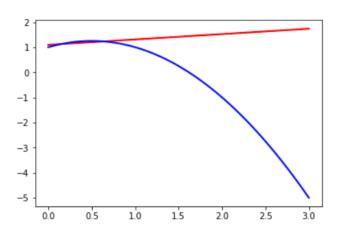
ECE-GY 6143 Machine Learning HW 04

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1. Question 1:

Out[20]: [<matplotlib.lines.Line2D at 0x18794bd0860>]



2. Question 3:

BIAS(x) =
$$E(f(x, \beta)) - f(x, \beta_0)$$

= $E(\frac{\Sigma \beta_0 x_i^2}{\Sigma x_i^2} x) - f(x, \beta_0)$
= 0

b.
$$Bias(x) = E(\frac{\sum \beta_0 x_i^2 + \sum \epsilon}{\sum x_i^2} x^2) - f(x, \beta_0)$$
$$= \frac{x}{\sum x_i} \sum E(\epsilon)$$
$$= 0$$

c.
$$Bias(x) = E(\frac{\Sigma\beta_0 x_i^2 + \Sigma2\beta_0 x_i \epsilon + \Sigma\beta_0 \epsilon^2}{\Sigma x_i^2} x^2) - f(x, \beta_0)$$
$$= \frac{\beta_0 x^2}{\Sigma x_i} \Sigma E(\epsilon^2)$$
$$= \frac{\beta_0 x^2 N}{\Sigma x_i} \delta^2$$

3. Question 4

$$\begin{aligned} &\mathbf{a.}\\ &\hat{\beta} = [(1,x)^T(1,x)]^{-1}(1,x)^Ty\\ &\mathbf{b.}\\ &\hat{\beta} = [(1,x)^T(1,x)]^{-1}(1,x)^T(1,x,x^2)\beta_0 \end{aligned}$$

$$X = np.random.rand(10)$$

 $y = 1 + X - X**2$
 $A = np.zeros([10, 2])$

d.

from the Graph, x = 3

lation, we should reach the same result

But there should be a prove analytically, solving β is to minimize: $E\{(f(X) - \hat{f}(X))^2\} = \int_0^1 (1 + 2x - x^2 - \beta_0 - \beta_1 x)^2 Pr(x) dx$ Since Pr(X) is a constant line, after some complex polynomial calcu-

4. Question 5

a.

 $\begin{array}{l} c_{i} = cancer - volume, a_{i} = age, t1_{i} = is - Type - 1, t2_{i} = is - Type - 2\\ Model1: \hat{y} = (1, c) \hat{\beta}\\ Model2: \hat{y} = (1, c, a) \hat{\beta}\\ Model3: \hat{y} = (1, c, a, t1, t2) \hat{\beta}\\ \mathbf{b.}\\ [2, 3, 5], Model3 \end{array}$

c.

$$M_{1} = \begin{bmatrix} 1 & 0.7 \\ 1 & 1.3 \\ 1 & 1.6 \\ \vdots & \vdots \end{bmatrix}$$

$$M_{2} = \begin{bmatrix} 1 & 0.7 & 55 \\ 1 & 1.3 & 65 \\ 1 & 1.6 & 70 \\ \vdots & \vdots & \vdots \end{bmatrix}$$

$$M_{3} = \begin{bmatrix} 1 & 0.7 & 55 & 1 & 0 \\ 1 & 1.3 & 65 & 0 & 1 \\ 1 & 1.6 & 70 & 0 & 1 \\ \vdots & \vdots & \vdots & \vdots & \vdots \end{bmatrix}$$

d.

Model2: 0.72 < 0.70 + 0.05