

An Interactive Tool to Visualize Results from Uncertainty Quantification

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Abstract

Uncertainty quantification is a class of methods used to simulate the ways that variations to inputs of a system can potentially change the end state of that system. This article outlines the implementation of an interactive tool to visualize the results of an uncertainty quantification analysis. The interactive tool is a deployable web application built with the R `Shiny` framework. Users can create, adjust, and save custom visualizations to assist in interpreting and presenting results.

Key Words: Interactive Visualization; `shiny` R Package

1. Introduction

Uncertainty quantification is a methodological framework used with some frequency in engineering analysis (Ewing et al., 2018). It is used to understand how variability within the parameters (i.e. inputs) to some system impact the end state of that system. Engineering analysts use uncertainty quantification to assess and find the balance between design sufficiency and design efficiency. This is particularly important in fields where large-scale prototypes, testing, and data collection are extremely expensive. Engineers in these types of applications are increasingly relying on computational simulations to assess system designs.

In the following article, I outline the implementation of an interactive tool to visualize uncertainty quantification results. The outline of this article will proceed as follows: In Section 2, a brief overview of uncertainty quantification is given. In Section 3, the methods by which the visualization tool was developed are described. In Section 4, the resulting web application is described and screenshots of the web application are shown. In Section 5, future enhancements to the web application are discussed. The code written to generate the `shiny` app is included in the Appendix.

2. Uncertainty Quantification Overview

The following description of the uncertainty quantification algorithm is adapted from Ewing et al. (2018). First, a few terms and definitions will be described.

system response quantity (SRQ): A parameter of particular interest directly related to the engineering system in question. The SRQ is the output (i.e. prediction) from the engineering model.

engineering model: A mathematical model that defines the relationship between the parameters (model inputs) and SRQ (model output).

aleatory uncertainty: Uncertainty resulting from randomness inherent to a given parameter. Gaining more knowledge about the parameter will not reduce the uncertainty of the parameter.

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epistemic uncertainty: Uncertainty resulting from a lack of knowledge about a given parameter. Gaining more knowledge about the parameter could reduce the uncertainty of the parameter.

The first step of uncertainty quantification is to identify sources of uncertainty (model parameters) and classify them as either aleatory or epistemic. This classification process has been somewhat debated in literature (Kiureghian and Ditlevsen, 2009), and will not be discussed as it is outside the scope of this project. Once these uncertainties related to the model parameters have been identified and classified as aleatory or epistemic, the uncertainty for each parameter must somehow be described. Traditionally, epistemic uncertainties have been described by an interval over which any value in the interval is equally likely, while aleatory uncertainties have been assigned probability distributions. Some more recent publications (Ewing et al., 2018) propose that all uncertainties, aleatory or epistemic, be described using probability distributions. This debate will not be discussed here as it is, again, outside the scope of this project. Once these distributions and/or intervals have all been assigned, they are carried through the model using Monte Carlo techniques.

Let m denote the number of iterations of an outer for loop, and let n denote the number of iterations in an inner for loop. In the outer for loop, values for the epistemic uncertainty parameters are selected randomly from the intervals/distributions assigned. Upon entering the inner loop, values for the aleatory uncertainty parameters are randomly chosen from the distributions assigned. The values chosen for the parameters in both the outer loop and the inner loop are then used as inputs in the engineering model to calculate a value for the SRQ. This value is stored and the inner loop continues running for the rest of the $n - 1$ iterations. All of the n SRQ values calculated from the n iterations of the inner loop are used to calculate an empirical cumulative distribution function (CDF) of SRQ values and the CDF is stored. The outer loop then begins its second iteration, and new values for the empirical uncertainty parameters are chosen. The inner loop then runs another n iterations, producing another CDF. This process continues until the outer loop has run all of its m iterations.

