



P1	P2	P3	P4	P5	P6	TOTAL
Name Surname						
Registration No						
Department						
Group No	Exam Hall	Signature of the Student	The 9 th article of Student Disciplinary Regulations of YÖK Law No.2547 states " Cheating or helping to cheat or attempt to cheat in exams " de facto perpetrators takes one or two semesters suspension penalty. Calculators are not allowed. Do not ask any questions about the problems. There will be no explanations. Use the allocated areas for your answers and write legible.			
Lecturer's Name Surname						

PROBLEM 1 (12p)

The velocity of a particle moving in the xy-plane is given by the velocity vector $\vec{v} = 2t\hat{i} - 3t^2\hat{j}$ (m/s).

The particle is at the origin at $t = 0$.

a) Find the position of the particle (\vec{r}) as a function of time.

b) Find the total acceleration (\vec{a}) of the particle.

c) Find the magnitude of the tangential acceleration (a_t) at $t = 1s$.

d) Find the power transferred to the mass $m=1kg$ at $t=1s$.

PROBLEM 2 (13p)

A projectile is fired uphill with a speed of $v_0 = 10$ (m/s) and a horizontal angle of θ_0 , over an incline which slopes at an angle of α to the horizontal as shown.

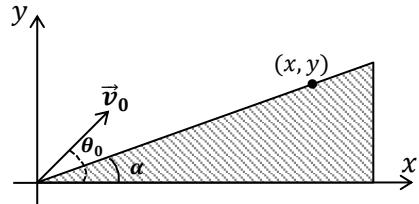
$$\cos\theta_0 = 0.7$$

$$\sin\theta_0 = 0.7$$

$$\cos\alpha = 0.8$$

$$\sin\alpha = 0.6$$

$$g = 10 \text{ m/s}^2$$



a) Write components of the position as a function of time $x(t)$ and $y(t)$.

b) Express y as a function of x only ($y = f(x)$) for the projectile.

c) Find the position (x,y) where the projectile hits the incline.

d) Determine the time taken by the projectile to hit the incline.

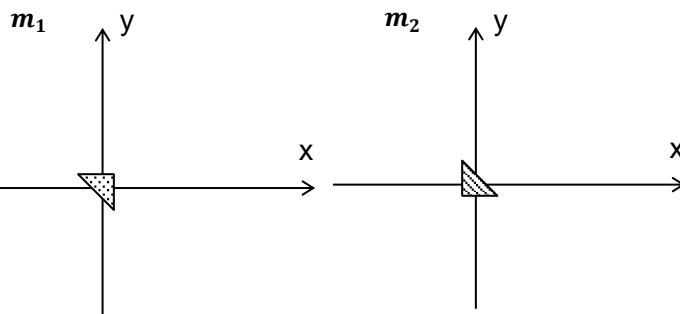
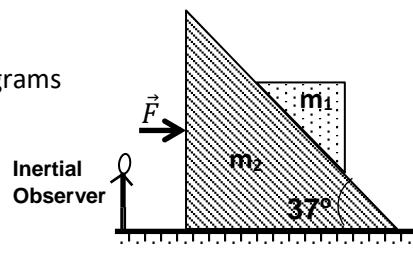
PROBLEM 3 (25p)

In the system of triangle shaped blocks illustrated in the figures, a constant external force \vec{F} is applied in such a way that m_1 stays stationary relative to m_2 . The whole system is frictionless.

Here, $m_1 = 2.4 \text{ kg}$, $m_2 = 4.0 \text{ kg}$, $\cos 37^\circ = 0.8$, $\sin 37^\circ = 0.6$ and $g = 10 \frac{\text{m}}{\text{s}^2}$.

a) For an inertial observer standing still on the ground:

a-1) Draw free body diagrams



a-2) Write the equation of motions for:

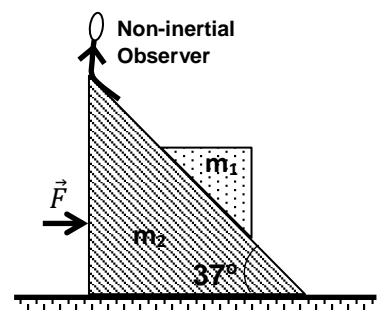
m_1 :

m_2 :

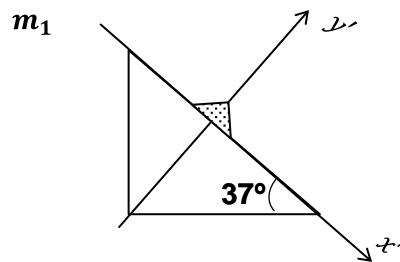
a-3) Find the accelerations of the masses.

a-4) Find the force F .

b) Now, \vec{F} is reduced in such a way that m_2 has an acceleration of $A = 5 \text{ m/s}^2$ relative to the ground (inertial observer), and m_1 has an acceleration of a'_1 relative to non-inertial observer (observer on m_2).



b-1) Draw free body diagram of m_1 according to non-inertial observer.

