



M.Sc in Biomedical Engineering and Medical Physics Technical University of Munich

# Robust Single Point Ultra Short Echo Time Water Fast Separation

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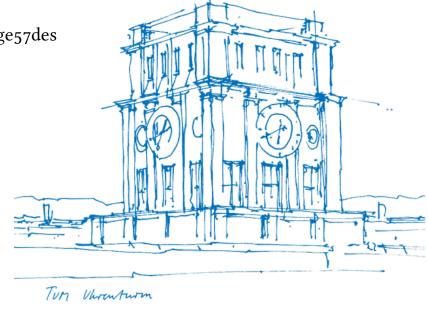
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#### ABSTRACT

Water-fat (WF) MRI is a set of techniques used in the assessment of metabolic dysfunction-related diseases. These techniques leverage the frequency shift between water and fat MR signals to separate them into two images, needing the acquisition of images at multiple echo times which extends the already prolonged MRI scan duration.

To shorten this acquisition time water-fat imaging has been combined with ultra-short echo time (UTE) techniques. The combination of these two methods are called UTE-Dixon imaging. These techniques have been used to suppress the fat signal in the MRI acquisitions and to determine tissue electron density properties. However, the need of two complex images to separate water and fat prolongs the scan time. A solution is to separate water and fat with the use of a single complex image instead of two, shortening scan time. This technique in combination with UTE acquisitions is called single-point UTE (sUTE) Dixon imaging. The use of a single image to separate water and fat introduces complexity to the problem, since some background phase contributions, coming from  $B_0$  and  $B_1$  field inhomogeneities cannot be implicitly deduced from only one echo. Hence, the problem becomes ill posed.

New techniques have arisen to tackle this problematic such as Kronthaler [citeKronthaler] with the use of a second order iterative optimization method (Gauss-Newton Method) with a smoothness constraint. Because the problem is ill posed initialization is necessary to ensure a proper convergence path and a better result of the water-fat separation.

This study aims to explore different methods to improve sUTE-Dixon imaging by addressing two different points:

- 1. Characteristics of background phase contributions and different approaches to modeling them.
- 2. How initialization techniques changes the behavior of the iterative optimization method results?.

We developed a sUTE-Dixon reconstruction framework based on the latest literature and integrated initialization techniques to further improve the method. This framework is used to compare reconstructions of different phantoms and anatomies with different hyper-parameters and initialization approaches.

Our findings reveal that initialization, not only prevents artifacts in reconstructed images but also significantly enhances the achievable water-fat separation quality. Additionally, we highlight two principal limitations of the current framework:

- 1. Its inability to accurately reconstruct water and fat at the anatomy/object edges.
- 2. Its sensitivity to mean phase shifts from the scan.

We have seen that computer programming is an art, because it applies accumulated knowledge to the world, because it requires skill and ingenuity, and especially because it produces objects of beauty.

- knuth:1974 [knuth:1974]

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## Part I

# INTRODUCTION TO WATER FAT SEPARATION IN MRI

1

#### INTRODUCTION

Magnetic Resonance Imaging (MRI) is a fundamental tool in radiology and biomedical research, offering capabilities for both anatomical and functional imaging. MRI excels in providing superior soft-tissue contrast compared to CT scans and delivers higher resolution images than ultrasound, all while being a generally safe method with infrequent occurrences of patient harm [5] and no exposure to ionizing radiation.

MRI operates based on the Nuclear Magnetic Resonance (NMR) phenomenon to create changes in magnetization that are detectable by its receiver systems. It achieves spatial localization by stimulating nuclear spins within an external magnetic field. By modifying the imaging sequences, MRI can manipulate spin systems to produce various contrasts, such as relaxation, proton density, diffusion, and phase contrasts. Beyond producing diagnostic-quality images, MRI can also be adapted for quantitative analysis, which has spurred developments in creating maps of tissue physical properties for quantitative clinical interpretations.[4]

Globally, over 25,000 MRI scanners are in use, supporting a wide range of diagnostic and therapeutic applications. In neuroimaging, MRI is crucial for distinguishing between gray and white matter, aiding in the diagnosis of conditions like dementia, Alzheimer's disease, demyelinating diseases, epilepsy, and anomalies in the brain and spinal cord. It also facilitates diffusion and functional imaging techniques that can map neuronal tracts and blood flow. Cardiovascular uses of MRI include examining the structure and function of the heart and assessing vascular diseases. In musculoskeletal imaging, MRI is used for evaluating joints, spine, soft tissue tumors, and muscle disorders. Additionally, MRI is employed in abdominal assessments for the liver, gastrointestinal tract, breasts, and prostate, particularly useful in detecting cysts, tumors, and other abnormalities. Functional imaging of metabolites through spectroscopy is also a capability of MRI. [1]

