

Level 3 – AS91582 – 4 Credits – Internal

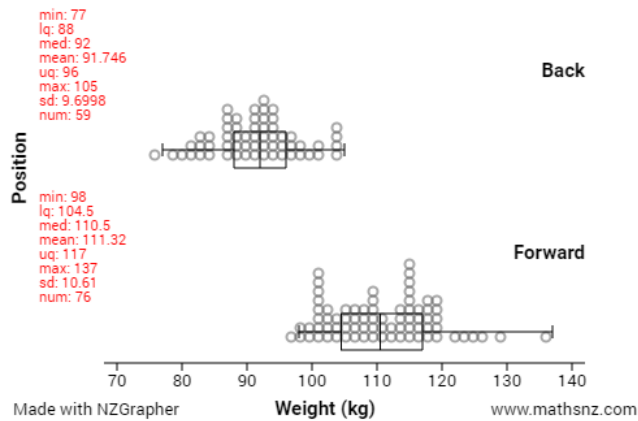
## Use Statistical Methods to Make a Formal Inference

Written by J Wills – MathsNZ – [jwills@mathsnz.com](mailto:jwills@mathsnz.com)

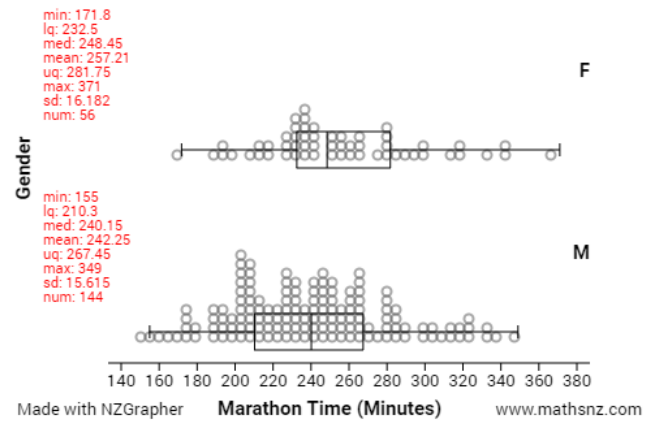
Achievement	Achievement with Merit	Achievement with Excellence
Use statistical methods to make a formal inference.	Use statistical methods to make a formal inference, with justification.	Use statistical methods to make a formal inference, with statistical insight.

Part 1: Problem and Plan.....	3
Part 1.1: Writing a Good Question.....	3
Part 1.2: Defining the Variables.....	4
Part 2: Sampling Variability.....	5
Part 3: The Effect of Sample Size .....	6
Part 4: Data – Using NZGrapher.....	7
Part 5: Analysis.....	8
Part 5.1: Centre – The Difference Between Medians.....	8
Part 5.2: Centre – Middle 50% .....	9
Part 5.3: Shift – Comparing the Medians and Quartiles .....	10
Part 5.4: Spread.....	11
Part 5.5: Shape .....	12
Part 5.6: Special Features.....	13
Part 6: Bootstrapping Activity.....	14
Part 7: Using NZGrapher to Create a Bootstrap Confidence Interval .....	17
Part 7a: Making a Formal Inference.....	18
Part 8: Writing a Conclusion .....	19
Part 9a: Writing Your Own Internal 1 .....	21
Part 9b: Writing Your Own Internal 2 .....	23
Sample Internal (at Achieved level) .....	25
Data Set Information.....	28
Assessment Guidelines – 91582 – Use Statistical Methods to Make a Formal Inference .....	32

