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# Notched stress-strain behavior of a conventional and a sequentially annealed highly crosslinked UHMWPE

Michael C. Sobieraj <sup>a,b</sup>, Steven M. Kurtz <sup>c</sup>, A. Wang <sup>d</sup>, Michael M. Manley <sup>e</sup>, Clare M. Rimnac <sup>a,b,\*</sup>

- <sup>a</sup> Musculoskeletal Mechanics and Materials Laboratories, Department of Mechanical and Aerospace Engineering, Case Western Reserve University, Cleveland, OH, USA
- <sup>b</sup> Department of Orthopaedics, Case Western Reserve University, Cleveland, OH, USA
- <sup>c</sup> Drexel University and Exponent, Inc., Philadelphia, PA, USA
- d Stryker Orthopaedics, Mahwah, NJ, USA
- <sup>e</sup> Homer Stryker Center for Orthopaedic Education, Mahwah, NJ, USA

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## ABSTRACT

Contemporary total joint replacement designs contain stress-risers such as fillets, grooves, and undercuts; therefore, it is of interest to analyze the behavior of UHMWPEs in the presence of such designrelated stress-risers. This study examined the engineering and true axial stress-strain behavior of smooth cylindrical and notched cylindrical test specimens, under applied axial tensile loading (2 displacement rates, 37 °C) for a conventional and a highly crosslinked second generation UHMWPE. Both materials were prepared from ram extruded GUR 1050. The conventional material (30 kGy) was gamma sterilized at 30 kGy in an inert N<sub>2</sub> environment. The sequentially annealed material (SA) was gamma irradiated at 30 kGy and annealed for 8 h at 130 °C. The irradiation-annealing process was repeated two more times for an overall irradiation dose of 90 kGy. Differential scanning calorimetry (DSC) was utilized to investigate changes in crystallinity and lamellar thickness distributions upon loading, Fractographic analysis of scanning electron microscope (SEM) images of fracture surfaces was performed to investigate changes in fracture micromechanism with notching. Both the 30 kGy and SA materials, in the smooth condition, demonstrated substantial ductility and orientation hardening. With the introduction of a notch, both materials demonstrated an elevation in the yield stress (notch strengthening) and a reduction in the ultimate stress and ultimate strain at both displacement rates. Additionally, it was found that the uniaxial stress-state (smooth condition) allowed for greater changes in crystallinity and the lamellar thickness distributions, when compared to the untested materials, than the triaxial stressstate induced by the notched geometry.

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## 1. Introduction

For almost four decades ultra-high molecular weight polyethylene (UHMWPE) has been used for bearing component of total joint replacements (TJR). Over one million people a year are treated for various joint problems with TJRs that use UHMWPE as the bearing material. Projections show increasing numbers of younger, more active, patients receiving TJRs, necessitating longer performance of these devices [1,2].

Wear of UHMWPE components is a significant problem due to formation of UHMWPE debris that can cause a biological cascade of events leading to bone resorption and periprosthetic osteolytic implant loosening [3]. To combat this wear problem, crosslinking, using ionizing radiation was reintroduced in the 1990s [4] with

E-mail address: clare.rimnac@case.edu (C.M. Rimnac).

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precautions taken to reduce the amount of residual free radicals generated in the crosslinking process. Both remelting, done above, and annealing, done below the peak melt temperature ( $T_{\rm m}$ ), have been used to combat residual free radicals. Remelting is highly effective at eliminating free radicals [5], but has been shown to decrease crystallinity and lamellar thickness resulting in a decrease in yield stress, ultimate stress, and fatigue crack propagation resistance [4,6]. Annealing does not adversely affect crystallinity [4,6], but does leave some free radicals, which can lead to oxidative degradation of the material [7,8].

Sequential irradiation and annealing has been introduced as a means by which to more effectively reduce free radicals without remelting the material and without adverse changes in crystallinity [9,10]. Sequentially irradiated and annealed UHMWPE has shown promising results in mechanical and aging studies [9,10]. X3<sup>TM</sup> (Stryker Orthopaedics, Mahwah, NJ) is currently the only sequentially irradiated annealed UHMWPE on the market.

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<sup>\*</sup> Corresponding author. Tel.: +1 216 368 6442; fax: +1 216 368 3007. E-mail address: clare.rimnac@case.edu (C.M. Rimnac).

Implant designs contain stress-risers such as fillets, grooves, and undercuts. Therefore, it is of interest to analyze the behavior of UHMWPEs in the presence of design-related stress-risers. Notched monotonic tensile tests of conventional and highly crosslinked UHMWPEs demonstrated that the triaxial stress state induced by the notch resulted in an elevation of axial yield stress (a phenomenon known as notch strengthening), a decrease in orientation hardening, and a change in the fracture micromechanism [11].

The purpose of this study was to investigate the effects of notching and displacement rate on the material properties, notch strengthening, orientation hardening, fracture micromechanism, and concomitant changes in the crystalline regions upon deformation for a conventional and a sequentially annealed UHMWPE. We hypothesized that the sequentially annealed UHMWPE would show notch strengthening, a truncation of orientation hardening, and a change in fracture micromechanism upon notching.

