

**FORMULAE LIST****Circle**

$x^2 + y^2 + 2gx + 2fy + c = 0$  represents a circle centre  $(-g, -f)$ , radius  $\sqrt{g^2 + f^2 - c}$ .

$(x - a)^2 + (y - b)^2 = r^2$  represents a circle centre  $(a, b)$  and radius  $r$ .

**Scalar product**

$\mathbf{a} \cdot \mathbf{b} = |\mathbf{a}||\mathbf{b}| \cos \theta$ , where  $\theta$  is the angle between  $\mathbf{a}$  and  $\mathbf{b}$

or

$$\mathbf{a} \cdot \mathbf{b} = a_1b_1 + a_2b_2 + a_3b_3 \text{ where } \mathbf{a} = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix} \text{ and } \mathbf{b} = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$$

**Trigonometric formulae**

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\sin 2A = 2 \sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A$$

$$= 2 \cos^2 A - 1$$

$$= 1 - 2 \sin^2 A$$

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1. (a) Show that  $(x - 3)$  is a factor of  $x^3 - 6x^2 + 5x + 12$ . (2)

(b) Hence, or otherwise, solve  $x^3 - 6x^2 + 5x + 12 = 0$ . (3)

2. P and Q are the points  $(7, 2)$  and  $(1, 6)$ . (4)  
Find the equation of the perpendicular bisector of PQ.

3. Given that  $f(x) = x^{\frac{3}{2}} - \frac{5}{x^6}$ , where  $x > 0$ , find  $f'(x)$ . (3)

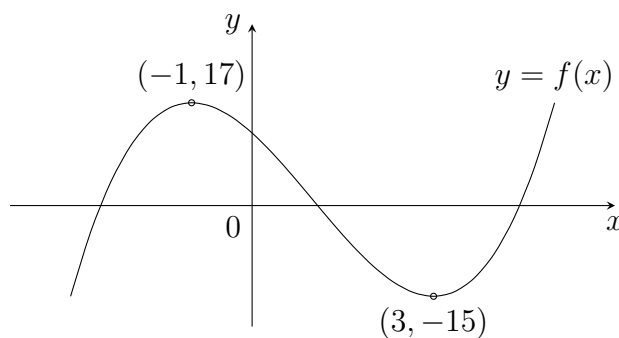
4. A sequence is defined by the recurrence relation  $u_{n+1} = -\frac{1}{3}u_n + 8$  with  $u_3 = 15$ .

(a) Calculate the value of  $u_4$ . (1)

(b) i. Explain why this sequence approaches a limit as  $x \rightarrow \infty$ . (1)

ii. Calculate this limit. (2)

5. The diagram shows part of the graph of a cubic function with equation  $y = f(x)$ . The curve has stationary points at  $(-1, 17)$  and  $(3, -15)$ .

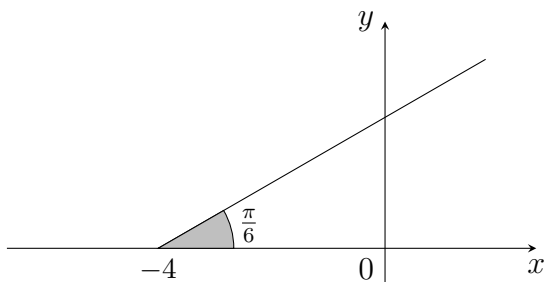


(a) Sketch the graph of  $y = 1 + f(-x)$ . (3)

(b) State the coordinates of the minimum turning point on the graph of  $y = -f(x)$ . (1)

6. Express  $3x^2 - 12x + 25$  in the form  $p(x + q)^2 + r$ . (3)

7. A line passing through  $(-4, 0)$  makes an angle of  $\frac{\pi}{6}$  with the  $x$ -axis, as shown. (3)



Determine the equation of the line.

8. Point Q divides the line PR in the ratio 1 : 3, where  $P(-2, 5, 1)$  and  $Q(-6, -3, 5)$ . (3)  
Determine the coordinates of Q.

9. A function,  $g$ , is defined by  $g(x) = \frac{2 - x}{5}$  where  $x \in \mathbb{R}$ . (3)  
Find the inverse function,  $g^{-1}(x)$ .