At this point, there will be m empirical CDFs that have been calculated, representing various possible realized values of the SRQ. These CDFs can then be plotted and interpreted. Ewing et al. (2018) suggests constructing a “P-box”. This P-box is found by calculating a lower percentile (e.g. the 5th percentile) and an upper percentile (e.g. the 95th percentile) of the CDF ensemble. This P-box can then be interpreted in several ways, including (1) selecting a SRQ value and extracting a probability interval, and (2) selecting a probability value and extracting an SRQ interval.

3. Methods

In order to assist analysts in visualizing and interpreting results from an uncertainty quantification analysis as described in Section 2, an interactive visualization tool was developed. Since the actual uncertainty quantification analysis can be carried out with greater speed and computational power elsewhere, this implementation does not include the Monte Carlo portion of the implementation described in Section 2. The web application was built using the `shiny` R package and the code for this application is contained in two files. The first file, `ui.R` (short for ‘user interface’) contains the code that controls the layout of the various panels and panes in the application, as well as the placement of the user interface elements (i.e. text inputs, sliders, etc.). The `server.R` file contains the computational code that performs calculations, data manipulation, and generates the plots. See Section A for the source code.

3.1 R Packages

The following packages and methods were used in the development of the web application:

dplyr: The `dplyr` package (Wickham et al., 2013) is a data-wrangling and manipulation package implemented in R. The methods in this package were used to manage and manipulate the CDFs from the `.csv` file into a convenient format for plotting.

shiny: The `shiny` package and framework (Chang et al., 2018) constitutes the backbone of this project. `shiny` provides a way to create and deploy web applications through RStudio (RStudio Team, 2016). It also contains the implementations for all user-interface components (toggle buttons, check boxes, numeric inputs, sliders, etc.). The `shinydashboard` package (Chang and Borges Ribeiro, 2018) was also used as an aesthetic wrapper around the `shiny` framework. The `shiny` package was used to create and will be used to deploy the web application.

ggplot2: The plotting functionality of the `ggplot2` package (Wickham, 2016) was used to generate the actual visualization and to add, remove, or adjust components on the plot.

plotly: The `plotly` package (Sievert, 2018) is not currently used in the implementation, but may be used to add additional interactive capabilities to the plot. `plotly` includes a method called `ggplotly()` which could be used to convert the `ggplot` plot object to a `plotly` plot object. The `plotly` plots contain options to zoom in and out on a plot, show plot values when hovering with mouse, download and save a `.png` version of the plot, and download and save an interactive `html` version of the plot.

Since the existing R packages already implemented most of the tools needed to generate the plot and implement user interface elements, the primary task on this project was to seamlessly combine elements from the packages above (particularly the `shiny`, `ggplot2`, and `plotly` packages) to create a user-friendly interactive visualization tool.

4. Results

4.1 Features

The resulting web application currently has the several features implemented. First, the capability was added to allow the user to upload their own data from a `.csv` file to be used in the visualization. If users want to experiment with the visualization but don't have their own data readily on hand, they can also choose to use some provided sample data. Once the data source is specified by the user, several options are provided to allow customization of the visualization. Users can show or hide the P-box, as well as specify the upper and lower percentiles to be used in the P-box calculation. The CDF ensemble can also be toggled on and off so only the P-box is shown. Oftentimes there are hundreds or thousands of CDFs to be plotted, so naturally a lot of overplotting can occur. A slider is included in the control panel to adjust the transparency of the CDFs. A download button has also been provided so users can download and save a `.png` file of the current rendering of the plot.

A few preliminary screenshots from the web application are included in this article. Figure 1 shows downloaded plots with various plotting options selected (show/hide P-box and CDFs). Figure 2 shows a full-view screenshot of the application.