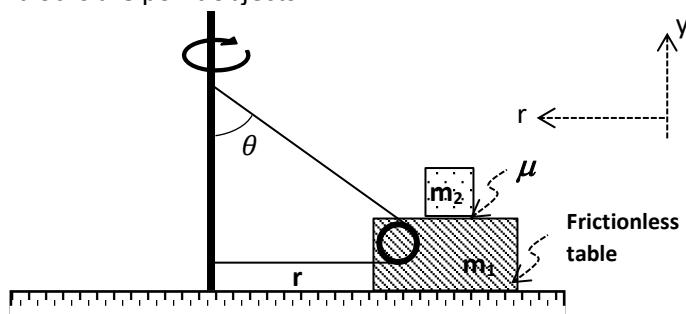


b-2) Write the equation of motion for m_1 according to non-inertial observer.

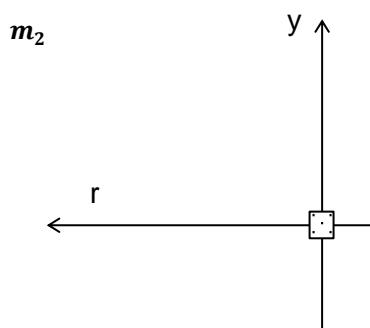
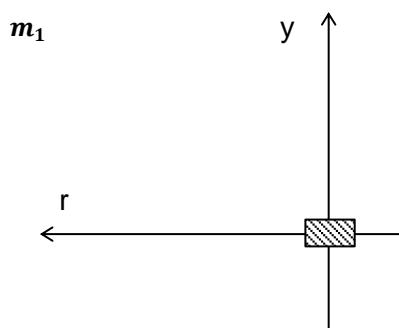
b-3) Find the acceleration a'_1 .

PROBLEM 4 (25p)

A block of mass m_1 is attached to a vertical rod by a single string which passes around a pulley and attached to the block as shown in figure. The block m_1 rotates on a frictionless table. Another block of mass m_2 is placed onto rough surface of mass m_1 . The coefficient of static friction between the two masses is μ . The entire system rotates on a frictionless table so that the blocks are moving in a horizontal circle of r with a constant speed v . The block of mass m_2 stays stationary relative to block of mass m_1 . Assume that the pulley and the string are weightless and frictionless and the blocks are point objects.



a-1) Draw the free body diagrams for m_1 and m_2 .



a-2) Write the equation of motions for:

m_1 :

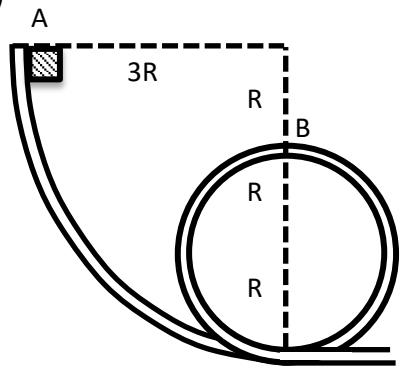
m_2 :

b) Find the maximum value of the speed that the mass m_2 can stay stationary relative to m_1 while entire system rotates, in terms of μ , g and r .

c) Find the tension on the string while the system rotates at the maximum speed obtained in b, in terms of μ , θ , m_1 , m_2 and g .

PROBLEM 5 (13p)

A small block of mass m starts from rest at point A and slides along a rough loop-the-loop rail as shown in the figure. Assume that a constant kinetic friction force f_k is acting on the block during its travel on the rail.



a) What is the work done between A and B by

a-1) Conservative forces

a-2) Normal force

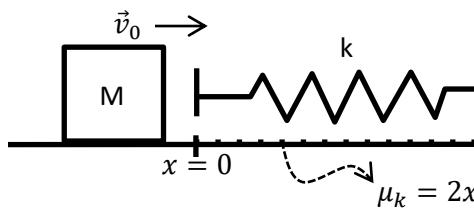
a-3) Force of friction

b) Write equation of the conservation of energy for the block between A and B.

c) What should be the magnitude of the force of friction, so that the magnitude of normal force \vec{N} acting on the block is equal to its weight $m\vec{g}$ at point B.

PROBLEM 6 (12p)

A block of mass M slides along a horizontal table with speed \vec{v}_0 . At $x = 0$, it hits a spring with spring constant k and begins to experience a friction force. The coefficient of friction is variable and is given by $\mu_k = 2x$. The block first comes momentarily to rest at $x = L$.



a) Find the work done by the forces acting on the block between $x = 0$ and $x = L$.

a-1) Gravitational force

a-2) Spring force

a-3) Normal force

a-4) Force of friction

b) If the loss of mechanical energy, between $x = 0$ and $x = L$, due to the friction is half of the energy of the block at $x = 0$, what is the spring constant in terms of M, v_0 and L .