

Why APL is a language worth knowing

by Rodrigo Girão Serrão

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About me

Rodrigo Girão Serrão

Formal education: maths

Coding in:

- Python for 9 years
- APL for 2 years

Training/teaching:

- APL (Dyalog Ltd.)
- Python, maths, etc (mathspp.com)



Why APL is a language
worth knowing

“

A LANGUAGE THAT DOESN'T
AFFECT THE WAY YOU THINK
ABOUT PROGRAMMING, IS
NOT WORTH KNOWING.

— Alan J. Perlis

“

A LANGUAGE THAT AFFECTS
THE WAY YOU THINK ABOUT
PROGRAMMING IS WORTH
KNOWING.

— Rodrigo Girão Serrão, 2022?

Disclaimer

Mileage may vary!

What is APL?

What is APL?

- Programming language
 - (was “just” a mathematical notation)
- Array-oriented
- Concise
- Quirky symbols: $\Uparrow \ddot{\bigcirc} \boxtimes \boxdot \rho \neq$

What is APL?

```
15 + 16
31
15 - 14
1
```

What is APL?

31
1
0 1 2 3 4 5

15 + 16
15 - 14
16

What is APL?

			15	+	16	
31						
			15	-	14	
1						
			16			
0	1	2	3	4	5	

What is APL?

31
15 + 16
15 - 14
1
16
0 1 2 3 4 5

What is APL?

31
1
0 1 2 3 4 5

15 + 16
15 - 14
16

What is APL?

10 - 5 - 2

??

What is APL?

`(10 - 5) - 2`

`3`

What is APL?

$(10 - 5) - 2$

3

$10 - 5 - 2$

7

What is APL?

$(10 - 5) - 2$

3

$10 - (5 - 2)$

7

What is APL?

$$(10 - 5) - 2$$

3

$$10 - (5 - 2)$$

7

$$10 - 5 - 2$$



7

Scalar functions

Scalar functions

0 1 2 3 4 5

16

Scalar functions

				$i6$	
0	1	2	3	4	5
				$1+i6$	
1	2	3	4	5	6

Scalar functions

16

0 1 2 3 4 5

$1 + 16$

1 2 3 4 5 6

2×16

0 2 4 6 8 10

Scalar functions

- Scalars make up all arrays
- Scalar functions act on scalars
- Good for processing all data at once

Scalar functions

		10	+	0	1	2	3	4	5
10	11	12	13	14	15				

Scalar functions

10 11 12 13 14 15

10 + 0 1 2 3 4 5

10 11 12 13 14 15

0 1 2 3 4 5 + 10

Scalar functions

10 11 12 13 14 15

		0	1	2	3	4	5	+	10
10	11	12	13	14	15				

200 0 4 100 0 1 × 2 3 4

Scalar functions

Power *

			1	2	3	*	2
1	4	9					

Scalar functions

Power *

1 4 9 1 2 3*2

1 2 4 8 16 32 2*7 6

Scalar functions

Residue I

10 | 1 12 123 1234

1 2 3 4

Scalar functions

Residue |

				10 1	12	123	1234
1	2	3	4				

				2 1	5
0	1	0	1	0	

List comprehensions

List comprehensions

```
# Square integers from 0 to 9:
```


List comprehensions

Square integers from 0 to 9:

```
>>> squares = []
```

List comprehensions

Square integers from 0 to 9:

```
>>> squares = []
```

```
>>> for num in range(10):
```

List comprehensions

Square integers from 0 to 9:

```
>>> squares = []
```

```
>>> for num in range(10):
```

```
...     squares.append(num ** 2)
```

List comprehensions

Square integers from 0 to 9:

```
>>> squares = []
```

```
>>> for num in range(10):
```

```
...     squares.append(num ** 2)
```

```
>>> squares
```

```
[0, 1, 4, 9, 16, 25, 36, 49, 64, 81]
```

List comprehensions

Square integers from 0 to 9:

```
>>> squares = []
```

```
>>> for num in range(10):
```

```
...     squares.append(num ** 2)
```

List comprehensions

Square integers from 0 to 9:

1. Create empty result list

```
>>> for num in range(10):  
...     squares.append(num ** 2)
```

List comprehensions

Square integers from 0 to 9:

1. Create empty result list

2. Go over existing list

```
...     squares.append(num ** 2)
```

List comprehensions

Square integers from 0 to 9:

1. Create empty result list
2. Go over existing list
3. Add modified value to result

List comprehensions

```
# Square integers from 0 to 9:  
squares = []  
for num in range(10):  
    squares.append(num ** 2)
```

List comprehensions

```
# Square integers from 0 to 9:  
squares = [num ** 2 for num in range(10)]
```

List comprehensions

A Square integers from 0 to 9:

List comprehensions

```
a Square integers from 0 to 9:  
[10
```

List comprehensions

A Square integers from 0 to 9:

```
(i*10)*2
```

```
0 1 4 9 16 25 36 49 64 81
```

List comprehensions

```
>>> num = 42
```

```
>>> num % 10
```

```
2
```

List comprehensions

```
>>> numbers = [42, 73, 0, 16, 10]
```

```
>>> num % 10
```

```
2
```