## 2. Materials and methods

## 2.1. Mechanical properties

Two UHMWPE materials made from ram extruded GUR 1050 were examined. The conventional material (30 kGy) was gamma sterilized at 30 kGy in an inert  $N_2$  environment. The sequentially annealed material (SA) was gamma irradiated at 30 kGy and annealed for 8 h at 130 °C. The irradiation-annealing process was repeated two more times for an overall irradiation dose of 90 kGy; this approximated the process used by Stryker Orthopaedics to make  $X3^{\rm TM}$ .

Smooth specimens and notched specimens 100 mm in total length were machined (Fig. 1). The smooth specimens had a gauge diameter of 8 mm, with a tested gauge length of 10 mm. The notched specimens had an outer 8 mm and an inner diameter of 6 mm with a 0.45 mm notch radius (elastic stress concentration factor:  $k_t = 2.69$ ).

Specimens were soaked for 8 weeks in phosphate buffered saline at 37  $^{\circ}\text{C}$  then monotonically loaded to failure in air at 37  $^{\circ}\text{C}$  (4411 electromechanical frame, Instron, Canton, MA). Tests were conducted at both 30 mm/min and 150 mm/min. For each material, notch condition, and rate  $14\pm2$  specimens were tested (116 total specimens).

Smooth specimen engineering strain was obtained using a non-contacting video extensometer (Instron, Canton, MA). For the notched specimens, engineering strain was obtained using a previously developed non-contacting video based method [11]. Custom written MATLAB programs were used for the generation of both engineering and true stress strain curves [11].

## 2.2. Notch strengthening and hardening ratios

For each of the specimens, a notch strengthening ratio was calculated:

$$\varphi_{\sigma} = \frac{\sigma_{y}}{\sigma_{y,\text{smooth}|_{\text{rate}}}} \tag{1}$$

where  $\varphi_{\sigma}$  is the notch strengthening ratio,  $\sigma_{\rm y}$  is the true yield stress of an individual specimen and  $\overline{\sigma_{\rm y,smooth}}$  is the mean true yield stress of the smooth specimens tested at the same displacement rate.

A hardening ratio was also calculated for each of the specimens:

$$\psi_{\sigma} = \frac{\sigma_{\rm u}}{\sigma_{\rm V}} \tag{2}$$

where  $\psi_{\sigma}$  is the hardening ratio,  $\sigma_{u}$  is the true ultimate stress, and  $\sigma_{y}$  is the true yield stress for a specimen.

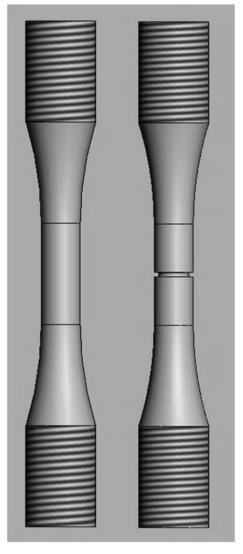
## 2.3. Crystallinity and lamellar thickness distributions

To examine the effect of deformation on crystallinity, differential scanning calorimetry (DSC, Mettler-Toledo DSC 823e, Columbus, OH) was performed on 5 specimens from each of the 8 possible material–geometry–rate combinations as well as for each of the two undeformed materials (60 total DSC crystallinity samples). The samples, approximately 5 mg, were cut from the notched region (notched samples) or from the gauge region directly adjacent to the fracture surface (smooth samples).

Samples were brought to thermal equilibrium at 25 °C and then heated at 10 °C/min to 180 °C. Crystallinity was then calculated using the heat of fusion of a perfect crystal of polyethylene ( $\Delta H_{\rm f}$ , 289.3 J/g), and the area under the curve between 50 °C and 160 °C ( $\Delta H_{\rm m}$ ) [12,13].

$$Crystallinity = \frac{\Delta H_m}{\Delta H_f} \tag{3}$$

Additionally, lamellar thickness (LT) distributions of the crystalline regions were calculated. One sample, approximately 10 mg, was cut from one specimen from each



**Fig. 1.** Illustration of the two geometries of specimens used in this study. Left: smooth; Right: notched.

of the eight material–geometry–rate combinations and from the two undeformed conditions. The samples were heated from 50 °C to 180 °C at 1 °C/min following Stephens et al. [14]. The probability distribution function of lamellar thicknesses, g(l), was found by plotting g(T), mass fraction of crystals melting at a given temperature, vs l(T), lamellar thickness based on the Gibbs equation, as shown in Eqs. (4a) and (4b)[12,15].

$$g(T) = KP(T)(T_{m0} - T)^2$$
 (4a)

$$I(T) = \frac{2\sigma_{\rm e}}{\Delta H_{\rm v}} \frac{T_{\rm m0}}{(T_{\rm m0} - T)} \tag{4b}$$

P(T) is the corrected DSC curve,  $\sigma_{\rm e}=93\times10^{-7}\,{\rm J/cm^2}$  (fold surface energy),  $\Delta H_{\rm v}=280\,{\rm J/cm^3}$  (heat of fusion of crystalline PE), and  $T_{\rm m0}=418.7\,{\rm K}$  (equilibrium melting temperature) [12].

