NAME:

Complete this section without your calculator.

1. (10 points) Define  $f(x) = x^4 - 5x^3 + 8x^2 - 20x + 16$ . One zero of this function is x = 2i. Find all remaining zeros, both real and complex.

- $2.\ (10\ \mathrm{points})$  Evaluate the following logs.
  - (a)  $\log_4 16$

(b)  $\log_2 \frac{1}{8}$ 

(c)  $\log_n n^{4.2}$ 

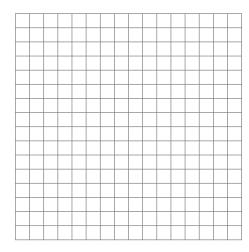
## NAME:

Use your calculator.

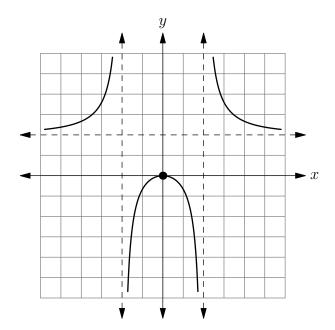
- 3. (5 points) What is the domain of the rational function  $g(x) = \frac{5}{x-3}$ ?
- 4. (22 points) Consider the rational function.

$$R(x) = \frac{x+1}{(x-1)(x+3)}$$

- (a) Analyze the ratio of leading terms to find the end behavior. If the function has a horizontal asymptote or a slant asymptote, give its equation.
- (b) Find the x-intercepts of the graph, if any.
- (c) Find the equations for the vertical asymptotes, if any.
- (d) Give the x-coordinates for the holes, if any.
- (e) Based on your previous work, make a table of x- and y-coordinates for an appropriate choice of test values.
- (f) Graph the function.



5. (10 points) Write an equation for the rational function shown in the graph. The asymptotes are shown as dashed lines.



6. (5 points) Define f(x) = 3x - 5 and  $g(x) = x^2$ . Simplify  $(g \circ f)(x)$ .

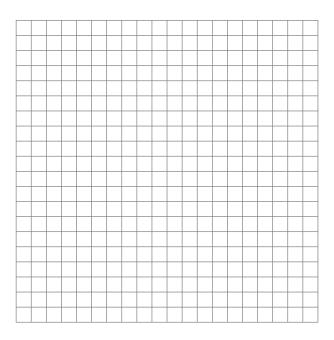
7. (11 points) Give the formula for the inverse function. You may assume that the function is one-to-one without testing.

$$g(x) = \frac{1}{x - 1}$$

8. (8 points) Sketch a picture of the function

$$y = 2 \cdot 3^{x-1}$$

by using transformations. Show the correct shape and at least three correct coordinates.



9. (4 points) Write the expression as a single log.

$$\log_2 u + \log_2 v - \log_2 w$$

10. (16 points) Solve each equation.

(a) 
$$e^x = 100$$

(b) 
$$11 \cdot 3^{x+1} = 88$$

(c) 
$$\log_2 x = 10$$

(d) 
$$\ln(3x+7) + 18 = 40$$

11. (5 points extra credit) Solve the equation  $\log_{15} x + \log_{15} (x-2) = 1$ .