

**MAT 115 Worksheet 10**  
**Thursday, Nov 2 2017**

**Important info:** Welcome to the MAT 115 workshop! My name is **Diego Avalos** (avalosgalvez@cpp.edu), and I will be your workshop facilitator. We meet on Tuesdays and Thursdays from 4 to 5:50 pm in room 4-1-314. My office hour is on Mondays from 11:30 am to 12:30 pm in room 94-219. All worksheets and solutions may be found at the website [www.diegoavalos.net/teaching/mat115workshop2017](http://www.diegoavalos.net/teaching/mat115workshop2017).

Use integration by parts to solve the following integrals.

- |                                |  |  |
|--------------------------------|--|--|
| 1. $\int x e^{3x} dx$          | 5. $\int x \tan^{-1} x dx$                       | 9. $\int \cos \sqrt{x} dx$                   |
| 2. $\int x \sec x \tan x dx$   | 6. $\int \frac{x e^x}{(x+1)^2} dx$               | 10. $\int_0^{\pi/3} \sin 3x \cos x dx$       |
| 3. $\int \ln 5x dx$            | 7. $\int \frac{x^3}{\sqrt{1-x^2}} dx$            | 11. $\int_1^4 \sqrt{x} \ln x dx$             |
| 4. $\int \frac{\ln^2 x}{x} dx$ | 8. $\int \frac{\cot^{-1} \sqrt{x}}{\sqrt{x}} dx$ | 12. $\int_{\pi/6}^{\pi/3} e^{4x} \sin 3x dx$ |

Evaluate the following integrals using trigonometric substitution.

- |                            |   |                                   |
|----------------------------|---|-----------------------------------|
| 13. $\int \sqrt{4-x^2} dx$ | 14. $\int \frac{x^2}{\sqrt{16-x^2}} dx$ | 15. $\int \frac{1}{(4+x^2)^2} dx$ |
|----------------------------|---|-----------------------------------|
16. The region bounded by the curves  $y = \sec x$  and  $y = 2$ , for  $0 \leq x \leq \pi/3$ , is revolved around the  $x$ -axis. What is the volume of the solid generated?
17. The region bounded by the graphs of  $y = (x-2)^2$  and  $y = 4$  is revolved about the line  $y = 4$ . What is the volume of the resulting solid?
18. The region bounded by the graphs of  $y = 2x$ ,  $y = 6 - x$ , and  $y = 0$  is revolved about the line  $y = -2$  and the line  $x = -2$ . Find the volumes of the resulting solids. Which one is greater?