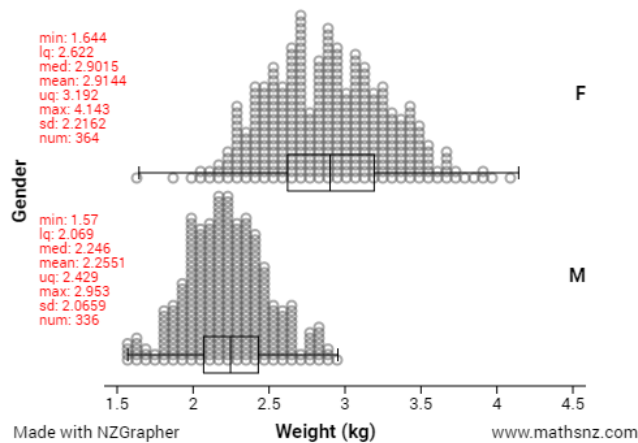
### 1. Rugby Players Weight by Position



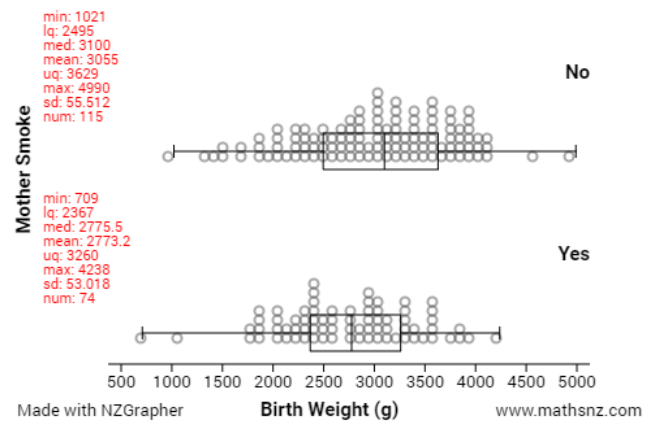
### 4. Marathon Times by Gender



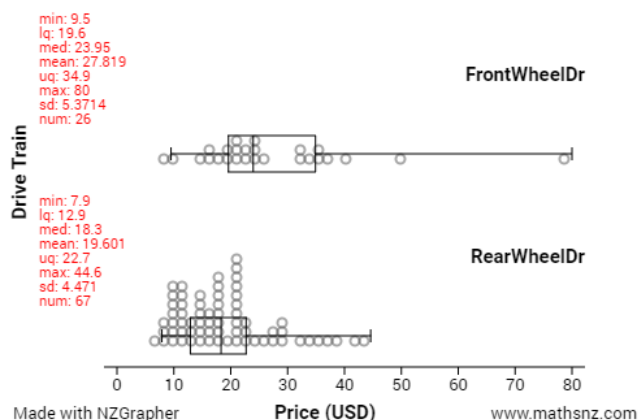
### 2. Weight of Kiwi Bird by Gender



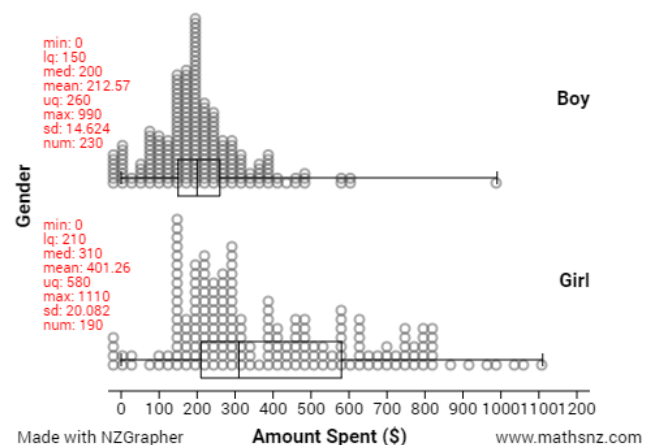
### 5. Birth Weight by Smoking Mother



### 3. Car Prices by Drive Train



### 6. Amount Spent on Ball by Gender



## Part 1: Problem and Plan

### Part 1.1: Writing a Good Question.

---

For each of the graphs write a good comparative question. A question should have:

- What you are comparing (including the parameter)
- The characteristic you are grouping by
- What the population is
- Where your data is sourced from

The first one has been done for you.

To be going for Merit you need to say why you are wanting to look at these variables.

To be going for Excellence you need to use research to develop the problem.

1. I wonder what the difference is between the median weight of forward and back rugby players in New Zealand and South Africa according to a sample from <http://www.rugby-sidestep-central.com/>

2. 

---

---

---

---

---
3. 

---

---

---

---

---
4. 

---

---

---

---

---
5. 

---

---

---

---

---
6. 

---

---

---

---

---

---

**Part 1.2: Defining the Variables**

---

The next thing that we need to do is define our variables.

Define the variables for each of the graphs, the first one has been done as an example for you.

To be going for Merit or Excellence you should be using research to define the variables.

1. The weight is the weight of the rugby players in kilograms, and the position is the player's normal position on the rugby field, either forward or back.

2. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

3. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

4. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

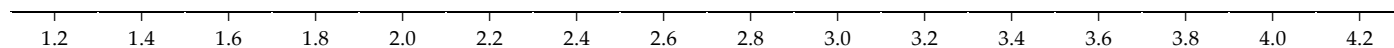
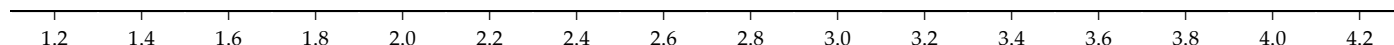
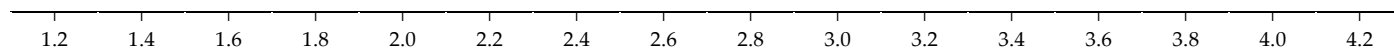
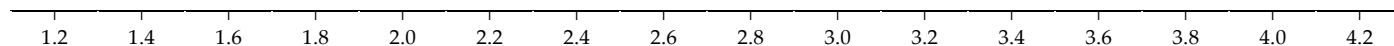
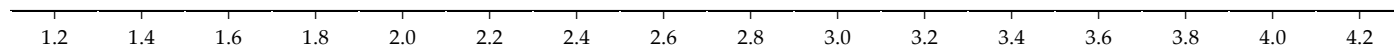
5. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

6. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

## Part 2: Sampling Variability

When we take a sample there are always variations in what we choose. The more varied the data is the more varied our samples will be.

Take 5 samples of the weight of 15 kiwis using the 'Kiwi Kapers' cards, and produce a dot plot for each one on the axis below.



What do you notice about the samples?

---



---



---

Teachers: please see the note on the dataset information on page for more information on this dataset.

Kiwi Kapers cards available from: <http://new.censusatschool.org.nz/resource/kiwi-kapers-1/>

## Part 3: The Effect of Sample Size

The size of our sample can also affect how reliable our sample is for predicting the population parameters.

We will use the Kiwi Kapers dataset again to investigate this. Using the Sampling module of NZGrapher do 5 sampling repetitions for each sample size and record the lower quartile, median and upper quartile.

Instructions on sampling: [http://students.mathsnz.com/nzgrapher/nzgrapher\\_a\\_4.html](http://students.mathsnz.com/nzgrapher/nzgrapher_a_4.html)

You can put the dataset back to the original by pressing the reset dataset button.

Use the same sampling method (either simple random or stratified each time).

