

How big is the pen?

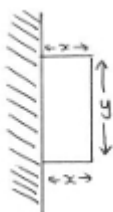
Annotation

Bill can work with multiple variables to form a quadratic equation to model a real-world situation. He uses systematic working, including the appropriate use of brackets, to simplify his model.

Problem: How big is the pen?

The teacher poses the following problem:

A farmer has a length of temporary fencing that he can place against an existing wall to form a rectangular pen.



1. Use the symbols x and/or y to

1. write an equation for L , the length of fencing used and
2. an equation for A , the area of the pen.

2. The total length of fencing to be used is 42 m. Use your answers for 1. to form an equation of the area of the pen in terms of x only.

Student Response

$$\begin{aligned}
 1. \quad L &= x+y+x = 2x+y \\
 a) \quad L &= 2x+y \\
 b) \quad A &= xy \\
 2. \quad L &= 42 \\
 2x+y &= 42 \\
 A &= xy \\
 &\quad \underline{\quad} \\
 &\quad \quad 2x+y=42 \\
 &\quad \quad \underline{-2x} \quad \underline{-2x} \\
 &\quad \quad \quad y = 42-x \\
 A &= x(42-x)
 \end{aligned}$$

Teacher: Talk me through your thinking for part 2 of this problem.

Bill: Well I had equations with area and length using xs and ys and you only wanted area with xs so I had to get rid of some of the letters. There had to be a reason that you gave us the 42. So I looked at that and saw it was what L is equal to so I just put that in straight away.

Teacher: So you substituted 42 for L. Then what did you think about?

Bill: The question was about area so I wrote out the area equation again and looked at what had to go there. The y. My length equation had a y in it too so I knew I had to do some substituting again. But it wasn't all easy and ready to go...I had to get y on its own. So that's what the working in the next bit is about.

Teacher: I was pleased to see that you used some brackets in your last step.

Bill: Oh yeah...thanks. A was x times y and if I didn't put the brackets in then I would be saying A is x times a bit of y. I had to make sure it was x times all of y so I put brackets round all of y.