

## Source Terms

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# From Conservation Laws to Balance Laws



#### Our reference equation is

$$q_t + f(q)_x = \psi(q) \tag{1}$$

#### where

- the homogeneous equation  $q_t + f(q)_x = 0$  is hyperbolic
- $lacktriangledown \psi(q)$  (the source terms) don't depend on derivatives of q
  - lacksquare  $\Rightarrow$   $q_t = \psi(q)$  is an independent system of ODEs