In diagnostic imaging, fat presents a crucial MR signal component that often needs to be suppressed or differentiated from water signals. This manipulation is vital for accurate quantification of MR properties in tissues characterized by mixed chemical shifts. Particularly, imaging of short- $T_2$  tissues requires significant suppression of long- $T_2$  signals from both water and fat to enhance image contrast and clarity. The technology of water-fat (WF) imaging has evolved into state-of-the-art imaging methodology essential for differentiating between water and fat signals. These methods are particularly useful for qualitative purposes, such as suppressing the fat signal, or they are used quantitatively to derive biomarkers of tissue fat concentration such as the Proton Density Fat Fraction (PDFF). Furthermore, water-fat MRI is particularly useful for assessing diseases linked to metabolic disorders, such as obesity, metabolic syndrome, and type-2 diabetes [2, 3]. The ability to effectively manage fat signals in MRI is useful for improving the diagnostic accuracy of MRI scans and they not only provide a clearer visualization of anatomical structures but also facilitate a better understanding of tissue compositions, which is crucial for accurate diagnosis and treatment planning. [chapter]

This method utilizes chemical shift encoding (CSE) techniques, also known as Dixon imaging, capitalizing on the chemical shift differences between water and fat MR signals to differentiate them and create the two respective distinct images. The water-fat separation process involves fitting the acquired signal to a physical model, typically necessitating multiple image captures at different echo times. This requirement extends the scan duration, and coupled with the inherently slow MRI acquisition speed, increases the susceptibility of the technique to motion artifacts from patient or physiological movement. Techniques such as respiratory triggering or breath-hold are employed to minimize these artifacts, though they may elevate patient discomfort. Therefore, there is a pressing need to develop methods to expedite the MRI scanning process.

The challenge of prolonged scanning times in MRI is well-recognized, with a significant body of research focused on accelerating the acquisition process through fast sequences and parallel imaging techniques. Under this context multi-echo and single-echo ultra short echo time (UTE) sequences have been developed and studied to accelerate this scanning time [**ute**]. Specifically single-echo/single-point UTE Dixon techniques have been developed for fast acquisition with promising separation results since the short echo times make the  $R_2^*$  relaxation negligible; but it amplifies the relative effects of  $B_0 \& B_1$ 

field inhomogeneities affecting the quality of the water-fat separation, since the signal is not strong. Moreover, by using only one complex image the time dependent effects of the signal cannot be inferred, translating into a more complex that requires background phase corrections for a reliable WF separation.

Because of these pitfalls some techniques have been developed for single-point UTE Dixon like Kronthaler S., et. al [kronthaler], which use an iterative optimization method to solve the water-fat separation problem, trying to capture the background phase to remove it from the signal and continue with the classic separation algorithm. Although the algorithm tries to regularize the image by rewarding smoothness of the fitted phase, the problem is still ill posed and without proper initialization the stability of the algorithm may not deliver its full potential.

The purpose of this study is to analyze different modeling approaches of background phase contributions and various initialization techniques for the algorithm in Kronthaler S., et. al.; comparing it qualitatively with the non-altered model and studying its effects on the resulting water-fat separation quality and stability of the algorithm.

#### 1.0.1 Thesis Structure

The thesis is organized into the following chapters:

- **Chapter 1**: The current chapter presents a brief introduction, motivation and purpose of the thesis.
- **Chapter 2**: Resumes the general theory of MRI, including physics theory, signal encoding, k-space and echo sequences.
- **Chapter 3**: Introduces the UTE sequences and the water fat separation of MRI signals.
- **Chapter 4**: Analyses the different background phase contributions and its effects in the resulting MRI acquisition.

- **Chapter 5**: Introduces the iterative optimization method used for waterfat separation and analyses the impact of different initialization strategies on its resulting water and fat images.
- **Chapter 6**: Summarizes the conclusions drawn from various results from the previous chapters.

## Part II

## THEORY OF MAGNETIC RESONANCE IMAGING

In this section we will introduce the theory of magnetic resonance imaging. We will start with the physics background in nuclear magnetic resonance, following to signal acquisition in k-space and signal encoding. Finally, echo sequences are introduced.