## 2.4. Fracture micromechanism

One fracture surface from each tested specimen was sputter coated with palladium and then documented photographically via stereomicroscopy. The fractures of the notched specimens either exhibited one or two distinct fracture zones (inner and outer zones); when present, the ratio of the radii of the inner zone to that of the entire fracture surface was calculated. A representative fracture surface from each of the eight material–geometry–rate combinations was also examined using scanning electron microscopy (SEM, Hitachi S-4500, Tokyo Japan) at 5 kV.

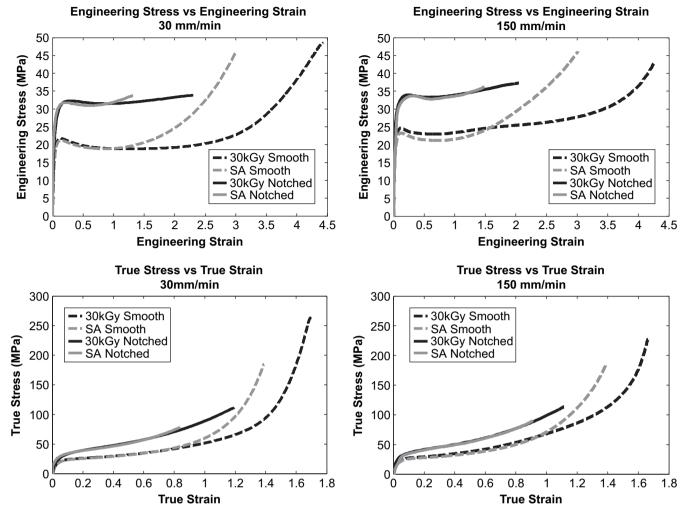


Fig. 2. Representative engineering and true stress-strain curves for each material-geometry-rate combination.

## 2.5. Statistical analyses

To explore differences between individual conditions, two sided *t*-tests were conducted [16]. The individual comparisons for the mechanical properties (true yield stress, and true ultimate stress and strain) along with the hardening ratio were considered. Comparisons were made as follows: *Material Comparisons* (rate and notch condition constant); *Notch Comparisons* (material and rate constant); and, *Rate Comparisons* (material and notch conditions constant). For individual comparisons of the strengthening ratio, only the notched specimens were compared leaving two *Material Comparisons* and two *Rate Comparisons*.

Definitions similar to those used above were used to test for differences between crystallinities of individual groups. The *Notch* and *Rate Comparisons* groups were

identical to those above; however, the *Material Comparisons* group additionally tested the difference between the undeformed (Control) samples of both materials. There were two more comparison groups, 30 kGy and SA *Control Comparisons*, which compared all the mechanically tested conditions of an individual material to the control of that material.

ANCOVAs were performed on the mechanical properties (true yield stress, and true ultimate stress and strain) and the hardening ratio:

$$X = \mu + \alpha[\text{Material}] + \beta[\text{Notch}] + \gamma[\text{Rate}] + \\ \kappa[\text{Material}: \text{Notch}] + \lambda[\text{Material}: \text{Rate}] + \nu[\text{Notch}: \text{Rate}]$$

$$(5)$$

In Eq. (5), "X" is the mechanical property or hardening ratio, "Material" (SA or 30 kGy), "Notch" (Smooth or Notched), and Rate (30 or 150 mm/min) were treated

**Table 1**Mechanical properties, notch strengthening, hardening ratio, and crystallinity for each material–geometry–rate combination ±1 standard deviation