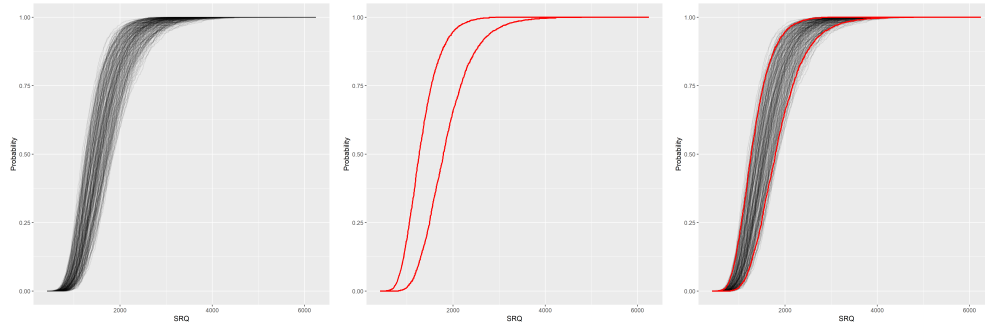


Figure 1: Plots downloaded and saved from the web application.

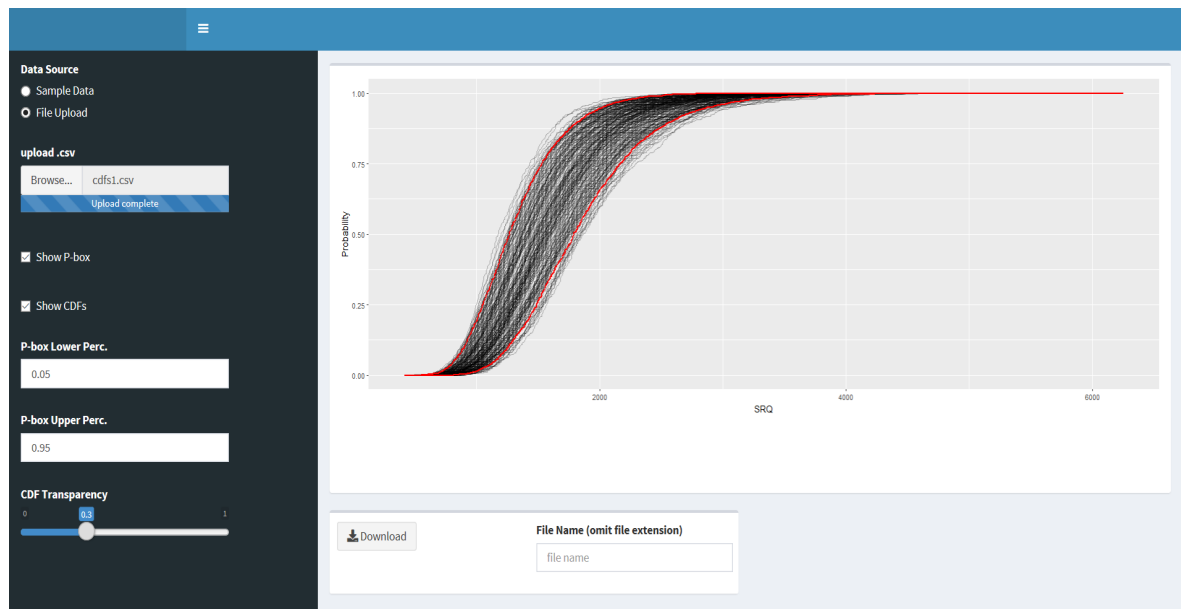


Figure 2: Full screenshot.

4.2 Challenges

One main challenge with this visualization tool that was unanticipated was the time that it would take to render the plot. The nature of uncertainty quantification and the nature of this kind of visualization leads to there being hundreds or even thousands of traces on a single plot. In addition, the way the `shiny` package is implemented causes the plot to completely re-render when user inputs change. Thus, whenever the user selects a new plotting option, he or she must wait several seconds (depending on the size of the data set being used) for the plot to re-render. This leads to a less ‘interactive’ feel for the user. As this application is still under development, possibilities for decreasing the re-rendering time of the plots are being explored.