## 2.1 NUCLEAR MAGNETIC RESONANCE (NMR)

Nuclear Magnetic Resonance (NMR) is the physical phenomenon underlying magnetic resonance imaging (MRI). NMR occurs when nuclei with non-zero spin absorb and emit electromagnetic radiation whey the nuclei are placed in an external magnetic field. Most isotopes with an odd number of protons and/or neutrons such as hydrogen (<sup>1</sup>H), carbon (<sup>13</sup>C), and phosphorus (<sup>31</sup>P) have a spin [12Sandy].

<sup>1</sup>H is the most abundant isotope inside the body and is the commonly used nuclei in magnetic resonance imaging. Its properties such as a high gyro-magnetic ratio, and a non-zero spin, makes it suitable for conducting measurements that provides information about the structure of the scanned tissue. For interest readers we refer to the standard literature [4and5Julio]

## 2.1.1 Nuclear Spin and Magnetic Moment

Nuclei with an odd number of protons and/or neutrons possess a property called nuclear spin  $\tilde{\mathbf{I}}$  of a nucleus with mass A. Since nuclei are not single entities,  $\tilde{\mathbf{I}}$  is composed of the spins  $\vec{s_i}$  and the orbital angular momenta  $\vec{l_i}$  of the protons and neutrons in the nucleus which have a spin  $s=\frac{1}{2}$ . Its relation is described by:

$$\tilde{\mathbf{I}} = \sum_{i=1}^{A} \left( \vec{s_i} + \vec{l_i} \right). \tag{2.1}$$

Different nuclear spin configurations can be achieved depending on the number of protons and neutrons in the nucleus, with the quantum relations given by:

$$\hat{\vec{\mathbf{I}}}|I,m\rangle = \hbar^2 I(I+1)|I,m\rangle \tag{2.2}$$

$$\hat{I}_z |I, m\rangle = \hbar m |I, m\rangle \tag{2.3}$$

with  $\|\vec{\mathbf{I}}\| > 0$ , using the spin operator  $\hat{\vec{\mathbf{I}}}$ , m as the magnetic quantum number, and constant  $\hbar = \frac{h}{2\pi}$  is the reduced Plank's constant  $6.6 \times 10^{-34}\,\mathrm{J\,s}$  divided by  $2\pi$ .

The nuclear spin can be related to a microscopic magnetic field which is formed by the charged nuclei rotating around its axis. The nuclear magnetic moment  $\vec{\mu}$  is directly to the total spin angular momentum  $\vec{\mathbf{I}}$ :

$$\vec{\mu} = \gamma \vec{\mathbf{I}},$$
 (2.4)

where the proportionality constant  $\gamma$ , known as gyro-magnetic ratio, depends on the atomic nucleus.

To get the magnitude of  $\vec{\mu}$  we use:

$$|\vec{\mu}| = \gamma \hbar \sqrt{I(I+1)},\tag{2.5}$$

where I is the nuclear spin quantum number with values  $I=0,\frac{1}{2},1,\frac{3}{2},...$  With the help of 2.1 we can derive:

- nuclei with odd A have half-integer *I*, e.g.: <sup>1</sup>H, <sup>13</sup>C.
- nuclei with even A and charge have I=0, e.g.:  $^{12}\mathrm{c},$   $^{16}\mathrm{O}.$
- nuclei with even A and odd charge have integer I, e.g.:  $^2\mathrm{H}$ ,  $^6\mathrm{Li}$ ,  $^{14}\mathrm{N}$ .

Hydrogen (<sup>1</sup>H) has a relatively high gyro-magnetic ratio and is also one of the most abundant nuclei with non-zero spin in human tissue, which makes it perfect for MRI acquisitions.

## 2.1.2 Zeeman Effect

This magnetic moment points at a random direction in absence of a magnetic field, thus free spin sistems have a spherical distribution of spin orientations due to the Boltzmann equation for thermal energy. In the presence of a magnetic field  $\vec{B_0}$ , we can obtain the energy:

$$\mathcal{H} = -\vec{\mu} \cdot \vec{B_0}. \tag{2.6}$$

Without loss of generality we can assume that  $\vec{B_0} = B_z \vec{e_z}$ . Then, the hamiltonian can be reformulated using Equation 2.4 to:

$$\mathcal{H} = -\gamma I_z B_0. \tag{2.7}$$

Hence, the eigenstates of  $\hat{\mathcal{H}}$  correspond to the eigenstates of  $\hat{I}_z$ , which in turn comprise of 2l+1 different values. Thus, we can denote the energy levels by:

$$E_m = -\gamma \hbar B_0 m, \quad -I \le m \le I, \tag{2.8}$$

which resembles an angular momentum  $\vec{mu}$  precessing with the angular frequency  $\gamma B_0 = \omega_L$ , known as the *Larmor* frequency. [Larmor]