Material	30 kGy				SA			
Geometry	Smooth		Notched		Smooth		Notched	
Rate	30 (n = 12)	150 (n = 13)	30 (n = 14)	150 (n = 14)	30 (n = 16)	150 (n = 16)	30 (n = 15)	150 (n = 16)
Engineering yield stress (MPa)	$21.81 \pm 0.46$	$24.01 \pm 0.46$	$31.55 \pm 1.24$	$34.46 \pm 0.50$	$21.26 \pm 0.88$	$23.39 \pm 0.80$	$31.21 \pm 1.05$	$33.31 \pm 1.49$
Engineering yield strain	$\boldsymbol{0.132 \pm 0.007}$	$\textbf{0.123} \pm \textbf{0.005}$	$\boldsymbol{0.283 \pm 0.077}$	$\textbf{0.223} \pm \textbf{0.040}$	$\textbf{0.134} \pm \textbf{0.009}$	$\textbf{0.125} \pm \textbf{0.003}$	$\textbf{0.253} \pm \textbf{0.056}$	$\textbf{0.261} \pm \textbf{0.045}$
True yield stress (MPa)	$24.70 \pm 0.43$	$26.96 \pm 0.45$	$40.40\pm1.03$	$\textbf{42.14} \pm \textbf{1.22}$	$24.10 \pm 0.89$	$26.30 \pm 0.86$	$39.10 \pm 2.05$	$42.00 \pm 2.13$
True yield strain	$\boldsymbol{0.125 \pm 0.007}$	$\textbf{0.116} \pm \textbf{0.004}$	$\boldsymbol{0.248 \pm 0.057}$	$\textbf{0.201} \pm \textbf{0.032}$	$\textbf{0.125} \pm \textbf{0.008}$	$\textbf{0.117} \pm \textbf{0.003}$	$\textbf{0.224} \pm \textbf{0.046}$	$\boldsymbol{0.232 \pm 0.036}$
Engineering ultimate stress (MPa)	$47.80 \pm 1.84$	$42.14 \pm 6.03$	$33.41 \pm 0.63$	$37.05 \pm 0.58$	$43.61 \pm 4.44$	$44.36 \pm 4.70$	$\textbf{33.14} \pm \textbf{1.26}$	$36.20 \pm 1.61$
Engineering ultimate strain	$4.353 \pm 0.118$	$4.251\pm0.285$	$\boldsymbol{2.084 \pm 0.274}$	$\boldsymbol{2.030 \pm 0.357}$	$2.972 \pm 0.185$	$\boldsymbol{2.923 \pm 0.271}$	$\textbf{1.465} \pm \textbf{0.194}$	$\textbf{1.444} \pm \textbf{0.242}$
True ultimate stress (MPa)	$256.05 \pm 14.733$	$222.82 \pm 43.13$	$103.10 \pm 10.32$	$112.39 \pm 14.49$	$173.91 \pm 24.06$	$175.15 \pm 28.43$	$81.71 \pm 7.25$	$88.33 \pm 8.23$
True ultimate strain	$\boldsymbol{1.677 \pm 0.022}$	$1.657 \pm 0.055$	$\textbf{1.122} \pm \textbf{0.088}$	$1.103 \pm 0.113$	$\textbf{1.378} \pm \textbf{0.048}$	$\textbf{1.364} \pm \textbf{0.074}$	$\boldsymbol{0.899 \pm 0.079}$	$\boldsymbol{0.889 \pm 0.100}$
Notch strengthening	$\boldsymbol{1.000 \pm 0.018}$	$\boldsymbol{1.000 \pm 0.017}$	$\textbf{1.635} \pm \textbf{0.042}$	$\textbf{1.563} \pm \textbf{0.045}$	$\boldsymbol{1.000 \pm 0.037}$	$\boldsymbol{1.000 \pm 0.033}$	$\textbf{1.622} \pm \textbf{0.087}$	$\boldsymbol{1.555 \pm 0.045}$
Hardening ratio	$10.37\pm0.652$	$\textbf{8.267} \pm \textbf{1.612}$	$2.552 \pm 0.243$	$\boldsymbol{2.664 \pm 0.293}$	$7.230 \pm 1.071$	$6.676\pm1.158$	$\boldsymbol{2.096 \pm 0.219}$	$2.112 \pm 0.258$
Undeformed (control) crystallinity ( $n = 5$ )	$60.37 \pm 1.68$				$58.94 \pm 2.04$			
Crystallinity $(n = 5)$	$56.98 \pm 0.98$	$\textbf{56.27} \pm \textbf{3.29}$	$56.45 \pm 1.54$	$60.25 \pm 5.43$	$54.08 \pm 1.11$	$55.49 \pm 2.25$	$58.06 \pm 2.18$	$\textbf{56.76} \pm \textbf{1.26}$

Note that the *n* values presented at the column headings are for the tensile tests, not for the crystallinity data.

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1

as categorical variables. ANCOVAs were also used to compare notch strengthening between notched test groups:

$$\varphi_{\sigma} = \mu + \alpha[\text{Material}] + \gamma[\text{Rate}] + \lambda[\text{Material}: \text{Rate}]$$
 (6)

An ANCOVA was performed on the crystallinity data:

Crystallinity = 
$$\mu + \alpha[\text{Material}] + \beta[\text{Deformation}] + \gamma[\text{Rate}] + \kappa[\text{Material}: \text{Deformation}] + \lambda[\text{Material}: \text{Rate}] + \nu[\text{Deformation}: \text{Rate}]$$
 (7)

where "Material" has the same definition as above and "Deformation" describes one of three specimen stress states: None (control/undeformed material); Uniaxial (smooth specimen); Triaxial (notched specimen). Also, for "Rate," in addition to the 30 and 150 mm/min rates, a rate of 0 mm/min was used for the control/undeformed specimens.

The ANCOVAs were conducted so that the interaction terms (e.g., "Material:Notch,") could be included to test for interactions between predictor variables.

Student's t-test was used to examine the differences in the  $r_{\rm inner\ zone}/r_{\rm specimen}$  ratio (calculated when specimens had a two-zone fracture mechanism) between material–rate combinations for the notched geometry. For all analyses, p < 0.05 was taken as significant.

## 3. Results

## 3.1. Mechanical properties

Both the 30 kGy and SA materials, in the smooth condition, demonstrated substantial ductility and orientation hardening (Fig. 2). With the introduction of a notch, both materials demonstrated an elevation in the yield stress (notch strengthening) and a reduction in the ultimate stress and ultimate strain at both displacement rates (Table 1).