### Sample Size 15

Sample	Lower Quartile	Median	Upper Quartile
1			
2			
3			
4			
5			

### Sample Size 30

Sample	Lower Quartile	Median	Upper Quartile
1			
2			
3			
4			
5			

### Sample Size 60

Sample	Lower Quartile	Median	Upper Quartile
1			
2			
3			
4			
5			

What do you notice as the sample size increases?

---



---



---



---

## Part 4: Data – Using NZGrapher

The next section that we need to do is the data section. This is reproducing the graphs using NZGrapher. The example below will go through using the Rugby dataset for weight by position. NZGrapher runs on anything with a browser... Macs, PCs, iPad, Android, ChromeBooks and more. You can see a video version of this at [students.mathsnz.com](https://students.mathsnz.com)

First up we need to start NZGrapher by going to the link in the box to the right.

[www.jake4maths.com/grapher](https://www.jake4maths.com/grapher)

To draw a dot plot there are just three things you need to do.

1. Select the graph type... for this we want the "Dot Plot".
2. Select the x-variable... this is your numerical variable that will be on the x-axis, in this case it's weight.
3. Select the y-variable... this is your categorical variable and should have two categories, in this case it's position.

You then just need to check the graph title and axis labels to make sure they are appropriate (include units where necessary) and add press update graph to save the titles. To add in the summary statistics and box plots just tick these options down the bottom.

To save the graph just right click on it and press 'Save Image As' or whatever your device says that is similar, or copy it by right clicking and pressing copy.

Note 1: sometimes you may want to only use some of the dataset... you can either delete each row you don't want in the data viewer, or sample or filter the dataset (under sample and more) to remove points you don't want.

Note 2: If you want to identify the extreme points, if you click the 'Point Labels' checkbox this will add little numbers next to the points that match the point id.



Now it is your turn. For each dataset you need to produce the box and whisker plot with the summary statistics overlaid.

## Part 5: Analysis

---

We now start on the Analysis section of our report. This section can be abbreviated to CSI. The C stands for Centre, then there are 4 S's, Shift, Spread, Shape and Special Features. I stands for Inference.

### Part 5.1: Centre – The Difference Between Medians

---

We now need to state what the difference between the medians is. This is calculated by subtracting one median from the other.

Again the first one has been done for you.

To be going for Merit you need to say why you are looking at the median rather than the mean and state if this lines up with expectations. To be going for Excellence you need to link this to research.

1. The forwards' median weight is 18.50 kg higher than the backs' median weight.

2. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_
3. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_
4. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_
5. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_
6. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_



---

**Part 5.2: Centre – Middle 50%**

---

The centre is looking at what is happening with the middle 50% of the data, which is between the lower quartile (1<sup>st</sup> Qu.) and the upper quartile (3<sup>rd</sup> Qu.).

Discuss the centre for each of the sets of data, the first one has been done for you.

To be going for Merit you need to say if there is an overlap and state if this lines up with expectations.

To be going for Excellence you need to link this to research.

1. The middle 50% of the forward's weights are between 104.8 kg and 117.0 kg whereas the middle 50% of the back's weights are between 88.0 kg and 95.5 kg.

2. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

3. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

4. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

5. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

6. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

---

**Part 5.3: Shift – Comparing the Medians and Quartiles**

---

With the shift we need to look at what parts of the box and whisker graphs overlap, and which parts are shifted along. You need to consider where the median and upper / lower quartiles are for the two groups of data.

Compare the medians and quartiles for each of the sets of data, the first one has been done for you.

1. The lower quartile for the forwards weight is higher than the upper quartile of the weight of the backs.

2. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

3. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

4. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

5. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

6. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

---

**Part 5.4: Spread**

---

To calculate the spread we normally look at the inter-quartile range (IQR) for the two data sets. The IQR is calculated by subtracting the lower quartile off the upper quartile. You can also look at the standard deviation for each of the two data sets. You should also comment on what you see visually.

Discuss the spread for each of the sets of data, the first one has been done for you.

1. The inter quartile range for the forwards is 12.2 kg whereas the interquartile range for the backs is 7.5 kg indicating that the forwards have more variation in their weights than the backs. The standard deviation is also higher for the forwards. Overall visually the forwards seem to be slightly more spread out than the backs.

2. 

---

---

---

---

---
3. 

---

---

---

---

---
4. 

---

---

---

---

---
5. 

---

---

---

---

---
6. 

---

---

---

---

---

### Part 5.5: Shape

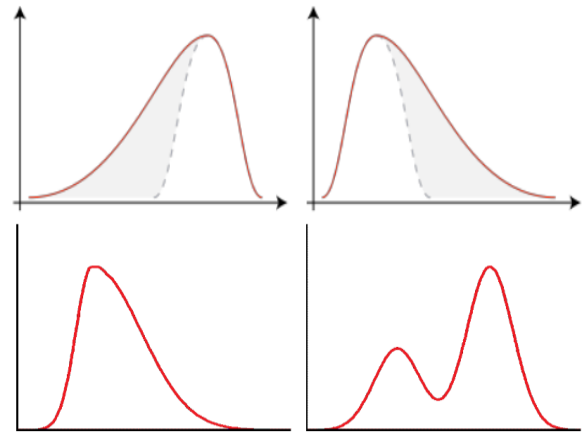
In the shape we need to look at two things... the skew and the modality.

If the distribution has a long tail to the left, it is skewed to the left (like left diagram).

If it has a long tail to the right it is skewed to the right (like right diagram).

