

Part 8.3: Probability it is More Than

Again, just like with the binomial, we often need to work out the probability that it is more than a certain amount. Let's look at an example.

Example

My car has broken down 10 times in the last 8 years. What is the probability it breaks down more than once in the next year?

Answer

Again, the first thing we should do is draw a number line and highlight the part that we want...

0 1 **2 3 4 5...**

And from the last time we did this question we can remember that the mean is 1.25.

(Graphics Calculator)

We go to STAT (2) → DIST (F5) → Across (F6) → Poissn (F1). We want Pcd as we are after up to. In this case $x = 1$ and $\mu = 1.25$ which looks like this:

Poisson C.D
Data : Variable
x : 1
μ : 1.25
Save Res: None

When we press calculate we get 0.6446 (4sf) which is the probability of the part we do not want.

We then do $1 - 0.6446$ to find the probability of the car breaking down more than once is 0.355 (3sf).

(Formula)

We can see that x is not 0 or 1 and $\lambda = 1.25$. This means we need to substitute into the formula 2 times, once for each value of x ... we get

$$P(X = 1) = \frac{1.25^1 e^{-1.25}}{1!} = 0.35813$$

$$P(X = 0) = \frac{1.25^0 e^{-1.25}}{0!} = 0.28650$$

We then add these up giving 0.6446 (4sf).

We subtract from 1 giving 0.355 (3sf).

As you can see these two answers match up.

Exercise 8.3

- The number of kiwi birds in a km^2 in a particular area is on average 20. Calculate the probability there are:
 - More than 25 kiwi birds in a 1 km^2 area.
 - 50 or more kiwi birds in a 3 km^2 area.
 - Exactly 58 kiwi birds in a 3 km^2 area.
 - Between 18 and 22 kiwi birds (inclusive) in a 1 km^2 area.
- The number of books on a shelf in the library is on average 50. What is the probability there are:
 - 60 or more books on a shelf
 - More than 90 books on two shelves?
 - Exactly 95 books on two shelves?
 - Between 45 and 55 books (inclusive) on a shelf?
- The number of cups of coffee sold at a café is on average 15 per hour. Calculate the probability the café sells:
 - More than 20 cups of coffee in a hour.
 - 10 or more cups of coffee in half an hour.
 - Less than 5 cups of coffee in 15 minutes.
 - Between 3 and 5 cups of coffee (inclusive) in 10 minutes.
- The number of calls to a call centre is on average 10 per minute. What is the probability there are:
 - More than 12 calls in a minute?
 - 100 or more calls in 10 minutes?
 - Less than 10 calls in a minute?
 - Between 8 and 12 calls (inclusive) in a minute?