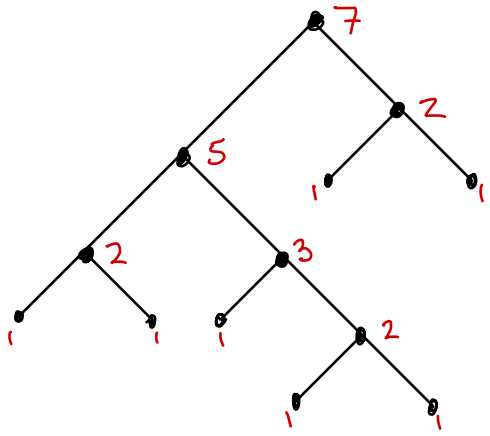
Indexing paths in a binary tree:

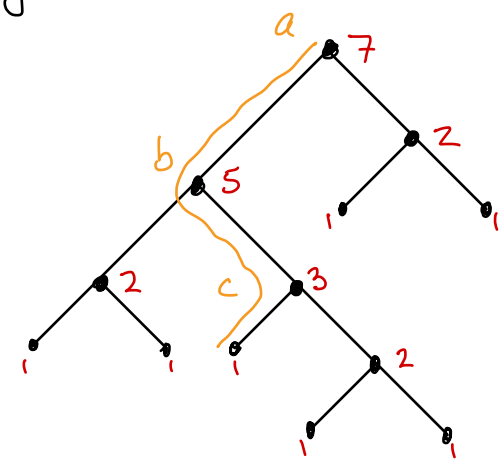
(ignoring the fact that to choose a path is to choose a leaf node)

Number of sub-paths below each node



(so there are paths w/ indices 1 through 7.

e.g. find path with index 3.



at (a) we go left because $5 \geq 3$

at (b) we go right because $2 < 3$,
and we adjust the sub-index to $3 - 2 = 1$.

at (c) we go left because $1 \leq 1$

Algorithm: Indexing paths in a binary tree:

Inputs: A binary tree and an index

Set the subindex i to the index

set current node to root node

while current node is not a leaf node;

let n be subpaths below left child of current node.

If $n \geq i$;

set new current node to left child of old current node

Otherwise;

set new current node to right child of old current node
set new subindex i to $i - n$.

The final 'current node' is the node with the provided index.