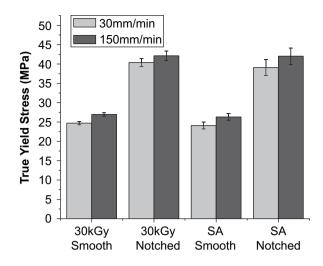
For true yield stress, three of the *Material Comparisons*, all of the *Notch Comparisons*, and *Rate Comparisons* were found to be significantly different (Fig. 3, Table 2). The true yield stress was generally lower for the SA compared to the 30 kGy material (2.4–3.2%), notching increased the true yield stress for both materials (55–64%), and increasing rate increased true yield stress (4.3–9.1%). Material, Notch, and Rate were the only significant predictors for true yield stress (Eq. (5), Table 3).

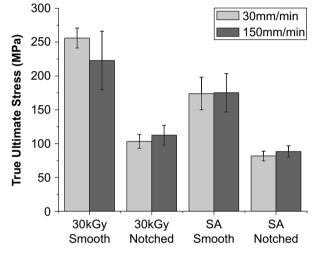
For the true ultimate stress, all of the *Material Comparisons*, all of the *Notch Comparisons*, and two of the *Rate Comparisons* were found to be significantly different (Fig. 3, Table 2). The true ultimate stress of the SA material was lower than that of the 30 kGy material (21–32%) notching decreased the true ultimate stress for both materials (50–60%). Material, Notch, and the Material:Notch interaction were the only significant predictors for true ultimate stress.

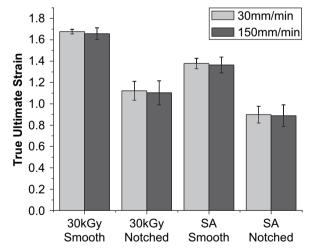
For the true ultimate strain, all of the *Material Comparisons* and all of the *Notch Comparisons* were found to be significantly different, however, none of the *Rate Comparisons* were found to be significantly different (Fig. 3, Table 2). The true ultimate strain of the SA material was lower than that of the 30 kGy material (18–20%) notching decreased in the true ultimate strain for both materials (33–35%). Material, Notch, and the Material:Notch interaction were the only significant predictors for true ultimate strain (Eq. (5), Table 3).

For notch strengthening, none of the *Material Comparisons* and one of the *Rate Comparisons* were found to be significantly different. An increase rate was found to lower notch strengthening (4.3%) for the 30 kGy material (Fig. 4, Table 2). Rate was the only significant predictor for notch strengthening (Eq. (6), Table 3).

For the hardening ratio, all of the *Material Comparisons*, all of the *Notched Comparisons*, and only one of *Rate Comparisons* were found to be significantly different (Fig. 4, Table 2). The SA material had a lower hardening ratio compared to the 30 kGy material (18–30%), notching decreased the hardening ratio for both materials (68–75%), and increasing rate decreased the hardening ratio (20.3%) for the smooth 30 kGy material. All of the predictors were found to be significant with the exception of the Notch:Rate interaction for the hardening ratio (Table 3, Eq. (5)).







**Fig. 3.** Bar charts showing the true yield stress, true ultimate stress, and true ultimate strain for each material–rate–geometry combination. Error bars indicate  $\pm 1$  standard deviation.

## 3.2. Crystallinity and lamellar thickness distributions

The crystallinity of all of the specimens, regardless of deformation, was between 54 and 60% (Table 1). For the crystallinity, three of the 30 kGy *Control Comparisons*, two of the SA *Control Comparisons*, two of the *Material Comparisons*, one of the *Notch Comparisons*, and none of the *Rate Comparisons* were found to be

**Table 2**Table showing the *p*-values of the individual *t*-tests for the true mechanical properties and the notch strengthening and hardening ratios

			True yield stress	True ultimate stress	True ultimate strain	Notch strengthening	Hardening ratio
Material comparisons		_					
30 kGy vs SA	Smooth	30 mm/min	0.0284	< 0.001	< 0.001		< 0.001
		150 mm/min	0.0144	0.0027	< 0.001		0.0070
	Notched	30 mm/min	0.0450	< 0.001	< 0.001	0.6052	< 0.001
		150 mm/min	0.8176	< 0.001	< 0.001	0.1675	< 0.001
Notch comparisons							
Smooth vs notched	30 kGy	30 mm/min	< 0.001	< 0.001	< 0.001		< 0.001
		150 mm/min	< 0.001	< 0.001	< 0.001		< 0.001
	SA	30 mm/min	< 0.001	< 0.001	< 0.001		< 0.001
		150 mm/min	< 0.001	< 0.001	< 0.001		< 0.001
Rate comparisons							
30 mm/min vs 150 mm/min	30 kGy	Smooth	< 0.001	0.0194	0.2364		< 0.001
		Notched	< 0.001	0.0625	0.6057	< 0.001	0.2818
	SA	Smooth	< 0.001	0.8951	0.5389		0.1702
		Notched	< 0.001	0.0240	0.7499	0.4025	0.8479

significantly different (Table 4). Only Deformation was found to be significant for crystallinity (p = 0.009).