5. Future Work

In the next two weeks I plan to fine-tune the visualization tool and produce a polished final product. There is also one more major feature to implement that will greatly aid in the interpretability of the visualization. This feature is the ability for a user to input an SRQ

value and extract a probability range, as well as the ability to input a probability and extract an SRQ range. Finishing touches will also include adjusting the spacing between controls to improve aesthetics and adding a user manual/help page.

References

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A. Appendix

R code for shiny web application.

A.1 ui.R

```
library(shiny)
library(shinydashboard)
library(plotly)
library(shinyalert)
library(shinyWidgets)

dashboardPage(
  dashboardHeader(
    title = "UQViz"
  ),
  dashboardSidebar(
  ),
  dashboardBody(
    useShinyalert(),
    tabsetPanel(
      tabPanel("Data Source",
        fluidRow(
          column(
            width = 3,
            radioButtons(inputId = "radioDataSource",
              label = "Data Source",
              choices = c("Sample Data",
                "File Upload"),
              selected = "Sample Data"),
            uiOutput(outputId = "fileInput")
          )
        ),
      tabPanel("Visualization Options",
        fluidRow(
          column(
            width = 2,
            offset = 0,
            verticalLayout(
              br(),
              uiOutput(outputId = "pbxBtnn"),
              br(),
              uiOutput(outputId = "cdfBtnn")
            )
          ),
          column(
            width = 2,
            offset = 0,
            numericInput(inputId = "pbxLower",
              label = "Lower P-box Percentile",
              value = 0.05,
              width = 250),
            numericInput(inputId = "pbxUpper",
              label = "Upper P-box Percentile.",
              value = 0.95,
              width = 250)
          ),
          column(
            width = 3,
            offset = 0,
            sliderInput(inputId = "sliderAlpha",
              label = "CDF Transparency",
              value = 0.2,
              min = 0,
              max = 1,

```

```

        step = 0.1,
        ticks = FALSE)
    ),
    column(
        width = 1,
        offset = 0,
        checkboxInput(inputId = "extractInt",
            label = "Extract Interval",
            value = FALSE)
    ),
    column(
        width = 2,
        uiOutput(outputId = "extractTypeInput"),
        uiOutput(outputId = "valInput")
    )
)

),
tabPanel("Labeling",
    fluidRow(
        column(
            width = 2,
            textInput(inputId = "titleInput",
                label = "Title",
                placeholder = "Plot Title",
                value = "")
        ),
        column(
            width = 2,
            textInput(inputId = "xaxisInput",
                label = "X axis Label",
                placeholder = "X-axis",
                value = "SRQ") #,
            # textInput(inputId = "yaxisInput",
            #     label = "Y axis Label",
            #     placeholder = "Y-axis",
            #     value = "Probability")
        )
    ),
tabPanel("User Guide",
    h3("Overview"),
    h5("UQViz is an interactive tool that can be used
to create meaningful visualizations of
'2D Uncertainty Quantification' (for more
information on 2D UQ, see ",
tags$a(href = "http://verification.asmedigitalcollection.asme.org/article.aspx?articleid=
        "this article",
        target="_blank"),
    "). Users can select data source and adjust various
visual components and labels. The title and axis
label can also be customized, and the visualization
can be downloaded and saved."),
    h3("Data Source"),
    tags$p("The 'Data Source' tab contains controls for
the user to select the source from
which data for the visualization will be obtained.
If ",
tags$b('Sample Data'),
    "is selected, a small built-in data set is used as
the data source for the
visualization. This feature is provided for convenience,
and can be used for experimentation and
exploration. If ",
tags$b('File Upload'), "
is selected, users can upload a ",
tags$code(".csv"),
    "file containing
data to be used in the visualization. This ",
tags$code(".csv"),
    "file should be formatted such that the 'x' values over

