

$$B = (-b, a)$$

$$D = (r_3 \cos \alpha, r_3 \sin \alpha)$$

$$C = (-b + r_2 \cos \theta, a + r_2 \sin \theta)$$

$$d = d(C, D) = \sqrt{(r_3 \cos \alpha + b - r_2 \cos \theta)^2 + (r_3 \sin \alpha - a - r_2 \sin \theta)^2}$$

$$P = r_3 \cos \alpha + b, \quad Q = r_3 \sin \alpha - a$$

$$\Rightarrow (P - r_2 \cos \theta)^2 + (Q - r_2 \sin \theta)^2 = d^2$$

$$P^2 - 2Pr_2 \cos \theta + r_2^2 \cos^2 \theta + Q^2 - 2Qr_2 \sin \theta + r_2^2 \sin^2 \theta = d^2$$

$$P^2 + Q^2 + r_2^2 - 2r_2(P \cos \theta + Q \sin \theta) = d^2$$

$$K = \frac{P^2 + Q^2 + r_2^2 - d^2}{2r_2}$$

$$\Rightarrow P \cos \theta + Q \sin \theta = K$$

$$X = \frac{P}{\sqrt{P^2 + Q^2}}; \quad Y = \frac{Q}{\sqrt{P^2 + Q^2}} \Rightarrow X^2 + Y^2 = 1$$

$$\beta = \arccos(X) = \arcsin(Y)$$

$$\begin{aligned} \Rightarrow P \cos \theta + Q \sin \theta &= \sqrt{P^2 + Q^2} (X \sin \theta + Y \cos \theta) = \\ &= \sqrt{P^2 + Q^2} \sin(\theta + \beta) \end{aligned}$$

$$\Rightarrow \theta = \arcsin\left(\frac{K}{\sqrt{P^2 + Q^2}}\right) - \arcsin\left(\frac{Q}{\sqrt{P^2 + Q^2}}\right)$$