We also need to say if there is one mode (unimodal, left diagram) or two modes (bimodal, right diagram).

Discuss the shape for each of the sets of data, the first one has been done for you.



1. The forwards weights appear to be skewed to the right whereas the backs weights seem reasonably symmetrical. The backs appear to be unimodal whereas the forwards are potentially bimodal.

2. \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_
3. \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_
4. \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_
5. \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_
6. \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_

---

**Part 5.6: Special Features**

---

We also need to discuss any unusual features that we notice with the data sets. This could be an extreme value (a point with a much higher value than the others) or anything else that you notice. It is good to give a possible explanation for anything you notice. Going back to the original data set to find out more information about the data point is often useful as well.

Discuss the special features for each of the sets of data, the first one has been done for you.

1. Looking at the graphs I can see that the forwards have one player that weighs more than most of the other forwards. He is a New Zealander weighing 137 kg and is 1.81 m tall. This could be because he is a stockier player that is quite large with more muscles causing him to weigh more.

2. 

---

---

---

---

3. 

---

---

---

---

4. 

---

---

---

---

5. 

---

---

---

---

6. 

---

---

---

---

## Part 6: Bootstrapping Activity

Bootstrapping is sampling from the sample with replacement. It normally involves sampling until you have the same number as in your original sample, but for the sake of this activity when we are doing it manually we are just going to take samples of 30 in total, which means we may end up with different numbers of forwards and backs.

Record the weights of the forwards and backs below (you won't end up filling up the whole table), and then use your calculator to work out the median for the forwards and the backs from the bootstrap, and find the difference between the two.

This activity can also be done online at: <http://www.jake4maths.com/mboot.php>

## Bootstrap 1

[illegible]

## Bootstrap 2

[illegible]

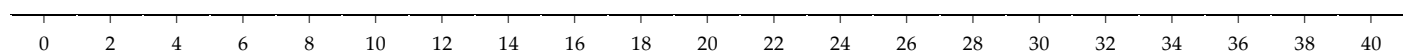
## Bootstrap 3

Forwards	Backs
Med:	Med:
Difference:	

## Bootstrap 4

Forwards	Backs
Med:	Med:
Difference:	

Plot the differences from both your bootstraps, as well as the bootstraps from your class as a dot plot on the axis below.



This gives us a fairly good idea of how accurate our samples are going to be, and if there is going to be a difference between the two groups (in this case the forwards' and the backs' weights). It is a very tedious process though, so we normally will use a computer to speed it up.

## Bootstrapping Activity

Below is all of the rugby players from Data Set 1. You will need to cut them all out in order to do the activity on page 15. This activity can also be done online at:

<http://www.jake4maths.com/mboot.php>

Back	82
Back	84
Back	93
Back	93
Back	105
Back	82
Back	93
Back	89
Back	90
Back	85
Back	101
Back	89
Back	94
Back	85
Back	87
Back	93
Back	88
Back	89
Back	100
Back	104
Back	92
Back	92
Back	94
Back	95
Back	97
Back	104
Back	80

Back	84
Back	90
Back	99
Back	83
Back	87
Back	88
Back	85
Back	93
Back	96
Back	105
Back	89
Back	92
Back	93
Back	95
Back	97
Back	92
Back	92
Back	94
Back	77
Back	92
Back	87
Back	96
Back	89
Back	91
Back	94
Back	93
Back	99

Back	88
Back	96
Back	79
Back	97
Back	101
Forward	116
Forward	120
Forward	102
Forward	110
Forward	137
Forward	102
Forward	112
Forward	103
Forward	123
Forward	114
Forward	115
Forward	116
Forward	118
Forward	125
Forward	102
Forward	120
Forward	101
Forward	104
Forward	107
Forward	109
Forward	118
Forward	127

Forward	119
Forward	100
Forward	109
Forward	114
Forward	115
Forward	117
Forward	105
Forward	108
Forward	107
Forward	111
Forward	117
Forward	118
Forward	102
Forward	103
Forward	107
Forward	117
Forward	107
Forward	113
Forward	106
Forward	113
Forward	101
Forward	108
Forward	106
Forward	115
Forward	104
Forward	110
Forward	129

Forward	102
Forward	120
Forward	98
Forward	115
Forward	99
Forward	100
Forward	103
Forward	110
Forward	115
Forward	103
Forward	115
Forward	124
Forward	110
Forward	116
Forward	99
Forward	101
Forward	110
Forward	110
Forward	106
Forward	106
Forward	112
Forward	114
Forward	114
Forward	117
Forward	120
Forward	119
Forward	120

This page has been deliberately left blank (as you are cutting out the other side)

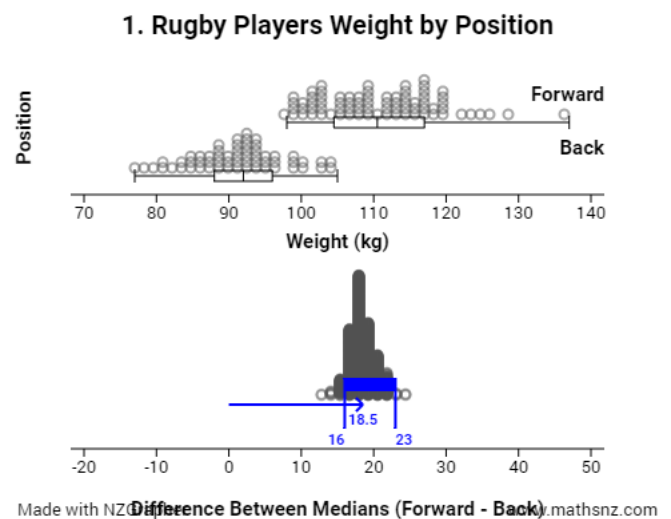


## Part 7: Using NZGrapher to Create a Bootstrap Confidence Interval

This part is really easy... all you need to do is change the graph type from the graph that we did earlier to a bootstrap confidence interval.