```



```

        which the CDFs are evaluated
        are in the first column, and the CDFs are
        in the following columns."
    ),
    h3("Visualization Options"),
    tags$p("Several visualization options are provided to
allow customizable graphics to be
created. The ",
tags$b("Show/Hide P-box"), " and the ",
tags$b("Show/Hide CDFs"), " buttons toggle
back and forth between showing and
hiding the red P-box and the black ensemble of CDFs.
Note that showing the CDF
ensemble may (depending on the size of the uploaded
file) significantly increase
plot rendering times. If the user wishes to
display the CDFs on the final version
of the plot, it is suggested to adjust all
visualization options and controls
while the CDFs are hidden, keeping the plot
rendering times to a reasonable
length. Then, as the last step, show the CDF
ensemble. This way, the user will only
have to wait once for the lengthened rendering time."),
    tags$p("The ",
tags$b("Lower P-box Percentile"),
" and ",
tags$b("Upper P-box Percentile"),
"values can also be adjusted. This will
shift the boundaries of the P-box on
the visualization."),
    tags$p("Adjusting the ",
tags$b("CDF Transparency"),
" slider will adjust the
transparency of each CDF in the CDF ensemble.
A value of 0 corresponds to
completely transparent, while a value
of 1 corresponds to completely opaque.
This control will only affect the visualization
when the CDFs are being shown.
This feature can be useful when there is a
high degree of overplotting due to
a large number of CDFs. Allowing transparency
on the CDFs can assist in
visualizing high-density regions on the plot."),
    tags$p("When the ",
tags$b("Extract Interval"),
" box is checked,
several more controls appear.
Extracting an interval is one way that
P-boxes can be interpreted in practice.
Users can decide whether to extract an ",
tags$b("SRQ Interval"),
" or a ",
tags$b("Probability Interval"),
". If extracting an SRQ interval, users
will need to select a probability value; if
extracting a probability interval, users
will need to select an SRQ value.
Labels and dotted lines will be displayed
on the visualization, showing the
probability or SRQ value selected and the
corresponding interval."),
    h3("Labeling"),
    tags$p("Users also have the capability to choose
a custom ",
tags$b("Title"),
" and a custom ",
tags$b("X axis Label"),
"to further customize the plot to a
specific context or application. Since this

```



```

# Load needed packages
library(shiny)
library(ggplot2)
library(plotly)
library(shinyalert)
library(shinyWidgets)

## Increase max file upload size
options(shiny.maxRequestSize = 15*1024^2)

#####
# Functions #####
#####

# Function to calculate p-box lower and upper bounds
calc_pbox <- function(data, p_upper, p_lower){
  pbox <- apply(values$data,
    1,
    FUN = quantile,
    probs = c(p_lower, p_upper))

  pbox <- t(pbox)

  values$pbox <- data.frame(x = values$data[,1],
    lower = pbox[,1],
    upper = pbox[,2])

  return(pbox)
}

# function to calculate the SRQ value for a given probability level
calc_srq <- function(prob_in){
  srq_l <- values$pbox[which.min(abs(values$pbox$lower - prob_in)),]$x
  srq_u <- values$pbox[which.min(abs(values$pbox$upper - prob_in)),]$x

  return(c(srq_l, srq_u))
}

# function to calculate the probability value for a probability level
calc_probs <- function(srq_in){
  prob_l <- values$pbox[which.min(abs(values$pbox$x - srq_in)),]$lower
  prob_u <- values$pbox[which.min(abs(values$pbox$x - srq_in)),]$upper

  return(c(prob_l, prob_u))
}

#####
# Reactive Values#####
#####

values <- reactiveValues()

#####
# Read in Sample Data #####
#####
cdf_arr <- read.csv("data/cdfs.csv", header = FALSE)
cdf_arr <- t(cdf_arr)
cdf_df <- data.frame(cdf_arr)

values$valmax <- max(cdf_df[,1])
values$valmin <- min(cdf_df[,1])
values$userin <- NULL
values$showcdf <- FALSE
values$showpbx <- TRUE

#####
# Server Logic #####
#####
shinyServer(function(input, output) {

  # toggle button to show/hide cdf ensemble
  observeEvent(input$cdfToggle, {