For both materials, the LT distributions (Fig. 5) for the smooth specimens demonstrated a qualitative difference compared to the control (undeformed) condition. The 30 kGy LT distribution showed a distinct narrowing of the peak, while the SA material showed a broadening of the peak and the emergence of a bimodal shape. The LT distributions of the notched specimens were qualitatively similar to the control (undeformed) conditions.

## 3.3. Fracture micromechanism

The fracture surfaces of all the smooth specimens (both materials and both rates) were consistent with a previously described fracture micromechanism: void coalescence, slow crack growth to

critical flaw, followed by fast fracture (Fig. 6) [17]. The notched specimens showed either a one-zone or two-zone type fracture pattern (Fig. 7). Fractures showing the one-zone pattern all appeared to have a fracture initiation point on the notch surface, with fast fracture first propagating inward and then radiating outward (Fig. 7). Fracture surfaces showing the two-zone pattern all had an outer stress whitened region. The fractures appeared to have initiated circumferentially at the notch surface; this was followed by a region of stable crack growth, and then by fast fracture (Figs. 7 and 8). The stable crack growth region for the two-zone fracture showed ripples and buckles [17] consistent with the stable crack growth region of the smooth specimens. The one-zone versus two-zone fracture pattern was affected by material; all of the SA specimens at both displacement rates failed by a one-zone fracture mechanism. For the 30 kGy material, all of the 30 mm/min

**Table 3**ANCOVA results for mechanical properties and the hardening and notch strengthening ratios

X	Materi	al	Notch		Rate		Material:Notch	Material:Rate	Notch:Rate
True yield stress	_	0.017	+	< 0.001	+	< 0.001	0.869	0.260	0.776
True ultimate stress	_	< 0.001	_	< 0.001	_	0.379	< 0.001	0.065	0.008 <sup>a</sup>
True ultimate strain	_	< 0.001	_	< 0.001	_	0.269	0.009	0.779	0.946
Notch strengthening	_	0.444			+	0.008		0.225	
Hardening ratio	-	< 0.001	_	< 0.001	-	0.004	<0.001	0.030	0.120

For the first order predictors the first column shows whether increasing the predictor variable was found to increase or decrease X. The baseline values for the three predictors are 30 kGy, smooth, and 30 mm/min, respectively.

<sup>&</sup>lt;sup>a</sup> Indicates interaction terms that were found significant numerically but are not considered significant because at least one of the two individual predictors in the interaction were not found significant.

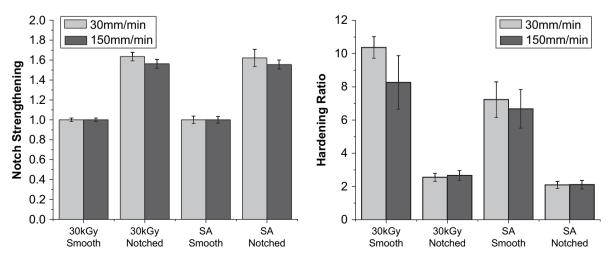


Fig. 4. Bar charts showing the notch strengthening and the hardening ratios for each material-geometry-rate combination. Error bars indicate  $\pm 1$  standard deviation.

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**Table 4**Table showing the results of the individual *t*-tests for percent crystallinity for each material–geometry–rate combination along with the respective control (undeformed) data

30 kGy control comparisons			p-value
30 kGy Control vs 30 kGy	Smooth	30 mm/min	0.0046
		150 mm/min	0.0380
	Notched	30 mm/min	0.0049
		150 mm/min	0.9635
SA control comparisons			
SA Control vs SA	Smooth	30 mm/min	0.0016
		150 mm/min	0.0349
	Notched	30 mm/min	0.5317
		150 mm/min	0.0767
Material comparisons			
30 kGy vs SA	Control		0.2596
	Smooth	30 mm/min	0.0023
		150 mm/min	0.6732
	Notched	30 mm/min	0.2133
		150 mm/min	0.1992
Notch comparisons			
Smooth vs Notched	30 kGy	30 mm/min	0.5326
		150 mm/min	0.1989
	SA	30 mm/min	0.0066
		150 mm/min	0.3043
Rate comparisons			
30 mm/min vs 150 mm/min	30 kGy	Smooth	0.6557
		Notched	0.1708
	SA	Smooth	0.2434
		Notched	0.2805

specimens failed by a two-zone fracture mechanism, whereas at 150 mm/min 7/15 (46.7%) failed by a one-zone fracture mechanism. For the 30 kGy specimens that failed by a two-zone fracture mechanism, the ratio of radii ( $r_{\rm zone1}/r_{\rm specimen}$ ) was not significantly different between 30 mm/min and 150 mm/min groups (p=0.29).

