Name:

Mat 115 Worksheet 3 Tuesday, Oct 10 2017

Important info: Welcome to the mat 115 workshops! My name is **Diego Avalos** (avalosgalvez@cpp.edu), and I will be your workshop facilitator. We meet on Tuesdays and Thursdays from 4 to 5:50 pm. My office hour is on Mondays from 11:30 am to 12:30 pm in room 3-2117. All worksheets and solutions may be found at the website **www.diegoavalos.net/teaching/mat115workshop2017**. I want to thank the SIAM president **Camille Michaluk** for covering my workshop today. Thank you **pres**!

Compute the definite integrals in problems 1 to 9.

1.
$$\int_{-\pi}^{\pi} \sin^3(x^5) dx$$

$$4. \int_{-1/2}^{1/2} \frac{1}{\sqrt{1-x^2}} \, dx$$

7.
$$\int_{\pi/4}^{\pi/3} \sec^2 x \, dx$$

2.
$$\int_{\pi/12}^{\pi/6} \sin(2x)\cos(2x) dx$$

5.
$$\int_{-1}^{1} x^{4/3} + 4x^{1/3} dx$$

8.
$$\int_0^{\pi/2} \cos^2 x \, dx - \int_0^{\pi/2} \sin^2 x \, dx$$

3.
$$\int_{-\sqrt{3}}^{1} \frac{1}{1+x^2} \, dx$$

6.
$$\int_{e^{-3}}^{e^3} x^2 + x^{-1} \, dx$$

9.
$$\int_{\pi/6}^{\pi/3} x + \frac{2}{\sin^2 x} - \csc x \cot x \, dx$$

Compute the derivatives in problems 10 to 15.

$$10. \ \frac{d}{dx} \int_1^x \sin(t^2) \, dt$$

$$12. \ \frac{d}{dx} \int_{x}^{0} t \sec t \, dt$$

14.
$$\frac{d}{dx} \int_{1}^{x^3} \sqrt[3]{t} \, dt$$

11.
$$\frac{d}{dx} \int_1^x \sqrt{1-\cos t} \, dt$$

$$13. \ \frac{d}{dx} \int_{-1}^{x} |t| \, dt$$

15.
$$\frac{d}{dx} \int_{x^3}^{x^2} \frac{t^6}{1+t^4} dt$$

16. Let
$$F(x) = \int_4^x \sqrt{t^2 + 9} dt$$
. Find

b.
$$F'(4)$$

c.
$$F''(4)$$

Find the average value of the functions in 17 to 20 in the respective interval.

17.
$$f(x) = 3x$$
; [1, 3]

19.
$$f(x) = \sec x \tan x$$
; $[0, \pi/3]$

18.
$$f(x) = \sin x$$
; $[0, \pi]$

20.
$$f(x) = \sec^2 x$$
; $[-\pi/4, \pi/4]$