```

```

    if (values$showcdf == FALSE){
      shinyalert(
        title = "",
        callbackR = function(x){
          values$showcdf <- x
        },
        text = paste("Showing the CDF ensemble on the plot may significantly",
                     "increase plot render times. Do you want to continue?"),
        showCancelButton = TRUE,
        confirmButtonText = "Show CDFs",
        cancelButtonText = "Don't Show CDFs",
        confirmButtonCol = "#52D755",
        type = "info"
      )
    } else {
      values$showcdf <- FALSE
    }
  })

  observeEvent(input$pbxToggle, {
    if (values$showpbx == FALSE){
      values$showpbx <- TRUE
    } else {
      values$showpbx <- FALSE
    }
  })

  # toggle button to show/hide p-box
  output$pbxBtn <- renderUI({
    if (values$showpbx == TRUE){
      lbl = "Hide P-box"
      sty = "bordered"
    } else {
      lbl = "Show P-box"
      sty = "simple"
    }

    actionBttn(inputId = "pbxToggle",
               label = lbl,
               style = sty,
               size = "sm",
               color = "primary")
  })

  output$cdfBttn <- renderUI({
    if (values$showcdf == TRUE){
      lbl = "Hide CDFs"
      sty = "bordered"
    } else {
      lbl = "Show CDFs"
      sty = "simple"
    }

    actionBttn(inputId = "cdfToggle",
               label = lbl,
               style = sty,
               size = "sm",
               color = "primary")
  })

  output$uqPlot <- renderPlot({
    # Use selected data source
    if (input$radioDataSource == "Sample Data"){
      values$data <- cdf_df
    } else {
      req(input$fileIn)
      df <- read.csv(input$fileIn$datapath,
                    header = FALSE)
      df <- data.frame(df)
      values$data <- df
    }
  })

```

```

# set up initial plot
req(values$data)
plt <- ggplot(data = values$data,
              aes(values$data[,1]))

# plot cdf ensemble if user selects
if (values$showcdf == TRUE){
  for(i in names(values$data)[-1]){
    plt <- plt +
      geom_line(aes_string(y = i,
                          color = shQuote("CDFs")),
                alpha = input$sliderAlpha)
  }
  plt <- plt
}

# get nice breaks for x-axis
px <- pretty(values$data[,1])

# Labels and additional plot formatting
plt <- plt +
  xlab(input$xaxisInput) +
  # ylab(input$yaxisInput) +
  ylab("Probability") +
  scale_x_continuous(breaks = px,
                    limits = range(px)) +
  ggtitle(input$titleInput) +
  theme_bw() +
  theme(plot.title = element_text(hjust = 0.5,
                                  size = 18,
                                  face = "bold"),
        panel.grid.minor = element_blank(),
        axis.text = element_text(size = 12),
        axis.title = element_text(size = 14))

# show p-box if user selects
if (values$showpbx == TRUE){
  pbx <- calc_pbox(values$data,
                  (1 - input$pbxLower),
                  (1 - input$pbxUpper))

  plt <- plt +
    geom_line(aes(y = pbx[,1], col = "Pbox"), lwd = 1) +
    geom_line(aes(y = pbx[,2], col = "Pbox"), lwd = 1) +
    scale_colour_manual(name="", values=c("Pbox"="red"))
}

# Calculate and show extracted interval on plot
# if user selects
if (input$extractInt == TRUE){
  req(input$valIn)

  # if interval is an SRQ interval
  if (input$extractType == "SRQ Interval"){
    if (input$valIn < 0){
      values$userin <- 0
    } else if (input$valIn > 1) {
      values$userin <- 1
    } else {
      values$userin <- input$valIn
    }
    srq_vec <- calc_srq(values$userin)
    plt <- plt +
      geom_hline(yintercept = values$userin, lty = 2) +
      geom_segment(mapping = aes(x = srq_vec[1],
                                y = 0,
                                xend = srq_vec[1],
                                yend = 1),
                  lty = "longdash") +
      geom_segment(mapping = aes(x = srq_vec[2],
                                y = 0,