#### 4. Discussion

The objectives of this study were to investigate the effects of notching and displacement rate on the material properties, the fracture micromechanism, and the amount and nature of the crystalline regions for a conventional and a sequentially annealed UHMWPE. It was found that several of the mechanical properties were rate dependent and all of them were stress-state (notch) dependent. It was also found that the effect of stress-state (notch) was much larger in magnitude than the effect of rate on mechanical properties.

Both the 30 kGy and SA materials showed an increase in true yield stress and a decrease in true ultimate stress and strain upon the introduction of a notch. This is consistent with our previous study of four different formulations of UHMWPE (two conventional and two highly crosslinked) tested under ambient laboratory conditions [11].

The 30 kGy and SA materials were found to have similar tensile stress–strain behavior up to yield, in both the smooth and notched specimen test conditions; accordingly, they also had similar notch strengthening ratios. In contrast, the ultimate properties of the two materials were found to be significantly different in both the smooth and notched specimen conditions. The SA material had a lower ultimate stress and strain in both the smooth and notched conditions compared with the 30 kGy material. However, the presence of a notch decreased both the ultimate properties and hardening ratio more for the 30 kGy material than for the SA material. This is consistent with the fact that the SA material is more crosslinked than the 30 kGy material, and hence, undergoes more limited orientation hardening even in the smooth condition.

An increase in rate resulted in an increase in yield stress for both materials in both the smooth and notched conditions, as would be expected [18]. Interestingly, rate was not found to significantly

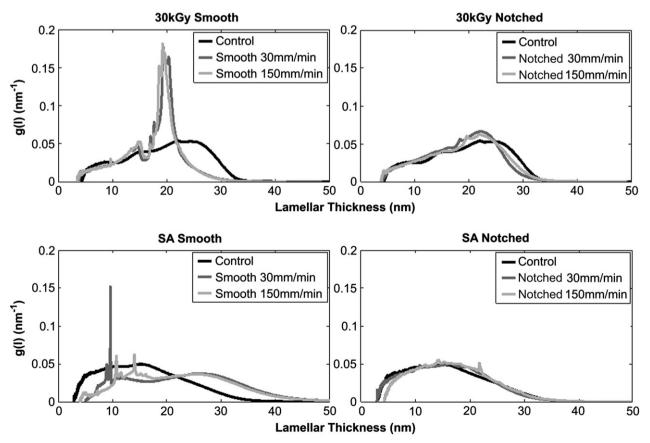
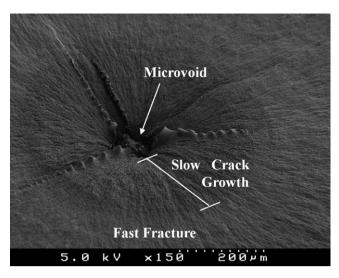


Fig. 5. Lamellar thickness distributions for all material-geometry-rate combinations with their respective control (undeformed) distributions.



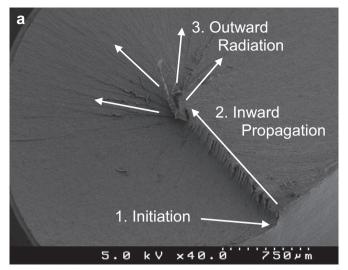
**Fig. 6.** Representative SEM fractograph of a smooth specimen fracture surface showing the three regions of fracture present for all the smooth specimens in both materials. (This image is of a SA specimen tested at 150 mm/min.)

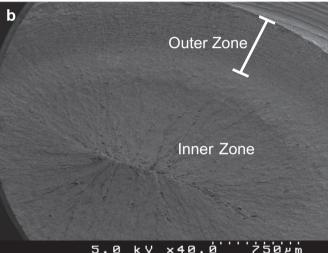
influence true ultimate stress, nor true ultimate strain, and therefore the ultimate properties of the two materials showed similar rate sensitivities. However, the hardening ratio was rate dependent (due to the rate dependency of the yield stress), with rate appearing to affect the 30 kGv material more than the SA material.

Several studies have shown that there are changes in crystal-linity, orientation, and/or lamellar morphology that occur to the crystalline regions of UHMWPE upon loading under a variety of stress states, both in laboratory tests [19–21] and in retrieval studies [22,23]. To our knowledge, however, this is the first study to directly consider the difference in morphological evolution of crystalline lamellae of UHMWPE under uniaxial and triaxial stress states.

The uniaxial tensile deformation process for a non-crosslinked semicrystalline polymer is a several stage process involving tie molecule stretching, crystalline lamellar rotation and alignment, fine slip, course slip (which is when yielding occurs [25,26]), fragmentation of lamellae, and finally chain alignment with further destruction of lamellae [24]. Together, these events can result in a decrease in crystallinity due to tensile deformation. Therefore, since there is an elevation in the axial yield stress of these materials upon notching, it is likely that the triaxial stress state has hindered these mechanisms. In support of this is the finding that the smooth specimens demonstrated a small but generally significant reduction in crystallinity compared to the undeformed condition, while the notched specimens generally did not (Table 4).