The resulting splitting of a single non-excited energy level into several new excited levels in the presence of an external magnetic field is called Zeeman effect depicted in Figure ??. With the energy difference between energy levels:

$$\Delta E = |E_{m+1} - E_m| = \hbar \gamma B_0 = \hbar \omega_L. \tag{2.9}$$

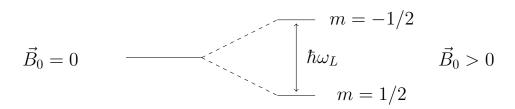


Figure 2.1: Zeeman effect on an energy level for a nucleus with nuclear spin I = 1/2. The energy difference between the levels is half the Larmor frequency  $\omega_L$  multiplied by  $\hbar$ .

A spin system may have multiple resonant frequencies when presented with field inhomogeneities, shielding from neighboring spins, etc. This is called *chemical shift* which is described by a shielding constant  $\delta$ :

$$B_0^{eff} = B_0(1 - \delta)$$

$$\omega = \omega_0 - \Delta\omega = \omega_0(1 - \delta)$$
(2.10)

As an example, the hydrogen nuclei in a fat molecule  ${\rm CH_2}$  have a shielding constant of  $\delta=3.35\,{\rm ppm}$  with respect to a proton in water.

The gyro-magnetic ratio of the proton (<sup>1</sup>H) is  $\gamma = 1.675\,221\,9 \times 10^8\,\mathrm{s^{-1}\,T^{-1}}$ , which corresponds to a frequency of  $f = \frac{\omega_L}{2\pi} = 127.732\,\mathrm{MHz}$  for  $B_0 = 3\,\mathrm{T}$ 

#### 2.1.3 Bulk Magnetization

The magnetic moments of N atomic nuclei sum up to a net bulk magnetization that describes the behaviour of the system:

$$\vec{M} = \sum_{i=1}^{N} \vec{\mu_i}.$$
 (2.11)

Because in absence of an external magnetic field the nuclei in the human body are at thermal equilibrium, and the thermal energy is large compared to the energy of the non-excited spin state ( $k_BT\gg\gamma\hbar B_0$ ) the occupation density of the spin states can be expressed using Boltzmann statistics. Hence, we can derive that the excess rate of spins pointing on a specific direction vs the spins pointing at the opposite direction can be described by the Boltzmann distribution:

$$\frac{N_{\uparrow}}{N_{\downarrow}} = \exp(\frac{\Delta E}{k_B T}). \tag{2.12}$$

where  $k_B$  is the Boltzmann constant.

Since  $k_BT \gg \Delta E$  we can approximate to the first order Equation 2.12. Thus denoting the excess spins  $N_s$  we derive the bulk magnetization as:

$$M_z^0 = \|\mathbf{M}\| \approx \frac{\gamma^2 h^2 B_0 N_s}{4k_B T}$$
 (2.13)

At room temperature ( $T=300\,\mathrm{K}$ ), the number of spins in the up-state is almost equal to the number of spins in the down-state. Nevertheless, the high abundance of hydrogen in the human body generates sufficient bulk magnetization for imaging purposes.[aizada14].

#### 2.1.4 Resonance and RF Excitation

When nuclei are subjected to an RF pulse at the Larmor frequency ( $\omega_0 = \gamma B_0$ ), they absorb energy and are excited to a higher energy state. The resonance condition is met when the frequency of the RF pulse matches the Larmor frequency. This causes the net magnetization vector to tip away from the  $B_0$  axis, creating transverse magnetization.

#### 2.1.5 Relaxation Mechanisms

After the RF pulse is turned off, the excited nuclei return to their equilibrium state through relaxation processes:

- T1 (Longitudinal) Relaxation: The recovery of longitudinal magnetization along the  $B_0$  axis.
- **T2** (**Transverse**) **Relaxation**: The decay of transverse magnetization due to spin-spin interactions.

#### 2.1.6 Chemical Shift

The chemical shift refers to the variation in resonance frequency of nuclei due to their chemical environment. This shift is crucial for distinguishing between water and fat signals in MRI, as the resonance frequency of fat protons is slightly lower than that of water protons.

#### 2.2 MRI HARDWARE COMPONENTS

The main components of an MRI system include:

- Static Magnetic Field: Produced by a superconducting magnet, creating a strong and uniform field ( $B_0$ ).
- **RF Coils:** Used for both transmitting the RF pulse and receiving the MR signal.
- Gradient Coils: Generate magnetic field gradients for spatial encoding.
- **Signal Reception:** The precessing transverse magnetization induces a voltage in the RF coils, which is detected and processed to form images.