```

```

                                xend = srq_vec[2],
                                yend = 1),
                                lty = "longdash") +
  geom_text(aes(srq_vec[1], 0.05,
                label = round(srq_vec[1], 2),
                vjust = 3,
                hjust = 0.5),
            size = 5) +
  geom_text(aes(srq_vec[2], 0.05,
                label = round(srq_vec[2], 2),
                vjust = 3,
                hjust = 0.5),
            size = 5) +
  geom_text(aes(min(values$data[, 1]),
                values$userin,
                label = round(values$userin, 2),
                vjust = -0.5,
                hjust = 2),
            size = 5)
} else {
  # if interval is a probability interval
  req(input$valIn)
  if (input$valIn < values$valmin){
    values$userin <- values$valmin
  } else if (input$valIn > values$valmax) {
    values$userin <- values$valmax
  } else {
    values$userin <- input$valIn
  }
  prob_vec <- calc_probs(values$userin)
  plt <- plt +
    geom_segment(mapping = aes(x = values$userin,
                              y = 0,
                              xend = values$userin,
                              yend = 1),
                lty = 2) +
    geom_hline(yintercept = prob_vec[1],
               lty = "longdash") +
    geom_hline(yintercept = prob_vec[2],
               lty = "longdash") +
    geom_text(aes(min(values$data[, 1]),
                  prob_vec[1],
                  label = round(prob_vec[1], 2),
                  vjust = -0.5,
                  hjust = 2),
              size = 5) +
    geom_text(aes(min(values$data[, 1]),
                  prob_vec[2],
                  label = round(prob_vec[2], 2),
                  vjust = -0.5,
                  hjust = 2),
              size = 5) +
    geom_text(aes(values$userin,
                  0.05,
                  label = round(values$userin, 2),
                  vjust = 3,
                  hjust = 0.5),
              size = 5)
}
}

if (values$showpbx && values$showcdf){
  plt <- plt +
    scale_color_manual(name = "",
                       values = c("CDFs" = "black",
                                  "Pbox" = "red")) +
    guides(colour =
           guide_legend(override.aes =
                        list(linetype = c(1, 1),
                               lwd = c(0.5, 1)))) +
    theme(legend.text = element_text(size = 12))
}

```

```

    } else if (values$showpbx){
      plt <- plt +
        scale_color_manual(name = "",
                           values = c("Pbox" = "red")) +
        theme(legend.text = element_text(size = 12))
    } else if (values$showcdf){
      plt <- plt +
        scale_color_manual(name = "",
                           values = c("CDFs" = "black")) +
        theme(legend.text = element_text(size = 12))
    }

    values$plot <- plt

    plt
  })

output$extractTypeInput <- renderUI({
  if (input$extractInt == TRUE){
    radioButtons(inputId = "extractType",
                 label = "Interval Type: ",
                 choices = c("SRQ Interval",
                             "Probability Interval"))
  }
})

output$valInput <- renderUI({
  if (input$extractInt == TRUE){
    if (input$extractType == "Probability Interval"){
      lbl = "SRQ Input Value"
      val = round(quantile(values$data[,1], 0.1), 0)
    } else {
      lbl = "Probability Input Value"
      val = 0.95
    }
    numericInput(inputId = "valIn",
                  label = lbl,
                  value = val)
  }
})

output$fileInput <- renderUI({
  if (input$radioDataSource == "File Upload"){
    fileInput(inputId = "fileIn",
              label = "Upload .csv File")
  }
})

# help from https://stackoverflow.com/questions
# /14810409/save-plots-made-in-a-shiny-app
output$savePng <- downloadHandler(
  filename = function(){
    paste(input$pngName,
          ".png",
          sep="")
  },
  content = function(file){
    ggsave(file,
            plot = values$plot,
            device = "png",
            width = 12)
  }
)
})

```