I recommend you use the median, as that is what we focus on in this booklet, but if you think the mean is better for your dataset, then use that... just justify it in your report somewhere.

This gives the output shown to the right, which tells us the difference between the medians is 18.50kg, but that we can be reasonably confident that forwards will be between 16kg and 23kgs on average heavier than the backs.



Now it is your turn. For each dataset you need to produce the bootstrap confidence interval... don't forget to write down the confidence intervals so you can refer back to them later.

1. \_\_\_ 16 kg \_\_\_ to \_\_\_ 23 kg \_\_\_
2. \_\_\_ to \_\_\_
3. \_\_\_ to \_\_\_
4. \_\_\_ to \_\_\_
5. \_\_\_ to \_\_\_
6. \_\_\_ to \_\_\_

---

**Part 7a: Making a Formal Inference**

---

We now come to the most important part of the internal, where we have been leading up to the whole time, making a formal inference. This is about linking it back to the population that we care about. To get the interval we look at the bootstrap distributions that we produced earlier.

Make a formal inference for each of the sets of data, the first one has been done for you.

1. From the bootstrapping confidence interval it is a fairly safe bet that forwards median weight will be between 16.0 kg and 23.0 kg more than backs median weight.

2. 

---

---

---

---

---
3. 

---

---

---

---

---
4. 

---

---

---

---

---
5. 

---

---

---

---

---
6. 

---

---

---

---

---

## Part 8: Writing a Conclusion

We also need to make a conclusion that summarises what we have found so far. We need to say what the call is that we are making and why we can make the call (or if we can't make the call). We can only make the call if the entire interval is positive or the entire interval is negative, as if zero is in the interval then there might be a difference of zero or the difference might be the other way round. You also need to discuss the sampling variability. For Merit and Excellence it would be good to talk about what you think the population looks like (and why) and how this will affect the sample.

Make a conclusion for each of the sets of data, the first one has been done for you. You will need to use some extra paper for the last few.

1. Based on looking at my sample I am reasonably confident that back in the population of all rugby players in New Zealand and South Africa that forwards median weight will be more than backs median weight. I can make this call as the confidence interval says that forwards median weight is likely to be between 16.0 kg and 23.0 kg more than backs median weight. I can make the call as the entire confidence interval is positive.  
I am basing this conclusion on the bootstrap confidence interval that I calculated. This involves re-sampling from my original sample of 145 rugby players. I am assuming my original sample was representative of the population of all rugby players. If I were to take another sample, the results may have differed as that sample will contain a different makeup of rugby players.

[illegible][illegible][illegible]

5.

6.

Congratulations, you now have written up a report for 5 different sets of data.

## Part 9a: Writing Your Own Internal 1

Using the framework below write a report on the diamonds data. You can use the sample internal at the end of the booklet to help you if you need it.

