

1. The .csv file <http://scofield.site/teaching/data/csv/aspirinAndStrokes.csv> contains raw data from a blind experiment to look at the effect of aspirin on instances of stroke. Here are some of the cases:

	progress	treatment
139	unfavorable	placebo
49	favorable	aspirin
106	favorable	placebo
9	favorable	aspirin
127	unfavorable	placebo
149	unfavorable	placebo
92	favorable	placebo
50	favorable	aspirin

- Summarize the data in this file.
- State a research question that may have prompted the collection of this data. (I suggest you access one appropriately-chosen app from the "Descriptive Statistics and Graphs" section of StatKey, import the data, and work from there to obtain the desired value.)
- Write hypotheses ( $H_0$  and  $H_a$ ) appropriate for your stated research question.
- With regard to the hypotheses you wrote, what is the *test statistic* (write it symbolically, and compute its value) produced from the data.
- In StatKey, produce a randomization distribution appropriate for an hypothesis test from this data. Then compute the corresponding  $P$ -value, and state a conclusion at the  $\alpha = 5\%$  level.
- The original data had two variables, "progress" and "treatment". The Lock text describes how to produce a randomization statistic in two-variable settings, *without* using software:

quantitative data for samples taken from 2 groups: p. 273, Example 4.32

binary categorical data for samples taken from 2 groups: p. 268, Example 4.28

bivariate quantitative data: p. 242, the first three paragraphs

Tailor one of these descriptions to the data at hand, and give a thorough set of instructions (like the instructions you might read for setting up and playing a game like Uno, Risk, or Chess) for how you could produce a

- randomization sample,
  - randomization statistic, and
  - randomization distribution.
- What steps in your prior instructions would be different if you needed to produce a
    - bootstrap sample,
    - bootstrap statistic, and
    - bootstrap distribution?

2. Suppose you are interested in the variable *height* (measured in inches) for the population "current female students at Calvin". Suppose a sample of size  $n$  is taken from this population motivated by the question, "Is the average height of a female Calvin student above 68 inches?"
- (a) If  $\bar{X}$  denotes the mean of a random sample, where would the given distribution be centered? (Answer using an appropriate name or symbol.)
- the sampling distribution of  $\bar{X}$
  - a bootstrap distribution
  - a randomization distribution
- (b) Tailor the description of a bootstrap sample in Example 3.20 (specifically, part (b) of that example) to the current setting, and describe how you would produce a single bootstrap statistic.
- (c) Assuming that you have already found
- the mean height  $\bar{x}$  for a *sample* of female Calvin students, and
  - a bootstrap distribution
- describe **two** different ways you might construct an 80% confidence interval for  $\mu$ , the mean height of the population.
- (d) Tailor the description given on p. 270, Example 4.30 so as to describe how you would produce a single randomization statistic.
3. Let  $p$  represent the proportion of people who voted in the 2020 Presidential election who would, if given the opportunity to vote again today, cast that vote for a different candidate. If a 90% confidence interval for  $p$  were  $(0.06, 0.31)$ , then what could you say about the  $P$ -value associated with the hypotheses
- (a)  $H_0: p = 0.25$  vs.  $H_a: p \neq 0.25$ ?
- (b)  $H_0: p = 1/3$  vs.  $H_a: p \neq 1/3$ ?
4. TRUE OR FALSE. Place a "T" by those statements that are true without reservation. Place an "F" by those statements which are not unequivocally true.
- (a) \_\_\_\_\_ A Type I error occurs when we reject a null hypothesis which is true.
- (b) \_\_\_\_\_ Using significance level  $\alpha = 0.05$ , the chance of committing a Type II error is 5%.
- (c) \_\_\_\_\_ The  $P$ -value one obtains in an hypothesis test is the probability that the null hypothesis is true.
- (d) \_\_\_\_\_ We reject the null hypothesis in precisely those instances where an effect is *significant*.
- (e) \_\_\_\_\_ When  $P = 0.97$ , we would reject the null hypothesis at the 5% level.
- (f) \_\_\_\_\_ If a  $P$ -value is significant at the 5% level, then it is also significant at the 1% level.
5. Why don't we ever construct 100% confidence intervals?