

Case 1 (sampling without replacement) Case 2 (sampling with replacement)

H_1 : the first card to be a heart

K_1 : the first card to be a heart

H_2 : the second card to be a heart

K_2 : the second card to be a heart

Then we have

Then we have

$$P(H_1) = \frac{1}{4}$$

$$P(K_1) = \frac{1}{4}$$

$$P(H_2) = P(H_2 \cap H_1) + P(H_2 \cap H_1^c)$$

$$P(K_2) = \frac{1}{4}$$

$$= P(\text{Both 1st and 2nd are hearts}) +$$

$$+ P(\text{1st is NOT a heart and 2nd is a heart})$$

$$= \frac{13 \times 12}{52 \times 51} + \frac{39 \times 13}{52 \times 51}$$

$$= \frac{1 \cdot 12}{4 \cdot 51} + \frac{3 \cdot 13}{4 \cdot 51}$$

$$= \frac{1}{4}$$

$$P(H_1 \cap H_2) = \frac{13 \times 12}{52 \times 51} = \frac{1}{17}$$

$$\neq P(H_1) \cdot P(H_2) = \frac{1}{16}$$

$$P(K_1 \cap K_2) = \frac{13 \times 13}{52 \times 52} = \frac{1}{16}$$

$$= P(K_1) \cdot P(K_2)$$