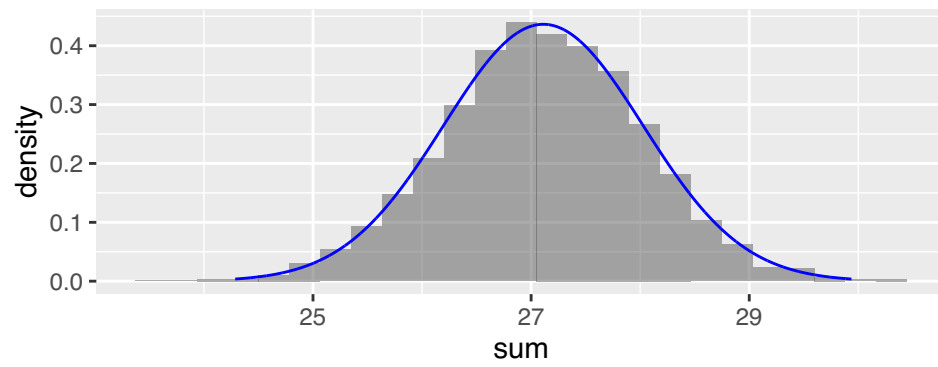
The population from which we are drawing an iid random sample of size 50 is Beta(7.51, 6.34). As per Table 4.5, the mean and variance of this population are

$$\mu = 0.5422383 \quad \text{and} \quad \sigma = 0.129286.$$

Thus, the sum of an iid random sample of size 50, by the central limit theorem, as an approximate normal distribution,

$$S \sim \text{Norm}(27.1119134, 0.9141903)$$

```
gf_dhistogram(~sum, data=manySums) |>
  gf_dist("norm", params=c(50*mu, sqrt(50*myVar)), color="blue")
```



(d)

```
fitdistr(manySums$sum, "normal")
```

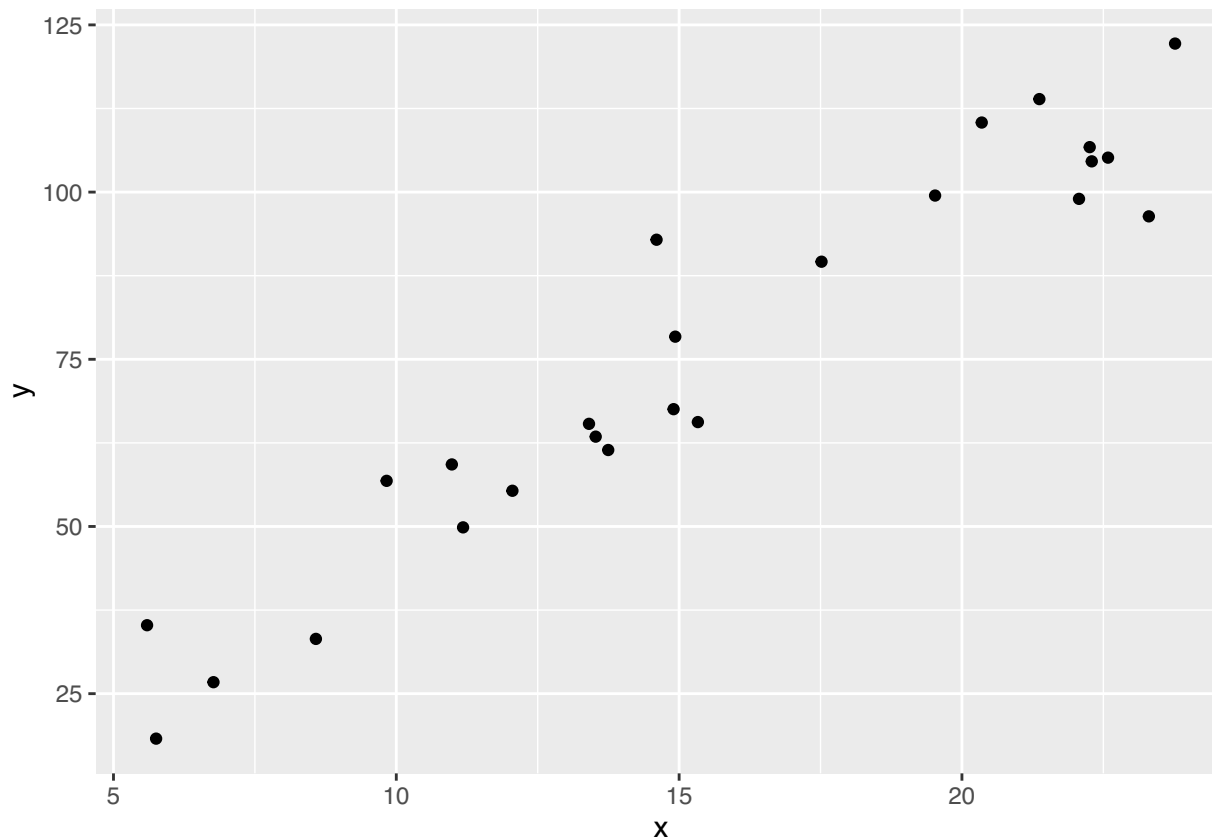
```
##      mean      sd  
## 27.104725682 0.912193801  
## ( 0.012900368) ( 0.009121938)
```

