

	Cas général (q_1, q_2, q_3)	Coordonnées cartésiennes (x, y, z)	Coordonnées cylindriques (r, ϕ, z)
Les équations	$\begin{cases} x = x(q_1, q_2, q_3) \\ y = y(q_1, q_2, q_3) \\ z = z(q_1, q_2, q_3) \end{cases}$	$\begin{cases} x = x \\ y = y \\ z = z \end{cases}$	$\begin{cases} x = r \cos \phi \\ y = r \sin \phi \\ z = z \end{cases}$
Les limites		$\begin{aligned} -\infty < x < \infty \\ -\infty < y < \infty \\ -\infty < z < \infty \end{aligned}$	$\begin{aligned} 0 \leq r \\ 0 \leq \phi < 2\pi \\ -\infty < z < \infty \end{aligned}$
Facteurs d'échelle	$\begin{aligned} h_1 \\ h_2 \\ h_3 \end{aligned}$	$\begin{aligned} h_1 &= 1 \\ h_2 &= 1 \\ h_3 &= 1 \end{aligned}$	$\begin{aligned} h_1 &= 1 \\ h_2 &= r \\ h_3 &= 1 \end{aligned}$
Élément de déplacement	$d\vec{l} = h_1 dq_1 \hat{e}_1 + h_2 dq_2 \hat{e}_2 + h_3 dq_3 \hat{e}_3$	$d\vec{l} = dx \hat{x} + dy \hat{y} + dz \hat{z}$	$d\vec{l} = dr \hat{r} + r d\phi \hat{\phi} + dz \hat{z}$
Élément de surface	$\begin{aligned} ds_1 &= h_2 h_3 dq_2 dq_3 \\ ds_2 &= h_1 h_3 dq_1 dq_3 \\ ds_3 &= h_1 h_2 dq_1 dq_2 \end{aligned}$	$\begin{aligned} ds_x &= dy dz \\ ds_y &= dx dz \\ ds_z &= dx dy \end{aligned}$	$\begin{aligned} ds_r &= r d\phi dz \\ ds_\phi &= r dr dz \\ ds_z &= r dr d\phi \end{aligned}$
Élément de volume	$dV = h_1 h_2 h_3 dq_1 dq_2 dq_3$	$dV = dx dy dz$	$dV = r dr d\phi dz$
Gradient	$\vec{\nabla} f = \frac{1}{h_1} \frac{\partial f}{\partial q_1} \hat{e}_1 + \frac{1}{h_2} \frac{\partial f}{\partial q_2} \hat{e}_2 + \frac{1}{h_3} \frac{\partial f}{\partial q_3} \hat{e}_3$	$\vec{\nabla} f = \frac{\partial f}{\partial x} \hat{x} + \frac{\partial f}{\partial y} \hat{y} + \frac{\partial f}{\partial z} \hat{z}$	$\vec{\nabla} f = \frac{\partial f}{\partial r} \hat{r} + \frac{1}{r} \frac{\partial f}{\partial \phi} \hat{\phi} + \frac{\partial f}{\partial z} \hat{z}$
Divergence	$\vec{\nabla} \cdot \vec{A} = \frac{1}{h_1 h_2 h_3} \left[\frac{\partial}{\partial q_1} (A_1 h_2 h_3) + \frac{\partial}{\partial q_2} (A_2 h_1 h_3) + \frac{\partial}{\partial q_3} (A_3 h_1 h_2) \right]$	$\vec{\nabla} \cdot \vec{A} = \frac{\partial}{\partial x} A_x + \frac{\partial}{\partial y} A_y + \frac{\partial}{\partial z} A_z$	$\vec{\nabla} \cdot \vec{A} = \frac{1}{r} \left[\frac{\partial}{\partial r} (r A_r) + \frac{\partial}{\partial \phi} A_\phi \right]$
Rotationnel	$\vec{\nabla} \times \vec{A} = \frac{1}{h_1 h_2 h_3} \begin{vmatrix} h_1 \hat{e}_1 & h_2 \hat{e}_2 & h_3 \hat{e}_3 \\ \frac{\partial}{\partial q_1} & \frac{\partial}{\partial q_2} & \frac{\partial}{\partial q_3} \\ h_1 A_1 & h_2 A_2 & h_3 A_3 \end{vmatrix}$	$\vec{\nabla} \times \vec{A} = \begin{vmatrix} \hat{x} & \hat{y} & \hat{z} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ A_x & A_y & A_z \end{vmatrix}$	$\vec{\nabla} \times \vec{A} = \frac{1}{r} \begin{vmatrix} \hat{r} & r \hat{\phi} & \hat{z} \\ \frac{\partial}{\partial r} & \frac{\partial}{\partial \phi} & \frac{\partial}{\partial z} \\ A_r & r A_\phi & A_z \end{vmatrix}$
Laplacien		$\nabla^2 \Phi = \frac{\partial^2 \Phi}{\partial x^2} + \frac{\partial^2 \Phi}{\partial y^2} + \frac{\partial^2 \Phi}{\partial z^2}$	$\nabla^2 \Phi = \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \Phi}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 \Phi}{\partial \phi^2} + \frac{\partial^2 \Phi}{\partial z^2}$
Vecteur position		$\vec{r} = x \hat{x} + y \hat{y} + z \hat{z}$	$\vec{r} = r \hat{r}(\theta) + z \hat{z}$
Vecteur position unitaire		$\hat{r} = \frac{x \hat{x} + y \hat{y} + z \hat{z}}{(x^2 + y^2 + z^2)^{\frac{1}{2}}}$	$\hat{r} = \frac{r \hat{r}(\theta) + z \hat{z}}{(r^2 + z^2)^{\frac{1}{2}}}$

