

Where to find material in Lock5 textbook:

- Lock5 Chapter 11: the entire chapter, but focus will be on Sections 11.3-11.4.
- Lock5 Section 3.1
- Lock5 Section 5.1
- Central limit theorem and related results: some at [this link](#) and some in Section 6.1 (when applied to  $\hat{p}$ )

### Terminology of Data

- population vs. sample
- sampling
  - SRS (sampling without replacement) vs. i.i.d. (sampling with replacement)
  - sample statistics and their sampling distributions
    - \* When can they be well approximated using a normal distribution model?
    - \* What is meant by  $SE_{\bar{x}}$ ? by  $SE_{\hat{p}}$ ?

### Probability (general)

- terminology: random process, outcomes, sample space, event, complement, independence, mutual exclusivity (a.k.a. "disjointness")
- conditional probability, independent events
- rules
  - axioms
  - addition/multiplication rules
  - Bayes' rule
- (discrete) random variables (r.v.s)
  - the role of the probability (mass) function  $f(x) = \Pr(X = x)$  and cumulative distribution function giving  $\Pr(X \leq x)$
  - computing the mean of an r.v.  $X$  from the formula  $\mu_X = \sum_x x f(x)$
  - computing the variance from the formula  $\sigma_X^2 = \sum_x (x - \mu_X)^2 f(x)$
  - formulas:  $\mu_{X+Y} = \mu_X + \mu_Y$  and  $\mu_{X-Y} = \mu_X - \mu_Y$  when r.v.s are combined through addition/subtraction
  - formulas:  $\sigma_{X+Y}^2 = \sigma_X^2 + \sigma_Y^2$  and  $\sigma_{X-Y}^2 = \sigma_X^2 + \sigma_Y^2$  when independent r.v.s are combined through addition/subtraction

**Binomial Random Variables**

- recognizing a binomial scenario, identifying parameters  $n$  and  $p$
- mean and standard deviation, when r.v.  $X \sim \text{Binom}(n, p)$
- the probability function to go with  $X \sim \text{Binom}(n, p)$ 
  - how to read it from a table and understand what it provides
  - the command, `dbinom()`, in R that provides its values
  - how to graph it
  - how to simulate it
- role of the cdf, and the R command, `pbinom()`, used to evaluate it

**Normal distributions**

- Empirical (68-95-99.7%) Rule
- Z-scores (or standardized scores), and using the standard normal distribution
- normal distributions in play if you are taking the
  - sum of  $n \geq 30$  iid variables from a population with mean  $\mu$ , standard deviation  $\sigma$ :  $\text{Norm}(n\mu, \sigma \sqrt{n})$
  - sample mean of  $n \geq 30$  iid variables from a population with mean  $\mu$ , standard deviation  $\sigma$ :  $\text{Norm}(\mu, \sigma / \sqrt{n})$
  - sum of two independent variables from normal populations,  $X \sim \text{Norm}(\mu_1, \sigma_1)$  and  $Y \sim \text{Norm}(\mu_2, \sigma_2)$ :  $(X + Y) \sim \text{Norm}(\mu_1 + \mu_2, \sqrt{\sigma_1^2 + \sigma_2^2})$
  - difference of two independent variables from normal populations,  $X \sim \text{Norm}(\mu_1, \sigma_1)$  and  $Y \sim \text{Norm}(\mu_2, \sigma_2)$ :  $(X - Y) \sim \text{Norm}(\mu_1 - \mu_2, \sqrt{\sigma_1^2 + \sigma_2^2})$
- R commands
  - Evaluating probabilities of normal variable  $X \sim \text{Norm}(\mu, \sigma)$  using `pnorm()`
  - Finding quantiles of a normal variable  $X \sim \text{Norm}(\mu, \sigma)$  using `qnorm()`