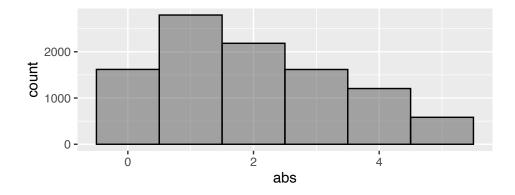
E3.2

First, we simulate many differences.

```
die <- 1:6
manyTrials <- do(10000) * abs( diff( resample(die, size=2) ) )
tally( ~abs, format="proportion", data=manyTrials )</pre>
```

abs

The probability of a difference of 2 is approximately 0.21. The approximately probability histogram follows.



E3.4

Let us define

- event A: "a part passes inspection A"
- event B: "a part passes inspection B"

Then event $A \cup B$ has probability

$$Pr(A \cup B) = 1 - Pr(A^c \cap B^c) = 1 - 0.05 = 0.995.$$

The addition rule (Inclusion-Exclusion Principle) says

$$Pr(A \cup B) = Pr(A) + Pr(B) - Pr(A \cap B).$$

Rearranging this, we get the desired probability of passing both inspections, or $Pr(A \cap B)$, as

$$Pr(A \cap B) = Pr(A) + Pr(B) - Pr(A \cup B) = 0.99 + 0.98 - 0.995 = 0.975.$$

E3.6

For Y, the absolute difference of two fair dice, we may again look at the listing of the sample space in Example 3.4(c).

$$\Pr(Y=2) \; = \; 4 \left(\frac{2}{36}\right) \; = \; \frac{2}{9}.$$

The values of Y must lie in the set $\{0, 1, 2, 3, 4, 5\}$.

The probability function of Y is given by

\overline{y}	0	1	2	3	4	5
$\Pr(Y=y)$	$\frac{6}{36}$	$\frac{10}{36}$	8 36	$\frac{6}{36}$	$\frac{4}{36}$	$\frac{2}{36}$

E3.10

Let's denote events

• S: "is a smoker"

• W: "is a woman"

• M: "is a man"

• C: "has cancer"

The given information is

• $Pr(C \mid M \cap S) = 23 \cdot Pr(C \mid M \cap S^c)$

• $\operatorname{Pr}(C \mid W \cap S) = 13 \cdot \operatorname{Pr}(C \mid W \cap S^c)$

• $Pr(S \mid M) = 0.231$, which means $Pr(S^c \mid M) = 0.769$

• $Pr(S \mid W) = 0.183$, which means $Pr(S^c \mid W) = 0.817$

First,

$$\Pr(W \mid S) \ = \ \frac{\text{number of women smokers}}{\text{number of smokers}} \ = \ \frac{21.1}{21.1 + 24.8} \ = \ 0.46.$$

Next,

$$\begin{split} \Pr(S \mid C \cap W) &= \frac{\Pr(C \cap W \cap S)}{\Pr(C \cap W)} = \frac{\Pr(C \cap W \cap S)}{\Pr(C \cap W \cap S) + \Pr(C \cap W \cap S^c)} \\ &= \frac{\Pr(C \mid W \cap S) \cdot \Pr(W \cap S)}{\Pr(C \mid W \cap S) \cdot \Pr(W \cap S)} \\ &= \frac{13 \cdot \Pr(C \mid W \cap S^c) \cdot \Pr(W \cap S)}{13 \cdot \Pr(C \mid W \cap S^c) \cdot \Pr(W \cap S)} \\ &= \frac{13 \cdot \Pr(C \mid W \cap S^c) \cdot \Pr(W \cap S)}{13 \cdot \Pr(C \mid W \cap S^c) \cdot \Pr(W \cap S)} \\ &= \frac{13 \cdot \Pr(W \cap S)}{13 \cdot \Pr(W \cap S) + \Pr(W \cap S^c)} = \frac{13 \cdot \Pr(S \mid W) \Pr(W)}{13 \cdot \Pr(S \mid W) \Pr(W) + \Pr(S^c \mid W) \Pr(W)} \\ &= \frac{13 \cdot \Pr(S \mid W)}{13 \cdot \Pr(S \mid W) + \Pr(S^c \mid W)} = \frac{13(0.183)}{13(0.183) + 0.817} \stackrel{.}{=} 0.744. \end{split}$$

Thus, after the manner of computing $Pr(S \mid W \cap C)$, we have

$$\Pr(S \mid M \cap C) = \frac{23(0.231)}{23(0.231) + 0.769} \doteq 0.874.$$