List comprehensions

```
>>> numbers = [42, 73, 0, 16, 10]
>>> [num % 10 for num in numbers]
[2, 3, 0, 6, 0]
```


List comprehensions

```
number ← 42  
10 | number
```

2

List comprehensions

```
numbers ← 42 73 0 16 10  
10 | number
```

2

List comprehensions

```
numbers ← 42 73 0 16 10
```

```
10 | numbers
```

```
2 3 0 6 0
```

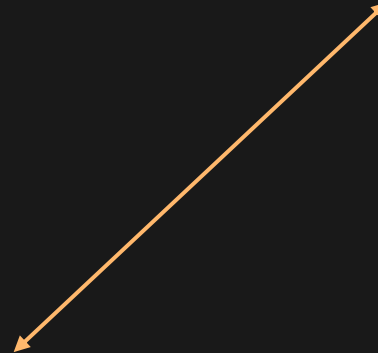
List comprehensions

10 | number

10 | numbers

num % 10

↔ [num % 10 for num in numbers]



List comprehensions

To write:

- Focus on transformation wanted
- Fill in the syntax

Why bother?

- Data transformation is highlighted

Boolean values

Boolean values

- Python, Haskell, ...
 - `True, False`
- Java, JavaScript, ...
 - `true, false`

Boolean values

3 > 2

1 a "true"

Boolean values

3 > 2

1 or "true"

2 > 3

0 or "false"

Boolean values

Maybe weird at first..?

Actually very convenient!

`if` statements:

- If condition is true, run
- If condition is false, don't run

Fine-grained control over arrays?

- Use maths

Data-driven
conditionals

Data-driven conditionals

if statements: “Should we do X?”

vs

DDC: “How should we do X?”

Data-driven conditionals

Car rental:

- \$40/day base price
- + extra fees:
 - \$200 if age ≥ 25
 - \$500 if age ≤ 24

Data-driven conditionals

```
def rental_cost(days, age):  
    price = 40 * days
```

Data-driven conditionals

```
def rental_cost(days, age):  
    price = 40 * days  
    if age >= 25:
```

Data-driven conditionals

```
def rental_cost(days, age):  
    price = 40 * days  
    if age >= 25:  
        price += 200  
    else:  
        price += 500
```


Data-driven conditionals

```
def rental_cost(days, age):  
    price = 40 * days  
    if age >= 25:  
        price += 200  
    else:  
        price += 500  
    return price
```

Data-driven conditionals

```
def rental_cost(days, age):  
    base = 40 * days  
    fees = 200 if age >= 25 else 500  
    return base + fees
```

Data-driven conditionals

$$(40 \times \text{days}) + 200 + 300 \times \text{age} \leq 24$$

Data-driven conditionals

```
age ← 56
```

```
(40 × days) + 200 + 300 × age ≤ 24
```

Data-driven conditionals

```
age ← 56
```

```
(40 × days) + 200 + 300 × 0
```

Data-driven conditionals

```
age ← 56  
(40 × days) + 200 + 0
```

Data-driven conditionals

```
age ← 56  
(40 × days) + 200
```

Data-driven conditionals

```
age ← 23
```

```
(40 × days) + 200 + 300 × age ≤ 24
```


Data-driven conditionals

```
age ← 23
```

```
(40 × days) + 200 + 300 × 1
```

Data-driven conditionals

```
age ← 23
```

```
(40 × days) + 200 + 300
```

Data-driven conditionals

```
age ← 23
```

```
(40 × days) + 500
```

Data-driven conditionals

$$(40 \times \text{days}) + 200 + 300 \times \text{age} \leq 24$$

Data-driven conditionals

Car rental:

- \$40/day base price
- + extra fees:
 - \$200 if age ≥ 25
 - \$500 if age ≤ 24

Data-driven conditionals

Car rental:

- \$40/day base price
- \$200 extra fees
- \$300 possible surcharge (age ≤ 24)

Data-driven conditionals

age \leftarrow 33

days \leftarrow 40

price $\leftarrow (40 \times \text{days}) + 200 + 300 \times \text{age} \leq 24$

price

1800

Data-driven conditionals

```
age ← 33 22 45 73
```

```
days ← 40 40 18 6
```

```
price ← (40×days)+200+300×age≤24
```

```
price
```

```
1800 2100 920 440
```


Data-driven conditionals

```
age ← 33 22 45 73
```

```
days ← 40 40 18 6
```

```
price ← (40×days)+200+300×age≤24
```

```
price
```

```
1800 2100 920 440
```

```
+price
```

```
5260
```

Data-driven conditionals

```
age = [33, 22, 45, 73]  
days = [40, 40, 18, 6]  
prices = []
```

Data-driven conditionals

```
age = [33, 22, 45, 73]
```

```
days = [40, 40, 18, 6]
```

```
prices = []
```

```
for a, d in zip(age, days):
```

Data-driven conditionals

```
age = [33, 22, 45, 73]
days = [40, 40, 18, 6]
prices = []
for a, d in zip(age, days):
    base = 40 * d
    fees = 200 if a >= 25 else 500
```