Additional support for this hypothesis comes from the results of the LT distribution plots (Fig. 5). Both materials showed LT distributions for uniaxial deformation that were distinct in shape from that of the control (undeformed) condition, while the LT distributions of the notched specimens were qualitatively similar to those of their respective controls. The LT distributions of the uniaxially stressed 30 kGy material show a narrowed and elevated peak when compared to the LT distribution of the undeformed 30 kGy material. This is consistent with experiments by Alberola and Perez [27] on a high molecular weight linear PE (approximate molecular weight of  $6 \times 10^{5}$ ) in which they concluded that the narrowing of the LT distribution upon plastic deformation via rolling was due to breakdown of thicker crystals. Additionally, the narrowing of the LT distribution for the 30 kGy material was likely due in part to relaxation of the sample during partial melting and reorganization [28]. The finding that the notched samples (exposed to a triaxial stress state), had an LT distribution similar to the controls is indicative of suppression of these deformation mechanisms within the crystalline lamellae.

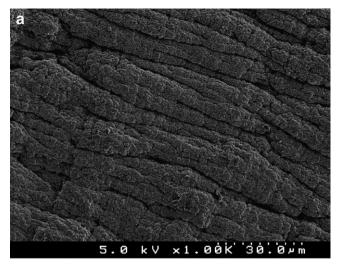


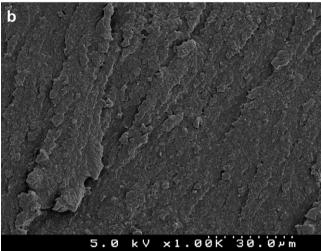


**Fig. 7.** Representative SEM fractographs showing the two fracture patterns seen in the notched specimens in this work. (a) One-zone pattern (SA 30 mm/min); (b) two-zone pattern (30 kGy 30 mm/min).

For the SA material, the uniaxially deformed specimens showed a broadening of the peak, which could be mistaken for growth of thicker crystals upon the onset of uniaxial plastic deformation. However, if molecules are permanently crosslinked, the melt temperature of some of the crystals is increased due to elastic strains that remain on them due to the deformed network [28]. This would result in the broadening of the LT distribution. Therefore, it is likely that there is no growth of thicker crystals, as the distribution curve suggests, but that broadening is an artifact of residual elastic strains in some of the crystalline regions. The shape of the LT distribution for the smooth specimens includes other features that are distinct from both the notched and control specimens such as spikes (that could be indicative of increased populations of crystals of specific sizes, or of relaxation phenomena) and a bimodal shape. The LT distributions of the notched samples (exposed to a triaxial stress state) were similar to the control LT distributions. This suggests that the crystalline regions in the notched specimens are not subjected to residual elastic strains nor are they subjected to the other deformation mechanisms that could be present in the smooth SA specimens.

A two-zone fracture pattern was observed for all of the notched 30 kGy specimens at the lower displacement rate and for 46.7% of them at the higher displacement rate, but not for any of the SA notched specimens (Figs. 7 and 8). The outer zone resembles what





**Fig. 8.** Representative SEM fractographs showing higher magnification view of both zones in the two-zone fracture pattern. (a) Outer Zone; (b) Inner Zone (notched 30 kGy 30 mm/min).

has previously been identified, in smooth specimen studies by both Medel et al. [29] and Gencur et al. [17], as a region of slow stable crack growth. The inner zone resembles the fast fracture region reported in these two works. In tests of notched specimens of HDPE, Goolsby and Chatterjee [30] observed stress whitened zones on the fracture surface in the region of crack initiation. They concluded that these regions were regions of slow stable deformation and crack growth, while the interior regions were regions of rapid, final specimen separation. In our study, we observed that the outer zone was stress whitened relative to the inner zone. Taken together, the works of Medel et al., Gencur et al., and that of Goolsby and Chatterjee support the conclusion that the outer zone underwent slow/ductile crack growth and that the inner zone underwent fast/brittle fracture.

A one-zone fracture appearance (Fig. 7) was observed for all the notched SA specimens at both displacement rates, and only for 53.3% of the 30 kGy specimens at the higher displacement rate. The fracture surfaces are similar to the inner zone of the two-zone fractures in this work, and to the fast fracture region in the work of Medel et al. [29] and Gencur et al. [17]. Therefore, it appears as if the one-zone fracture appearances are indicative of a completely brittle/fast fracture micromechanism of fracture. These findings support the conclusion that the 30 kGy material is capable of more ductile fracture than the SA material.

A limitation of the study was that only one notch geometry was examined. Therefore, the differences or the magnitude of the differences between the materials and geometries observed within this study may change with more or less severe notch geometries. Another limitation of this work was that only one sample from each test group was used to examine differences in LT distribution between groups. Thus, the LT distribution findings are suggestive, but not conclusive.

## 5. Conclusions

This work supports that the monotonic stress–strain and fracture behavior of UHMWPE materials is a function of stress-state (uniaxial vs triaxial) and material (conventional vs second generation highly crosslinked). It has also been shown that a triaxial stress-state alters crystalline morphology of UHMWPE materials to a lesser degree than a uniaxial stress-state. This study also demonstrates that changes in fracture micromechanism induced by a triaxial stress state can be further affected by changes in the displacement rate.

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