10. The equation  $x^2 + (2k - 1)x + k^2 = 0$  has real, distinct roots. (3)  
Determine the range of values for  $k$ .

11. Functions  $f$  and  $g$  are defined by:

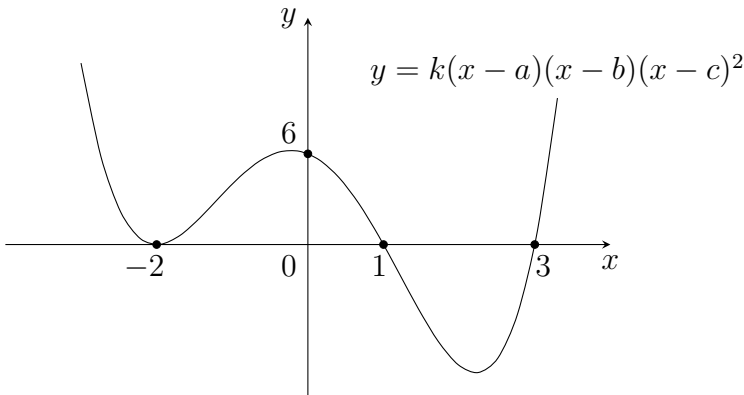
- $f(x) = 2x$
- $g(x) = 2 \cos x$

(a) Determine an expression for  $g(f(x))$ . (1)

(b) Hence, or otherwise, evaluate  $g\left(f\left(\frac{\pi}{3}\right)\right)$ . (2)

(c) Solve  $g(f(x)) = \sqrt{3}$  where  $0 < x < 2\pi$ . (3)

12. The diagram shows  $y = f(x)$  where  $f(x)$  is a quartic function. (3)

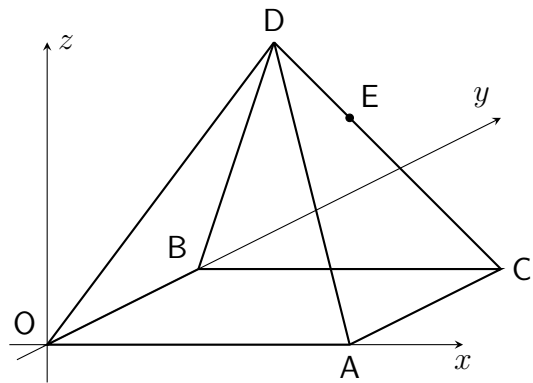


Express  $f(x)$  in the form  $f(x) = k(x - a)(x - b)(x - c)^2$ .

13. (a) Find the  $x$ -coordinates of the stationary points on  $y = x^3 - \frac{9}{2}x^2 + 6x$ .
(3)
- (b) Determine their nature.
(2)
- (c) Hence find the greatest and least values of  $y$  on the interval  $1 \leq x \leq 2$ .
(2)

14. A square based pyramid is shown on the diagram below.

- $\overrightarrow{OD} = 3\mathbf{i} + 3\mathbf{j} + 9\mathbf{k}$
- $\overrightarrow{OA} = 6\mathbf{i}$
- $\overrightarrow{OB} = 6\mathbf{j}$
- E divides CD in the ratio 2:1



- (a) Express vector  $\overrightarrow{CD}$  in terms of  $\mathbf{i}$ ,  $\mathbf{j}$  and  $\mathbf{k}$ .
(2)
- (b) Hence calculate  $|\overrightarrow{ED}|$ .
(2)

Question	Topic	Marks Available	Marks Awarded
1	Polynomials	5	
2	Straight Line	4	
3	Differentiation	3	
4	Recurrence Relations	4	
5	Graph Transformations	4	
6	Quadratic Theory	3	
7	Straight Lines	3	
8	Vectors	3	
9	Sets and Functions	3	
10	Quadratic Theory	3	
11	Sets and Functions/Trigonometry	6	
12	Polynomials	3	
13	Differentiation II	7	
14	Vectors	4	
<b>Total</b>		55	

# ANSWERS - Practice Exam A Paper 1

1. (a) Remainder of 0 so  $(x - 3)$  is a factor.  
(b)  $x = -1, 3, 4$
2.  $2y = 3x - 4$  or  $y = \frac{3}{2}x - 2$
3.  $f'(x) = \frac{3}{2}x^{\frac{1}{2}} + 30x^{-7}$
4. (a)  $u_4 = 3$ 
  - i.  $-1 < -\frac{1}{3} < 1$  so a limit exists.
  - ii. Limit = 6
5. (a) Positive cubic with minimum turning point at  $(-3, -14)$  and maximum turning point at  $(1, 18)$ .  
(b)  $(-1, -17)$
6.  $3(x - 2)^2 + 13$
7.  $y = \frac{1}{\sqrt{3}}x + \frac{4}{\sqrt{3}}$
8.  $Q(-3, 3, 2)$
9.  $g'(x) = 2 - 5x$
10.  $\frac{1}{4} > k$
11. (a)  $g(f(x)) = 2 \cos 2x$   
(b)  $-1$   
(c)  $x = \frac{\pi}{12}, \frac{11\pi}{12}, \frac{13\pi}{12}, \frac{23\pi}{12}$
12.  $f(x) = \frac{1}{2}(x - 1)(x - 3)(x + 2)^2$
13. (a)  $x = 1, x = 2$   
(b) Maximum turning point when  $x = 1$   
Minimum turning point when  $x = 2$   
(c) Max value =  $\frac{5}{2}$ , min value = 2
14. (a)  $-3\mathbf{i} - 3\mathbf{j} + 9\mathbf{k}$   
(b)  $\sqrt{11}$