Data-driven conditionals

```
age = [33, 22, 45, 73]
days = [40, 40, 18, 6]
prices = []
for a, d in zip(age, days):
    base = 40 * d
    fees = 200 if a >= 25 else 500
    prices.append(base + fees)
total = sum(prices)
```

Data-driven conditionals

```
age = [33, 22, 45, 73]
days = [40, 40, 18, 6]
netted = sum(
    40 * d + 200 + 300 * (a <= 24)
    for a, d in zip(age, days)
)
```

Data-driven conditionals

```
age = [33, 22, 45, 73]
days = [40, 40, 18, 6]
netted = sum(
    40 * d + 200 + 300 * (a <= 24)
    (40*days)+200+300 * age<=24
    for a, d in zip(age, days)
)
```

Filtering list comprehensions

Filtering list comprehensions

```
# Square integers:
```

```
>>> nums = [42, 73, 0, 16, 10]
```

```
>>> [n ** 2 for n in nums]  
[1764, 5329, 0, 256, 100]
```

Filtering list comprehensions

Square even integers:

```
>>> nums = [42, 73, 0, 16, 10]
```

```
>>> [n ** 2 for n in nums if n % 2 == 0]  
[1764, 0, 256, 100]
```

Filtering list comprehensions

```
1 0 1 1 1 / 42 73 0 16 10
42 0 16 10
```

Filtering list comprehensions

1 0 1 1 1 / 42 73 0 16 10
42 0 16 10

numbers ← 42 73 0 16 10
0=2 | numbers
1 0 1 1 1

Filtering list comprehensions

1 0 1 1 1 / 42 73 0 16 10
42 0 16 10

numbers ← 42 73 0 16 10
0=2 | numbers
1 0 1 1 1

(0=2 | numbers) / numbers
42 0 16 10

Filtering list comprehensions

```
(0=2 | numbers) / numbers  
42 0 16 10
```

Filtering list comprehensions

```
    (0=2 | numbers) / numbers  
42 0 16 10
```

```
    ((0=2 | numbers) / numbers) * 2  
1764 0 256 100
```

Filtering list comprehensions

List comprehensions with filters:

1. Filter
2. Transform

Counting over a
predicate

Counting over a predicate

Q How many 5s in here?

nums ← 5 3 7 6 4 1 9 2 5 6

Counting over a predicate

Q How many 5s in here?

nums ← 5 3 7 6 4 1 9 2 5 6

5=nums

1 0 0 0 0 0 0 0 1 0

Counting over a predicate

Q How many 5s in here?

nums ← 5 3 7 6 4 1 9 2 5 6

5=nums

1 0 0 0 0 0 0 0 1 0

+ 5=nums

2

Counting over a predicate

How many 5s in here?

```
nums = [5, 3, 7, 6, 4, 1, 9, 2, 5, 6]
```

Counting over a predicate

How many 5s in here?

```
nums = [5, 3, 7, 6, 4, 1, 9, 2, 5, 6]
```

```
count = 0
```

```
for num in nums:
```

Counting over a predicate

How many 5s in here?

```
nums = [5, 3, 7, 6, 4, 1, 9, 2, 5, 6]
```

```
count = 0
```

```
for num in nums:
```

```
    if num == 5:
```

Counting over a predicate

How many 5s in here?

```
nums = [5, 3, 7, 6, 4, 1, 9, 2, 5, 6]
```

```
count = 0
```

```
for num in nums:
```

```
    if num == 5:
```

```
        count += 1
```


Counting over a predicate

How many 5s in here?

```
nums = [5, 3, 7, 6, 4, 1, 9, 2, 5, 6]
```

```
count = 0
```

```
for num in nums:
```

```
    count += (num == 5)
```

Counting over a predicate

How many 5s in here?

```
nums = [5, 3, 7, 6, 4, 1, 9, 2, 5, 6]
```

```
count = sum(num == 5 for num in nums)
```

Counting over a predicate

How many 5s in here?

```
nums = [5, 3, 7, 6, 4, 1, 9, 2, 5, 6]
```

```
count = sum(num == 5 for num in nums)
```

~~+=~~ nums = 5

Counting over a predicate

How many values satisfy the predicate?
`sum(pred(value) for value in values)`

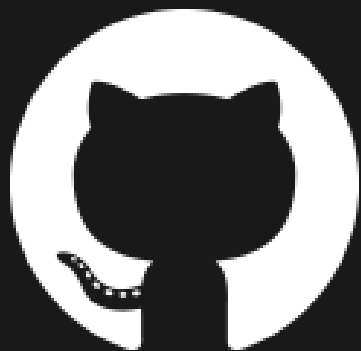
Recap

Recap

- Scalar functions
- Maths instead of branching
 - (data-driven conditionals)
- Compressing vs filtering in list comprehensions
- Counting idiom

References

“Why APL is a language worth knowing”,
<https://mathspp.com/blog/why-apl-is-a-language-worth-knowing>



/mathspp/talks

email

rodrigo@dyalog.com

name

company

site