#### 2.3 SPATIAL ENCODING

Spatial encoding in MRI is achieved through the application of magnetic field gradients, which cause the Larmor frequency to vary with position.

#### 2.3.1 Slice Selection

A gradient field applied along one axis (e.g., the z-axis) during RF excitation selectively excites a slice of tissue. The RF pulse is designed to match the Larmor frequency of the nuclei in the desired slice.

#### 2.3.2 Frequency Encoding

Following slice selection, a gradient applied along a second axis (e.g., the x-axis) causes the resonance frequency to vary linearly with position. This frequency variation is used to encode spatial information.

#### 2.3.3 Phase Encoding

A third gradient applied along a perpendicular axis (e.g., the y-axis) introduces a position-dependent phase shift. By incrementally changing the phase-encoding gradient, spatial information along this axis is encoded.

#### 2.3.4 k-Space and Image Reconstruction

The combination of frequency and phase encoding gradients fills k-space, a matrix representing spatial frequencies. The MR image is reconstructed from the k-space data using the inverse Fourier transform.

#### 3.1 IMPORTANCE OF WATER-FAT SEPARATION

Water-fat separation in MRI is essential for assessing metabolic disorders such as obesity, metabolic syndrome, and type-2 diabetes. The technique provides insights into body fat distribution and helps derive biomarkers like the Proton Density Fat Fraction (PDFF).

## 3.2 CHEMICAL SHIFT ENCODING (CSE)

Chemical shift encoding (CSE) leverages the resonance frequency differences between water and fat protons to separate their signals. Multi-echo acquisitions are used to encode these differences, enabling the separation of water and fat signals into distinct images.

#### 3.3 DIXON TECHNIQUES

The Dixon method involves acquiring images at multiple echo times to exploit the phase differences between water and fat signals. This technique can be applied both qualitatively, to suppress fat signals, and quantitatively, to measure fat concentration.

#### 3.4 APPLICATIONS IN CLINICAL DIAGNOSTICS

Water-fat MRI techniques are widely used in clinical diagnostics to evaluate liver fat content, muscle composition, and other metabolic parameters. The separation of water and fat signals enhances the accuracy of these assessments.

## CHALLENGES AND TECHNIQUES FOR ACCELERATION

#### 4.1 MOTION ARTIFACTS

Motion artifacts arise from patient movement or physiological motion during MRI acquisition. These artifacts can degrade image quality and diagnostic accuracy.

## 4.2 RESPIRATORY TRIGGERING AND BREATH-HOLD TECH-NIQUES

Respiratory triggering and breath-hold techniques are employed to mitigate motion artifacts. While effective, these methods can increase patient discomfort and extend scan times.

## 4.3 COMPRESSED SENSING (CS)

Compressed Sensing (CS) is a mathematical framework that accelerates MRI acquisition by reconstructing images from undersampled data.

## 4.3.1 Principles of Compressed Sensing

CS exploits the sparsity of MR images in a transform domain, enabling the reconstruction of high-quality images from fewer k-space samples.

#### 4.3.2 *CS in MRI*

CS has been successfully applied to various MRI techniques, reducing scan times and improving image quality. The reconstruction process involves solving an optimization problem to recover the image from undersampled data.

#### 4.3.3 CS in Water-Fat MRI

In water-fat MRI, CS can be used to accelerate the acquisition process by exploiting the redundancy in multi-echo data. This approach enhances the efficiency of water-fat separation and reduces scan times.

## ADVANCED TECHNIQUES IN WATER-FAT MRI

#### 5.1 FIELD MAPPING

Accurate field mapping is crucial for water-fat separation. Various algorithms have been developed to estimate the field map and correct for inhomogeneities.

#### 5.2 IDEAL METHOD

The Iterative Decomposition of Water and Fat with Echo Asymmetry and Least-squares (IDEAL) method iteratively estimates water and fat signals, field map, and transverse relaxation rates.

#### 5.3 GRAPH CUT ALGORITHMS

Graph cut algorithms provide an efficient approach for field map estimation, improving the accuracy of water-fat separation by minimizing artifacts.

#### 5.4 CONCLUSION

MRI, leveraging the NMR phenomenon, offers unparalleled capabilities in both anatomical and functional imaging. The ongoing development of advanced techniques like CS in WF-MRI continues to enhance the efficiency and effectiveness of this imaging modality, making it invaluable in the clinical assessment of metabolic and other disorders.

## MATH TEST CHAPTER

# Part III

# APPENDIX



## APPENDIX TEST

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