### Diamond Testing

Title is given

#### Problem

---

---

---

---

---

---

Comparative question posed and source identified

---

---

---

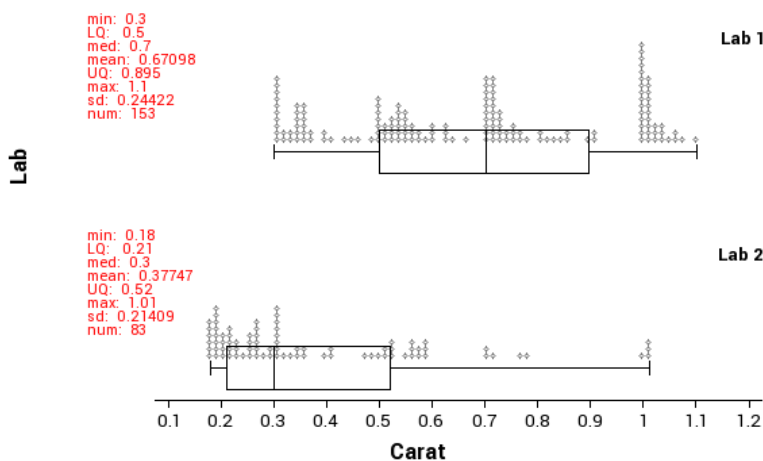
---

---

Variables Identified

#### Data

Diamond Carat by Lab



Dot plots and box and whisker plots are produced with summary statistics

#### Analysis

---

---

---

---

Centre

---

---

---

---

Shift / Overlap

---

---

---

---

Spread

---

---

---

---

Shape

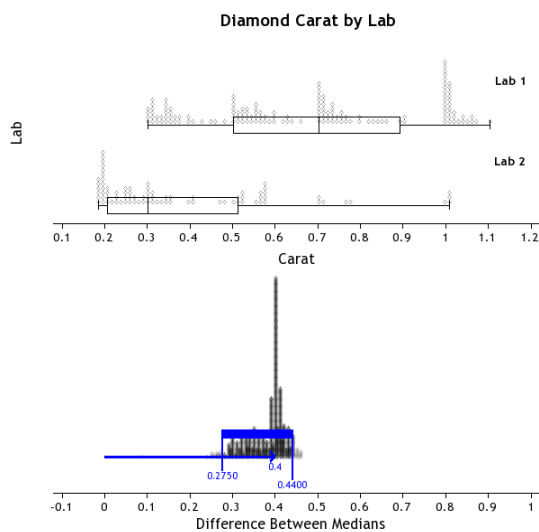
---

---

---

---

Unusual  
Features given  
with possible  
explanations



### Conclusion

---

---

---

---

A formal  
inference is  
made using  
resampling

---

---

---

---

---

---

The question is  
answered

and

---

---

---

---

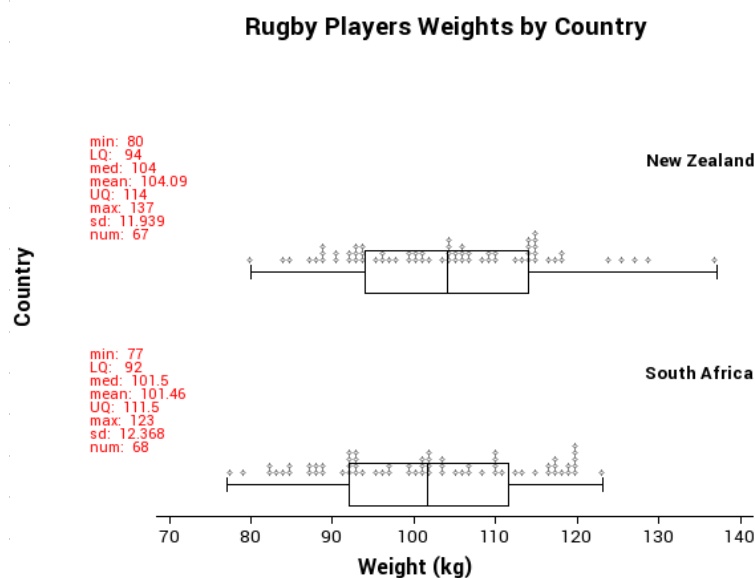
---

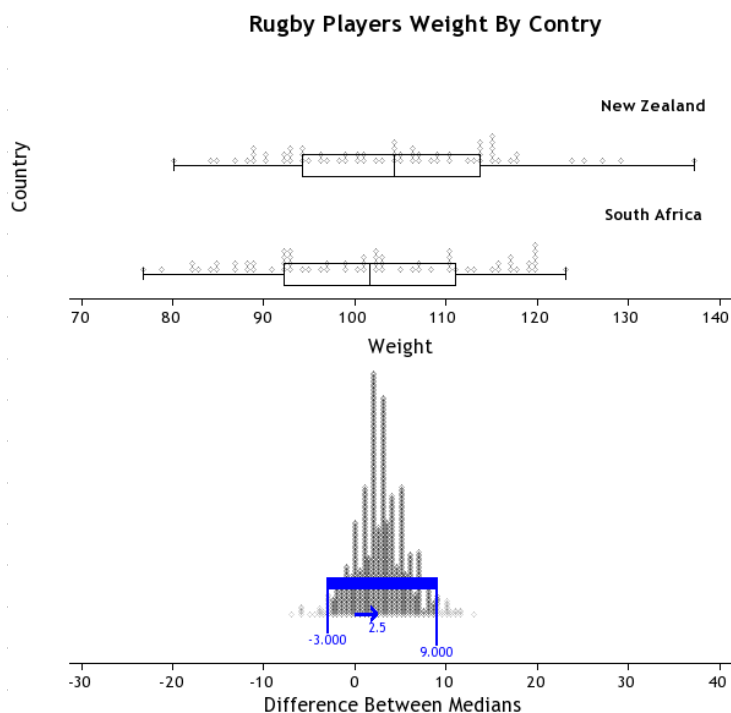
---

sampling  
variation is  
discussed.

This time you have just been provided with a title and graphs. Using these write your own internal.

## Rugby Players and their Country







## Sample Internal (at Achieved level)

### Sports Science and BMI

Title is given

#### Problem

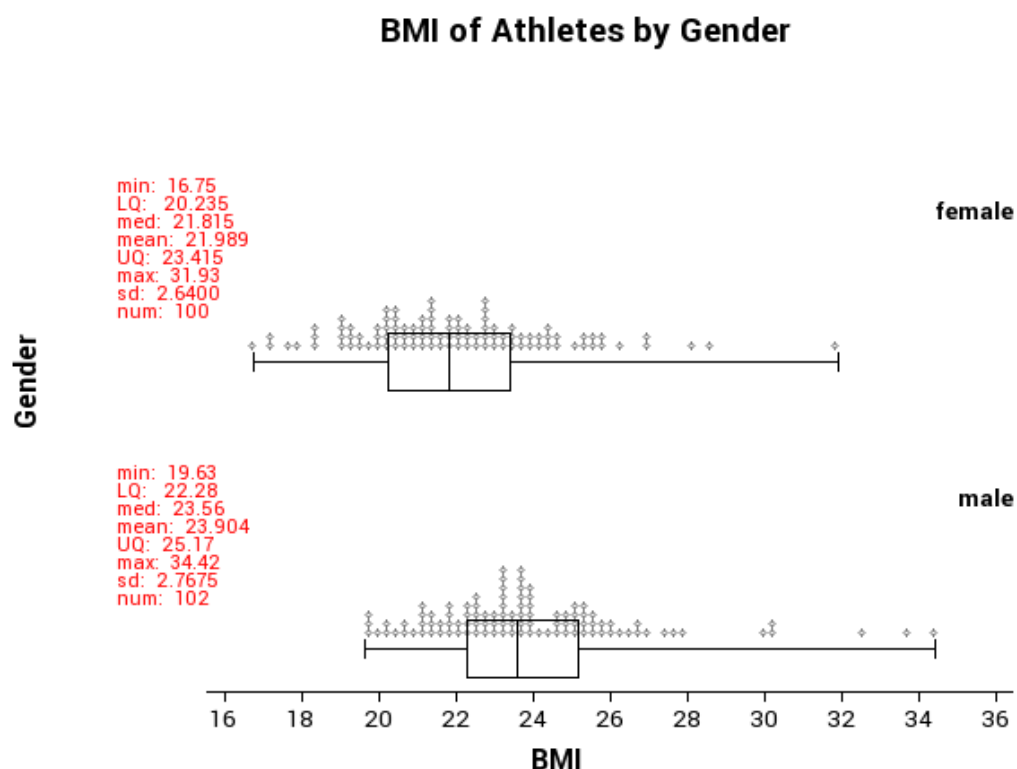
I wonder what the difference is between the median Body Mass Index (BMI) of male and female athletes in the Australian Institute of Sport (AIS) according to a sample provided from the AIS.