How code for Problem 2 solutions might look

```
set.seed(1234567)
c0 = round(runif(1, -8, 12), 2)
c1 = round(runif(1, 2.1, 5.4), 2)
xs = runif(25, 5, 25)
ys = c0 + c1 * xs + rnorm(25, 0, 8)
mydat <- data.frame(x = xs, y = ys)
```

(a)

```
gf_point(y~x, data=mydat)
```



(b)

```
cor(y~x, data=mydat)
```

```
## [1] 0.9567243
```

(c)

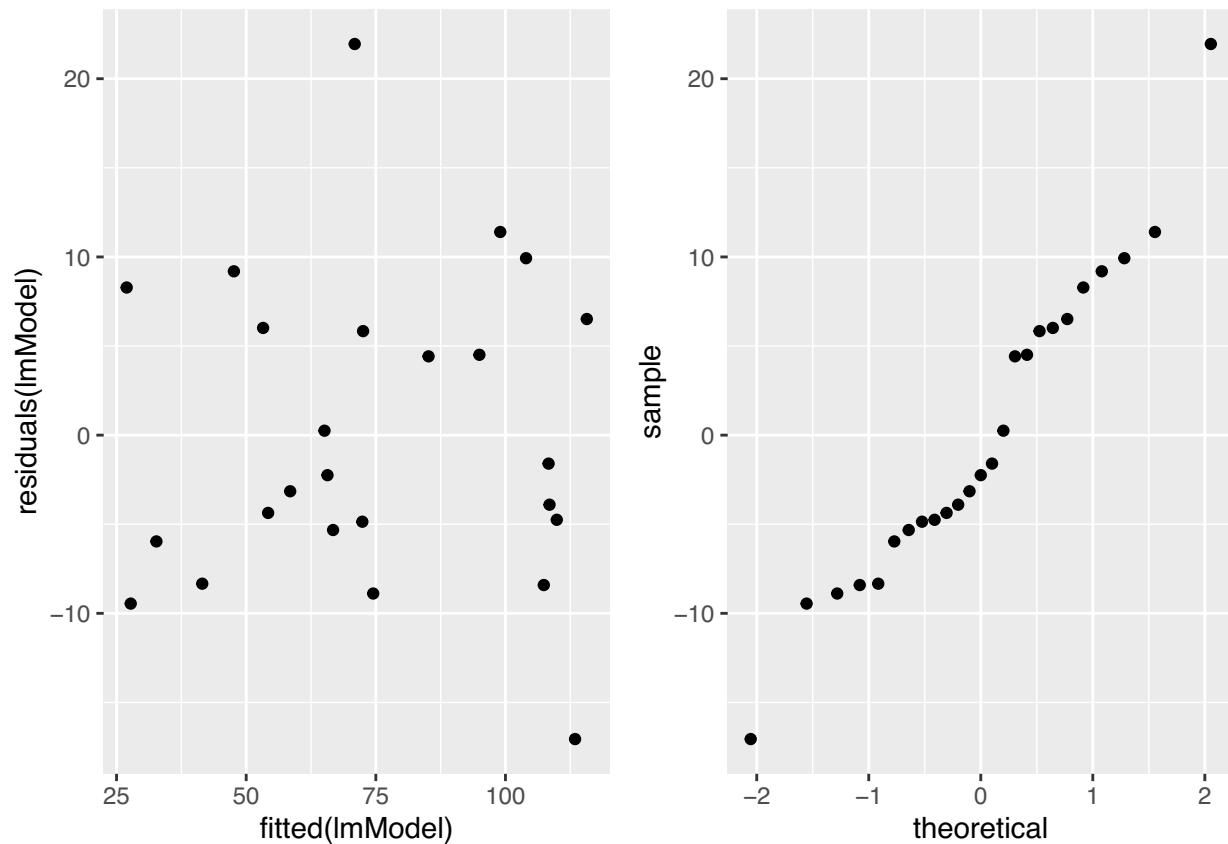
```
lmModel <- lm(y~x, data=mydat)
coef(lmModel)
```

```
## (Intercept)          x
## -0.3611503    4.8826449
```

(d)

```
p1 <- gf_point(residuals(lmModel) ~ fitted(lmModel))
p2 <- gf_qq(~ residuals(lmModel))
```

```
grid.arrange(p1, p2, ncol=2)
```



(e)

```
confint(summary(lmModel), level=.9)
```

```
##              5 %      95 %
## (Intercept) -9.096575  8.374275
## x              4.351920  5.413370
```

(f)

```
yPred <- makeFun(lmModel)
yPred(x=18, interval="prediction", level=0.92)
```

```
##      fit      lwr      upr
## 1 87.52646 71.04278 104.0101
```