

The Glass Wedge

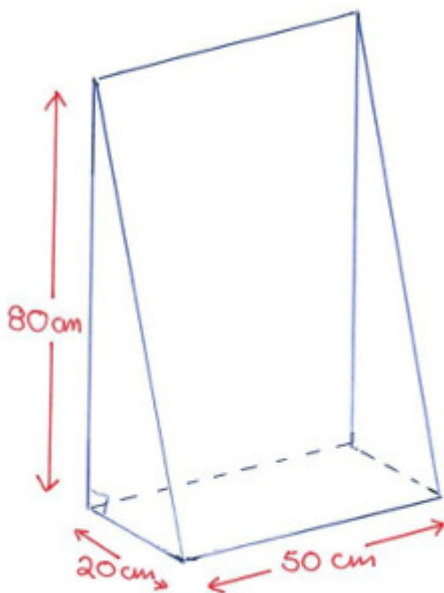
Annotation

Paula shows that she can use the scale factor of an enlargement to calculate volumes of a triangular prism under transformation.

Problem: The Glass Wedge

The teacher poses this problem:

*An artist has been commissioned by a gallery to make a sculpture of a giant glass wedge. The gallery plans to sell small-scaled copies of the wedge as souvenirs. To produce the souvenirs, The artist builds a model that will be scaled up by a factor of $n = 8$ to produce the sculpture and scaled down by a factor of $n = 0.1$ to produce the souvenirs. Investigate the relationship between the volume of the wedge before and after scaling **and** the scale factor for the dimensions.*



Artist's Model

Student Response

$$\underline{\text{Volume}} = \text{Area} \times \text{length}$$

$$V = \frac{1}{2} \times 20 \times 80 \times 50$$

$$= 40,000 \text{ cm}^3$$

Model

$$V = \frac{1}{2} \times \underline{8} \times \underline{20} \times \underline{8} \times \underline{80} \times \underline{8} \times 50$$

$$= 20,480,000 \text{ cm}^3$$

Sculpture

$$40,000$$

$$\downarrow$$

$$40,000 \times 8^3$$

$$= 20,480,000$$

$$V = \frac{1}{2} \times \underline{0.1} \times \underline{20} \times \underline{0.1} \times \underline{80} \times \underline{0.1} \times 50$$

$$= 40 \text{ cm}^3$$

Souvenir

$$40,000 \times 0.1^3$$

$$= 40$$

What I found out:-

$$\text{New Volume} = \text{Old Volume} \times n^3$$

\uparrow
n is the scale factor

Teacher: Tell me about your investigation.

Well, I started out the long way, calculating volume by using the height and width of the triangle and then timesing the area of that by the length. So when I went to get a new volume for the sculpture or the souvenir, I changed the height, width and length by the scale factor each time.

Teacher: I notice that you've underlined parts of your calculation.

Yeah. When I was doing the long calculations, I saw that I had the scale factor in there three times. So it was like $8 \times 8 \times 8$ and I could just go 8^3 and get straight to the answer. The same thing worked for when the scale factor was 0.1. I could have just taken the volume of the model and timesed it by 0.1^3 .

Teacher: Do you think this would always work.

Yeah. Cos when you are working out volume, its length x width x height.

When you enlarge, you go n times length and n times width and n times height and then times all those together. So you might as well do the n's first and go n^3 on its own and then times that by the original volume. It's the same thing as doing it the long way, just a different order.