Comparative question posed and source identified

BMI is the Body Mass Index, and is calculated by taking the weight in kilograms and dividing by the height in meters squared. Gender is either male or female.

Variables Identified

#### Data



Dot plots and box and whisker plots are produced with summary statistics

#### Analysis

The males' median BMI is 1.74 higher than the females. The middle 50% of the data for females goes from 20.27 to 23.39 whereas the middle 50% of the data goes from 22.29 to 25.16 for the males.

Centre

The median BMI of the males is higher than the upper quartile for the females, and the median BMI for the females is lower than the lower quartile for the males. The males median is 1.74 (3sf) higher than for the females which appears to be about a third of the overall visual spread indicating there might be a difference in the population.

Shift / Overlap

The interquartile range of the BMI for the males is 2.87 whereas for the females it is 3.12. This shows that the females are more spread out than the males, however the standard deviation of the BMI for the males (2.77) is higher than for the females (2.64) indicating that the males are slightly more spread out. Overall visually there is not much difference between how spread out the males and females are.

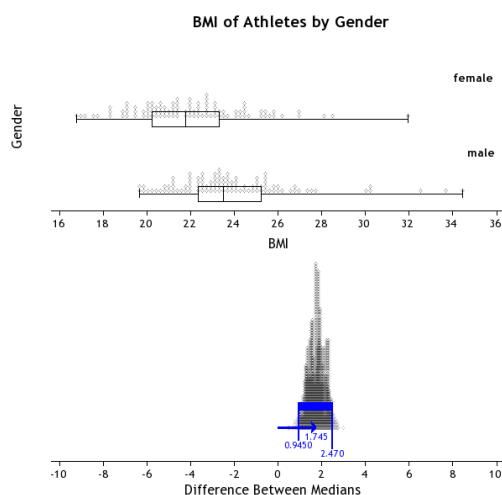
Spread

Both the males and the females BMI is skewed to the right as indicated by the longer tails to the right. Both seem to be reasonably unimodal.

Shape

The females have one data point that is significantly higher than the others. This indicates this female has a much larger BMI than the other female athletes. On looking her up in the data set I found that she is a field athlete with quite a large weight, so she quite possibly is a shot-putter.

Unusual  
Features given  
with possible  
explanations



From the bootstrapping confidence interval I can be reasonably confident that male athletes will have a median BMI that is between 0.97 and 2.44 higher than female athletes median BMI.

A formal  
inference is  
made using  
resampling

### Conclusion

Based on looking at my sample it is a fairly safe bet that back in the population of all athletes at the AIS that male athletes will have a higher median BMI than female athletes. I can make this call as the confidence interval says that

The question is  
answered and

males are likely to have a median BMI between 0.97 and 2.44 higher than females. I can make the call as the entire confidence interval is positive. I am basing this conclusion on the bootstrap confidence interval that I calculated. This involves re-sampling from my original sample of 202 athletes. I am assuming my original sample was representative of the population of all athletes. If I were to take another sample, the results may have differed as that sample will contain a different makeup of athletes.

sampling  
variation is  
discussed.



## Data Set Information

### Babies

The data on 189 births were collected at Baystate Medical Center, Springfield, Mass. during 1986. The goal of this study was to identify risk factors associated with giving birth to a low birth weight baby (weighing less than 2500 grams). Data was collected on 189 women, 59 of which had low birth weight babies and 130 of which had normal birth weight babies.

Variable	Description
LowBirthWeight	No = Birth Weight $\geq$ 2500g Yes = Birth Weight < 2500g
MothersAge	Age of the Mother in Years
Race	Race of the mother
MotherSmoke	Smoking Status During Pregnancy
FTV	Number of Physician Visits During the First Trimester
BirthWeight	Birth Weight in Grams

### BallWear

Data was recorded of students going to the school ball in 2012 as to how much they spent on their clothing and accessories.

Variable	Description
Gender	Boy = new student is male Girl = new student is female
Amount.spent	The amount spent on clothing and accessories in New Zealand Dollars.

### Cars

With rising costs of owning and running a car, and environmental awareness, buyers are becoming more conscious of the features when purchasing new cars. The data supplied is for new vehicles sold in America in 1993.

