

2. (a), (c), (d) and (e)
3. (c)
4. (a)
5. (c)
6. (c)
7. (a) Since an IQ of 130 is 2 standard deviations above the mean of 100, the adults with IQs below 130 include all those with 2 standard deviations (the 95%) plus those in the lower tail of the distribution (2.5%). Thus, adults with IQs below 130 are about 97.5% of the population.
- (b) Our standardized score, since we know  $\sigma = 15$ , is a Z-score. We do not have to standardize, in fact, but noting that  $\sigma$  is available tells us we can use `pnorm`:

```
1 - pnorm(110, 100, 15/4)
```

9. (a) From the back sheet, the critical value is  $z^* = 2.0537$ . We have point estimate

$$\hat{p} = \frac{53}{144} \doteq 0.368, \quad \text{and} \quad SE_{\hat{p}} \approx \sqrt{\frac{(0.368)(0.632)}{144}} \doteq 0.04019,$$

so our 96% confidence interval is

$$0.368 \pm (2.0537)(0.04019), \quad \text{or} \quad (0.285, 0.451).$$

- (b) Our  $z^*$ -value for the requested level of confidence is  $z^* = 1.751$ . Applying the formula, we have

$$n \geq \left( \frac{1.751}{0.02} \right)^2 (0.15)(0.85) \doteq 977.29.$$

Thus, the minimum  $n$  is 978.

10. (a) Letting  $\mu$  represent the average pulse among U.S. adult males, we have null hypothesis

$$H_0: \mu = 72 \quad \text{with alternative} \quad H_a: \mu \neq 72.$$

- (b) The test statistic most directly of use in determining a  $P$ -value is the  $t$ -score:

$$t = \frac{69.4 - 72}{11.3 / \sqrt{40}} \doteq -1.455.$$

In this command we have used that the point estimate is the sample mean  $\bar{x} = 69.4$ , the sample standard  $s = 11.3$ , and the sample size is  $n = 40$ . Using  $40 - 1 = 39$  degrees of freedom, our  $P$ -value is the result of the command

```
2 * pt(-1.455, 39)
```

- (c) Our critical value is appropriately named  $t^*$ , coming from a  $t$ -distribution with 39 degrees of freedom. As a 94% CI leaves 3% in each tail, the command that yields  $t^*$  is

```
qt(0.97, 39)
```

- (d) A 94% CI is

$$69.4 \pm (1.937) \frac{11.3}{\sqrt{40}}, \quad \text{or} \quad [65.94, 72.86].$$

11. (a) Integrating  $f$  gives

$$\begin{aligned}\Pr(X < 0) &= \int_{-\infty}^0 f(x) dx = \int_{-1}^0 \left( \frac{8}{27} + \frac{4}{9}x - \frac{4}{27}x^3 \right) dx \\ &= \left[ \frac{8}{27}x + \frac{2}{9}x^2 - \frac{1}{27}x^4 \right]_{-1}^0 = 0 - \left( -\frac{8}{27} + \frac{2}{9} - \frac{1}{27} \right) \\ &= \frac{8}{27} - \frac{6}{27} + \frac{1}{27} = \frac{1}{9}.\end{aligned}$$

(b) From what we just learned in part (a), 0 is at the position dividing the lowest  $1/9$  from the upper  $8/9$  of the total area 1; that is, it is at approximately the 11<sup>th</sup> percentile. The median is the 50<sup>th</sup> percentile, and hence further to the right of 0 (i.e., it is positive).

(c) The expected value

$$\begin{aligned}E(X) &= \int_{-\infty}^{\infty} xf(x) dx = \int_{-1}^2 \left( \frac{8}{27}x + \frac{4}{9}x^2 - \frac{4}{27}x^4 \right) dx \\ &= \left[ \frac{4}{27}x^2 + \frac{4}{27}x^3 - \frac{4}{135}x^5 \right]_{-1}^2 = \left( \frac{16}{27} + \frac{32}{27} - \frac{128}{135} \right) - \left( \frac{4}{27} - \frac{4}{27} + \frac{4}{135} \right) \\ &= \frac{80}{135} + \frac{160}{135} - \frac{128}{135} - \frac{4}{135} = \frac{108}{135} = \frac{4}{5}.\end{aligned}$$

(d)  $F(5) = 1$ , having accumulated all the area there is under the pdf.