WT 2022/2023

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Lab Course Scientific Computing

Worksheet 1

distributed: Thu., 10.11.2022 due: Sun., 20.11.2022, 23:59 (submission on the Moodle page) oral examination: Tue., 22.11.2022 (exact time slots announced on the Moodle page)

In this worksheet, we study some numerical aspects of the classical two-player game rock-paper-scissors, using MATLAB. In particular, we focus on simple strategies that, in the long run, could benefit both the computer and the human player. The provided files are:

- game.m contains the initialization of the game and most of the logic (e.g. handling events) related to the GUI. Use this to run the game. The file may be modified
- game.fig contains the graphical user interface and should not be modified
- mchoice.m contains the "brain" of the game. The file may be modified
- gen_human_move.m is a function that generates moves for the human player. It can be used to run a user-defined number of rounds automatically. For the purposes of this worksheet, it should not be modified

The GUI contains a button Save data that permits you to create a .mat file containing the last transition matrix of the game and the results after each round.

- a) In mchoice.m, fill in the implementation of predict1 such that
 - i) it takes two input arguments, j the previous move of the human player, and transm the current predicted transition matrix for the human player
 - ii) it prints the input parameter transm
 - iii) it uses two global variables $param_{-}a, param_{-}b$ satisfying $0 \le param_{-}a \le param_{-}b \le 1$
 - iv) it computes the variable *hnext*, representing the *predicted next move of the human player*, using the following algorithm:
 - 1) Generate a sample from the standard *uniform* probability distribution using the built-in function rand.
 - 2) Using the modulo function, compute *hnext* as

$$hnext = \begin{cases} mod(j,3) + 1 & \text{with probability } param_a \\ mod(j+1,3) + 1 & \text{with probability } param_b - param_a \\ j & \text{with probability } 1 - param_b \end{cases}$$
(1)

using the generated uniform random variable to decide which branch to follow.

- v) it returns the variable next = winchoice(hnext)
- b) Analyze the three prediction policy functions (the one implemented in a) and the two existing ones, found in mchoice.m) and fill in the entries of the following table with yes/no:

Property Method	Deterministic	With memory
predict1		
predict2		
predict3		

c) Find (experimentally) the convergence limit of the transition matrix *transm* using the *predict2* policy for the computer player and the default strategy (implemented in gen_human_move.m) for the human player.

Hint: Perform simulations with an increasing number of rounds.

- d) Using the functions initmchoice, updatesamplem, and updatetransm, implement the matrices samplem2 and transm2 corresponding to the sample matrix and transmition matrix of the computer player, respectively. Use the last two moves of the computer player saved in the *history* array as additional parameters of the mchoice function. Print the computed *transm2* matrix at the end of mchoice. Additionally, add *transm2* to the list of variables saved to file in game.m.
- e) Similarly to c), find (experimentally) the convergence limit of the transition matrix transm2 using the predict3 policy for the computer player and the default of the User-defined transition matrix (check the box in the GUI and use the default values).
- f) Fill in the matrices below with the results from c) and e)

Questions:

- Q1 What is the type of the transition matrix of the game? What properties does it possess?
- Q2 Related to exercise c): For which of the three prediction strategies of the computer player can it be (intuitively) guaranteed that, in the long run (i.e. an infinite number of rounds), a winning strategy for the human player can be found?
- Q3 How can the modeling approach used in this worksheet be extended to study (slightly) more complex games or more complex player behaviors?
- Q4 Where do similar scenarios to the one in this worksheet show up in real-world applications?