Variable	Description
Vehicle Name	
Origin	Country of manufacture <ul style="list-style-type: none"> <li>America</li> <li>Foreign</li> </ul>
Price	US \$1000
Type	Small, midsize, large, compact, sporty, van
City	Fuel efficiency in kilometres per litre in cities and on motorways
OpenRoad	Fuel efficiency in kilometres per litre on country and open roads
Drive Train	Front Wheel Drive Rear Wheel Drive
Engine Size	Size in litres
Manual Transmission	Yes No
Weight	Weight of car in Kg

## Diamonds

Every diamond is unique, and there are a variety of factors which affect the price of a diamond. Insurance companies in particular are concerned that stones are valued correctly.

Data on 308 round diamond stones was collected from a Singapore based retailer of diamond jewellery, who had the stones valued.

Variable	Description
Carat	Weight of diamond stones in carat units 1 carat = 0.2 grams
Colour	Numerical value given for quality of colour ranging from 1=colourless to 6=near colourless
Clarity	Average = score 1, 2 or 3 Above average = score 4, 5 or 6
Lab	Laboratory that tested & valued the diamond 1 = laboratory 1 2 = laboratory 2
Price	Price in US dollars

## Kiwi

A sample of kiwi birds around New Zealand was collected in order to help with conservation efforts. The original data is from: <http://www.kiwisforkiwi.org/> and was sourced from the secondary school guides (<http://seniorsecondary.tki.org.nz/Mathematics-and-statistics/Achievement-objectives/AOs-by-level/AO-S7-1>)

Variable	Description
Species	GS-Great Spotted NIBr-North Island Brown Tok-Southern Tokoeka
Gender	M-Male F-Female
Weight(kg)	The weight of the kiwi bird in kg
Height(cm)	The height of the kiwi bird in cm
Location	NWN-North West Nelson    SF-South Fiordland CW-Central Westland    N-Northland EC-Eastern Canterbury    E-East North Island StI-Stewart Island    W-West North Island NF-North Fiordland

Teachers note: this is a synthesised dataset based on real data. At the time of creating the data set there were around 25,000 brown, 17,000 great spotted and 34,500 southern tokoeka. These numbers formed the basis of the data set, but instead of being out of around 76,000 the data set contains around 700 birds.

The data was generated using the population parameters, including gender, location, height, weight and species in Fathom. The size of the population was so that it was too big to use all the data (when doing by hand) but not too big that it couldn't be created for students to use as a "population" to sample from.

### Marathon

The data is a sample taken from marathons in NZ.

It is a simple random sample of 200 athletes.

Variable	Description
Minutes	How many minutes they completed the marathon in
Gender	Male (M) or Female (F)
AgeGroup	Younger (under 40) or older (over 40)
StridelenngthCM	The persons average stride length over the marathon in cm.

### Rugby

The data is real data and comes from <http://www.rugby-sidestep-central.com/>

Variable	Description
Country	New Zealand or South Africa
Position	Forward or Back
Weight	The weight of the player in kilograms (kg)
Height	The height of the player in metres (m)



## Assessment Guidelines – 91582 – Use Statistical Methods to Make a Formal Inference

Text in bold indicated a change from the previous level of achievement.

	Achieved	Merit	Excellence
<b>Problem</b>	The question is a comparison investigative question that clearly identifies the comparison and the population(s).	A comparison investigative question has been posed and <b>includes an explanation for the choice of variables for the investigation.</b>	<b>The research is used to develop the purpose</b> for their investigation and the <b>contextual knowledge is used to pose a comparison investigative question.</b>
<b>Data</b>	Dot plots and box and whisker plots are produced and summary statistics, including the difference between the sample medians, have been calculated.  A bootstrap interval must be constructed and displayed	Dot plots and box and whisker plots are produced and summary statistics, including the difference between the sample medians, have been calculated.  A bootstrap interval must be constructed and displayed	Dot plots and box and whisker plots are produced and summary statistics, including the difference between the sample medians, have been calculated.  A bootstrap interval must be constructed and displayed
<b>Analysis</b>	The sample distributions are discussed and compared in context. This could involve comparing the shift/centre, spread, shape, and unusual features – using features of the displays and the summary statistics.  A formal statistical inference is made by using resampling (bootstrapping) to construct a confidence interval.	The sample distributions are discussed and compared in context. This <b>will</b> involve comparing the shift/centre, spread, shape, and unusual features, <b>with reference to features of the displays and the summary statistics and links to the population or investigative question.</b>  A formal statistical inference is made by using resampling (bootstrapping) to construct a confidence interval.	The sample distributions are discussed and compared in context. This <b>includes seeking explanations</b> for features of the data, which have been identified <b>including justifying the choice of using median and considering the impact</b> of these on the context or investigative question. <b>Reference to knowledge from the research needs to be included in the discussion.</b>  A formal statistical inference is made by using resampling (bootstrapping) to construct a confidence interval <b>with insight.</b>
<b>Conclusion</b>	The formal inference is used to answer the investigative question.  An understanding of sampling variability is evident.	The formal inference is used to answer the investigative question, <b>justifying the call and making links to the context. The conclusion includes an interpretation of the confidence interval.</b>  An understanding of sampling variability is evident.	The formal inference is used to answer the investigative question, justifying the call and <b>linking back to the purpose of the investigation with insight.</b>  The conclusion includes an interpretation of the confidence interval <b>and a discussion of sampling variability. Findings are clearly communicated and linked to the context and populations. There is a reflection on the process or other explanations for the findings have been considered which may involve re-examining the data from a different perspective.</b>

Final grades will be decided using professional judgement based on a holistic examination of the evidence provided against the criteria in the Achievement Standard.