NAME:

Solve the following problems without using a calculator.

1. (15 points) Solve the system using Gaussian elimination. Describe the row operation you are using at each step. (Other methods of solving this problem will not be given credit.)

$$2x + y + z = 22$$
$$x - y = 11$$
$$y - z = -4$$

2. (10 points) Define the following matrices.

$$A = \begin{bmatrix} 4 \\ 2 \\ 6 \end{bmatrix} \qquad B = \begin{bmatrix} -1 & 1 \\ 2 & 0 \end{bmatrix} \qquad C = \begin{bmatrix} -6 & 3 & -3 \end{bmatrix} \qquad D = \begin{bmatrix} -5 & 4 & 7 \\ -1 & 3 & 6 \end{bmatrix}$$

- (a) Based on these definitions, describe each of the following products as defined or undefined.
 - i. DA

iv. DB

ii. DC

v. AC

iii. BD

- vi. CA
- (b) Choose ONE of the answers from part (a) that you said was defined. Calculate the matrix product.